Full Name:	·	ExamID: 010001
EEL 4750	/ EEE 5502 (Fall 2018) - Practice Exam #02	Date: Oct. 30, 2018

Question	# of Points Possible	# of Points Obtained	Grader
# 1	18		
# 2	17		
# 3	17		
# 4	16		
# 5	16		
# 6	16		
Total	100		

For full credit when sketching: remember to label axes and make locations and amplitudes clear.

## Before starting the exam, read and sign the following agreement.

By signing this agreement, I agree to solve the problems of this exam while adhering to the policies and guidelines of the University of Florida and EEL 4750 / EEE 5502 and without additional external help. The guidelines include, but are not limited to,

- The University of Florida honor pledge: "On my honor, I have neither given nor received unauthorized aid in doing this assignment."
- Only one 8.5 by 11 inch cheat sheet (double-sided) may be used
- No calculators or computers may be used
- No textbooks or additional notes may be used
- No collaboration is allowed
- No cheating is allowed

Student	Date

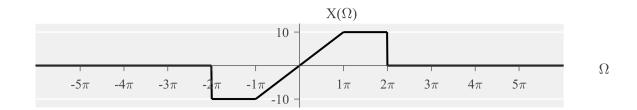
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**Question #1:** Consider the Fourier Transform of a continuous-time signal x(t) shown below.



(a) (4 pts) Determine the Nyquist sampling rate for  $z(t) = 2x(t)\cos(12\pi t)$ .

(b) (6 pts) Sketch (for  $\Omega = -6\pi$  to  $\Omega = +6\pi$ ) the Fourier transform  $X_s(\Omega)$  of the sampled  $X(\Omega)$  with a sampling rate of  $\Omega_s = 5\pi$ . Do we experience aliasing?

(c)  $(6 \ pts)$  Sketch (for  $\Omega = -6\pi$  to  $\Omega = +6\pi$ ) the Fourier transform  $X_s(\Omega)$  of the sampled  $X(\Omega)$  with a sampling rate of  $\Omega_s = 3\pi$ . Do we experience aliasing?

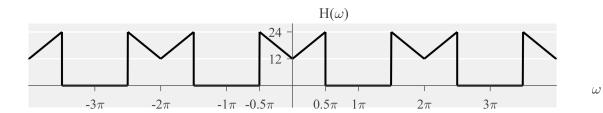
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Question #2: Consider the impulse response h[n] below with frequency response  $H(\omega)$ .



(a) (6 pts) Sketch (for  $-3\pi < \omega < 3\pi$ ) the magnitude of the DTFT of x[n] = -2h[n-10]

(b) (5 pts) Sketch (for  $-3\pi < \omega < 3\pi$ ) the magnitude of the DTFT of  $y[n] = h[n] * (2/\pi)$ 

(c) (6 pts) Sketch (for  $-3\pi < \omega < 3\pi$ ) the magnitude of the DTFT of

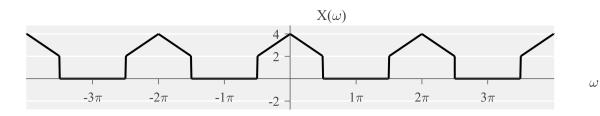
$$z[n] = H(\omega) \left[ \sum_{k=-\infty}^{\infty} u(\omega + \pi/4 + 2\pi k) - u(\omega - \pi/4 + 2\pi k) \right]$$

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**Question #3:** Consider the DTFT signal  $X(\omega)$  shown below.



(a) (5 pts) Sketch the DTFT (from  $\omega = -3\pi$  to  $\omega = 3\pi$ ) of  $y[n] = x[n]\cos(\pi n)$ . Remember to label important locations / values.

(b) (5 pts) Sketch the DTFT (from  $\omega = -3\pi$  to  $\omega = 3\pi$ ) of  $y[n] = x[n]\cos(10\pi n)$ . Remember to label important locations / values.

(c) (7 pts) Sketch the result of the length-6 discrete-time circular convolution defined by  $z[n] = [\delta[n-2] + \delta[n-4]] \circledast [\delta[n-1] - \delta[n-2]] .$ 

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**Question #4:** Consider the z-transform causal transfer function H(z) defined by

$$H(z) = z^{-1} + 2z^{-3} + z^{-5}$$

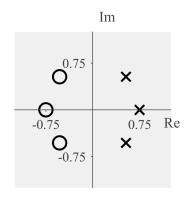
(a) (6 pts) Compute the phase response for  $\angle H(\omega)$ .

(b) (5 pts) Compute the phase response for the DTFT of v[n] = h[n] \* h[-n].

(c) (5 pts) Compute the phase response for  $G(\omega) = j$ .

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Question #5: Consider the following pole-zero plot, representing a causal LTI system.



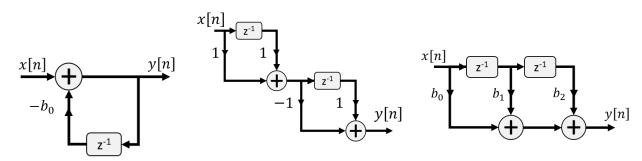
(a) (4 pts) Is this a low pass filter, bandpass filter, high pass filter, all-pass filter, or none-of-the above? Explain why.

(b) (4 pts) Is the system stable? Explain why.

(c) (4 pts) Is this a minimum phase system? Explain why.

(d) (4 pts) Is this a linear phase system? Explain why.

**Question #6:** (10 pts) Consider the IIR all-pole direct form (left), FIR cascade form (center), and FIR direct form (right) implementations below.



(a) (5 pts) Write the difference equation for the IIR all-pole direct form (left).

(b) (5 pts) Write the z-transform transfer function for to the FIR cascade form (center).

(c) (6 pts) Determine the weights  $b_0, b_1, b_2$  for the FIR direct form (right) transfer function  $H(z) = [1 - (1/2)z^{-1}][1 - (1/4)z^{-1}]$ 

## Table of Discrete-Time Fourier Transform Pairs:

Discrete-Time Fourier Transform : 
$$X(\omega)=\sum_{n=-\infty}^{\infty}x[n]e^{-j\omega n}$$
  
Inverse Discrete-Time Fourier Transform :  $x[n]=\frac{1}{2\pi}\int_{2\pi}X(\omega)e^{j\omega t}\;d\omega$ .

x[n]	$X(\omega)$	condition
$a^n u[n]$	$rac{1}{1-ae^{-j\omega}}$	a  < 1
$(n+1)a^nu[n]$	$\frac{1}{(1 - ae^{-j\omega})^2}$	a  < 1
$\frac{(n+r-1)!}{n!(r-1)!}a^nu[n]$	$\frac{1}{(1 - ae^{-j\omega})^r}$	a  < 1
$\delta[n]$	1	
$\delta[n-n_0]$	$e^{-j\omega n_0}$	
x[n] = 1	$2\pi \sum_{k=-\infty}^{\infty} \delta(\omega - 2\pi k)$	
u[n]	$\frac{1}{1 - e^{-j\omega}} + \sum_{k = -\infty}^{\infty} \pi \delta(\omega - 2\pi k)$	
$e^{j\omega_0 n}$	$2\pi \sum_{k=-\infty}^{\infty} \delta(\omega - \omega_0 - 2\pi k)$	
$\cos(\omega_0 n)$	$\pi \sum_{k=-\infty}^{\infty} \{\delta(\omega - \omega_0 - 2\pi k) + \delta(\omega + \omega_0 - 2\pi k)\}\$	
$\sin(\omega_0 n)$	$\frac{\pi}{j} \sum_{k=-\infty}^{\infty} \{ \delta(\omega - \omega_0 - 2\pi k) - \delta(\omega + \omega_0 - 2\pi k) \}$	
$\sum_{k=-\infty}^{\infty} \delta[n-kN]$	$\frac{2\pi}{N} \sum_{k=-\infty}^{\infty} \delta\left(\omega - \frac{2\pi k}{N}\right)$	
$x[n] = \begin{cases} 1 & , &  n  \le N \\ 0 & , &  n  > N \end{cases}$	$\frac{\sin(\omega(N+1/2))}{\sin(\omega/2)}$	
	$X(\omega) = \begin{cases} 1 & , & 0 \le  \omega  \le W \\ 0 & , & W <  \omega  \le \pi \end{cases}$	
	$X(\omega)$ is periodic with period $2\pi$	

## Table of Discrete-Time Fourier Transform Properties: For each property, assume

$$x[n] \overset{DTFT}{\longleftrightarrow} X(\omega) \quad \text{and} \quad y[n] \overset{DTFT}{\longleftrightarrow} Y(\omega)$$

Property	Time domain	DTFT domain
Linearity	Ax[n] + By[n]	$AX(\omega) + BY(\omega)$
Time Shifting	$x[n-n_0]$	$X(\omega)e^{-j\omega n_0}$
Frequency Shifting	$x[n]e^{j\omega_0n}$	$X(\omega-\omega_0)$
Conjugation	$x^*[n]$	$X^*(-\omega)$
Time Reversal	x[-n]	$X(-\omega)$
Convolution	x[n] * y[n]	$X(\omega)Y(\omega)$
Multiplication	x[n]y[n]	$\frac{1}{2\pi} \int_{2\pi} X(\theta) Y(\omega - \theta) d\theta$
Differencing in Time	x[n] - x[n-1]	$(1 - e^{-j\omega})X(\omega)$
Accumulation	$\sum_{k=-\infty}^{\infty} x[k]$	$\frac{1}{1 - e^{-j\omega}} + \pi X(0) \sum_{k = -\infty}^{\infty} \delta(\omega - 2\pi k)$
Frequency Differentiation	nx[n]	$j\frac{dX(\omega)}{d\omega}$
Parseval's Relation for Aperiodic Signals	$\sum_{k=-\infty}^{\infty}  x[k] ^2$	$\frac{1}{2\pi} \int_{2\pi}  X(\omega) ^2 d\omega$

## Table of Z-Transform Pairs:

Z-Transform : 
$$X(z)=\sum_{n=-\infty}^\infty x[n]z^{-n}$$
   
 Inverse Z-Transform :  $x[n]=\frac{1}{2\pi j}\oint_{\mathcal C} X(z)z^{n-1}\;dz$  .

x[n]	$X(\omega)$	ROC
$a^n u[n]$	$\frac{1}{1 - az^{-1}}$	z  >  a
$-a^n u[-n-1]$	$\frac{1}{1 - az^{-1}}$	z  <  a
$na^nu[n]$	$\frac{az^{-1}}{(1-az^{-1})^2}$	z  >  a
$-na^nu[-n-1]$	$\frac{az^{-1}}{(1-az^{-1})^2}$	z  <  a
$\delta[n]$	1	All $z$
$\delta[n-n_0]$	$z^{-n_0}$	All $z$
u[n]	$\frac{1}{1-z^{-1}}$	z  > 1
$\cos(\omega_0 n)u[n]$	$\frac{1 - z^{-1}\cos(\omega_0)}{1 - 2z^{-1}\cos(\omega_0) + z^{-2}}$	z  > 1
$\sin(\omega_0 n)u[n]$	$\frac{z^{-1}\sin(\omega_0)}{1 - 2z^{-1}\cos(\omega_0) + z^{-2}}$	z  > 1
$a^n \cos(\omega_0 n) u[n]$	$\frac{1 - az^{-1}\cos(\omega_0)}{1 - 2az^{-1}\cos(\omega_0) + a^2z^{-2}}$	z  >  a
$a^n \sin(\omega_0 n) u[n]$	$\frac{az^{-1}\sin(\omega_0)}{1 - a2z^{-1}\cos(\omega_0) + a^2z^{-2}}$	z  >  a

 Table of Z-Transform Properties:
 For each property, assume

$$x[n] \stackrel{Z}{\longleftrightarrow} X(z)$$
 and  $y[n] \stackrel{Z}{\longleftrightarrow} Y(z)$ 

Property	Time domain	Z-domain
Linearity	Ax[n] + By[n]	AX(z) + BY(z)
Time Shifting	$x[n-n_0]$	$X(z)z^{-n_0}$
Z-scaling	$a^n x[n]$	$X(a^{-1}z)$
Conjugation	$x^*[n]$	$X^*(z^*)$
Time Reversal	x[-n]	$X(z^{-1})$
Convolution	x[n] * y[n]	X(z)Y(z)
Differentiation in z-domain	nx[n]	$-z\frac{dX(z)}{dz}$
Initial Value Theorem	x[n] is causal	$x(0) = \lim_{z \to \infty} X(z)$