

EEE 5502 HW #06

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Question #1

I spent 8 hours

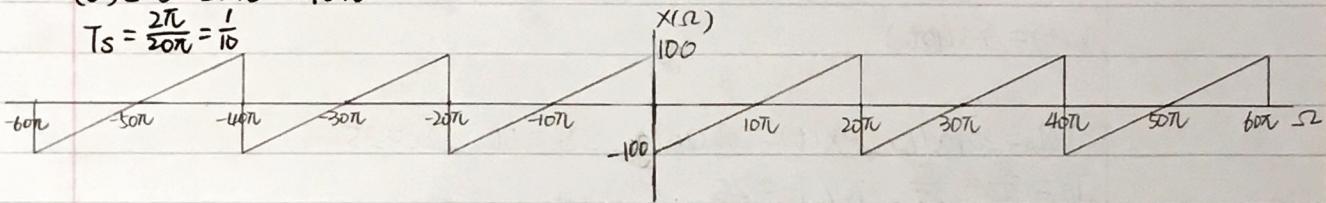
Question #2

$$(a) \Omega_N = 2(20\pi) = 40\pi$$

$$(b) \Omega_N = 2(20\pi)(4) = 160\pi$$

$$(c) \Omega_s = 20\pi < 40\pi$$

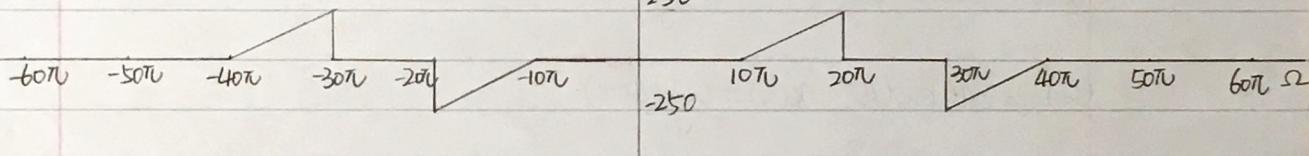
$$T_s = \frac{2\pi}{20\pi} = \frac{1}{10}$$



Yes we experience aliasing.

$$(d) \Omega_s = 50\pi > 40\pi$$

$$T_s = \frac{2\pi}{50\pi} = \frac{1}{25}$$

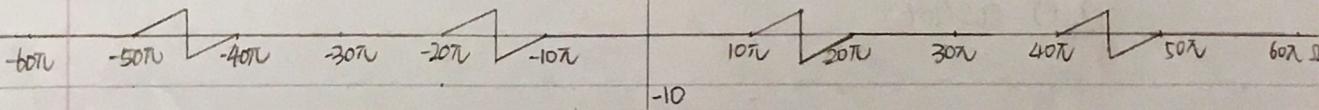
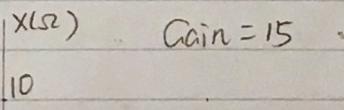
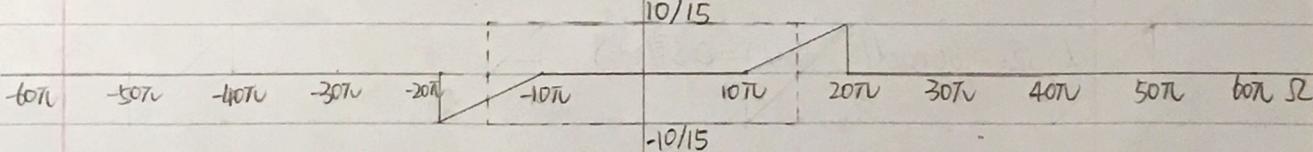


No we don't experience aliasing.

$$(e) \Omega_s = 30\pi < 40\pi, \Omega_c = 15\pi$$

$$T_s = \frac{2\pi}{30\pi} = \frac{1}{15}$$

$$\text{Gain: } K = \frac{1}{15}$$

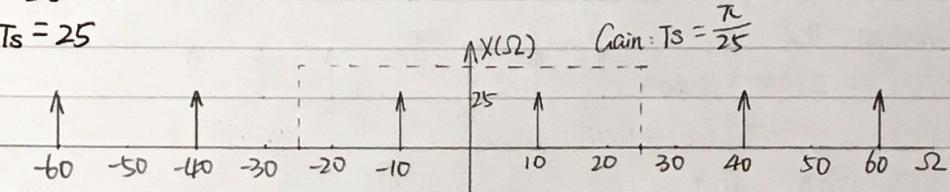


Question #3

(a)  $\Omega_0 = 10 \text{ rad/s}$ ,  $x(t) = \cos(10t)$ .  $\Omega_s = 50$ ,  $\Omega_c = 25$

$$T_s = \frac{2\pi}{\Omega_s} = \frac{2\pi}{50} = \frac{\pi}{25}$$

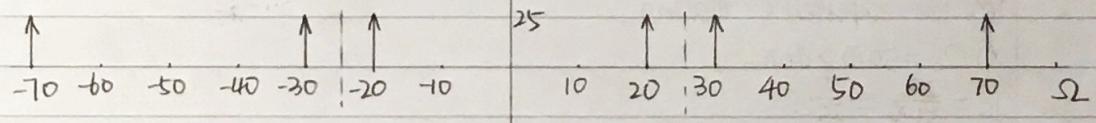
$$\pi/\Omega_s = 25$$



$$x(t) = \cos(10t)$$

(b)  $\Omega_0 = 20 \text{ rad/s}$ ,  $x(t) = \cos(20t)$ .  $\Omega_s = 50$ ,  $\Omega_c = 25$

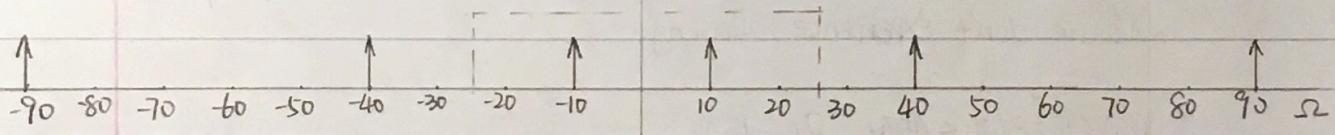
$$T_s = \frac{2\pi}{\Omega_s} = \frac{\pi}{25}, \quad \pi/\Omega_s = 25$$



$$x(t) = \cos(20t)$$

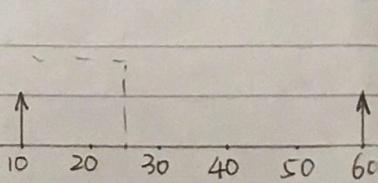
(c)  $\Omega_0 = 40 \text{ rad/s}$ .  $x(t) = \cos(40t)$

$$X(\Omega)$$



$$x(t) = \cos(40t)$$

(d)  $\Omega_0 = 60 \text{ rad/s}$ .  $x(t) = \cos(60t)$



$$x(t) = \cos(60t)$$

FIVE STAR.

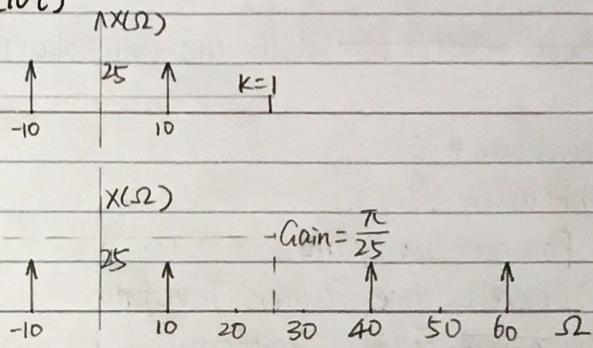
### Question #4

$$\Omega_s = 50 \text{ rad/s}, \Omega_c = 25 \text{ rad/s}, K = 1$$

Before: low-pass anti-aliasing filter:  ~~$\Omega_c = 25 \text{ rad/s}$~~ ,  $K = 1$

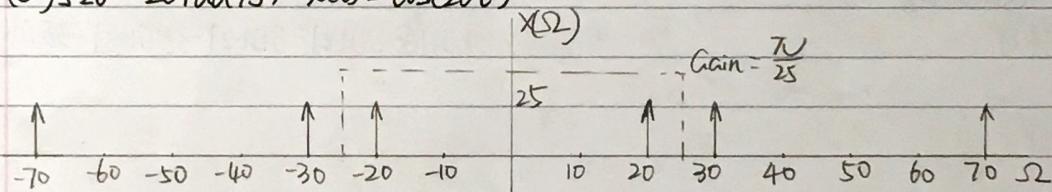
$$\text{After: } \Omega_c = 25 \text{ rad/s}, T_s = \frac{2\pi}{50} = \frac{\pi}{25} = K$$

$$(a) \Omega_0 = 10 \text{ rad/s}, x(t) = \cos(10t)$$



$$x(t) = \cos(10t)$$

$$(b) \Omega_0 = 20 \text{ rad/s}, x(t) = \cos(20t)$$



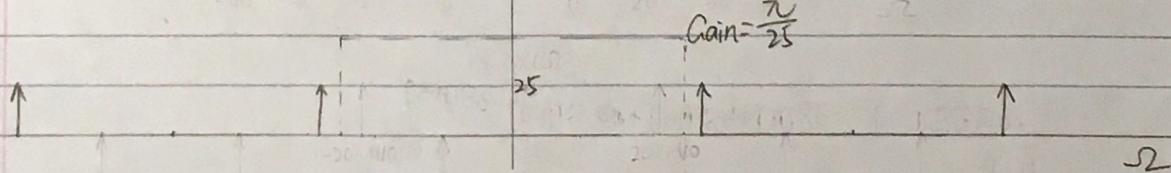
$$x(t) = \cos(20t)$$

$$(c) \Omega_0 = 40 \text{ rad/s}, x(t) = \cos(40t)$$

the signal is gone

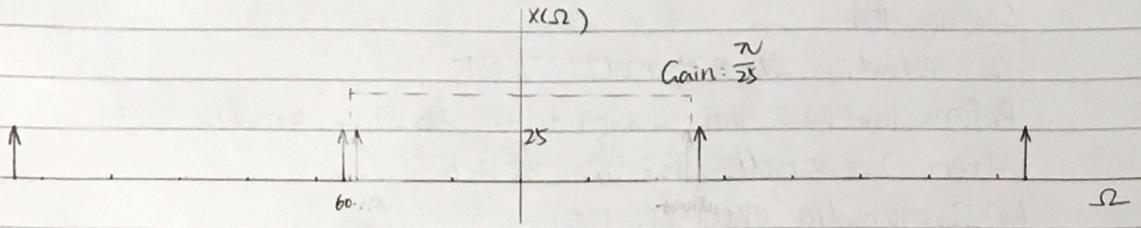
With the ~~tos~~ low-pass anti-aliasing filter before sampling,  ~~$\Omega_{2\max} = -40 + 20\pi$~~   
Magnitude = 25.

$$x(t) = \cos(40t)$$



$$(d) \Omega_0 = 60 \text{ rad/s}, x(t) = \cos(60t)$$

With the low-pass anti-aliasing filter before sampling,  $\Omega_{2\max} = -60 + 27\pi$ . Magnitude = 25.



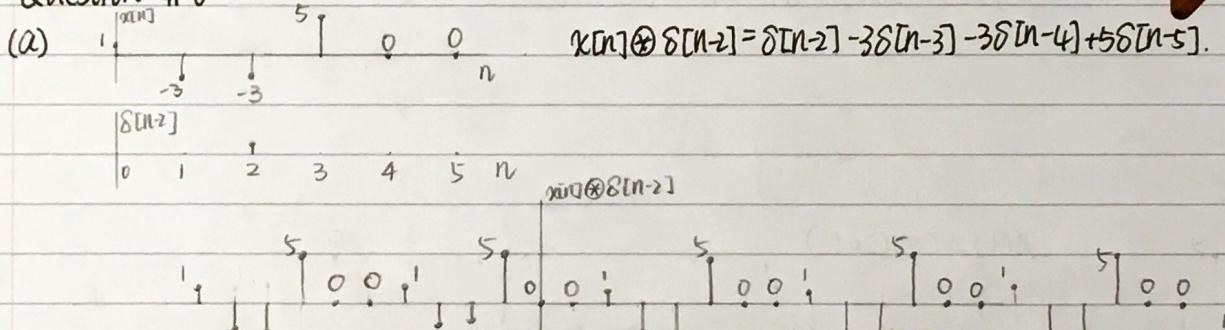
$\& x(t) = \cos(6\pi t)$  — With the anti-aliasing filter, the signal is gone

Question # 5

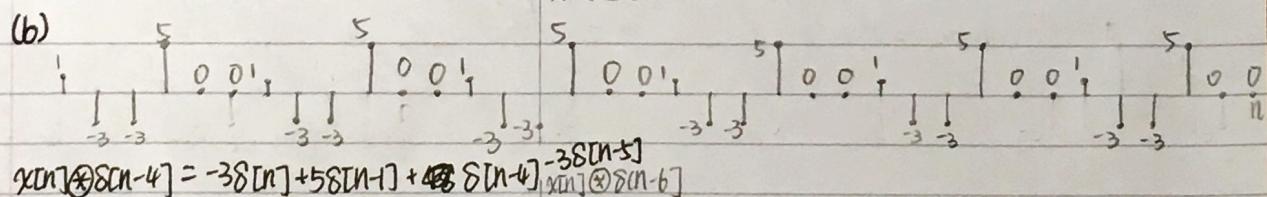
- (a) Fourier Series
- (b) Fourier Transform
- (c) Discrete time Fourier Transform
- (d) ~~Discrete~~ Fourier Transform
- (e) Discrete Fourier Series

Question # 6

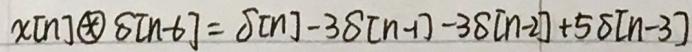
$$(a) \quad x[n] * \delta[n-2] = \delta[n-2] - 3\delta[n-3] - 3\delta[n-4] + 5\delta[n-5].$$



$$(b) \quad x[n] * \delta[n-4] = -3\delta[n] + 5\delta[n-1] + 4\delta[n-4] - 3\delta[n-5]$$



$$(c) \quad x[n] * \delta[n-6] = \delta[n] - 3\delta[n-1] - 3\delta[n-2] + 5\delta[n-3]$$



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(d)

$$\frac{1}{3}(6[n+1] + \delta[n-2] + \delta[n-3])$$

Within one period:

$$x[n] \oplus \frac{1}{3} \delta[n-1]$$

$$x[n] \oplus \frac{1}{3} \delta[n-1]$$

$$x[n] \oplus \frac{1}{3} \delta[n-2]$$

$$x[n] \oplus \frac{1}{3} \delta[n-2]$$

$$x[n] \oplus \frac{1}{3} \delta[n-3]$$

$$x[n] \oplus \frac{1}{3} \delta[n-3]$$

$$y[n] = x[n] \oplus \left( \frac{1}{3}(6[n+1] + \delta[n-2] + \delta[n-3]) \right)$$

in one period.

$$\dots \quad \begin{matrix} \frac{1}{3} \\ -\frac{2}{3} \\ -\frac{1}{3} \end{matrix} \quad \begin{matrix} \frac{2}{3} \\ \frac{1}{3} \\ -\frac{2}{3} \end{matrix} \quad \begin{matrix} \frac{5}{3} \\ -\frac{1}{3} \\ -\frac{2}{3} \end{matrix} \quad \begin{matrix} \frac{2}{3} \\ \frac{1}{3} \\ -\frac{2}{3} \end{matrix} \quad \begin{matrix} \frac{5}{3} \\ -\frac{1}{3} \\ -\frac{2}{3} \end{matrix} \quad \dots$$

$$y[n] = \frac{5}{3} \delta[n] + \frac{1}{3} \delta[n-1] - \frac{2}{3} \delta[n-2] - \frac{5}{3} \delta[n-3] - \frac{1}{3} \delta[n-4] + \frac{2}{3} \delta[n-5]$$

$$x[5-n] = 5 \delta[n-2] - 3 \delta[n-3] - 3 \delta[n-4] + \delta[n-5]$$

(e)

$$x[n]$$

$$x[5+n]$$

$$x[5-n] \oplus 5 \delta[n-2]$$

$$x[n] \oplus (-3 \delta[n-4])$$

$$x[5-n] \oplus (-3 \delta[n-4])$$

$$x[5-n] \oplus 9 \delta[n-5]$$

$$x[5-n] \oplus 44 \delta[n-5]$$

$$x[5-n] \oplus 44 \delta[n-5]$$

$$\dots \quad \begin{matrix} 10 \\ -9 \\ -18 \end{matrix} \quad \dots$$

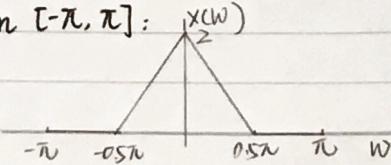
$$x[n] \oplus x[5+n] = -9 \delta[n] - 18 \delta[n-1] + 10 \delta[n-2] - 18 \delta[n-3] - 9 \delta[n-4] + 44 \delta[n-5]$$

Question #7

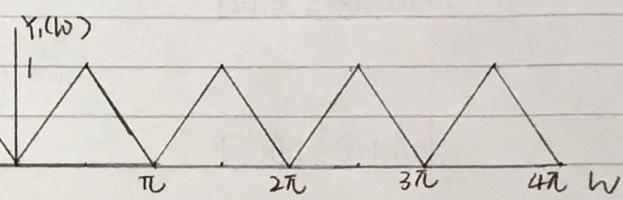
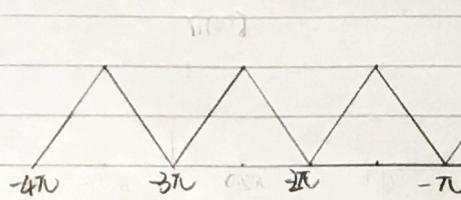
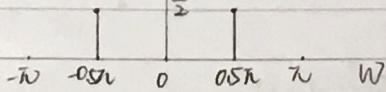
$$(a) Y_1(w) = \frac{1}{2\pi} X(w) \otimes \pi [\delta(w - \frac{\pi}{2}) + \delta(w + \frac{\pi}{2})]$$

$$= \frac{1}{2} X(w) \oplus [\delta(w - \frac{\pi}{2}) + \delta(w + \frac{\pi}{2})]$$

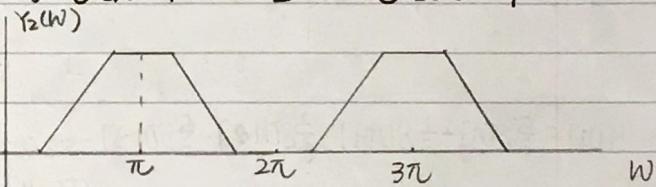
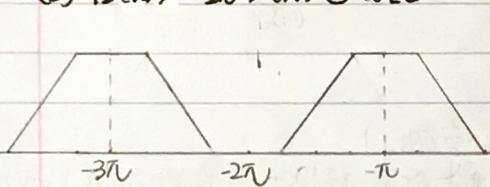
In  $[-\pi, \pi]$ :



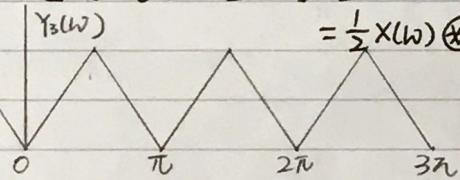
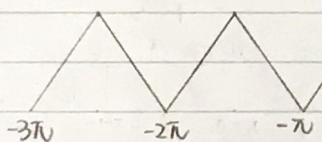
$$\frac{1}{2} [\delta(w - \frac{\pi}{2}) + \delta(w + \frac{\pi}{2})]$$



$$(b) Y_2(w) = \frac{1}{2\pi} X(w) \otimes \pi [\delta(w - \frac{3}{4}\pi) + \delta(w + \frac{3}{4}\pi)] = \frac{1}{2} X(w) \oplus [\delta(w - \frac{3}{4}\pi) + \delta(w + \frac{3}{4}\pi)]$$



$$(c) Y_3(w) = \frac{1}{2\pi} X(w) \otimes \pi [\delta(w - \frac{3}{2}\pi) + \delta(w + \frac{3}{2}\pi)] = \frac{1}{2} X(w) \oplus [\delta(w - \frac{3}{2}\pi) + \delta(w + \frac{3}{2}\pi)]$$



$$= \frac{1}{2} X(w) \oplus [\delta(w + \frac{\pi}{2}) + \delta(w - \frac{5\pi}{2})]$$

$$(d) Y_4(w) = \frac{1}{2\pi} X(w) \otimes \pi [\delta(w - 102\pi) + \delta(w + 102\pi)] = \frac{1}{2} X(w) \oplus [\delta(w) + \delta(w)] = X(w) * \delta(w)$$

