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Coefficientes Binomiais

$$01) \binom{8}{3} = \frac{8!}{3!(8-3)!} = \frac{8!}{3!5!} = \frac{8 \cdot 7 \cdot 6 \cdot 5!}{3!5!} = \frac{336}{6} = 56 \quad \text{resposta letra B}$$

$$02) \binom{200}{198} = \frac{200!}{198!(200-198)!} = \frac{200!}{198!2!} = \frac{200 \cdot 199 \cdot 198!}{198! \cdot 2!} = \frac{39800}{2} = 19900 \quad \text{resposta letra A}$$

$$03) \binom{n-1}{2} = \binom{n+1}{4} \quad \frac{(n-1)!}{2!} = \frac{(n+1)!}{4!} \quad \frac{(n-1)!}{2!} = \frac{(n+1)!}{4 \cdot 3 \cdot 2!} \quad \frac{(n-1) \cdot (n+1)}{12!}$$

$$n^2 + n \cdot n - 1 \quad n^2 - 1 \quad n = \sqrt{1} \quad n = 1$$

$$2 = 4 \quad 4 - 2 = 2 \quad V = \{1, 2, 3\} \quad \leftarrow \text{resposta}$$

$$04) \binom{20}{13} + \binom{20}{14} = \frac{\binom{20}{13}}{14} + \frac{\binom{20}{14}}{13} = \frac{(20 \cdot 14) + (20 \cdot 13)}{m \cdot m \cdot 13 \cdot 14}$$

$$\begin{array}{r|l} 14, 13 & 2 \\ 7, 13 & 7 \\ 1, 13 & 13 \\ 1, 1 & 1 \end{array} \quad m \cdot m \cdot c = 2 \cdot 7 \cdot 13 = 182 \quad \left(\frac{280 + 260}{182} \right) = \frac{540}{182} / 25 = \frac{21}{7}$$

resposta letra C

$$05) \frac{(n+1)! - n!}{(n-1)!} = \frac{(n+1)n(n-1)! - n(n-1)!}{(n-1)!} = \frac{n(n-1)!(n+1-1)}{(n-1)!} = n^2$$

$$06.a) \sum_{p=0}^{10} \binom{10}{p} = \binom{10}{0} + \binom{10}{1} + \binom{10}{2} + \binom{10}{3} + \dots + \binom{10}{10} \quad 2^{10} = 1024$$

$$06.b) \sum_{p=0}^9 \binom{10}{p} = \binom{10}{0} + \binom{10}{1} + \binom{10}{2} + \binom{10}{3} + \dots + \binom{10}{9} \quad 2^{10} - \frac{10}{10} = 1024 - 1 = 1023$$

$$06.c) \sum_{p=2}^9 \binom{9}{p} = \binom{9}{2} + \binom{9}{3} + \binom{9}{4} + \binom{9}{5} + \dots + \binom{9}{9} = 2^9 - \frac{9}{0} - \frac{9}{1} = 512 - 1 - 9 = 502$$

$$07) \sum_{k=0}^m \binom{m}{k} = 512 \quad m \cdot m \cdot m \cdot m \quad 512 = 2^9 \quad 2^m \quad \text{resposta}$$

$$m = 9 \quad \text{letra E}$$