

Aula 17 - 15.3/8

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• Coordenadas polares

$$\iint_R (2x - y) dA = \iint_R (2r \cdot \cos(\theta) - r \cdot \sin(\theta)) dr d\theta = \int_R \int_0^2 r^2 (2 \cdot \cos(\theta) - \sin(\theta)) dr d\theta$$

• Limites do retângulo

$$x=0 ; \theta = \pi/2 ; y=x ;$$

$$x=y$$

$$r \cdot \sin(\theta) = r \cdot \cos(\theta)$$

$$\tan(\theta) = 1 \Rightarrow \theta = \pi/4$$

$$\cdot \quad 0 \leq r \leq 2$$

$$\cdot \quad \int_{\pi/4}^{\pi/2} \int_0^2 r^2 (2 \cdot \cos \theta - \sin \theta) dr d\theta$$

$$\cdot \quad \int_{\pi/4}^{\pi/2} \frac{8}{3} (2 \cdot \cos(\theta) - \sin(\theta)) d\theta$$

$$\cdot \quad \frac{8}{3} (2 \cdot \sin \theta + \cos(\theta)) \Big|_{\pi/4}^{\pi/2} = \frac{8}{3} \cdot \left[(2+0) - \left(\sqrt{2} + \frac{\sqrt{2}}{2} \right) \right] = \frac{32 - 24\sqrt{2}}{6}$$