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Program Structures & Algorithms

Fall 2021

Assignment No. 3

◉ **Task**

There are three parts of overall tasks:

- 1. Implement height-weighted Quick Union with Path Compression and check the unit tests.**
- 2. Use implementation of UF_HWQUPC, develop a UF ("union-find") client that takes an integer value n from the command line to determine the number of "sites." Then generates random pairs of integers between 0 and $n-1$, calling `connected()` to determine if they are connected and `union()` if not. Loop until all sites are connected then print the number of connections generated. Package the program as a static method `count()` that takes n as the argument and returns the number of connections; and a `main()` that takes n from the command line, calls `count()` and prints the returned value. Show evidence of the run(s)**
- 3. Determine the relationship between the number of objects (n) and the number of pairs (m) generated to accomplish this.**

◉ **Relationship Conclusion:**

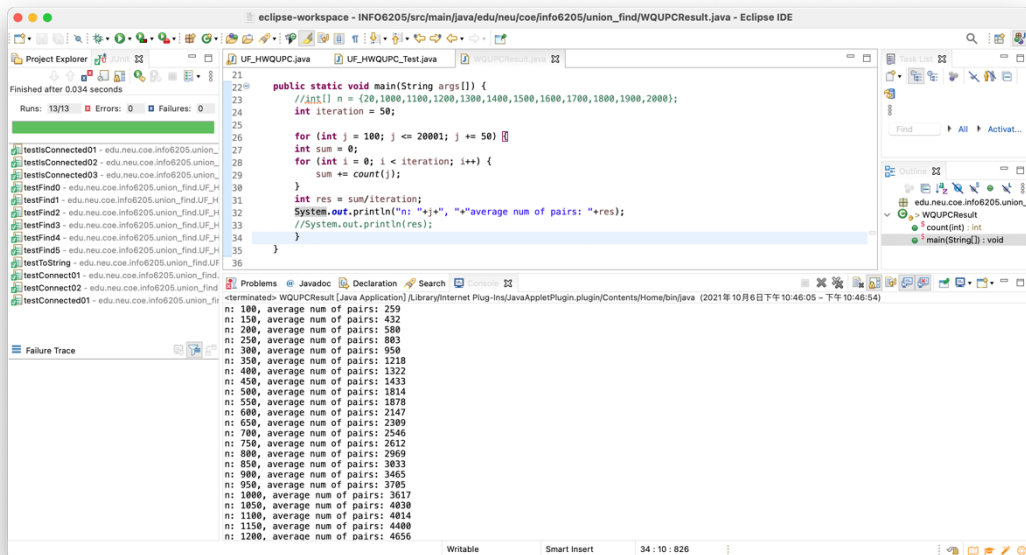
- 1. The relationship between N and M is linear.**

2. The observed line approaches $\frac{1}{2} N \ln(N)$. So, I think the relationship between two variables is $\frac{1}{2} N \ln(N)$.

◉ Evidence to support the conclusion:

1. Output

N is set from 100 to 20000 where the interval is 50, thus there are total 399 returned values. As it's hard to show all of 399 values here, only head and tail are shown up. For details, please check Assignment 3 result.xlsx within the Assignment 3 file.



```
21
22 public static void main(String args[]) {
23     //int[] n = {20,1000,1100,1200,1300,1400,1500,1600,1700,1800,1900,2000};
24     int iteration = 50;
25
26     for (int j = 100; j <= 2000; j += 50) {
27         int sum = 0;
28         for (int i = 0; i < iteration; i++) {
29             sum += count(i);
30         }
31         int res = sum/iteration;
32         System.out.println("n: "+j+", "+ "average num of pairs: "+res);
33         //System.out.println(res);
34     }
35 }
36
```

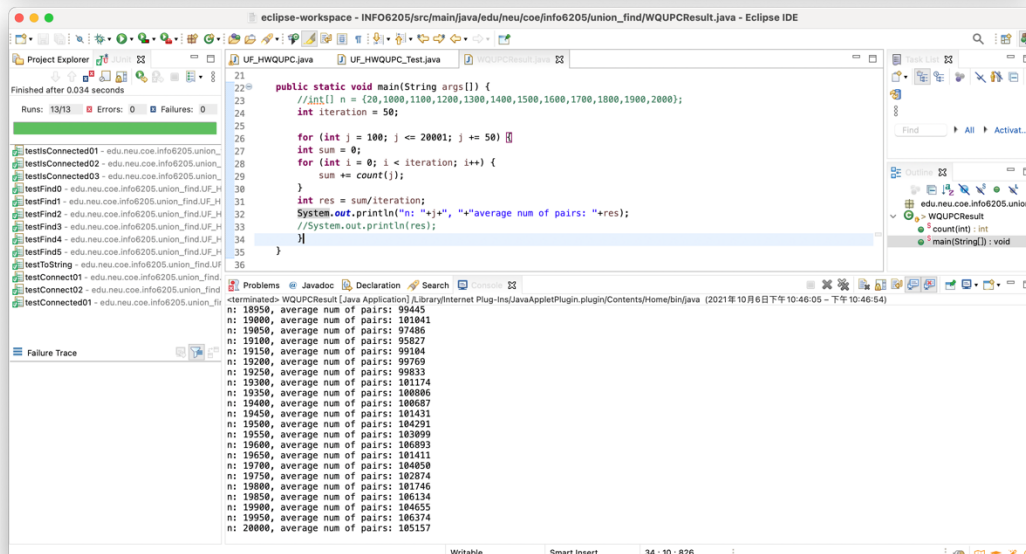
Finished after 0.034 seconds

Runs: 13/13 Errors: 0 Failures: 0

testisConnected01 - edu.neu.coe.info6205.union_...
testisConnected02 - edu.neu.coe.info6205.union_...
testisConnected03 - edu.neu.coe.info6205.union_...
testFind0 - edu.neu.coe.info6205.union_find_UF_H...
testFind1 - edu.neu.coe.info6205.union_find_UF_H...
testFind2 - edu.neu.coe.info6205.union_find_UF_H...
testFind3 - edu.neu.coe.info6205.union_find_UF_H...
testFind4 - edu.neu.coe.info6205.union_find_UF_H...
testFind5 - edu.neu.coe.info6205.union_find_UF_H...
testToString - edu.neu.coe.info6205.union_find_UF...
testConnect01 - edu.neu.coe.info6205.union_find...
testConnect02 - edu.neu.coe.info6205.union_find...
testConnect03 - edu.neu.coe.info6205.union_find...

terminated: WQUPResult [Java Application] [LibraryInternet Plug-Ins/JavaAppletPlugin.plugin/Contents/Home/bin/java (2021年10月6日下午10:46:05 - 下午10:46:54)]

n: 100, average num of pairs: 259
n: 150, average num of pairs: 432
n: 200, average num of pairs: 580
n: 250, average num of pairs: 803
n: 300, average num of pairs: 958
n: 350, average num of pairs: 1218
n: 400, average num of pairs: 1322
n: 450, average num of pairs: 1433
n: 500, average num of pairs: 1814
n: 550, average num of pairs: 1878
n: 600, average num of pairs: 2147
n: 650, average num of pairs: 2309
n: 700, average num of pairs: 2546
n: 750, average num of pairs: 2612
n: 800, average num of pairs: 2969
n: 850, average num of pairs: 3833
n: 900, average num of pairs: 3465
n: 950, average num of pairs: 3705
n: 1000, average num of pairs: 3617
n: 1050, average num of pairs: 4038
n: 1100, average num of pairs: 4014
n: 1150, average num of pairs: 4480
n: 1200, average num of pairs: 4656



```
21
22 public static void main(String args[]) {
23     //int[] n = {20,1000,1100,1200,1300,1400,1500,1600,1700,1800,1900,2000};
24     int iteration = 50;
25
26     for (int j = 100; j <= 2000; j += 50) {
27         int sum = 0;
28         for (int i = 0; i < iteration; i++) {
29             sum += count(i);
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31         int res = sum/iteration;
32         System.out.println("n: "+j+", "+ "average num of pairs: "+res);
33         //System.out.println(res);
34     }
35 }
36
```

Finished after 0.034 seconds

Runs: 13/13 Errors: 0 Failures: 0

testisConnected01 - edu.neu.coe.info6205.union_...
testisConnected02 - edu.neu.coe.info6205.union_...
testisConnected03 - edu.neu.coe.info6205.union_...
testFind0 - edu.neu.coe.info6205.union_find_UF_H...
testFind1 - edu.neu.coe.info6205.union_find_UF_H...
testFind2 - edu.neu.coe.info6205.union_find_UF_H...
testFind3 - edu.neu.coe.info6205.union_find_UF_H...
testFind4 - edu.neu.coe.info6205.union_find_UF_H...
testFind5 - edu.neu.coe.info6205.union_find_UF_H...
testToString - edu.neu.coe.info6205.union_find_UF...
testConnect01 - edu.neu.coe.info6205.union_find...
testConnect02 - edu.neu.coe.info6205.union_find...
testConnect03 - edu.neu.coe.info6205.union_find...

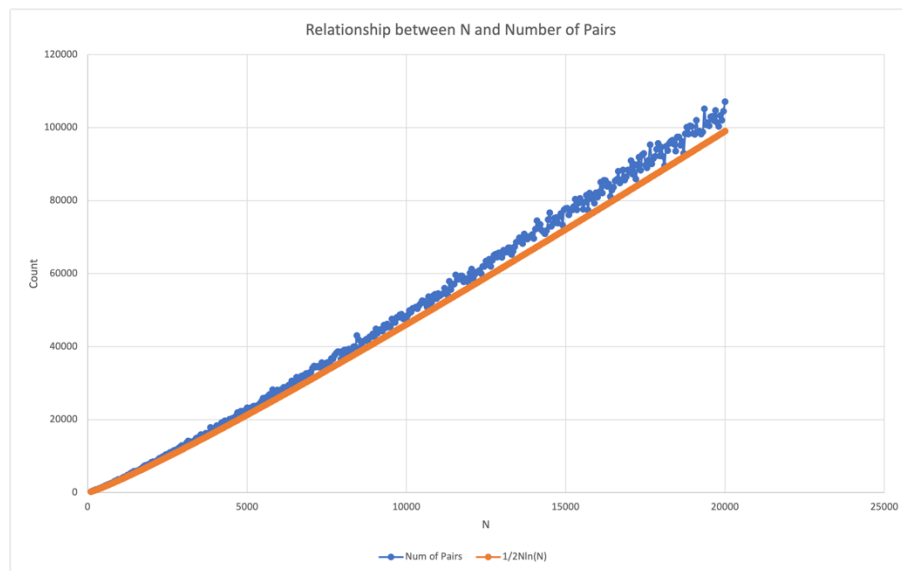
terminated: WQUPResult [Java Application] [LibraryInternet Plug-Ins/JavaAppletPlugin.plugin/Contents/Home/bin/java (2021年10月6日下午10:46:05 - 下午10:46:54)]

n: 18050, average num of pairs: 99445
n: 18100, average num of pairs: 101041
n: 18150, average num of pairs: 97486
n: 18200, average num of pairs: 95827
n: 18250, average num of pairs: 99104
n: 18300, average num of pairs: 99769
n: 18350, average num of pairs: 99833
n: 18400, average num of pairs: 101174
n: 18450, average num of pairs: 100886
n: 18500, average num of pairs: 100657
n: 18550, average num of pairs: 101431
n: 18600, average num of pairs: 104291
n: 18650, average num of pairs: 103899
n: 18700, average num of pairs: 106893
n: 18750, average num of pairs: 101411
n: 18800, average num of pairs: 104858
n: 18850, average num of pairs: 102874
n: 18900, average num of pairs: 101746
n: 18950, average num of pairs: 106134
n: 19000, average num of pairs: 104655
n: 19050, average num of pairs: 106374
n: 19100, average num of pairs: 105157

2. Graphical Representation

The graph observed with samples (details are in Assignment 3 result.xlsx):

N	Num of Pairs	$1/2N\ln(N)$
2050	8485	7816.23495
2100	8138	8032.17725
2150	8636	8248.71486
2200	9023	8465.8339



Unit tests result:

UF_HWQUPC_Test are passed and none of code is modified:

The screenshot shows the Eclipse IDE interface. The top toolbar indicates "Runs: 13/13", "Errors: 0", and "Failures: 0". The left sidebar shows a "Failure Trace" panel. The main editor displays the source code of the `UF_HWQUPC_Test` class. The code includes several test methods: `testToString()`, `testIsConnected01()`, `testIsConnected02()`, `testIsConnected03()`, `testFind0()`, `testFind1()`, `testFind2()`, `testFind3()`, `testFind4()`, and `testFind5()`. The right sidebar shows the "Outline" view, listing all the test methods. The status bar at the bottom indicates the file is "Writable" and "Smart Insert" is enabled, with a timestamp of "21:13:489".

