

- *1.1**
- (i) Prove, in every category \mathcal{C} , that each object $A \in \mathcal{C}$ has a unique identity morphism.
 - (ii) If f is an isomorphism in a category, prove that its inverse is unique.

(i) Let $1, 1' \in \text{Hom}(A, A)$ be identity morphisms. Then $1 = 11' = 1'$.

(ii) Let $A \xrightarrow{f} B$ have inverses $g, g' \in \text{Hom}(B, A)$. Then $g = gfg' = g'$.