

$$1.a) \quad \{0\}^* \{00\} = \{0^k \mid k \geq 2\}$$

$$\uparrow$$

$$\{\varepsilon, 0, 00, 000, \dots\} \{00\}$$

$$\Sigma = \{0, 1\}$$

$$\varepsilon \in \textcircled{L^*} = \{x_1 \dots x_n \mid n \geq 0, x_i \in L\}$$

$$\emptyset \cdot L = \emptyset$$

$$\emptyset^* = \{\varepsilon\}$$

$$3.a) \quad ((0^*)(00)) \quad R_a = 0^*00$$

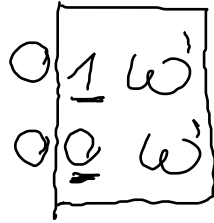
$$\uparrow$$

$$1$$

$$c) \{0\}^* \{1\}^* = \{0^m 1^n \mid m, n \geq 0\} \quad R = 0^* 1^*$$

$$d) \{01, 00\} \{0, 1\}^* = \{0w \mid w \in \Sigma^*, |w| \geq 1\}$$

$$R = (01 + 00) \cdot (0 + 1)^*$$



$$w' \in \Sigma^*$$

$$i) \{0\} \{00\}^* \cup \{1\}^* = \{0^{2k+1} \mid k \geq 0\} \cup \{1^k \mid k \geq 0\}$$

0, 000, ...

$$R = 0(00)^* + 1^*$$

$$j) \{000, 1\}^* \cap \{00, 1\}^* = \{0^{6n_1} 1^{n_2} 0^{6n_3} \dots 1^{n_m} \mid m \geq 0, n_1, n_m \geq 0, n_2, \dots, n_{m-1} \geq 1\}$$

$$\bullet 0^{3k_1} 1^{k_2} 0^{3k_3} 1^{k_4} \dots 1^{k_n} \quad k_2, \dots, k_{n-1} \geq 1$$

$$\bullet 0^{2l_1} 1^{l_2} 0^{2l_3} \dots 1^{l_n} \quad k_1, k_n \geq 0, l_i \dots$$

$$R = ((000000)^* 1^*)^*$$

$$2. a) A = \{0, 1\}^* \{1\} \{0, 1\}^* \neq \{0, 1\}^* \{1\} = B$$

$$\overline{pq} \quad 10 \in A \text{ mas } 10 \notin B$$

$$b) A = \{0\}^* \{00\} = \{00, 0000\}^* \setminus \{\epsilon\} = B$$

$$A = \{0^k \mid k \geq 2\}$$

00, 000, 0000, 00000, 000000, ...

~~0~~, ~~00~~

~~00~~ ~~000~~

00, 000, 0000,

$$B = A \quad \overline{pq} \quad 0, \epsilon \notin B \text{ e}$$

\overline{pq} seq. de 2 ou mais 0's pode
ser formada concatenando pal. de
2 ou 3 0's.

$$c) A = (\underbrace{\{0\}^* \{00\}^*}_{1 \notin A})^* \neq \{0, 1\}^* = B$$

c

0 ✓

$$A \neq B$$

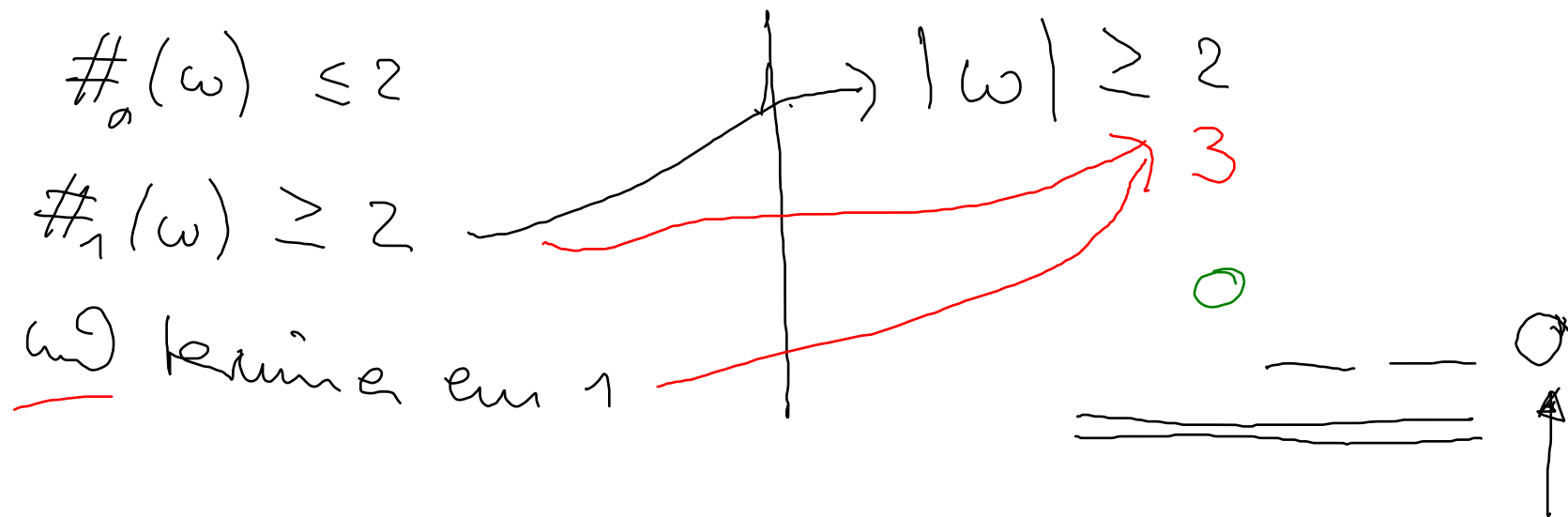
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pg $1 \in B$ was $1 \notin A$.

$$4. a) R = 1^* 0 1^* + 1^* 0 1^* 0 1^* + 1^* 0 1^* 0 1^* 0 1^* + 1^*$$

$$b) R = (0+1)^* 0 0 (0+1)^* 1 1 (0+1)^* + (0+1)^* 1 1 (0+1)^* 0 0 (0+1)^*$$

$$c) R = 1^* 1 1 0 + 1 1 1^* 0 0 + 1 1^* 0 1 0 + 1^* 0 1 1 0$$

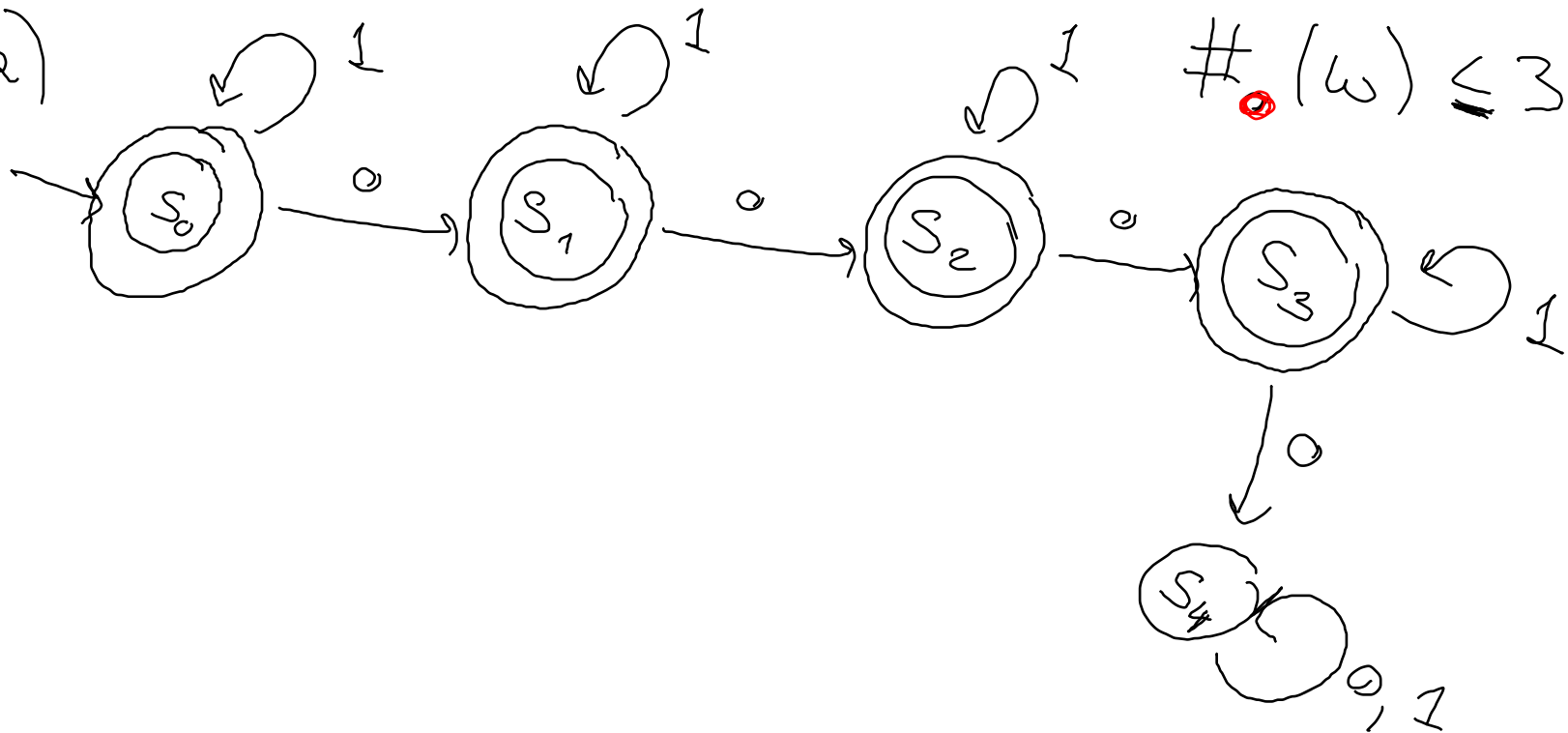


~~zero 0's~~

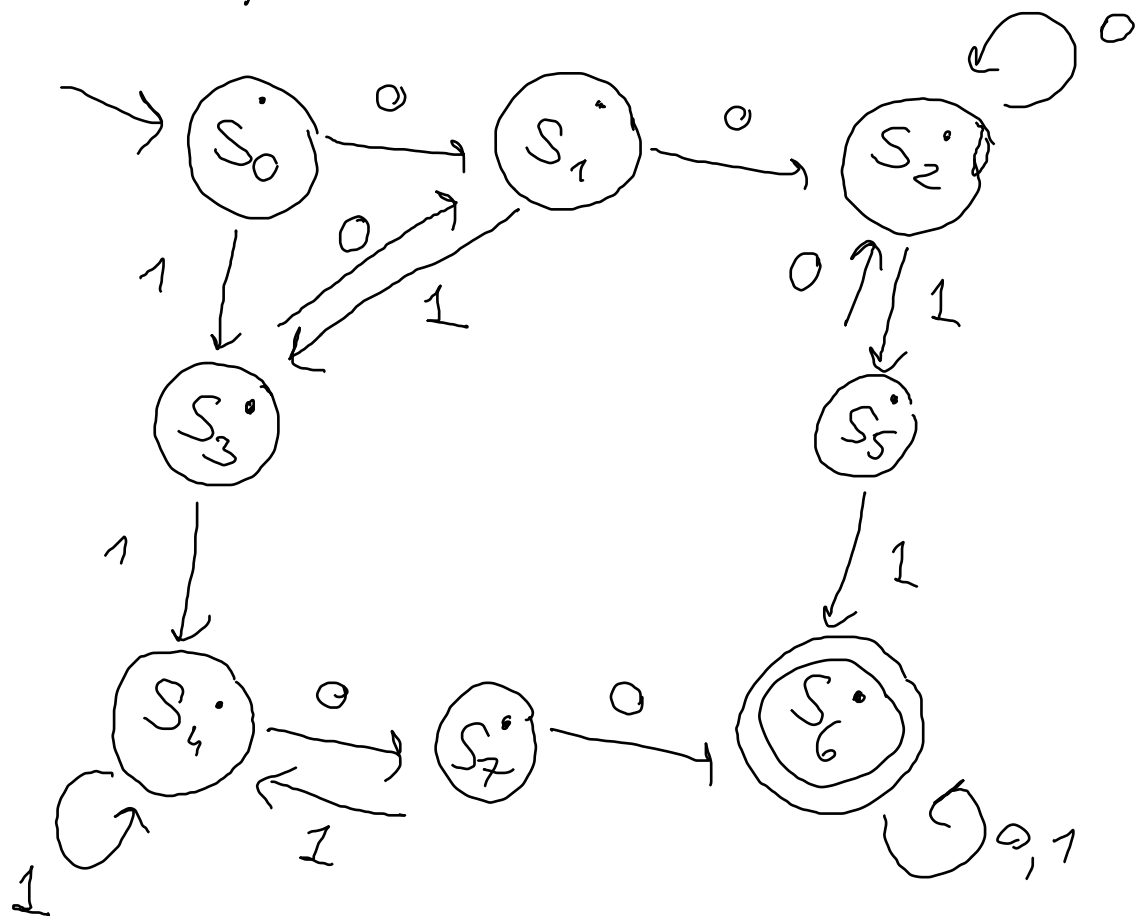
→ um 0 ✓

dois 0's

5.2)



5.6)



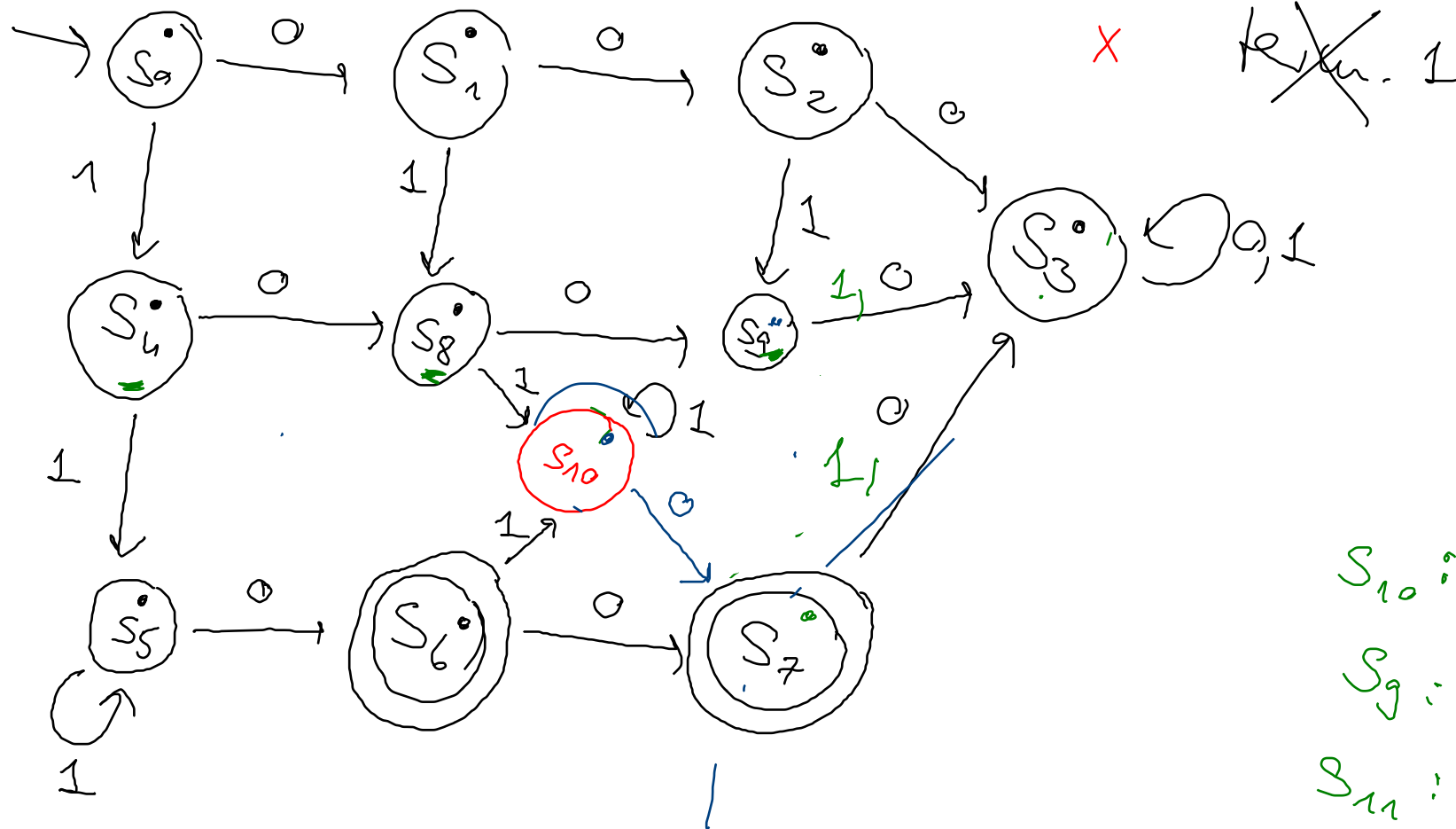
• 00
11 •

5.d)

$S_0: (0^s, 0^s, \text{cond } 3)$
 $S_1: (1, 0, \text{true})$

$$\checkmark : \#_o(\omega) \leq 2$$

✓ $\#_1(\omega) \geq 2$ ✗


$$S_{10}: \#_0 = 1 \wedge \#_1 \geq 2 \wedge be_1$$

$$S_9: \#_0 = 2 \wedge \#_1 = 1 \wedge be_1$$

$$S_{11}: \#_0 = 2 \wedge \#_1 \geq 2 \wedge be_1$$