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1. $X \sim \text{Geometric}(p)$

$$P[X=k] = (1-p)^{k-1}p \quad (k \geq 1, k \in \mathbb{Z})$$

$$E(X) = \frac{1}{p}$$

2. $X \sim \text{Discrete-Uniform}(1, m)$

$$P[X=k] = \frac{1}{m} \quad (1 \leq k \leq m, k \in \mathbb{Z})$$

$$E(X) = \frac{m+1}{2}$$

3. $X \sim \text{Binomial}(n, p)$

$$P(X=k) = \binom{n}{k} p^k (1-p)^{n-k}$$

$$E(X) = np$$

4. $X \sim \text{Bernoulli}(p)$

$$P(X=k) = \begin{cases} 1-p & (k=0) \\ p & (k=1) \end{cases}$$

$$E(X) = p$$

5. $X \sim \text{Poisson}(\gamma)$

$$P[X=k] = e^{-\gamma} \cdot \frac{\gamma^k}{k!} \quad (k \geq 1, k \in \mathbb{Z})$$

$$E(X) = \gamma$$

6. $X \sim \text{Exponential}(\gamma)$

$$f(x) = \begin{cases} 0 & (x \leq 0) \\ \gamma e^{-\gamma x} & (x > 0) \end{cases}$$

$$E(X) = \frac{1}{\gamma}$$

7. $X \sim N(\mu, \sigma^2)$

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

$$E(X) = \mu$$

8. $X \sim \text{Uniform}(a, b)$

$$f(x) = \begin{cases} \frac{1}{b-a} & (a \leq x < b) \\ 0 & (x < a \text{ OR } x \geq b) \end{cases}$$

$$E(X) = \frac{a+b}{2}$$