

6.945 Final Project

Dwimiykwim

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1 Argument Inference

We have written an interpreter for a Scheme-like language that supports automatic inference of procedure arguments. The core of the argument inference system is in three new special forms: `madlab`, `madblock`, and `~~`.

The `madlab` special form is a variation of `lambda`. Specifically, the form creates a procedure that can take its arguments in any order. Instead of using position to match given arguments to the variables they are bound to, a `madlab` specifies a predicate for each input variable that the argument bound to that variable must satisfy. For example,

```
(define madmap
  (madlab ((xs list?) (f procedure?))
    (map f xs)))
```

is a variant of `map` that can take its arguments in either order. We call the resulting procedures “madlab procedures” or simply “madlabs”. For most purposes, madlabs are ordinary compound procedures that happen to have unusually flexible interfaces. For example, if we define

```
(define (curry f . args)
  (lambda more-args
    (apply f (append args more-args))))
```

then both `(curry madmap exp)` and `(curry madmap (iota 16))` work as expected, raising `e` to each of the elements of an input list and mapping an input function over the integers from 0 to 15, respectively. Note that the argument matching is not done until the `madlab` is applied. To demonstrate this, consider

```
(define silly
  (madlab ((xy (member-of '(x y))) (yz (member-of '(y z))))
    (list xy yz)))
```

and the partial application (`curry silly 'y`), where `member-of` has the obvious namesake meaning. When it's applied to `'x`, the `'y` is matched with `yz`, but when it's applied to `'z`, the `'y` is matched with `xy`.

The `madblock` special form is a variation of `begin`. Just like `begin`, it groups together a sequence of expressions, evaluates each of them in turn, and returns the result of the last one. The only difference is that the result of each evaluation in the sequence is added to an *inference context*, which, as we will soon explain, is the list of values available to `??` (which performs inference). The inference context is dynamically bound (the interpreter uses MIT Scheme's `fluid-let`) to the empty list at the beginning of each `madblock`, so the inference context is empty at the start of the sequence. Our interpreter makes it easy to refer explicitly to values of expressions earlier in the sequence using the `define` special form by having `define` return the result of evaluating its body as opposed to an unspecified value or the name it was bound to.

The `??` special form is what `Dwimiykwim` is all about. It takes a `madlab` and any number of other expressions and applies the `madlab` to the given expressions plus any additional necessary values from the inference context. That is, it infers what arguments to pass to the given `madlab`. For instance,

```
(madblock
  (curry list 'say)
  'dont-pick-me-im-a-symbol-not-a-procedure-or-list
  "a very distracting string"
  '(1 2 5 3-sir 3)
  (?? madmap))
```

returns `((say 1) (say 2) (say 5) (say 3-sir) (say 3))`. Inference only succeeds if there is an unambiguous matching between the `madlab`'s predicates and the union of the given expressions and values from the inference context with the additional constraint that every given expression is matched. (See Section 3 for details.) For example, only the first two inferences in

```
(madblock
  (curry list 'say)
  (define xs '(1 2 5 3-sir 3))
  (?? madmap)
  (?? madmap xs)
  (?? madmap))
```

will succeed. A single procedure, `(curry list 'say)`, is in the inference context the whole time. When the first `infer` happens, there is also only one list, so inference succeeds. Note, however, that the resulting list is added to

the inference context. The second ?? is explicitly passed a list, and inference succeeds thanks to this constraint. By the time the third ?? happens there are three lists in the inference context, so inference fails due to ambiguity.

Just as the body of a `lambda` with multiple expressions desugars to a single `begin` expression, the body of a `madlab` desugars to a single `madblock`. Additionally, each of the argument variables is added as an expression to the beginning of the `madblock`. The effect of this is that ?? can be used freely in the body of a `madlab` and the arguments are automatically added to the inference context. If for some reason we need to keep the arguments out of the context, we can write `body` as a `madblock` explicitly. There is nothing to worry about with regards to nesting because each `madblock` starts with a fresh inference context. In fact, the intended style is for `madblock` to be rare and mostly invoked implicitly through `madlab`. This is because `madlab` creates a new environment, which is a good idea given the intended synergy with `define`.

2 Tagging

The first piece of this project that is intended to set groundwork for inference and matching is a lightweight system for tagging data. The motivation for this system is that it creates a method for describing data with useful characteristics that can be used for performing argument inference with tag checks as predicates. Since tags can be arbitrarily created by the user and are not limited like type systems usually are, the language becomes more flexible.

Tagged data consists of a value and a list of tags, which can be used to describe the significance of the data. We can add more tags to data as it moves through a program, and remove the tags if we would just like the value. However, we can always perform default operations on tagged data without removing the tags in advance because procedures `untag` data before processing it outside the interpreter. This is implemented by making a procedure "tag-aware". Being "tag aware" removes tags in logical places, so that Scheme functions and other necessary functions can operate as intended when the tags are not important. For example, `car` and `cdr` should be "tag aware" because the record type for tagged data is a list, but we only care for the actual data being tagged.

As stated earlier, since MIT Scheme does not come with a nice type system by default, tags allow us to work with variables by more generally describing their characteristics. The primary usefulness of these tags lies in argument matching. By giving values tags, we can match tags to tag predicates to determine if a variable is an appropriate argument to a function. Functions can request that certain variables have certain tags, or more generally, that these variables satisfy

arbitrary predicates. This allows us to verify that the user is performing the intended task by forcing him/her to think in advance about what really belongs in the function call.

A simple example to illustrate this point with out-of-order operands is ordering tagged operands after receiving them in the wrong order. As a quick note, the syntax for tagging data is $\sim\sim$. In this example, we tag the numbers 3 and 4 with x and y respectively. We make a function *x-then-y* that given a some x and some y , will make a list first containing x , then y . This utilizes the argument matching with tag checking predicates.

```
;dwimiykwim>
(define (x-then-y (x (has-tag? 'x)) (y (has-tag? 'y)))
  (list x y))
;dwimiykwim>
(x-then-y ( $\sim\sim$  'y 4) ( $\sim\sim$  'x 3))
;=> (#(<tagged> 3 (x)) #(<tagged> 4 (y)))
```

Although this tag system does not have to be used in order to perform the core features of Dwimiykwim - argument inference, and out of order operations - it is convenient to utilize it in many cases where the predicate one checks describes a characteristic of the data.

3 Bipartite Matching

Inferring arguments of madlabs reduces to the following problem in graph theory. We are given a bipartite graph with vertex partitions A and B satisfying $|A| \leq |B|$ along with a subset $B^* \subseteq B$ of “required” vertices, and we ask whether there exists a unique matching of size $|A|$ such that every vertex of B^* is matched. A is the set of predicates of the madlab’s arguments, B^* is the set of values passed in explicitly, B is the union of B^* and the set of values in the inference context, and there is an edge between $a \in A$ and $b \in B$ if and only if b satisfies a .

This problem is quite easily solved by a variation on the traditional maximum bipartite matching algorithm, which we review quickly here. We refer to vertices in A as “sources” and vertices in B as “targets”. Let E be the edge set of the graph and $M \subseteq E$ be a matching. We think of edges in M as being oriented from B to A and edges in $E \setminus M$ as being oriented from A to B . An *augmenting path* of M is a path from an unmatched source to an unmatched target that follows only edges in $E \setminus M$ from sources to targets and only edges in M from targets to sources. Given an augmenting path of a matching, swapping

the orientations (that is, inserting or removing from the matching as appropriate) of all the edges in the path yields a larger matching: all intermediate vertices in the path remain matched, but the previously unmatched endpoints are now matched. This means a maximum matching has no augmenting paths. It is well-known that the converse also holds: if a matching has no augmenting path, it is not maximal. Therefore, to find a maximum matching, we repeatedly search for augmenting paths, flipping edge orientations when we find them, until there are no more, at which point the edges from B to A are the edges of the maximum matching.

Our problem differs from traditional maximum matching in two ways. First, we require that some targets $B^* \subseteq B$ be matched because we must use every argument that was passed in explicitly. To do this, we start by finding a maximum matching M of B^* with A , reporting failure if $|M| < |B^*|$, and then matching A with B using M as a starting point, guaranteeing that all of B^* will remain matched. Second, we are concerned with whether the maximum matching is unique because there must not be multiple ways to match all the predicates with arguments. To do this, given a maximum matching M , for each edge $e \in M$, we attempt to find an augmenting path of the matching $M \setminus \{e\}$ in a graph with reduced edge set $E \setminus \{e\}$, with the additional requirement that if e was incident with a vertex $b \in B^*$ then the augmenting path must finish at b . That these algorithms are valid follows from the fact that, given a non-maximum matching M , there is a maximum matching containing a vertex unmatched by M only if there is an augmenting path of M containing that vertex, which is a slight strengthening of the result mentioned earlier.

Once the graph is constructed, all of this can be done in quadratic time. Our implementation is purely functional and makes liberal use of linear-time list procedures, so it is slower than this by approximately another quadratic factor, but procedures generally don't take in more than, say, 8 arguments, and $O(8^4)$ is perfectly acceptable running time for our prototype.

4 Debugging

In addition to constructing mechanisms for tagging, inferring arguments in function calls, and matching function arguments, we have created a way for the user to easily correct ambiguity errors that arise from more than one possible way to interpret an inference. For example, consider the simple *madlab* below:

```
(define num-str
  (madlab ((x number?) (y string?))
    (list y x)))
```

If we were to call a *madblock* that had two number values and strings, then upon inference, we would have an ambiguity error. To handle this case, we put the program into debug mode, and display the context, edges, and required args to the user. The context is indexed, so that the user does not have to spend time typing in every expression they would like to force in the matching. Using this information, the user is then expected to add new required args to settle any ambiguities. The reason we ask for required arguments is because those will be used in the matching and will usually eliminate multiple matchings. Once the user enters some combination of unambiguous args, we notify the user of the successful matching and exit debug mode. A sample workflow for *num-str* would be:

```
(madblock
  1
  "foo"
  2
  "bar"
  (?? num-str))
=== Dwimiykwim Tawimiydkwim ===
Context:
(0 "bar")
(1 2)
(2 "foo")
(3 1)
Edges:
(x 1 3)
(y 0 2)
Required:
()
New required:
(0)
Ambiguous matching!
New required:
(0 3)
Unambiguous matching! Terminate debugging mode!
```

In this example, the user was allowed to test multiple sets of required arguments, until one achieved a good matching. The user would then be expected

to go and correct the code by specifying those as required arguments in the inference. The new program would now be:

```
(madblock
  1
  "foo"
  2
  "bar
  (?? num-str 1 "bar"))
```

Since the user is providing so many arguments, it would not be very useful to use inference unless they modified the code to remove some expressions.

Under the hood of the debugger, when we encounter a bad matching, we enter debug mode, indexing each item in the context, and print all the information we know about the matching that had an error. We ask the user to give us a list of newly required arguments, verifying that this is indeed a list of numbers, and checking using the matching function if the ambiguity resolves. In the case where the user has not specified enough required arguments, we ask the user for a new set of required arguments, not saving the initial choice. This continues until either the user exits the debugger, or a good match is found and program terminates with an error.

5 Demo

As a taste of writing a real program with Dwimiykwim and a demonstration of how much data flow can be inferred, we devote this section to walking through the process of a sample program. We will start by building an evaluator for arithmetic expressions then extend it to include Scheme-style `let` bindings. Along the way, we'll discuss some further minor features of Dwimiykwim that would have been distracting details in the previous exposition but are nice to have in practice.

The main task for our arithmetic evaluator is evaluating binary operations. (We leave generalizing to n -ary operations as an exercise to the reader best tried after reading this entire section.) As a first step, we should be able to identify when an expression is a binary operation and, if it is one, extract the operation name and arguments. Just as `(define (f x1 ... xn) ...)` desugars to a lambda expression, `(define (f (x1 p1?) ... (xn pn?)) ...)` desugars to a madlab expression where `x1` must satisfy `p1?` and so on.

```

(define (binop? exp)
  (if (pair? exp)
      (member (car exp) '(+ - * /))
      #f))
(define (binop-op (exp binop?))
  (car exp))
(define (binop-left (exp binop?))
  (cadr exp))
(define (binop-right (exp binop?))
  (caddr exp))

```

Here we use madlabs not for disambiguating arguments but to allow inference of the single argument when there's only a single value in the inference context that could possibly be a binary operation expression.

Our application procedure is straightforward other than its use of the new `has-tag?` predicate: `((has-tag? t) x)` is true when `x` has tag `t`.

```

(define (apply-binop (op symbol?)
  (left (has-tag? 'left))
  (right (has-tag? 'right)))
  ((cadr (assq op
    (list (list '+ +)
          (list '- -)
          (list '* *)
          (list '/ /))))
    left
    right))

```

Even though `left` and `right` have tags, we can still apply procedures from the underlying Scheme to them. The tags are automatically stripped from the arguments of all such procedures with a short list of exceptions including `cons` and `list` that allow for tagged data to exist in larger data structures.

The plan for the evaluation procedure is to dispatch to two cases depending on whether the expression is a primitive number or a binary operation expression. We decide between the cases using the following madlabs, which are again madlabs for inference rather than argument ordering purposes.

```

(define (exp? x)
  (null? (tags x)))
(define (primitive? (exp exp?))
  (number? exp))
(define (operation? (exp exp?))
  (binop? exp))

```


At this point it is probably clear to the reader that we have not gone to great lengths to make all of our predicates air-tight, but our somewhat lenient definitions of `exp?` and `binop?` will suffice for this demo.

We can now finally define our main procedure. Recall that `??` invokes argument inference, `~~` tags its second argument with the first, and that the body of madlab expressions desugar to madblocks. The second case uses `madblock-inherit`, which is a variant of `madblock` that uses previous inference context in its starting inference context. It is probably not wise to use `madblock-inherit` widely given its dependence on context, but its use here is mostly harmless and slightly reduces clutter.

```
(define (eval (exp exp?))
  (cond
    ((?? primitive?)
     exp)
    ((?? operation?)
     (madblock-inherit
      (~~ 'left (eval (?? binop-left)))
      (~~ 'right (eval (?? binop-right)))
      (?? binop-op)
      (?? apply-binop))))))
```

Notice that we almost all of the data flow is inferred: the only explicit arguments given are for evaluating the left and right subexpressions, both of which are expressions, so we need to disambiguate them somehow.