

Question	# of Points Possible	# of Points Obtained	Grader
# 1	17		
# 2	16		
# 3	18		
# 4	18		
# 5	16		
# 6	14		
Total	100		

**For full credit when sketching:** remember to label axes and make locations and amplitudes clear.

**Before starting the exam, read and sign the following agreement.**

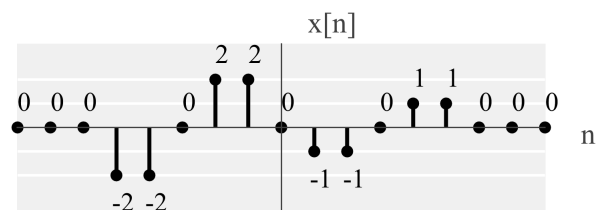
By signing this agreement, I agree to solve the problems of this exam while adhering to the policies and guidelines of the University of Florida and EEL 4750 / EEE 5502 and without additional external help. The guidelines include, but are not limited to,

- Only one 8.5 by 11 inch cheat sheet (double-sided) may be used
- No calculators or computers may be used
- No textbooks or additional notes may be used
- No collaboration is allowed
- No cheating is allowed

\_\_\_\_\_  
Student

\_\_\_\_\_  
Date

**Question #1:** Consider the discrete-time signal  $x[n]$  below.



(a) (4 pts) Sketch  $x[-2 - n]$  Remember to label your axes.

(b) (4 pts) Sketch  $2x[n] + x[n - 3]$  Remember to label your axes.

(c) (4 pts) Is the signal  $x[n]$  causal, anti-causal, or neither? **Briefly justify why.**

(d) (5 pts) Is  $x[n]$  an energy signal, a power signal, or neither? If  $x[n]$  is an energy signal, compute its energy. If  $x[n]$  is a power signal, compute its power. If  $x[n]$  is neither, explain why.

**Question #2:** Let the discrete-time signal  $z[n]$  defined by

$$z[n] = 3 \left[ \sum_{m=-\infty}^{\infty} \delta[n - (3m + 1)] - \delta[n - (3m + 2)] \right]$$

(a) (6 pts) Sketch  $z[n]$  for  $-6 \leq n \leq 6$ . Remember to label your axes.

(b) (5 pts) Is the signal  $z[n] + z[-n]$  even, odd, or neither? **Briefly justify why.**

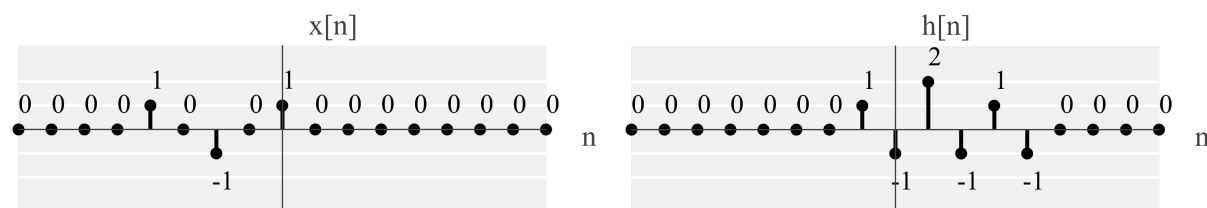
(c) (6 pts) Is  $z[n]$  an energy signal, a power signal, or neither? If  $z[n]$  is an energy signal, compute its energy. If  $z[n]$  is a power signal, compute its power. If  $z[n]$  is neither, explain why.

**Question #3:** Consider the discrete-time system expressed by the input-output relationship

$$y[n] = \sum_{m=-\infty}^n m e^{x[n]}$$

- (a) (5 pts) Is this system linear? **Justify why.**
- (b) (5 pts) Is this system time-invariant? **Justify why.**
- (c) (4 pts) Is this system causal? **Justify why.**
- (d) (4 pts) Is this system memoryless? **Justify why.**

**Question #4:** Consider a discrete-time input  $x[n]$  and impulse response  $h[n]$ .



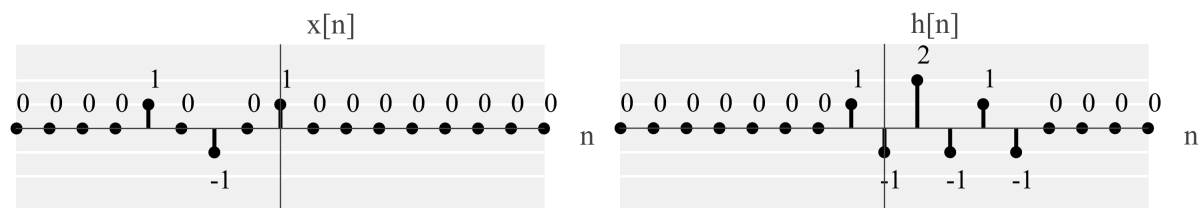
(a) (3 pts) Express  $h[n]$  as a sum of impulse signals.

(b) (3 pts) Is the system with impulse response  $h[n]$  causal?

(c) (5 pts) Sketch the output  $y[n]$  (for  $n = -8$  to  $n = 8$ ) of the discrete-time, LTI system

$$y[n] = x[n] * (3\delta[n - 2])$$

Consider a discrete-time input  $x[n]$  and impulse response  $h[n]$ .



- (d) (7 pts) Sketch the output  $y[n]$  (for  $n = -8$  to  $n = 8$ ) of the discrete-time, LTI system

$$y[n] = x[n] * h[n]$$

**Question #5:** Answer the following questions.

- (a) (5 pts) Determine the transfer function  $H(z)$  for the given difference equation

$$0 = x[n - 10] + x[n - 15] - y[n - 10] - y[n - 15]$$

- (b) (6 pts) Compute the impulse response  $h[n]$  for the given difference equation

$$y[n + 10] = (1/4)y[n + 9] + 2x[n + 10]$$

- (c) (5 pts) Determine the inverse discrete-time Fourier Transform (DTFT) of  $H(\omega)$  such that

$$H(\omega) = \frac{1 - (1/2)e^{-j\omega}}{1 + (1/2)e^{-j\omega}}$$

**Question #6:** Consider the z-transforms  $H_1(z)$  and  $H_2(z)$  below.

$$H_1(z) = \frac{4}{2 - z^{-1}} \quad , \quad H_2(z) = \frac{1 + 2z^{-1}}{1 + 4z^{-2}} + \frac{1}{1 - 2z^{-1}}$$

- (a) (5 pts) Compute the inverse z-transform of the  $H_1(z)$  such that the system is **causal**. Is the system **stable**?
- (b) (9 pts) Sketch the pole-zero plot and the region-of-convergence for  $H_2(z)$ . Assume  $H_2(z)$  is **stable**. Is the system **causal**, **anti-causal**, or **neither**?