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# Introduction

Hello Professor, I mainly wrote this to ensure that my logic was correct for each part of the project. I Chose to leave this in to explain my logic and help you grade

# Evaluation

# Basic Definitions

```
#[derive(Debug)]
#[derive(Clone)]
#[derive(PartialEq)]
pub struct Slot {
    pub value: Pvalue,
    pub lifetime: Lifetime,
}

#[derive(Debug)]
#[derive(PartialEq)]
#[derive(Clone)]
pub struct Store(pub HashMap<Location, Slot>);
```

# Implementing The Store

#### locs\_by\_lifetime

```
pub fn locs_by_lifetime(& self, l:Lifetime) -> Vec<Pvalue>{
    let mut result = Vec::new();
    for locs in self.0.keys(){
    let Some(s) = self.0.get(locs) else {panic!("Impossible")};
    if s.lifetime == 1{
        result.push(Some(Value::Ref(locs.to_string(),Owned::Yes)));
      }}
    return result;}
```

Pretty Simple Function, It just iterates through the keys of the Hashmap and finds all the values with the lifetime 1

#### insert

```
pub fn insert(&mut self, loc:&str, val:Pvalue, l:Lifetime){
    let slot = Slot{value:val, lifetime:l};
    self.0.insert(loc.to_string(),slot);}
```

Again Pretty Self Explanatory, We just insert the location and whatever slot it points to!

#### locate

```
pub fn locate<'a>(&'a self, w: &'a Lval) -> &'a Location {
    let mut current_def = &w.ident;
    for i in 0..w.derefs{

        let Some(slot) = self.0.get(current_def) else {panic!("Impossible")};
        match &slot.value{
            Some(Value::Unit) => {panic!("Impossible");;},
            Some(Value::Int(x)) => {panic!("Impossible");;},
            Some(Value::Ref(loc,owned)) =>{current_def = loc;},
            None =>{panic!("Impossible");}

        }
        return current_def;
}
```

In the paper the Locate Function is defined as the following

$$loc(S, w) =_{w}$$

Because there is very much an abstraction in the paper, I took a lot more liberty and simply followed the path of deference to get to a location

## read

```
pub fn read(&self, x: &Lval) -> &Slot { let loc = self.locate(x); return self.0.get(loc).expect("Impossible");} \operatorname{read}(S,w) = S(\ell_w) \quad \text{where loc}(S,w) = \ell_w
```

I followed this rule pretty literally and just used the locate function to fetch the location from our store

#### write

Once again pretty literal, I fetched the location and remapped it. Exactly as the function is defined

```
drop
```

```
pub fn drop(&mut self, values: Vec<Pvalue>) {
      let mut result = Vec::new();
      for value in values{
            match value {
            Some(Value::Ref(loc,Owned::Yes)) =>{
            let Some(next) = self.0.remove(&loc) else {panic!("Impossible")};;
                  result.push(next.value);}
            Some(Value::Ref(loc,Owned::No)) =>{},
            Some(literal) =>{},
            None =>{}}}
      if result.len() !=0{
      self.drop(result);
            }
}
                                                          drop(S, \xrightarrow{}) = S
                                                  \operatorname{drop}(S, \psi \cup \{v^{\perp}\}) = \operatorname{drop}(S, \psi) \quad \text{if } v^{\perp} \neq \ell^{\bullet}
                                                  \operatorname{drop}(S, \psi \cup \{\ell^{\bullet}\}) = \operatorname{drop}(S - \{\ell \mapsto \langle v^{\perp} \rangle^*\}, \ \psi \cup \{v^{\perp}\}) \quad \text{where } S(\ell) = \langle v^{\perp} \rangle^*
```

Here I recursively deallocated the location with in our store as described in the definition

# eval\_expr

#### Base Cases

```
Expr::Unit =>{return Value::Unit},
    Expr::Int(x)=>{return Value::Int(x.clone())}

Expr::Lv(x, Copyable::Yes)=>{

    let loc = self.store.locate(x);
    let Some( x_slot) = self.store.0.get(loc) else{panic!("Impossible");};
    let Some(ref x_val) = x_slot.value else {panic!("Impossible");};
    return x_val.clone(); }
```

Because the Function is Copyable We can simply return its cloned value!

```
Expr::Lv(x, Copyable::No)=>
Expr::Lv(x, Copyable::No)=>{
   let old_val = self.store.write(x, None)
        .expect("move out of a non-existent slot");
   return old_val; }
```

Because this Lval is not Copyable we must perform a move:

$$\frac{read(S1, w) = \langle v \rangle^m \quad S_2 = write(S_1, w, \bot)}{S_1 B \ w \to S_2 B v}$$

Hence, we simply perform a destructive read and return the value that was in our previous Store

Essentially, according to the rule, we evaluate the expression within our store, choose a fresh storage location and map our value to said location

```
\begin{split} & \texttt{Expr::Borrow(x, mutability)} \\ & \texttt{Expr::Borrow(x, mutability)=>} \{ \\ & \texttt{let place = self.store.locate(x);} \\ & \texttt{return Value::Ref(place.clone(), Owned::No);} \\ & \frac{ \log(S^{\mathbb{I}}, w) = \ell_w}{\langle S \rhd \& [\text{mut}] \, w \longrightarrow S \rhd \ell_w^{\circ} \rangle^l} (\text{R-Borrow}) \end{split}
```

Simply put according to the rule all we have to do is return a reference to the location in our store!

Essentially what this rule is saying is that we need to recursively evaluate each expression in our Store until we get to the last value in which case we drop the current lifetime and return the last value

```
{\tt eval\_stmt}
```

```
Stmt::Assign | Stmt::Assign(lv, expr) =>{ | let val_expr = self.eval_expr(expr,l); | let old_val= self.store.read(lv); | self.store.drop([old_val.value.clone()].to_vec()); | self.store.write(lv, Some(val_expr)); |  \frac{\operatorname{read}(S_1,w) = \langle v_1^{\perp} \rangle^m \quad S_2 = \operatorname{drop}(S_1, \{v_1^{\perp}\}) \quad S_3 = \operatorname{write}(S_2, w, v_2)}{\langle S_1 \rhd w = v_2 \longrightarrow S_3 \rhd \epsilon \rangle^l}
```

For an assignment, we read the old value stored at w then we drop it and write v2 to w

```
Stmt::LetMut
Stmt::LetMut(x, expr) =>{

let val_expr = self.eval_expr(expr,l.clone());
let s = Slot{value:Some(val_expr.clone()), lifetime:l.clone()};
    self.store.0.insert(x.to_string(),s);
},
```

$$\frac{S_2 = S_1[\ell_x \mapsto \langle v \rangle^l]}{\langle S_1 \rhd \mathtt{let} \; \mathtt{mut} \; x = v \longrightarrow S_2 \rhd \epsilon \rangle^l}$$

This one is thankfully simple, we map the location of x to its value within our store. Note I chose to assert  $x = l_x$  for simplicity and because it doesn't change our logic!

# Type Checking Part 1

Simply Put, we Map the Slot into our context

# Basic Definitions

```
#[derive(Debug)]
#[derive(Clone)]
#[derive(PartialEq)]
pub struct Slot {
 pub tipe: Type,
 pub lifetime: Lifetime,
#[derive(Clone)]
#[derive(PartialEq)]
#[derive(Debug)]
pub struct Env(pub HashMap<Ident, Slot>);
Implementing The Environment
insert
    pub fn insert(&mut self, var: &str, tipe: Type, lifetime: Lifetime) {
       let s = Slot{tipe:tipe, lifetime:lifetime};
        self.0.insert(var.to_string(), s);
   }
```

#### type\_lval

```
pub fn type_lval(&self, lval: &Lval) -> TypeResult<Slot> {
       let Some(slot) = self.0.get(&lval.ident) else{return Err(Error::UnknownVar(lval.ident.clone()))};
       let mut current_type = &slot.tipe;
       let mut current lifetime = &slot.lifetime;
       for i in 0..lval.derefs{
           if let Type::Undefined(_) = current_type {
               return Err(Error::MovedOut(lval.clone()));
           }
           match current_type{
           Type::TBox(x)=> {current_type=&*x;}
           Type::Ref(x,y)=>{
               let Some(slot) = self.0.get(&x.ident) else{return Err(Error::UnknownVar(x.ident.clone()))};
               let Some(tipe) = self.contained(&x.ident) else{return Err(Error::UnknownVar(x.ident.clone()))};
                current_type =tipe ;
                current_lifetime= &slot.lifetime;
           x=>{return Err(Error::CannotDeref(x.clone()));}
       let slot = Slot{tipe:current_type.clone(), lifetime:current_lifetime.clone());
       //self.0.insert(lval.ident.clone(), slot);
       return Ok(slot);
```

}

I assumed that this function takes in an Lval, and returns its type. Essentially we walk down the path of deferences, if we find an Undefined then that means that the Lval has already been moved out and we throw an error. Otherwise we return the fully deferenced type within a slot

```
contained
```

```
pub fn contained(&self, var: &Ident) -> Option<&Type> {
  let Some(slot) = self.0.get(var) else {panic!("Impossible")};
  let mut current_type = &slot.tipe;
  loop{
   match current_type{
   Type::TBox(x)=> {current_type=&*x;}
   Type::Undefined(x) =>{return None;}
   x=>{return Some(&x);},
  }
}
return None;
}
```

$$\operatorname{contains}(\Gamma, \widetilde{T}, T_y) = \begin{cases} \operatorname{contains}(\Gamma, \widetilde{T}', T_y) & \text{if } \widetilde{T} = \square \widetilde{T}' \\ \operatorname{true} & \text{if } \widetilde{T} = T_y \\ \operatorname{false} & \text{otherwise} \end{cases}$$

Essentially we recursively go inside each Box until we either arrive at a type or an undefined. If we arrive at an undefined we return None otherwise we return the type

## read\_prohibited

```
pub fn read_prohibited(&self, lval: &Lval) -> bool {
  for vars in self.0.keys(){
    let value = self.contained(vars);
    if let Some(Type::Ref(x, Mutable::Yes)) = value{
        if x.ident==lval.ident{
        return true;
      }
    }}

return false;
}
```

I came up with the following Definition from the Paper:

 $ReadProhibited = \{x | \Gamma \vdash x \leadsto \& mut \ \overline{u} \land \exists (PathConflict(x)) \}$ 

Where a Path conflict is defined as:

$$PathConflict = \{w | \exists x : x \leadsto y \land w \leadsto y\}$$

Essientially if there is a series of deferences between two Lvals that Point to the same variable we have a Path Conflict.

Thus if there is a Path Conflict AND the lval is a mutable reference, then the Lval is read prohibited

```
write_prohibited

pub fn write_prohibited(&self, lval: &Lval) -> bool {
    if self.read_prohibited(lval){
        return true;
    }

for vars in self.0.keys(){
    let value = self.contained(vars);
    if let Some(Type::Ref(x, y)) = value{
        if *x.ident==lval.ident{
            return true;
        }
    }}

    return false;
```

I came up with the following Definition from the Paper:

 $WriteProhibitied\{x|ReadProhibited(x) \lor (x \leadsto \& \overline{y} \land Pathconflict(x))\}$ 

Thus if the Lval is read prohibited OR Path Conflict AND the lval is a reference, then the Lval is Write Prohibited

```
moove
```

```
pub fn moove(&mut self, lval: &Lval) -> TypeResult<()> {
    if self.write_prohibited(lval){
        return Err(Error::MutBorrowAfterBorrow(lval.clone()));}

let Some(current) = self.0.get(&lval.ident) else {return Err(Error::UnknownVar(lval.ident.clone()))};

let result = self.moove_nested(current.tipe.clone(), lval.derefs.clone())?;

if let (tipe) = result{

    let Some(current) = self.0.get(&lval.ident) else {return Err(Error::UnknownVar(lval.ident.clone()))};

    let slot = Slot{tipe:tipe, lifetime:current.lifetime.clone()};

    self.0.insert(lval.ident.clone(), slot);

    return 0k(())

}

return Err(Error::Dummy);
}

\frac{\Gamma_1 \vdash w : \langle T \rangle^m \quad \neg writeProhibited(\Gamma_1, w) \quad \Gamma_2 = move(\Gamma_1, w)}{\Gamma_1 \vdash \langle w : T \rangle_{\sigma}^1 \rhd \Gamma_2}
```

Essentially if the Lval w is write prohibited then we can perform a move. Where a Move is defined as:

$$\frac{read(S1, w) = \langle v \rangle^m \quad S_2 = write(S_1, w, \bot)}{S_1 B \ w \to S_2 B v}$$

Although this is a Sementic Rule, We can infer that we have to walk down the path of dereferences and perform a destructive read in our Lval, like so

```
pub fn moove_nested(&mut self, tipe:Type, i:usize) -> Result<Type, Error> {
   if i ==0{
    return Ok(Type::Undefined(Box::new(tipe)))}

match tipe{

   Type::TBox(x) =>{
   let (rest) = self.moove_nested(*x,i-1)?;

   return Ok(Type::TBox(Box::new(rest)))},
   Type::Ref(lval, _) =>{ return Err(Error::MoveBehindRef(lval.clone()))},
   Type::Undefined(x)=>{return Err(Error::Dummy)},
   x=>{return Err(Error::CannotDeref(x))}
}
```

```
muut
pub fn muut(&self, lval: &Lval) -> bool {
let Some(tipe) = self.contained(&lval.ident) else{return false};
let mut current_type = tipe;
let mut i = lval.derefs;
while i >0{
 match current_type{
 Type::Ref(lv, Mutable::Yes) =>{
  i-=1;
   let Some(tipe) = self.contained(&lv.ident) else {return true;};
   current_type = tipe;},
 Type::Ref(lv, Mutable::No) =>{return false;},
 Type::TBox(x) \Rightarrow{
   current_type= &*x},
 Type::Undefined(x)=>{
   current_type = &*x},
 _ =>{return true;}
return true;
```

```
\begin{split} \operatorname{mutable}(\Gamma,\epsilon\mid\mathbb{T}) &= \operatorname{true} \\ \operatorname{mutable}(\Gamma,(\pi\cdot *)\mid\mathbb{T}) &= \operatorname{mutable}(\Gamma,\pi\mid\mathbb{T}) \\ \operatorname{mutable}(\Gamma,(\pi\cdot *)\mid \& \operatorname{mut} w) &= \bigwedge_{i} \operatorname{mut}(\Gamma,\pi\cdot w_{i}) \end{split}
```

All we have to do is recursively go down our path of derefences until we hit a mutable reference. If we don't hit one, then we simply return false

#### compatible

```
pub fn compatible(&self, t1: &Type, t2: &Type) -> bool {

    match (t1,t2){
        (Type::Int, Type::Int) => {return true;},
        (Type::Unit, Type::Unit) => {return true;},
        (Type::TBox(x), Type::TBox(y))=>{self.compatible(x,y)},
        (Type::Ref(x,Mutable::Yes), Type::Ref(y, Mutable::Yes))=>{return true;},
        (Type::Ref(x,Mutable::No), Type::Ref(y, Mutable::No))=>{return true;},
        (Type::Undefined(x), y) =>{self.compatible(x, y)},
        (y,Type::Undefined(x)) =>{self.compatible(x, y)},
        _=>{return false;}
}
```

Although I could not find a compatibility rule within our paper, I went ahead and assumed that two types are compatible if they have the same nested definition

```
write and update
    pub fn write(&mut self, w: &Lval, tipe: Type) -> TypeResult<()> {
        //self.0.insert(&w.ident, tipe);
        let current = self.0.remove(&w.ident)
             .ok_or(Error::UnknownVar(w.ident.clone()))?;
         let (rest) = self.update(current.tipe.clone(), tipe, w.derefs.try_into().unwrap())?;
        let slot = Slot{tipe:rest, lifetime:current.lifetime.clone()};
        self.0.insert(w.ident.clone(), slot);
        Ok(())
    }
We simply get the type of our lval here ,the real magic happens in our update function
pub fn update(&mut self, old: Type, new: Type, i: i32) -> Result<Type, Error>{
 if i ==0{
    return Ok(new);
 match old{
 Type::TBox(x) \Rightarrow{
 let (replaced) = self.update(*x,new,i-1)?;
 return Ok(Type::TBox(Box::new(replaced)))
   },
```

```
Type::Ref(lv, Mutable::Yes) =>{
    self.write(&lv, new.clone())?;

Ok(Type::Ref(lv,Mutable::Yes))
},

Type::Ref(lv, Mutable::No) =>{
    return Err(Error::UpdateBehindImmRef(lv.clone()));
},

Type::Undefined(x)=>{

let (replaced)= self.update(*x,new,i-1)?;
    return Ok(Type::Undefined(Box::new(replaced)))
}

x=>{Ok(new)}}
```

According to rule in the Final Project Landing Page:

$$\begin{aligned} \operatorname{update}(\Gamma, \epsilon, \tau_1, \tau_2) &= (\Gamma, \tau_2), \\ \operatorname{update}(\Gamma, *\pi, \Box \tau_1, \tau_2) &= (\Gamma', \Box \tau_1') & \text{where } (\Gamma', \tau_1') &= \operatorname{update}(\Gamma, \pi, \tau_1, \tau_2), \\ \operatorname{update}(\Gamma, *\pi, \& \operatorname{mut} u, \tau_2) &= (\Gamma', \& \operatorname{mut} u) & \text{where } \Gamma' &= \operatorname{write}(\Gamma, \pi u, \tau_2), \\ \operatorname{write}(\Gamma, w, \tau) &= \Gamma' \big[ x \mapsto \langle \sigma' \rangle^l \big] \\ \operatorname{where} w &= \pi \mid x, \ \Gamma(x) = \langle \sigma \rangle^l, \ (\Gamma', \sigma') &= \operatorname{update}(\Gamma, \pi, \sigma, \tau). \end{aligned}$$

We Recursively walk down the path of each Lval, if we encounter another Lval along the way we nest our selves deeper into the mix, Although The rule doesn't mention immutable references. I decided that it was appropriate to throw an error if we come across an immutable reference. Since we cannot write to an immutable reference

```
drop
pub fn drop(&mut self, l: Lifetime) {
  let mut to_drop = Vec::new();
  for value in self.0.keys(){
  let Some(slot) = self.0.get(value) else{panic!("Impossible");};
  if slot.lifetime==1{
  to_drop.push(value.clone());}}
  for value in to_drop{
    self.0.remove(&value);
  }}}
```

This is essentially the same definition as our semantic one with only slight modifications

$$drop(S, \stackrel{\rightarrow}{\rightarrow}) = S$$
 
$$drop(S, \psi \cup \{v^{\perp}\}) = drop(S, \psi) \quad \text{if } v^{\perp} \neq \ell^{\bullet}$$
 
$$drop(S, \psi \cup \{\ell^{\bullet}\}) = drop(S - \{\ell \mapsto \langle v^{\perp} \rangle^{*}\}, \ \psi \cup \{v^{\perp}\}) \quad \text{where } S(\ell) = \langle v^{\perp} \rangle^{*}$$

The only deference now being we are dropping by lifetime not by the lval thus we iterate over each value in our environment and if it matches the given life time we remove it from our environment!

# Type Checking Part 2

# **Basic Definitions**

```
#[derive(PartialEq)]
#[derive(Debug)]
   pub enum Error {
    Dummy,
    UnknownVar(String),
    CannotDeref(Type),
    MovedOut(Lval),
    MoveBehindRef(Lval),
    UpdateBehindImmRef(Lval),
    CopyAfterMutBorrow(Lval),
    MoveAfterBorrow(Lval),
    MutBorrowBehindImmRef(Lval),
    MutBorrowAfterBorrow(Lval),
    BorrowAfterMutBorrow(Lval),
    Shadowing(String),
    IncompatibleTypes(Type, Type),
    LifetimeTooShort(Expr),
    AssignAfterBorrow(Lval),
}
type TypeResult<T> = Result<T, Error>;
#[derive(Debug)]
#[derive(PartialEq)]
#[derive(Clone)]
```

```
pub struct Context {
    pub env: Env,
    // TODO: anything else you need
}
```

# Implementing the Context

```
well_formed
pub fn well_formed(&self, tipe: &Type, 1: Lifetime) -> bool {
    match tipe{
    Type::Unit=>{true},
    Type::Int=>{true},
    Type::TBox(x)=> {self.well_formed(x,1)},
    Type::Ref(lv, Mutable)=>{
    let Some(slot) = self.env.0.get(&lv.ident) else{return false};
    self.lifetime_contains(slot.lifetime.clone(), 1)}
    Type::Undefined(x)=>{return false;}
}
}
```

We know that a type is well formed if it respects the following rules :

This is an axiom, an int always lives as long as a given lifetime

$$\frac{\Gamma \vdash \operatorname{int} \geq l}{\Gamma \vdash \operatorname{int} \geq l} \quad \text{(L-Int)}$$
 
$$\frac{\Gamma \vdash u : \langle T \rangle^m \quad m \geq l}{\Gamma \vdash \&[\operatorname{mut}] \ u \geq l} \quad \text{(L-Borrow)}$$
 
$$\frac{\Gamma \vdash T \geq l}{\Gamma \vdash \Box \ T \geq l} \quad \text{(L-Box)}$$

For an Undefined, I decided that it would be appropriate to always return false, since we essentially are 'pretending' that the type no longer exists

# type\_expr Base Cases: Expr::Unit => Ok(Type::Unit), Expr::Int(\_) => Ok(Type::Int), Expr::Lv(x, Copyable::Yes)=> Expr::Lv(lv, Copyable::Yes) => { let slot = self.env.type\_lval(lv)?; Ok(slot.tipe) } Because the function is Copyable, there is really not much to check

```
Expr::Lv(x, Copyable::No)=>
Expr::Lv(lv, Copyable::No) => {
let slot = self.env.type_lval(lv)?;
let ty = slot.tipe.clone();
let contained = self.env.contained(&lv.ident);
 if None== contained {
  return Err(Error::MovedOut(lv.clone()));
if let Some(Type::Ref(x, _)) = contained{
 return Err(Error::MoveBehindRef(lv.clone()));}
if Self::is_copyable(&ty) {
 if self.env.read_prohibited(lv) {
  return Err(Error::CopyAfterMutBorrow(lv.clone()));
 *expr = Expr::Lv(lv.clone(), Copyable::Yes);
 return Ok(ty);
if self.env.write_prohibited(lv) {
   return Err(Error::MoveAfterBorrow(lv.clone()));
```

```
}
self.env.moove(lv)?;
Ok(ty)
}
```

Because this Lval is not Copyable we must perform a move:

T-Move

$$\frac{\Gamma_1 \vdash w : \langle T \rangle^m \quad \neg \text{writeProhibited}(\Gamma_1, w) \quad \Gamma_2 = \text{move}(\Gamma_1, w)}{\Gamma_1 \vdash \langle w : T \rangle_\sigma^1 \rhd \Gamma_2}$$

Here we ensure many more things one is that the lval is not write prohibited, we have to ensure that it has not already been moved out, that we are not moving behind a reference and finally that the inner type is indeed copyable and not Not Write prohibited

```
\begin{split} & \texttt{Expr::Borrow(x, Mutable::Yes)} \\ & \texttt{Expr::Borrow(lv, Mutable::Yes)} = > \{\\ & \texttt{let slot} = \texttt{self.env.type\_lval(lv)?};\\ & \texttt{let ty} = \texttt{slot.tipe.clone()};\\ & \texttt{let contained} = \texttt{self.env.contained(\&lv.ident);}\\ & \texttt{if self.env.write\_prohibited(lv)} \left\{\\ & \texttt{return Err(Error::MutBorrowAfterBorrow(lv.clone()));} \right\}\\ & \texttt{if None== contained} \left\{\\ & \texttt{return Err(Error::MovedOut(lv.clone()));} \right\}\\ & \texttt{if !self.env.muut(lv)} \left\{\\ & \texttt{return Err(Error::MutBorrowBehindImmRef(lv.clone()));} \right\}\\ & \texttt{Ok(Type::Ref(lv.clone(), Mutable::Yes))} \\ & \\ & \frac{\Gamma \vdash w : \langle T \rangle^m \quad \text{mut}(\Gamma_1, w) \quad \neg \text{writeProhibited}(\Gamma, w)}{\Gamma \vdash \langle \& \text{mut } w : \& \text{mut } w \rangle_{\sigma}^d \rhd \Gamma} (\text{T-MutBorrow}) \end{split}
```

We have to ensure that the value is not write prohibited, that it has not already been moved out AND that the inner reference is not immutable

```
\begin{split} & \operatorname{Expr::Borrow}(x, \operatorname{Mutable::No}) = \\ & \operatorname{Expr::Borrow}(\operatorname{lv}, \operatorname{Mutable::No}) = > \{ \\ & \operatorname{let} \ \operatorname{slot} = \operatorname{self.env.type\_lval}(\operatorname{lv})?; \\ & \operatorname{let} \ \operatorname{contained} = \operatorname{self.env.contained}(\&\operatorname{lv.ident}); \\ & \operatorname{let} \ \operatorname{ty} = \operatorname{slot.tipe.clone}(); \\ & \operatorname{if} \ \operatorname{self.env.read\_prohibited}(\operatorname{lv}) \ \{ \\ & \operatorname{return} \ \operatorname{Err}(\operatorname{Error}::\operatorname{BorrowAfterMutBorrow}(\operatorname{lv.clone}())); \\ & \} \\ & \operatorname{if} \ \operatorname{None==} \ \operatorname{contained} \ \{ \\ & \operatorname{return} \ \operatorname{Err}(\operatorname{Error}::\operatorname{MovedOut}(\operatorname{lv.clone}())); \\ & \} \\ & \operatorname{Ok}(\operatorname{Type}::\operatorname{Ref}(\operatorname{lv.clone}(), \operatorname{Mutable}::\operatorname{No})) \\ & \} \\ & \\ & \frac{\Gamma \vdash w : \langle T \rangle^m \quad \neg \operatorname{readProhibited}(\Gamma, w)}{\Gamma \vdash \langle \&w : \&w \rangle_\sigma^1 \rhd \Gamma} (\operatorname{T-ImmBorrow}) \end{split}
```

We have to ensure that the value is not read prohibited AND that it has not already been moved out

```
Expr:: OBox(e1)

Expr::OBox(e) => {
    let inner_type = self.type_expr(e)?;
    Ok(Type::TBox(Box::new(inner_type)))
}

\frac{\Gamma_1 \vdash \langle t:T \rangle_{\sigma}^l \triangleright \Gamma_2}{\Gamma_1 \vdash \langle \text{box } t: \Box T \rangle_{\sigma}^l \triangleright \Gamma_2}
```

Essentially, according to the rule, we evaluate the type within our Box

```
Expr::Block(statements, e1, 11)

Expr::Block(stmts, result_expr, lifetime) => {
  for stmt in stmts {
    self.type_stmt(stmt)?;
    if let Stmt::LetMut(x, _) = stmt{
        let Some(ty_of) = self.env.0.get(x) else {panic!("Impossible");};
        let slot = Slot{tipe:ty_of.tipe.clone(), lifetime:lifetime.clone()};
        self.env.0.insert(x.to_string(), slot);}

if let Stmt::Assign(lv, expr) = stmt{
    let slot = self.env.type_lval(&lv)?;
    if slot.lifetime < *lifetime{
        return Err(Error::LifetimeTooShort(expr.clone()));
    }
    }
}

let t = self.type_expr(result_expr)?;

self.env.drop(lifetime.clone());
Ok(t)</pre>
```

Unfortunately Due to the Structure of the Code we Need to Employ Some Work arounds, however the Type Checking for each block remains the same

$$\frac{\Gamma_1 \vdash \langle t : T \rangle_{\sigma}^m \triangleright \Gamma_2 \quad \Gamma_2 \vdash T \ge l \quad \Gamma_3 = \operatorname{drop}(\Gamma_2, m)}{\Gamma_1 \vdash \langle \{t\}^m : T \rangle_{\sigma}^l \triangleright \Gamma_3}$$

We type-check each expression within our block and then drop the lifetime. One of the Main differences is the 'sub evaluation' of the Let Rule:

$$\frac{x \notin \mathrm{dom}(\Gamma_1) \quad \Gamma_1 \vdash \langle t : T \rangle_\sigma^1 \triangleright \Gamma_2 \quad \Gamma_3 = \Gamma_2[x \mapsto \langle T \rangle^1]}{\Gamma_1 \vdash \langle \mathsf{let mut} \ x = t : \epsilon \rangle_\sigma^1 \triangleright \Gamma_3} (\mathsf{T\text{-}Declare})$$

Because our type\_stmt does not take in a life time parameter, each time we encounter a LetMut in our block, we manually have to go back and set the lifetime after calling type\_stmt

We also have to ensure that any time that we assign in our block that the lifetime of the assigned lval is greater than or equal to the lifetime of our hole block. Since otherwise the lval would not live until the entire execution of our program

```
type_stmt
Stmt::Assign
Stmt::Assign(lv, expr) =>{
let old_type = self.env.type_lval(lv)?;
println!("{:?}",old_type);
let new_type = self.type_expr(expr)?;
if !self.env.compatible(&new_type,&old_type.tipe){
  return Err(Error::IncompatibleTypes(old_type.tipe, new_type)); }
else if self.env.write_prohibited(lv){
  return Err(Error::AssignAfterBorrow(lv.clone()));}
self.env.write(lv, new_type)?;
return Ok(());
```

$$\frac{\Gamma_1 \vdash w : \langle \widetilde{T}_1 \rangle^m \quad \Gamma_1 \vdash \langle t : T_2 \rangle^1_{\sigma} \triangleright \Gamma_2 \quad \Gamma_2 \vdash \widetilde{T}_1 \approx T_2 \quad \Gamma_2 \vdash T_2 \succeq m \quad \Gamma_3 = \text{write}^{\theta}(\Gamma_2, w, T_2) \quad \neg \text{writeProhibited}(\Gamma_3, w)}{\Gamma_1 \vdash \langle w = t : \epsilon \rangle^1_{\sigma} \triangleright \Gamma_3} (\text{T-Assign})$$

For assignments we have to ensure several things, we first use the context to get the old type then we evaluate the new type. Then we have to ensure that the new type  $T_2$  and the old type  $T_1$  are compatible, we also have to ensure that the lifetime of the new old type  $T_2$  as a long as the lifetime of our new type (we perform this check within type\_expr) and finally we ensure that our lval is not write prohibited. If all conditions are met, we can write to our context ####

```
Stmt::LetMut(x, expr) =>{
  if self.env.0.contains_key(x) {
    return Err(Error::Shadowing(x.to_string()));}

let new_type = self.type_expr(expr)?;
  self.env.insert(x,new_type, Lifetime::global());
```

$$\frac{x \notin \mathrm{dom}(\Gamma_1) \quad \Gamma_1 \vdash \langle t : T \rangle_{\sigma}^1 \rhd \Gamma_2 \quad \Gamma_3 = \Gamma_2[x \mapsto \langle T \rangle^1]}{\Gamma_1 \vdash \langle \mathsf{let} \ \mathsf{mut} \ x = t : \epsilon \rangle_{\sigma}^1 \rhd \Gamma_3} (\mathsf{T\text{-}Declare})$$

We have to ensure that the variable x is fresh, denoted by  $x \notin dom(\Gamma_1)$ , then we evaluate the expression within x and map it within our context!

# Lexicalization

Admittedly my least favorite part of the project. I simply dislike string processing.

# Basic Definitions

```
use std::str::Lines;
#[derive(Clone)]
#[derive(Debug)]
#[derive(PartialEq)]
pub enum Token {
    Lparen,
    Rparen,
    Lbracket,
    Rbracket,
    Εq,
    Ampersand,
    Star,
    Comma,
    Semicolon,
    Fn,
    Let,
    Mut,
    Box,
   Int(i32),
    Var(String),
```

```
pub struct Lexer<'a> {
    contents: Lines<'a>,
    curr_line_num: usize,
    curr_col_num: usize,
    curr_line: &'a str,
const LEXEMES : [(&str, Token); 13] = [
    ("(", Token::Lparen),
    (")", Token::Rparen),
    ("{", Token::Lbracket),
    ("}", Token::Rbracket),
    ("=", Token::Eq),
    ("&", Token::Ampersand),
    ("*", Token::Star),
    (",", Token::Comma),
    (";", Token::Semicolon),
    ("fn", Token::Fn),
    ("let", Token::Let),
    ("mut", Token::Mut),
    ("Box::new", Token::Box),
];
#[derive(Debug)]
pub enum Error {
    Unknown(usize, usize),
```

```
type LexResult = Result<Token, Error>;

variable

fn variable(&mut self) -> LexResult {
  let mut len =0;
  for character in self.curr_line.chars(){
    if character.is_ascii_alphanumeric() || character == '_' {
      len += 1;
    } else {
      break;
    }
  }
  if len ==0{
    return Err(self.unknown());
    }
  let var = &self.curr_line[..len];
  self.consume(len);
  return Ok(Token::Var(var.to_string()));
```

Essentially we loop through each character in our current line, if we do not encounter a white space we simply add to len and slice it then consume that part of the current line.

```
int
fn int(&mut self) -> LexResult {
let mut len =0;
 for character in self.curr_line.chars(){
 if character.is_ascii_digit(){
     len+=1;
   }
  else{
     break;
    }
 if len ==0{
    return Err(self.unknown());
 let var = &self.curr_line[..len];
 let v = var.parse::<i32>().unwrap();
  self.consume(len);
 return Ok(Token::Int(v));
  }
```

Same idea as before, only difference is that we break is we see something that isn't a digit!

# skip\_whitespace fn skip\_whitespace(&mut self){ loop{ if self.curr\_line.is\_empty() || self.curr\_line.starts\_with("//"){ let Some(temp) = self.contents.next() else {return}; self.curr\_line= temp; self.curr\_line\_num += 1; self.curr\_col\_num = 1; continue; } let Some(ch) = self.curr\_line.chars().next() else{return;}; if ch.is\_whitespace(){ self.consume(1);} else { break; } } }

This is a function I incorporated that simply skips white spaces and and empty lines!

# Parsing

```
parse block
pub fn parse_block(&mut self) -> ParseResult<Expr> {
eprintln!("[parse_block] entering block parse");
self.next_token_match(Token::Lbracket)?;
let mut statements = Vec::new();
while *self.peek_token()? != Token::Rbracket {
 eprintln!("[parse_block] parsing statement, peek: {:?}", self.peek_token());
 let temp = self.parse_stmt()?;
 eprintln!("[parse_block] parsed statement: {:?}", temp);
 statements.push(temp);
eprintln!("[parse_block] parsing tail expression");
if let (Stmt::Expr(last)) = &statements[statements.len()-1]{
 let Some(Stmt::Expr(last)) = statements.pop() else {panic!("Impossible");};
 self.next_token_match(Token::Rbracket)?;
 eprintln!("[parse_block] exiting block parse");
 self.new_lifetime();
 return Ok(Expr::Block(statements, Box::new(last), Lifetime(self.lifetime)));
//All Functions return Unit;
self.next_token_match(Token::Rbracket)?;
eprintln!("[parse_block] exiting block parse");
```

```
self.new_lifetime();
return Ok(Expr::Block(statements, Box::new(Expr::Unit), Lifetime(self.lifetime)));
}
```

A block is essentially a scope, Thus we loop through our code and we keep calling parse\_stmt until we see a }. In which case we break out of the while loop and we check the last item within our vector of 'statements' to see if it is a expression or a statement. If it is a 'expression', we assign it to be the last expression within our Block, otherwise we assign a Unit to be the last expression within our block. (Since if a function does not return an explicit value it will always return a Unit). Any time we return a block, we must ensure a new unique lifetime, hence we call our self.new\_lifetime function to ensure this!

# parse\_box

```
fn parse_box(&mut self) -> ParseResult<Expr> {
  eprintln!("[parse_box] parsing box expression");
  self.next_token_match(Token::Box)?;
  self.next_token_match(Token::Lparen)?;
  let e = self.parse_expr()?;
  self.next_token_match(Token::Rparen)?;
  eprintln!("[parse_box] parsed inner expr: {:?}", e);
  Ok(Expr::OBox(Box::new(e)))
}
```

This one is Pretty simple, essentially we check if the first Token is a Box and the very next token is a ) if so, we parse the inner expression and ensure that the last token is a ) then we simply return the expression!

# parse\_stmt

```
Token::Star | Token::Var(_)
Token::Star | Token::Var(_) => {
  eprintln!("[parse_stmt] star found");
  let lv = self.parse_lval()?;
  if *self.peek_token()? == Token::Eq {
    eprintln!("[parse_stmt] assignment detected");
    self.next_token()?;
  let next_expr = self.parse_expr()?;
  self.next_token_match(Token::Semicolon)?;
```

```
Stmt::Assign(lv, next_expr)
} else {
  self.next_token_match(Token::Semicolon)?;
  Stmt::Expr(Expr::Lv(lv, Copyable::No))
}
```

Whether we have a \* or a Var(x) we know we are dealing with an lval, thus we call our parse\_lval() function. If the very next token is a "=" then we know we have an assignment in which case we parse the very next thing after the equal sign by calling self.parse\_expr(). If we do not see an equal sign then we know we are dealing with a simple lval in which case we return it and assign it to not be copy-able.

```
Token::Let => {
  eprintln!("[parse_stmt] let found");
  self.next_token()?;
  self.next_token_match(Token::Mut)?;
  let var = self.next_token_var()?;
  self.next_token_match(Token::Eq)?;
  let next_expr = self.parse_expr()?;
  self.next_token_match(Token::Semicolon)?;
  Stmt::LetMut(var, next_expr)
},
```

When we encounter a Let, we assert that the next token is a mut (I do this because we did not define not mutable declarations within our spec nor did I see a definition within the paper). Afterwards we assert that we see a variable next. Then we parse the inner expressions by calling self.parse\_expr()

# Else Case \_ => { eprintln!("[parse\_stmt] fallback expr stmt"); let next\_expr = self.parse\_expr()?; self.next\_token\_match(Token::Semicolon)?;

Stmt::Expr(next\_expr)

If we do not see any of the previous cases then we know we are dealing with a expression not a statement!

# parse\_expr Base Cases Token::Int(x) => { eprintln!("[parse\_expr] int literal: {}", x); let Token::Int(v) = self.next\_token()? else { unreachable!() }; Expr::Int(v) } Token::Var(\_) | Token::Star => { eprintln!("[parse\_expr] lval expression"); let lv = self.parse\_lval()?; Expr::Lv(lv, Copyable::No) } Token::Box => { return self.parse\_box(); }

Pretty Self Explanatory, If we see an int we return an int and so on.

# Token::Ampersand

```
Token::Ampersand => {
  eprintln!("[parse_expr] borrow expression");
  self.next_token()?;
  let mut muta = Mutable::No;
  if *self.peek_token()? == Token::Mut {
    self.next_token()?;
    muta = Mutable::Yes;
  }
  let inner_expr = self.parse_lval()?;
  Expr::Borrow(inner_expr, muta)
}
```

If we see an Ampersand then we know we are dealing with a borrow, then if next thing we see is a mute token then we can confirm it is a mutable borrow and set muta = Mutable::Yes otherwise muta = Mutable::No. Then we parse the inner l-val by calling self.parse\_lval()

```
Token::Lbracket => {
  return self.parse_block();
  },
If we see a { we simply have a Block so we fallback to self.parse_block()

Token::SemiColon
Token::Semicolon => Expr::Unit,
I allowed a simple empty semicolon to be of type unit, since all items in rust must have a type!
```

# parse\_lval

```
pub fn parse_lval(&mut self) -> ParseResult<Lval> {
   eprintln!("[parse_lval] entering lval parse, peek: {:?}", self.peek_token());
   let mut derefs = 0;
   while *self.peek_token()? == Token::Star {
      self.next_token()?;
      derefs += 1;
   }
   let var = self.next_token()?;
   if let Token::Var(x) = var {
      eprintln!("[parse_lval] exiting lval parse: {} with {} derefs", x, derefs);
      Ok(Lval { ident: x, derefs })
   } else {
      eprintln!("Got unexpected in LVAl");
      Err(Error::Unexpected(var))
   }
}
```

This function somewhat simple, all we do is each time we see a \* we add to the total number of deferences then we assert that we see a variable and return the Lval with proper number of recorded dereferences!

# Finally

Our Parser Should be able to Parse the following Expression

```
fn main () {
   let mut y =6;
   y =8888;
   //This is a comment;

let mut x = &y;
   let mut z = &x;
   {let mut i = 9;
   };
}
```

# **Evaluation**

For evaluation I chose to use the test that you gave me, with a few minor tweaks to the definition to fit my implementation - For example you used Type::boxx which I changed to Type:TBox - Overall the Logic Should be the exact same, I double checked of this but apologies if I missed anything peculiar

Here is the output on all the tests by running cargo test

```
test tests::tests1::tests::drop_owned ... ok
test tests::tests1::tests::drop_unowned ... ok
test tests::tests1::tests::drop_larger_example ... ok
test tests::tests1::tests::eval_block ... ok
test tests::tests1::tests::eval block mut ref ... ok
test tests::tests1::tests::eval block ref ... ok
test tests::tests1::tests::eval box ... ok
test tests::tests1::tests::eval_box_box ... ok
test tests::tests1::tests::eval_assign_copy ... ok
test tests::tests1::tests::eval_assign_move ... ok
test tests::tests1::tests::eval_copy ... ok
test tests::tests1::tests::eval_assign_move_deref ... ok
test tests::tests1::tests::eval_expr_stmt ... ok
test tests::tests1::tests::eval_assign_replace ... ok
test tests::tests1::tests::eval let mut ... ok
test tests::tests1::tests::eval lits ... ok
test tests::tests1::tests::eval move ... ok
test tests::tests1::tests::locate ref ... ok
test tests::tests1::tests::locate panic - should panic ... ok
test tests::tests1::tests::locate var ... ok
test tests::tests1::tests::read panic - should panic ... ok
```

```
test tests::tests::read_ref_owned ... ok
test tests::tests1::tests::read_var ... ok
test tests::tests::write_deref_read_diff ... ok
test tests::tests::write panic - should panic ... ok
test tests::tests2::tests::basic write prohibited ... ok
test tests::tests2::tests::basic write prohibited 2 ... ok
test tests::tests2::tests::compatible_basic ... ok
test tests::tests2::tests::compatible basic fail ... ok
test tests::tests2::tests::compatible_refs ... ok
test tests::tests2::tests::env_contained ... ok
test tests::tests2::tests::drop_basic ... ok
test tests::tests1::tests::write_two_deref ... ok
test tests::tests3::type_tests::assign_err_borrow ... ok
test tests::tests2::tests::mut_succ ... ok
test tests::tests3::type_tests::assign_err_update_imm ... FAILED
test tests::tests3::type_tests::assign_ok_ref ... ok
test tests::tests2::tests::env_lval_box ... ok
test tests::tests2::tests::env_var ... ok
test tests::tests2::tests::basic read prohibited ... ok
test tests::tests2::tests::env_lval_ref ... ok
test tests::tests2::tests::env_contained_undefined ... ok
test tests::tests3::type tests::cannot copy ... ok
test tests::tests2::tests::move_under_ref ... ok
test tests::tests3::type tests::cannot move ... ok
test tests::tests3::type tests::declare ok ... ok
test tests::tests3::type tests::declare shadow ... ok
test tests::tests3::type_tests::imm_borrow_err ... ok
```

```
test tests::tests3::type_tests::assign_err_incompat ... ok
test tests::tests3::type_tests::imm_borrow_ok ... ok
test tests::tests3::type_tests::invalid_lval ... ok
test tests::tests3::type_tests::keep_move ... ok
test tests::tests3::type tests::imm borrow err moved out ... ok
test tests::tests3::type tests::mut borrow err through imm ref ... ok
test tests::tests3::type_tests::mut_borrow_ok ... ok
test tests::tests3::type tests::still moved out ... ok
test tests::tests2::tests::mut fail ... ok
test tests::tests3::type_tests::assign_err_moved_out ... ok
test tests::tests3::type_tests::type_box ... ok
test tests::tests3::type_tests::assign_move_in ... ok
test tests::tests3::type_tests::assign_err_unknown ... ok
test tests::tests3::type_tests::assign_ok ... ok
test tests::tests3::type_tests::block_err_lifetime ... ok
test tests::tests2::tests::write_basic ... ok
test tests::tests3::type_tests::block_ok ... ok
test tests::tests3::type_tests::declare_moved_out ... ok
test tests::tests3::type_tests::copied ... ok
test tests::tests2::tests::write_ref ... ok
test tests::tests3::type_tests::type_value ... ok
test tests::tests2::tests::move under box ... ok
test tests::tests3::type_tests::make_copy ... ok
test tests::tests3::type tests::move behind ref ... ok
test tests::tests3::type tests::moved out ... ok
test tests::tests3::type tests::mut borrow err already borrowed ... ok
test tests::tests3::type_tests::mut_borrow_through_ref ... ok
```

```
test tests::tests3::type_tests::mut_borrow_err_moved_out ... ok
failures:
---- tests::tests3::type_tests::assign_err_update_imm stdout ----
Slot { tipe: Int, lifetime: Lifetime(0) }
thread 'tests::tests3::type_tests::assign_err_update_imm' panicked at src/tests/tests3.rs:459:9:
assertion `left == right` failed
    left: Ok(())
    right: Err(UpdateBehindImmRef(Lval { ident: "z", derefs: 2 }))

failures:
    tests::tests3::type_tests::assign_err_update_imm

test result: FAILED. 75 passed; 1 failed; 0 ignored; 0 measured; 0 filtered out; finished in 0.01s
As you can see I am failing one test, Which I could not for the life of me get it to pass. When I did, I would proceed to fail some other test
```