

**Homework learning objectives:** By the end of this homework, you should be able to:

- Determine if a system is linear, time-invariant, memoryless, and causal
- Compute the output of a system from a known input

**Question #1:** (2 pts) How many hours did you spend on this homework?

**Question #2:** (12 pts) Consider the system  $y[n] = \mathcal{H}\{x[n]\} = x[n+1] - 2x[n] + x[n-1]$

- Sketch the output of the system  $y_1[n] = \mathcal{H}\{x_1[n]\}$  for input  $x_1[n] = u[n] - u[n-5]$ .
- Sketch the output of the system  $y_2[n] = \mathcal{H}\{x_2[n]\}$  for input  $x_2[n] = 3\delta[n-2]$ .
- Sketch the output of the system  $y_3[n] = \mathcal{H}\{x_1[n] + x_2[n]\}$
- Sketch the output of the system  $y_4[n] = \mathcal{H}\{x_1[n]\} + \mathcal{H}\{x_2[n]\}$
- Is this system linear? Why?
- Based on the previous results, what to you think is an application of this system?

**Question #3:** (12 pts) Consider the system  $y[n] = \mathcal{H}\{x[n]\} = x[n+1]x[n]x[n-1]$

- Sketch the output of the system  $y_1[n] = \mathcal{H}\{x_1[n]\}$  for input  $x_1[n] = u[n] - u[n-5]$ .
- Sketch the output of the system  $y_2[n] = \mathcal{H}\{x_2[n]\}$  for input  $x_2[n] = 3\delta[n-2]$ .
- Sketch the output of the system  $y_3[n] = \mathcal{H}\{x_1[n] + x_2[n]\}$
- Sketch the output of the system  $y_4[n] = \mathcal{H}\{x_1[n]\} + \mathcal{H}\{x_2[n]\}$
- Is this system linear? Why?
- Based on the previous results, what to you think is an application of this system?

**Question #4:** (8 pts) Consider the system  $y[n] = \mathcal{H}\{x[n]\} = x[n]\cos(\pi n)$

- Sketch the output of the system  $y_1[n] = \mathcal{H}\{x_1[n]\}$  for input  $x_1[n] = u[n] - u[n-5]$ .
- Sketch the output of the system  $y_2[n] = \mathcal{H}\{x_2[n]\}$  for input  $x_2[n] = u[n-1] - u[n-6]$ .
- Is this system time-invariant? Why?
- Is this system memoryless? Why?
- Based on the previous results, what to you think is an application of this system?

**Question #5:** (10 pts) Consider the system  $y[n] = \mathcal{H}\{x[n]\} = \max(x[n], 1)$

- (a) Sketch the output of the system  $y_1[n] = \mathcal{H}\{x_1[n]\}$  for input  $x_1[n] = n(u[n+2] - u[n-2])$ .
- (b) Sketch the output of the system  $y_2[n] = \mathcal{H}\{x_2[n]\}$  for input  $x_2[n] = (n-1)(u[n+1] - u[n-3])$ .
- (c) Is this system time-invariant? Why?
- (d) Is this system causal? Why?
- (e) Based on the previous results, what to you think is an application of this system?