

Purpose of the lab:

Write your own arcsin, arccos, arctan, log functions to compare the result in <math.h>. We need to check the comparison results and analyze it to the writeup.pdf at the end.

Command-line option:

- a run all tests compare with <math.h>
- s only runs arcsin and compares with <math.h>'s arcsin
- c only runs arccos and compares with <math.h>'s arccos
- t only runs arctan and compares with <math.h>'s arctan
- l -t only runs log and compares with <math.h>'s log

Files:

Mathlib.c: define arcos, arccos, arctan, exp, and log functions

Mathlib-test.c: the main function, create command-line options and print out results comparison between math.h and mathlib.c functions.

Pesudocode:(x represents input)**Arcsin:**

few terms, then we get:

$$\arcsin(x) = x + \left(\frac{1}{2}\right) \frac{x^3}{3} + \left(\frac{1 \times 3}{2 \times 4}\right) \frac{x^5}{5} + \left(\frac{1 \times 3 \times 5}{2 \times 4 \times 6}\right) \frac{x^7}{7} + O(x^9).$$

Calculate the numerator and denominator for each term, and add it up:

Numerator = x, denominator = 1, sum = x, term = x, power = 3, count = 0

When power is smaller than EPSILON, power +=2{

Count = count + 1

int n = 1

int d = 2

for(int i = 1; i < count; i++){

n *= (n + 2)

d *= (n + 2)

}this part find (1x3x5x7...../ 2x4x6x8.....) for each term

numerator *= x * x * n

denominator = power * d

term = numerator / denominator

sum += numerator / denominator

Return sum

}

Arccos:

$\arcsin(M_{\pi}/2 - \arcsin(x))$

Arctan:

Variable = squareroot of (x square + 1)

$\arcsin(x/\text{variable})$

Log:

Create Exp function first:

```
double Exp(double x) {
    double term = 1, sum = 1;
    for (int k = 1; Abs(term) > EPSILON; k += 1) {
        term *= x / k;
        sum += term;
    }
    return sum;
}
```

a = 1

b = Exp(a)

while (Abs(b - x) > EPSILON) {

 a = a + (x - b) / b

 b = Exp(a)

}

return a

Update:

Rewrote arcsin formula ($a * (\text{pow}(2*i-1, 2) * \text{pow}(x,1) / (2*i)*(2*i+1))$)

And then add up all terms until last term > Epsilon

However, when $\frac{3}{4}$ and $-\frac{3}{4}$, the difference got bigger, so I created inverse method:

Create for loop when find $\sin(y) = x$, so $\sin(y) - x$ not equal to 0 keep looping:

Split $-\pi$ and π , find the middle, if middle not equal to $\sin(y)$, then resize to left part or right part, and find the new middle and continue the same thing

Until when $a > \text{Epsilon}$, the loop stop