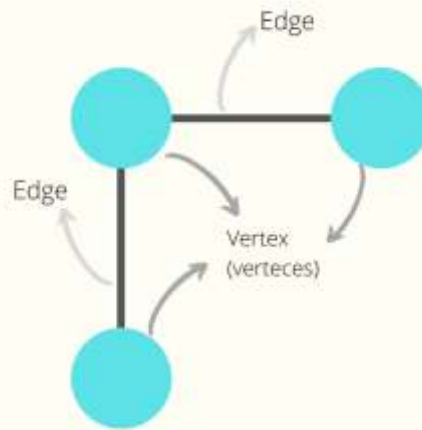


# ADT Graph

## ADT Graph <T>



Graph = { Directed = <directed>, Weighted = <weighted>, Vertices = <vertices>, Edges = <edges> }

{ inv: }

### Primitive Operations:

• Graph:	directed x weighted	→ Graph<T>
• getVertices:	Graph<T>	→ List of vertices
• isDirected:	Graph<T>	→ Boolean
• isWeighted:	Graph<T>	→ Boolean
• addVertex:	Graph<T> x T	→ Graph<T>
• addEdge:	Graph<T> x Vertex<T> x Vertex<T>	→ Graph<T>
• removeVertex:	Graph<T> x Vertex<T>	→ Graph<T>
• removeEdge:	Graph<T> x Vertex<T> x Vertex<T>	→ Graph<T>
• getNeighbors:	Graph<T> x Vertex<T>	→ List of vertices
• getNumberOfVertices:	Graph<T>	→ Number
• getNumberOfEdge:	Graph<T>	→ Number
• areAdjacent:	Graph<T> x Vertex<T> x Vertex<T>	→ Boolean
• isInGraph:	Graph<T> x T	→ Boolean
• getEdgeWeight:	Graph<T> x Vertex<T> x Vertex<T>	→ double
• setEdgeWeight:	Graph<T> x Vertex<T> x Vertex<T> x double	→ Graph
• bfs:	Graph<T> x Vertex<T>	→ List of vertices
• dfs:	Graph<T> x Vertex<T>	→ List of vertices
• dijkstra:	Graph<T> x Vertex<T>	→ List of vertices
• floydWarshall:	Graph<T>	→ Matrix of double
• prim:	Graph<T> x Vertex<T>	→ Graph<T>
• kruskal:	Graph<T>	→ List of edges
• searchVertex:	Graph<T> x T	→ Vertex<T>
• getEdges:	Graph<T>	→ List of edges
• getContests:	Graph<T>	→ List of T

### **Graph(directed, weighted)**

“Create a new Graph without edges”

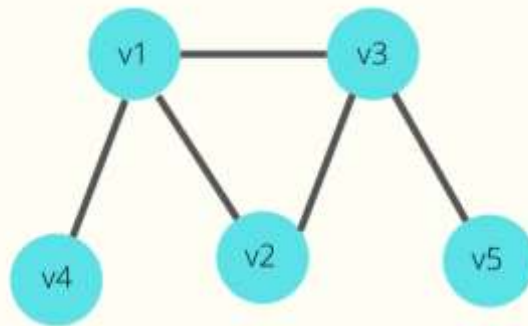
{ pre:  $\text{TRUE} \wedge \text{directed} \in \text{Boolean} \wedge \text{weighted} \in \text{Boolean}$  }

{ post: graph = { Directed = directed, Weighted = weighted, Vertices = 0, Edge = 0 } }

### **getVertices(graph)**

“Returns a collections of vertices”

{ pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges } }



{ post: = {v1, v2, .. vn } n = Vertices }



### **isDirected(graph)**

“Returns the directed value”

{ pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges } }

{ post: TRUE if graph is a directed graph  
FALSE if graph is a undirected graph }

### isWeighted(graph)

“Returns the weighted value”

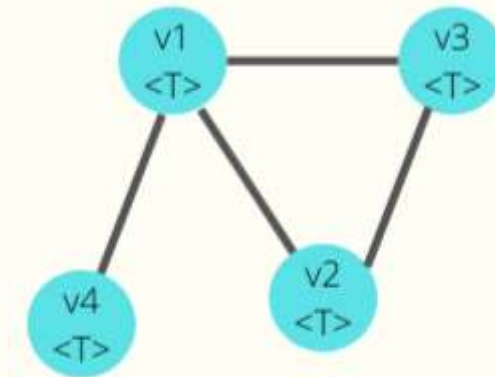
{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges } }

{post: TRUE if graph is a directed graph  
FALSE if graph is a undirected graph }

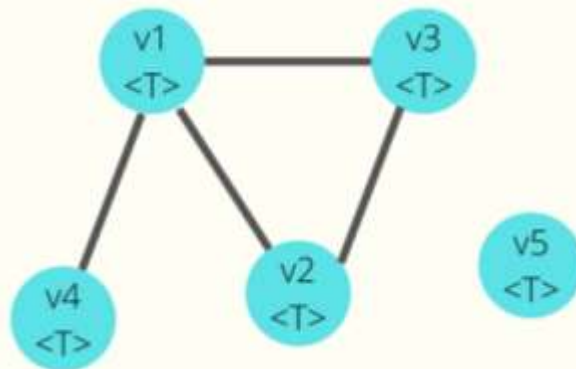
### addVertex(graph, object)

“Add a new vertex to graph”

{pre: graph = { ..., Vertices = vertices, .... }  $\wedge$  object  $\in T$  }



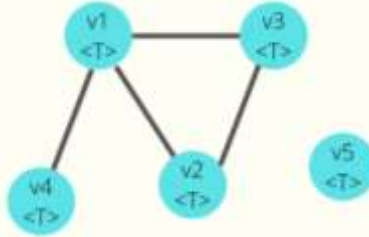
{post: graph = { Directed = directed, Weighted = weighted, Vertices = vertices+1, Edge = edges } }



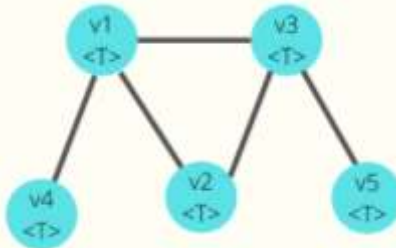
### **addEdge(graph, vertex1, vertex2)**

“Add a new edge between two vertex of graph”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
     $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph }



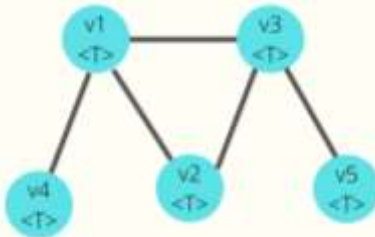
{post: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges + 1}}



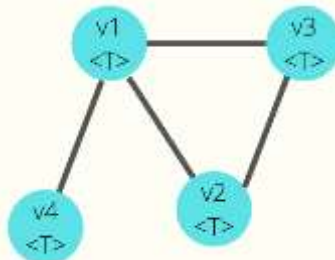
### **removeVertex(graph, vertex1)**

“Remove a vertex of the graph”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
     $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph }



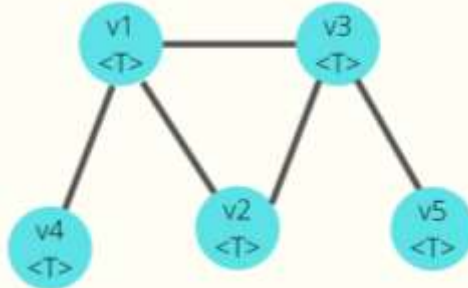
{post: graph = { Directed = directed, Weighted = weighted, Vertices = vertices-1, Edge <=edges}}



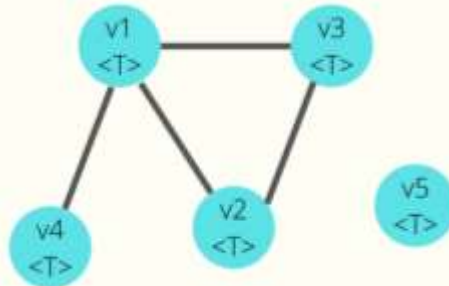
### **removeEdge(graph, vertex1, vertex2)**

“Remove a connection between two vertices of graph”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
     $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph }



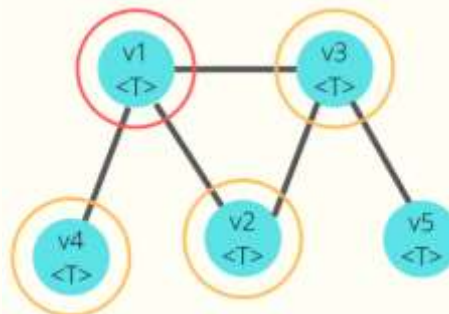
{post: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges-1}}



### **getNeighbors(graph, vertex)**

“Returns a collection of vertices that it are neighbor to vertex indicated”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges}  $\wedge$  vertex  $\in$  graph }



{post: = {v1, v2, .. vn } n  $\leq$  Vertices  $\wedge \forall i / 1 \leq i \leq$  Vertices  $\rightarrow \{v_i, \text{vertex}\} \in$  Edges of graph }



**getNumberOfVertices(graph)**

“Returns an integer represents the Vertices value”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges } }

{post: <vertices> }

**getNumberOfEdge(graph)**

“Returns an integer represents the Edge value”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges } }

{post: <edges> }

**areAdjacent(graph, vertex1, vertex2)**

“Verify if vertex1 and vertex2 area adjacent”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
           $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph }

{post: TRUE if {vertex1, vertex2}  $\in$  Edges of graph on the contrary FALSE}

**isInGraph(graph, object)**

“Verify if object is in graph”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  $\wedge$  object  $\in$  T }

{post: TRUE if object is in any vertex of graph on the contrary FALSE }

### **getEdgeWeight(graph, vertex1, vertex2)**

“Returns the edge weight of graph”

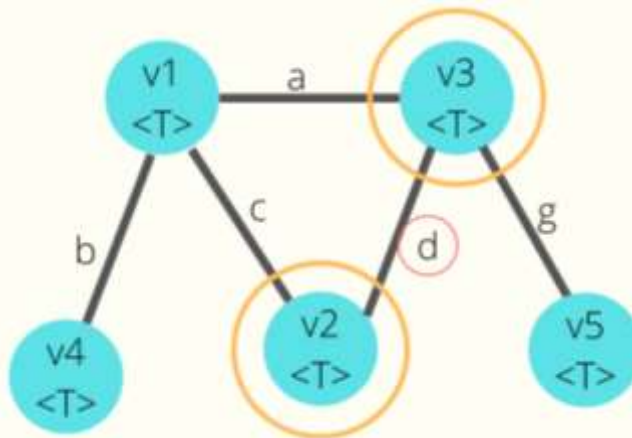
{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
     $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph }

{post: weight of {vertex1, vertex2} }

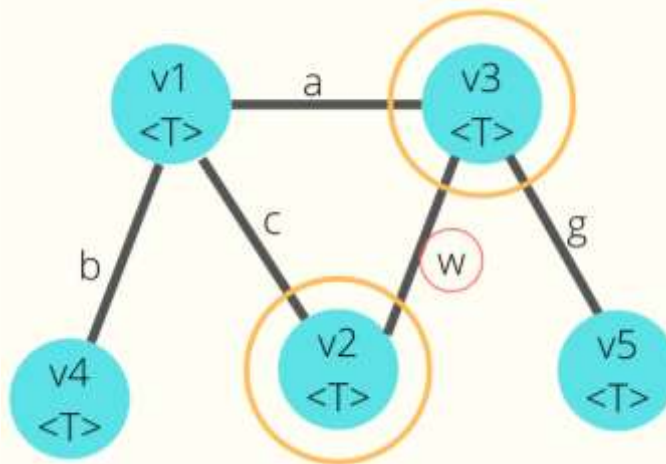
### **setEdgeWeight(graph, vertex1, vertex2, w)**

“Returns the edge weight of graph”

{pre: graph = { Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges }  
     $\wedge$  vertex1  $\in$  graph  $\wedge$  vertex2  $\in$  graph  $\wedge$  w  $\in$  double }



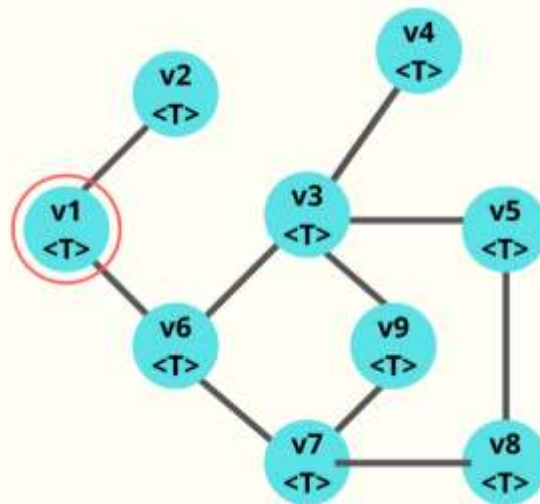
{post: weight of {vertex1, vertex2} = w }



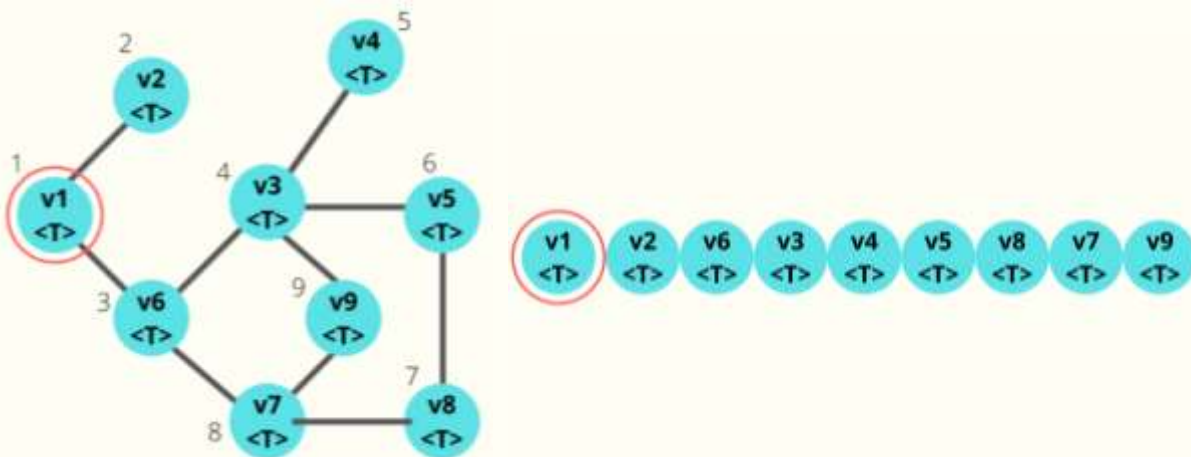
## dfs(graph, vertex)

“Returns an ordered collection of vertices that represents the deep path (Depth First Search) of the graph starting at vertex”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges}  
     $\wedge$  vertex  $\in$  graph  $\wedge$  graph is united}



{post: = {v1, v2, .. vn } n <= Vertices }

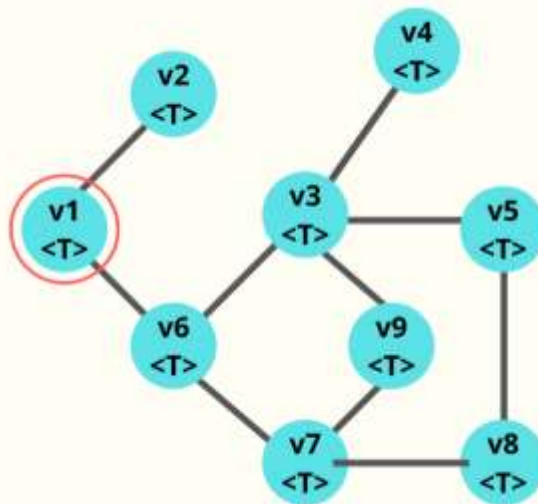




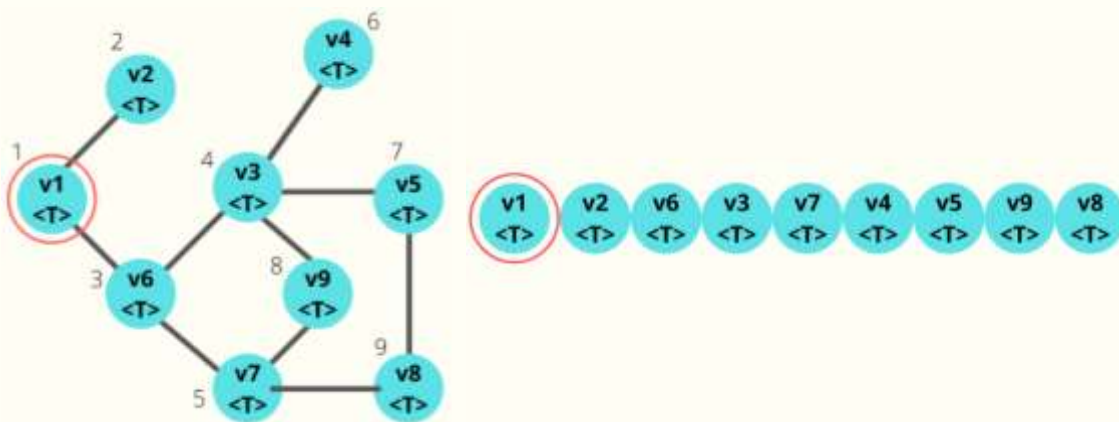
**bfs(graph, vertex)**

“Returns an ordered collection of vertices that represents the amplitude path (Breadth First Search) of the graph starting at vertex”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges}  
     $\wedge$  vertex  $\in$  graph  $\wedge$  graph is united}



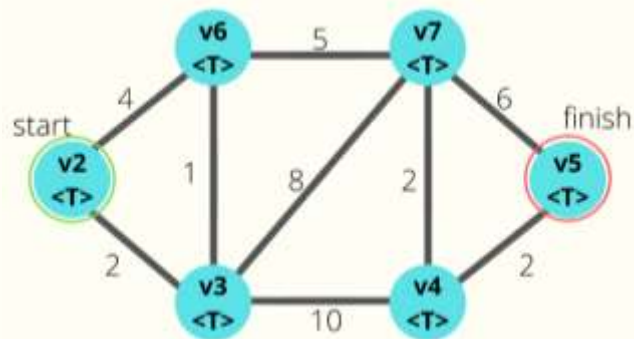
{post: = {v1, v2, .. vn } n <= Vertices }



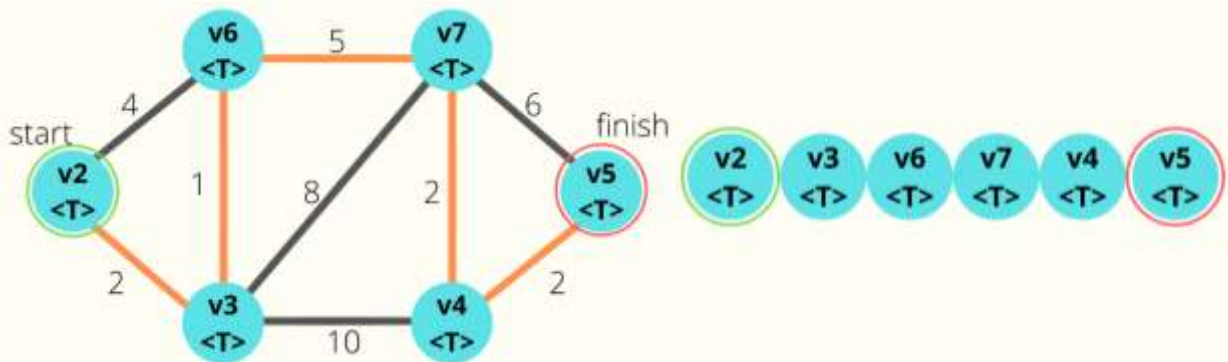
**dijkstra(graph, vertex1, vertex2)**

“Returns the path of least weight between vertex1 and vertex2”

{pre: graph = {Directed = directed, Weighted = TRUE, Vertices = vertices, Edge = edges}  
     $\wedge$  vertex1, vertex2  $\in$  graph  $\wedge$  graph is united}



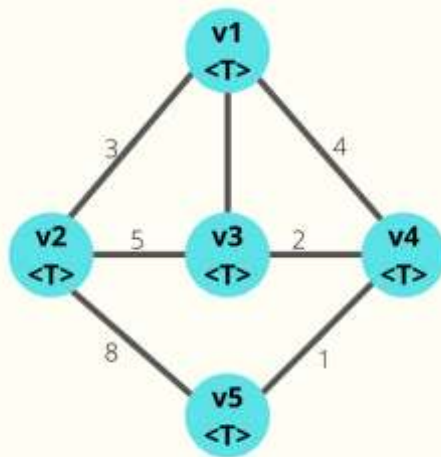
{post: g= {v1, v2, .. vn } n <= Vertices }



## floydWarshall(graph)

“Returns a matrix with the lowest weight between all the vertices”

{pre: graph = {Directed = directed, Weighted = TRUE, Vertices = vertices, Edge = edges}  $\wedge$  graph is united}



	v1	v2	v3	v4	v5
v1	0	3	1	4	$\infty$
v2	3	0	5	$\infty$	8
v3	1	5	0	2	$\infty$
v4	4	$\infty$	2	0	1
v5	$\infty$	8	$\infty$	1	0

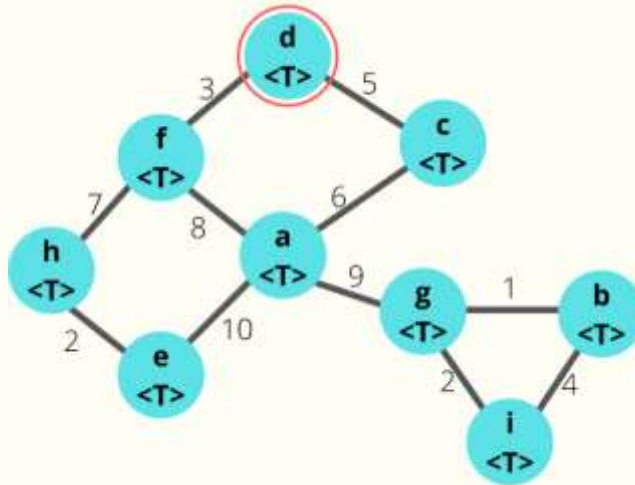
{post: the matrix with the lowest weight between all the vertices of graph }

	v1	v2	v3	v4	v5
v1	0	3	1	3	4
v2	3	0	4	6	7
v3	1	4	0	2	3
v4	3	6	2	0	1
v5	4	7	3	1	0

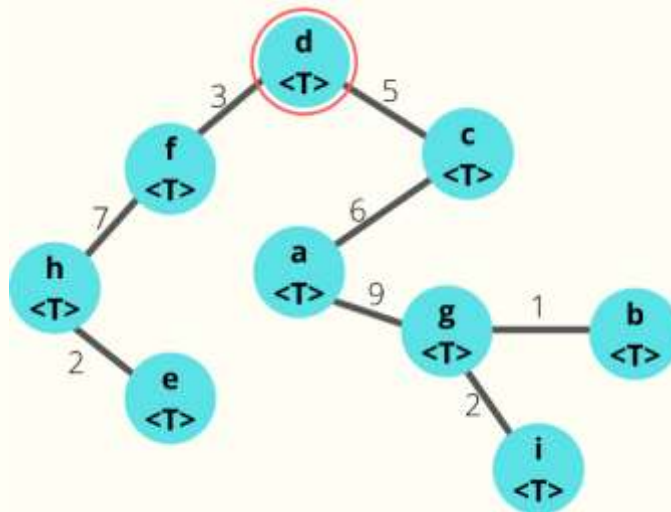
**prim(graph, vertex)**

“Returns the minimum spanning tree (MST) of graph, with root in vertex”

{pre: graph = {Directed = directed, Weighted = TRUE, Vertices = vertices, Edge = edges}  
     $\wedge$  vertex  $\in$  graph  $\wedge$  graph is united }



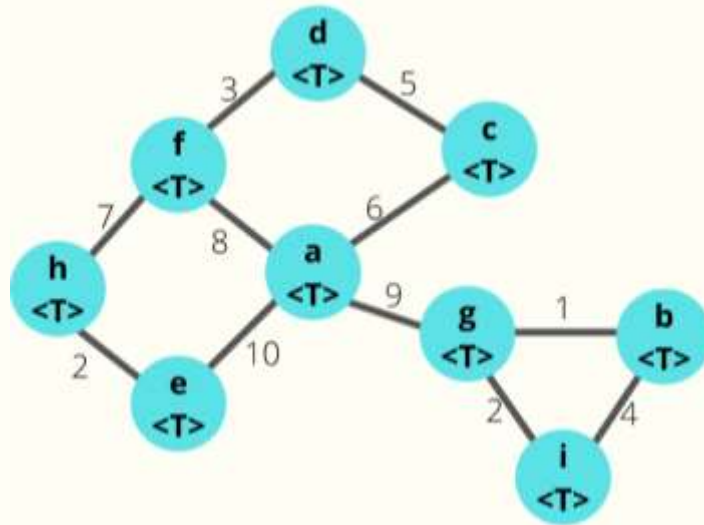
{post: new Graph = {Directed = TRUE, Weighted = TRUE, Vertices = vertices, Edge = vertices-1} }



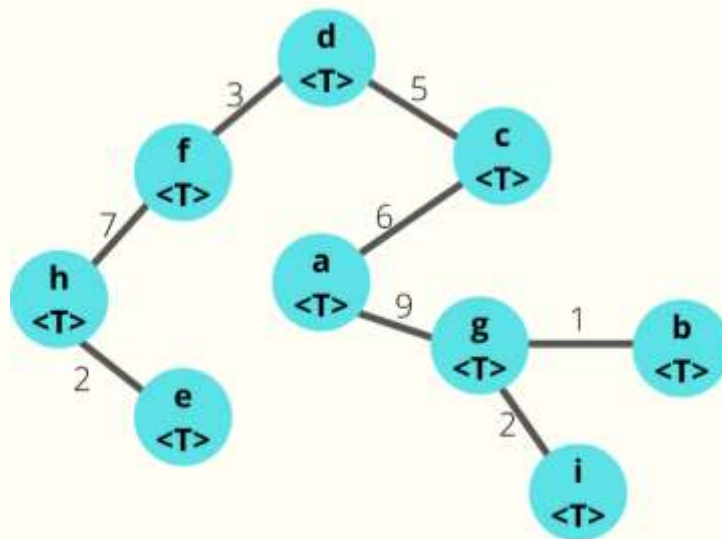
## kruskal(graph)

“Returns the minimum spanning tree (MST) of graph”

{pre: graph = {Directed = directed, Weighted = TRUE, Vertices = vertices, Edge = edges}  $\wedge$  graph is united}



{post: new Graph = {Directed = TRUE, Weighted = TRUE, Vertices = vertices, Edge = vertices-1} }



### **searchVertex(graph, object)**

“Returns the vertex that contains the object in the graph”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges}  $\wedge$  object  $\in T$  }

{post: vertex = {.., Value = object, ... }  $\in$  graph if it isn't in the graph returns null }

### **getEdges(graph)**

“Returns a collection with the edges of the graph”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges} }

{post: {E1, E2, E3, ..., En } n = Edges  $\wedge \forall i \forall j / 1 \leq i, j \leq \text{vertices} \rightarrow \{v_i, v_j\} \in \text{Edges of graph} \}$  }

### **getContexts(graph)**

“Returns a collection with the T type elements of the graph that represents the vertex”

{pre: graph = {Directed = directed, Weighted = weighted, Vertices = vertices, Edge = edges} }

{post: {E1, E2, ..., En } n = Vertices  $\wedge \forall i / 1 \leq i \leq \text{Edges} \rightarrow \exists j / 1 \leq j \leq \text{Vertices} v_j = \{.., \text{Value} = E_i, ... \}$   
 $\wedge v_j \in \text{Vertex} \langle T \rangle \wedge v_j \in \text{graph} \}$  }