Lemma 2.3.7. Let $\Sigma = \Sigma \times \{0\}$ be a convex hypersurface in $\Sigma \times \mathbb{R}$ equipped with an \mathbb{R} -invariant contact structure. Then, for all a > b > 0, there exists a contact embedding $i : \Sigma \times (-a, a) \to \Sigma \times (-b, b)$ such that $i|_{\Sigma \times \{0\}} = \mathrm{id}_{\Sigma \times \{0\}}$. In other words, any convex hypersurface has an arbitrarily large invariant neighborhood.

Let $\Delta = \beta + f dt$ with Relb VF R.

There is correspondence $C^{\circ}M \longrightarrow infinitesimal automorphisms of \Delta$ $(X \in \mathcal{L}M_{5.6}, \mathcal{L}_{\chi} \mathcal{L} = g \mathcal{L})$ $\mathcal{L}(X) \longleftarrow X$ $\mathcal{L}_{\chi_{H}} d \mathcal{L} = \mathcal{L}_{\chi_{H}} \mathcal{L}_{\chi_{H}} \mathcal{L}_{\chi_{H}} d \mathcal{L} = \mathcal{L}_{\chi_{H}} \mathcal{L}$

Dt 15 an infinitesimal automorphism, let H
be the contact Hamiltonian. One see = f = H.

H 15 independent of t. let g be cut of function

Supp $g \subseteq (-b,b)$, $g \equiv 1$ on $(-\frac{1}{4},\frac{1}{4})$.

H'= gH generates contact F supported

in $\{x \in [-b,b]$, agrees with ∂_t near $\{x \in [0]\}$.

The flow gives contact embedding for any a.