



scalafmt: opinionated code formatter for Scala

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Abstract

Automatic code formatters bring many benefits to software development, yet they can be tricky to implement. This thesis addresses the problem of developing a code formatter for the Scala programming language that captures many popular coding styles. Our work has been limited to formatting Scala code. Still, we have developed algorithms and tools, which we believe can be of interest to developers of code formatters for other programming languages.

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1 Introduction

The main motivation of this study is to bring scalafmt, a new Scala code formatter, to the Scala community. The goal is to capture many popular coding styles so that a wide part of the Scala community can enjoy the benefits that come with automatic code formatting.

Without code formatters, software developers are responsible for manipulating all syntactic trivia in their programs. What is syntactic trivia? Consider the Scala code snippets in listings 1 and 2.

Listing 1: Unformatted code	Listing 2: Formatted code
<pre>1 // Column 35 2 object ScalafmtExample { 3 function(arg1, arg2(arg3(4 "String literal"), 5 arg4 + arg5)) 6 } 7 8</pre>	<pre>1 // Column 35 2 object ScalafmtExample { 3 function(4 arg1, 5 arg2(arg3("String literal"), 6 arg4 + arg5)) 7 } 8</pre>

Both snippets represent the same program. The only difference lies in their syntactic trivia, that is where spaces and line breaks are used. Although the whitespace does not alter the execution of the program, listing 2 is arguably easier to read, understand and maintain for the software developer. The promise of code formatters is to automatically convert any program that may contain style issues, such as in listing 1, into a readable and consistent looking program, such as in listing 2. Automatic code formatting offers several benefits.

Code formatting enables large-scale refactoring. Google used ClangFormat[19], a code formatter, to migrate legacy C++ code to the modern C++11 standard[41]. ClangFormat was used to ensure that the refactored code adhered to Google’s extensive C++ coding style[13]. Similar migrations can be expected in the near future for the Scala community once new dialects, such as Dotty[30], gain popularity.

Code formatting is valuable in collaborative coding environments. The Scala.js project[34] has over 40 contributors and the Scala.js coding style[8] – which each Scala.js contributor is expected to know by heart – is written at a whooping 2.600 words. Each contributed patch is manually verified

against the coding style by the project maintainers. This adds a burden on both contributors and maintainers. Several prominent Scala community member have raised this issue. ENSIME[10] is a popular Scala interaction mode for text editor. Sam Halliday, a maintainer of ENSIME, says “I don’t have time to talk about formatting in code reviews. I want the machine to do it so I can focus on the design.”[15]. Akka[1] is Scala library to build concurrent and distributed applications. Viktor Klang, a maintainer of Akka, suggests a better alternative “Code style should not be enforced by review, but by automate rewriting. Evolve the style using PRs against the rewriting config.”[20]. With code formatters, software developers are not burdened by whitespace trivia and can instead direct their full attention on writing correct, maintainable and fast code.

1.1 Contributions

The main contribution presented in this thesis are the following:

- scalafmt, a code formatter for the Scala programming language. At the time of this writing, scalafmt has been available for 3 months, it has been installed over 5.000 times and has already been adopted by several open source Scala libraries. For details on how to install and use scalafmt, refer to the scalafmt online documentation[11].
- algorithms and data structures to implement line wrapping under a maximum column-width limit. This work is presented in section 3.
- tools to develop and test code formatters. This work is presented in section 4.

The scalafmt formatter itself may only be of direct interest to the Scala community. However, we hope the design of scalafmt can be inspiration to code formatter developers working with other programming languages.

2 Background

This chapter explains the necessary background to understand Scala and code formatting. More specifically, we motivate why Scala presents an interesting challenge for code formatters. We go into details on Scala’s rich syntax and popular idioms that introduced unique challenges to the design of scalafmt. We follow up with a history on code formatters that have been developed over the last 70 years. We will see that although code formatters have a long history, a new tradition of optimization based formatters – which scalafmt proudly joins – started only recently in 2013.

2.1 Scala the programming language

Scala[\[27\]](#) is a general purpose programming language that was first released in 2004. Scala combines features from object-oriented and functional programming paradigms, allowing maximum code reuse and extensibility.

Scala can run on multiple platforms. Most commonly, Scala programs compile to bytecode and run on the JVM. With the releases of Scala.js[\[8\]](#), JavaScript has recently become a popular target platform for Scala developers. Even more recently, the announcement of Scala Native[\[33\]](#) shows that LLVM and may become yet another viable platform for Scala developers.

Scala is a popular programming language. The Scala Center estimates that more than half a million developers are using Scala[\[26\]](#). Large organizations such as Goldman Sachs, Twitter, IBM and Verizon run Scala code in business critical systems. The 2015 Stack Overflow Developer Survey shows that Scala is the 6th most loved technology and 4th best paying technology to work with[\[37\]](#). The popularity of Apache Spark[\[2\]](#), a cluster computing framework for large-scala data processing, has made Scala a language of choice for many developers and scientists working in big data and machine learning.

Scala is a programming language with rich syntax and many idioms. The following chapters discuss in detail several prominent syntactic features and idioms of Scala. Most importantly, we highlight coding patterns that encourage developers to write larger statements instead of many small statements. In section [3](#), we explain why large statements introduce a

Listing 3: Higher order functions

```
1 def twice(f: Int => Int) = (x: Int) => f(f(x))
2 twice(_ + 2)(6) // 10
```

Listing 4: Higher order functions expanded

```
1 def twice(f: Function[Int, Int]) =
2   new Function[Int, Int]() { def apply(x: Int) = f.apply(f.apply(x)) }
3 twice(new Function[Int, Int]() { def apply(x: Int) = x + 2 }).apply(6) // 10
```

challenge to code formatting.

2.1.1 Higher order functions

Higher order functions (HOFs) are a common concept in functional programming languages and mathematics. HOFs are functions that can take other functions as arguments as well as return functions as values. Languages that provide a convenient syntax to manipulate HOFs are said to make functions first-class citizens.

Functions are first-class citizens in Scala. Consider listing 3. The method `twice` takes an argument `f`, which is a function from an integer to an integer. The method returns a new function that will apply `f` twice to an integer argument. This small example takes advantage of several syntactic conveniences provided by Scala. For example, in line 2 the argument `_ + 3` creates a new `Function[Int, Int]` object. The function call `f(x)` is in fact sugar for the method call `f.apply(x)` on a `Function[Int, Int]` instance. Listing 4 shows an equivalent program to listing 3 without using syntactic conveniences. Observe that what was expressed as a single statement in line 1 of listing 3 is expressed with multiple statements in lines 1 and 2 of listing 4.

2.1.2 Immutability

Functional programming encourages stateless functions which operate on immutable data structures and objects. An immutable object is an object that once initialized, cannot be modified. Immutability offers several

Listing 5: Manipulating immutable list

```
1 val input = List(1, 2, 3)
2 val output = input.map(_ + 1) // List(2, 3, 4)
3                      .filter(_ > 2) // List(3, 4)
```

Listing 6: Manipulating mutable list

```
1 val input = List(1, 2, 3)
2 val output = mutable.ListBuffer.empty[Int] // mutable list
3 input.foreach { elem =>
4   if (elem + 1 > 2) { // filter
5     output += elem + 1 // map
6   }
7 }
8 output // ListBuffer(3, 4)
```

benefits to software development in areas including concurrency and testing. Listing 5 shows an example of manipulating an immutable list. Note that each `map` and `filter` operation creates a new copy of the list with the modified contents. The original list remains unchanged. Listing 6 show the equivalent operation using a mutable list. Observe that listing 5 is a single statement while listing 6 contains multiple statements.

2.1.3 SBT build configuration

SBT[32] is an interactive build tool used by many Scala projects. SBT configuration files are written in `*.sbt` or `*.scala` files using Scala syntax and semantics. Although SBT configuration files use plain Scala, they typically use coding patterns which are different from traditional Scala programs. Listing 7 is an example project definition in SBT. Observe that

Listing 7: SBT project definition

```
1 lazy val core = project
2   .settings(allSettings)
3   .settings(
4     moduleName := "scalafmt-core",
5     libraryDependencies ++= Seq(
6       "com.lihaoyi" %% "sourcecode" % "0.1.1",
7       "org.scalameta" %% "scalameta" % Deps.scalameta))
```

Listing 8: Parsing different Scala dialects with scala.meta

```
1 import scala.meta._
2 dialects.Sbt0137(
3   """lazy val root = project.dependsOn(core)
4     lazy val core = project""").parse[Source] // OK
5 dialects.Sbt0136(
6   """lazy val root = project.dependsOn(core)
7     lazy val core = project""").parse[Source] // Missing blank line
8 // Default dialect, regular Scala compilation unit
9 """lazy val root = project""").parse[Source] // No top-level statements
```

the project is defined as a single statement and makes extensive use of symbolic infix operators. Due to the nature of build configurations, argument lists to can becomes unwieldy long and a single project statement can span over dozens or even hundreds of lines of code.

2.2 scala.meta

Scala.meta^[4] is a metaprogramming toolkit for Scala. Before scala.meta, the state-of-the-art metaprogramming facilities relied on the Scala compiler internals. This had several severe limitations such as too-eager desugaring resulting in loss of syntactic details from the original source code.

Scala.meta was designed to overcome these limitations and offer a more robust platform to develop metaprogramming tools for Scala. Several key features of scala.meta have made it an invaluable companion in the development of scalafmt. Most notably among these features are dialect agnostic syntax trees, syntax tree serialization, input fidelity and algebraically typed tokens.

Scala.meta provides facilities to tokenize and parse a variety of different Scala dialects. One such dialect is SBT configuration files, discussed in section 2.1.3. SBT adds custom support for top-level statements in *.sbt files, which would otherwise result in a parse error using the Scala compiler parser. To add insult to injury, top-level statements must be separated by a blank line if you use an SBT version lower than 0.13.6; a restriction that was lifted in SBT 0.13.7. Listing 8 show how to scala.meta makes it trivial to accommodate this zoo of nuances. The result after parsing is a dialect agnostic scala.meta tree structure.

The structure of scala.meta trees can be serialized to strip off all syntactic

Listing 9: Serializing scala.meta trees

```
1 import scala.meta._
2 > """ object Main extends App { self =>
3     println(s"Hello $self!") // This is a comment
4 }""".parse[Source].get.structure
5 res0: String = """
6 Source(Seq(Defn.Object(Nil, Term.Name("Main"), Template(Nil, Seq(Ctor.Ref.Name("App
7     ")), Term.Param(Nil, Term.Name("self"), None, None), Some(Seq(Term.Apply(Term.
    Name("println"), Seq(Term.Interpolate(Term.Name("s"), Seq(Lit("Hello "), Lit
    ("!")), Seq(Term.Name("self"))))))))))))
8 """)
```

details. Listing 9 shows how to serialize the tree structure of a simple hello world application. For example, observe that the comment has been stripped away. As we discuss in section 4, this feature was instrumental in testing scalafmt.

Tree node types in `scala.meta` preserve absolute fidelity with the original source file. This means we can obtain all syntactic details from a tree node such as whether a `for` comprehension uses parentheses or curly braces as delimiters, whitespace positions and comments. The Scala compiler is infamous for desugaring `for`-comprehensions into `map/withFilter/flatMap` applications during the parse phase. This made it impossible to implement metaprogramming tasks such as code formatting. Input source fidelity in `scala.meta` has been essential to implement `scalafmt` because we need to preserve some syntactic details like where `for`-comprehension and blank lines are used.

Tokens in `scala.meta` are strongly typed. Traditional object-oriented libraries treat tokens as a single type with multiple methods such as `isComma/isFor` which returns true if a token instance is a comma or a `for` keyword. However, `scala.meta` leverages algebraic data types in Scala to represent each different kind of token as a separate type. This feature plays nicely with the pattern matching capabilities of Scala and enabled design pattern for the *Router* described in section 3.3.1.

2.3 Code formatters

Code formatting and pretty printing¹ has a long tradition. In this chapter, we look at a variety of tools and algorithm that have been developed over the last 70 years.

2.3.1 Natural language

The science of displaying aesthetically pleasing text predates as early as 1956[16]. The first efforts involved inserting carriage returns in natural language text. Until that time, writers had been responsible for manually providing carriage returns in their documents before sending them off for printing. The motivation was to “save operating labor and reduce human error”. Once type-setting became more commonplace, the methods for breaking lines of text got more sophisticated.

Knuth and Plass developed in 1981 a famous line breaking algorithm[22] for \LaTeX , a popular typesetting program among scientific academic circles. \LaTeX is the program that was used to generate this very document. The line breaking problem was the same as in the 60s: how to optimally break a paragraph of text into lines so that the right margin is minimized. The primitive approach is to greedily fit as many words on a line as possible. However, such an approach can produce embarrassingly bad output in the worst case. Knuth’s algorithm uses dynamic programming to find an optimal layout with regards to a fit function that penalizes empty space on the right margin of the paragraph. This algorithm remains a textbook example of an application of dynamic programming[9, 21].

2.3.2 ALGOL 60

Scowen[35] developed SOAP in 1971, a code formatter for ALGOL 60. The main motivation for SOAP was to make it “easier for a programmer to examine and follow a program” as well as to maintain a consistent coding style. This motivation is still relevant in modern software development.

¹ This thesis uses the term *code formatting* over *pretty printing*. According to Hughes[17], pretty printing is a subset of code formatting where the former is only concerned with presenting data structures while the latter is concerned with the harder problem of formatting existing source code — the main topic of this thesis.

Listing 10: A LISP program

```
1 (defun factorial (n)
2   (if (= n 0) 1
3       (* n (factorial (- n 1)))))
```

SOAP did provide a line length limit. However, SOAP would fail execution if the provided line length turned out to be too small. With hardware from 1971, SOAP could format 600 lines of code per minute.

2.3.3 LISP

In 1973, Goldstein[12] explored code formatting algorithms for LISP[23] programs. LISP is a family of programming languages and is famous for its parenthesized prefix notation. Listing 10 shows a program in LISP to calculate factorial numbers. The simple syntax and extensive use of parentheses as delimiters makes make LISP programs an excellent ground to study code formatters.

Goldstein presented a *recursive re-predictor* algorithm in his paper. The recursive re-predictor algorithm runs a top-down traversal on the abstract syntax tree of a LISP program. While visiting each node, the algorithms tries to first obtain a *linear-format*, i.e. fit remaining body on a single line, with a fallback to *standard-format*, i.e. each argument is put on a separate line aligned by the first argument. Goldstein observes that this algorithm is practical despite the fact that its running time is exponential in the worst case. Bill Gosper used the re-predictor algorithm to implement GRINDEF[3], one of the first code formatters for LISP.

Goldstein's contributions extend beyond formatting algorithms. Firstly, in his paper he studies how to format comments. Secondly, he presents several different formatting layouts which can be configured by the users. Both relevant concerns for modern code formatters.

2.3.4 Language agnostic

Derek C. Oppen pioneered the work on language agnostic code formatting in 1980[28]. A language agnostic formatting algorithm can be used for a

variety of programming languages instead of being tied to a single language. Users provide a preprocessor to integrate a particular programming language with the algorithm. Oppen’s algorithm runs in $O(n)$ time and uses $O(m)$ memory for an input program of length n and maximum column width m . Besides impressive performance results, Oppen claims that a key feature of the algorithms is its streaming nature. The algorithm prints formatted lines as soon as they are input instead of waiting until the entire input stream has been read. However, Oppen’s algorithm shares a worrying limitation with SOAP: it cannot handle the case when the line length is insufficiently large.

Mark van der Brand presented a library that generates a formatter given a context-free grammar[39]. Beyond the usual motivations for developing code formatters, Brand mentions that formatters “relieve documentation writers from typesetting programs by hand”. The focus on documentation is reflected by the fact that the generated formatter could produce both ASCII formatted code as well as L^AT_EX markup. Since comments are typically not included in a syntax tree, the presented algorithm has an elaborate scheme to infer the location of comments in the produced output. Like Oppen’s algorithm, this library requires the user to plug in a preprocessor to integrate a particular programming language into the Brand’s library. Unlike Oppen’s algorithm, Brand does not consider line length limits in his algorithm.

John Hughes extended on Oppen’s work on language agnostic formatting in term of functional programming techniques[17]. Hughes presented a design of a *pretty-printing* library that leverages combinators with algebraic properties to express formatting layouts. Hughes claims that such a formal approach was invaluable when designing the pretty-printing library, which has been widely used including in the Glasgow Haskell compiler. Wadler[40] and Chitil[38] extend on Hughes’s and Oppen’s work in term of performance and programming techniques. However, this branch of work has been limited to printing data structures and not how to format existing source code.

2.3.5 gofmt

`gofmt`[14] is a code formatter for the Go programming language, developed at Google. `gofmt` was released in the early days of Go in 2009 and is

noteworthy for its heavy adoption by the Go programming community. Official Go documentation[5] claims that almost all written Go code, at Google and elsewhere, is formatted with `gofmt`. Besides formatting, `gofmt` is used to automatically migrate Go codebases from legacy versions to new source-incompatible releases. However, `gofmt` supports neither a column limit nor an opinionated setting. Line breaks are preserved in the user’s input. For example, listing 11 shows a Go program that uses the same layout as the “unformatted” code (listing 1) in the introduction.

Listing 11: Gofmt example input/output

```
1 package main
2
3 func main() int {
4     function(arg1, arg2(arg3(
5         "String literal"),
6         arg4+arg5))
7 }
```

The output of running `gofmt` through listing 11 is identical to the input. This un-opinionated behavior may be considered desirable by many software developers. However, this thesis is only concerned with opinionated code formatting.

2.3.6 Scalariform

Scalariform[31] was released in 2010 and is a widely used code formatter for Scala. Like `gofmt`, Scalariform does an excellent job of tidying common formatting errors. Moreover, Scalariform supports a variety of configuration options. Scalariform is also impressively fast, it can format large files with over 4.000 lines of code in under 250 milliseconds on a modern laptop. However, Scalariform shares the same limitations with `gofmt`: it lacks a line length and opinionated setting.

Firstly, the line length setting is necessary to implement many popular coding styles in the Scala community. For example, the Spark[42] and Scala.js[8] coding styles have 100 character and 80 character column limits, respectively. As we see in other code formatters, adding a line length setting is non-trivial and doing so would require a significant redesign of Scalariform.

Secondly, the lack of an opinionated setting makes it impossible to enforce

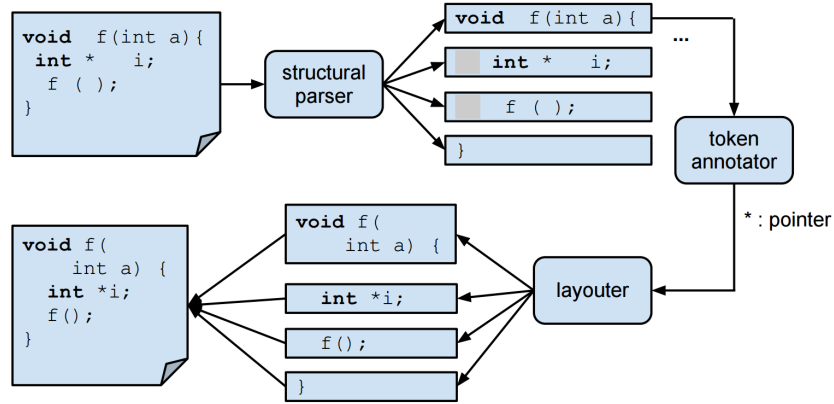


Figure 1: ClangFormat architecture

certain coding styles. For example, the Scala.js coding style enforces *bin-packing*, where arguments should be arranged compactly up to the column length limit. Listings 12 and 13 shows an example of bin packing enabled and disabled, respectively.

Listing 12: Bin-packing	Listing 13: No bin-packing
<pre> 1 // Column 35 2 class Foo(val x: Int, val y: Int, 3 val z: Int) 4 </pre>	<pre> 1 // Column 35 2 class Foo(val x: Int, 3 val y: Int, 4 val z: Int) </pre>

Since Scalariform preserves the line breaking decisions from the input, Scalariform has no setting to convert formatted code like in listing 13 to the code in listing 12.

2.3.7 clang-format

Daniel Jasper triggered a new trend in optimization based coded formatters with the release of *ClangFormat*[18] in 2013. ClangFormat is developed at Google and can format C, C++, Java, JavaScript, Objective-C and Protobuf code. Figure 1 shows the architecture of ClangFormat. The main components are the *structural parser* and the *layouter*.

ClangFormat employs a structural parser to split source code into a sequence of *unwrapped-lines*. An unwrapped line is a statement that should

Listing 14: Unformatted C++ code

```
1 int main(int argc, char const*argv[]) { Defn.Object( Nil, "ClangFormat", Term.Name("State"), Foo.Bar( Template( Nil, Seq( Ctor.Ref.Name("ClangLogger")), Term.Param( Nil, Name.Anonymous(), None, None)) ), Term.Name("clang-format" ) ); }
```

fit on a single line if given sufficient line length. A key feature of unwrapped lines is that they should not influence other unwrapped lines. The parser is lenient and parses even syntactically invalid code. The parsed unwrapped lines are passed onto the layouter.

The ClangFormat layouter uses a novel approach to implement line wrapping. Each line break is assigned a penalty according to several rules such as nesting and token type. At each token, the layouter can choose to continue on the same line or break. This forms an acyclic weighted directed graph with tokens representing vertices and splits (e.g., space, no space or line break) representing edges. The first token of an unwrapped line is the root of the graph and all paths end at the last token of the unwrapped line. The layouter uses Dijkstra's[7] shortest path algorithm to find the layout that has the lowest penalty. To obtain good performance, the layouter uses several domain specific optimizations to minimize the search space.

Despite being seemingly language independent, ClangFormat does not leverage the language agnostic formatting techniques described in section 2.3.4. Support for each language has been added as ad-hoc extensions to the ClangFormat parser and layouter. ClangFormat supports a variety of configuration options, including 6 out-of-the-box styles based on coding styles from Google, LLVM and other well-known organizations.

A notable feature of ClangFormat is that it's opinionated. ClangFormat produces well-formatted output for even the most egregiously formatted input. Listing 14 shows an offensively formatted C++ code snippet. Listing 15 shows the same snippet after being formatted with ClangFormat. ClangFormat is opinionated in the sense that it does not respect the user's line breaking decisions. This feature makes it possible to ensure that all code follows the same style guide, regardless of author.

Listing 15: ClangFormat formatted C++ code

```
1 int main(int argc, char const *argv[]) {  
2     Defn.Object(Nil, "ClangFormat", Term.Name("State"),  
3         Foo.Bar(Template(Nil, Seq(Ctor.Ref.Name("ClangLogger")),  
4             Term.Param(Nil, Name.Anonymous(), None, None))),  
5         Term.Name("clang-format"));  
6 }
```

Listing 16: Avoid dead ends

```
1 // Column 35 |  
2 function(  
3     firstCall(a, b, c, d, e),  
4     secondCall("long argument string"));
```

2.3.8 dartfmt

Dartfmt[24] was released in 2014 and follows the optimization based trend initiated by ClangFormat. Dartfmt is a code formatter for the Dart programming language, developed at Google. Like ClangFormat, dartfmt has a line length setting and is opinionated. Bob Nystrom, the author of dartfmt, discusses the design of dartfmt in an excellent post[25] on his blog. In his post, Nystrom argues that the design of a code formatters is significantly complicated by a column limit setting. The line wrapping algorithm in dartfmt employs a *best-first search*[29], a minor variant of the shortest path search in ClangFormat. As with ClangFormat, a range of domain-specific optimizations were required to make the search scale for real-world code. Listing 16 shows an example of such an optimization, *avoiding dead ends*. The snippets exceeds the 35 character column limit. A plain best-first search would perform a lot of redundant search inside the argument list of `firstCall`. However, `firstCall` already fits on a line and there is no need to explore line breaks inside its argument list. The dartfmt optimized search is able to eliminate such dead ends and quickly figure out to break before the `"long argument string"` literal.

2.3.9 rfmt

The most recent addition to the optimization based formatting trend is `rfmt`[43], a code formatter for the statistical programming environment *R*.

The formatter was released in 2016 – after the background work on this thesis started – and like its forerunners is also developed at Google. `rfmt` makes an interesting contribution in that it combines the algebraic combinator approach from Hughes[17] and the optimization based approach from L^AT_EX and ClangFormat.

The algebraic combinator approach makes it easy to express a variety of formatting layouts. `rfmt` uses 6 layout combinators or *blocks* as they are called in the report. The blocks are the following:

- *TextBlock*(*txt*): unbroken string literal.
- *LineBlock*(*b*₁, *b*₂, . . . , *b*_{*n*}): horizontal combination of blocks.
- *StackBlock*(*b*₁, *b*₂, . . . , *b*_{*n*}): vertical combination of blocks.
- *ChoiceBlock*(*b*₁, *b*₂, . . . , *b*_{*n*}): selection of a best block.
- *IndentBlock*(*n*, *l*): indent block *b* by *n* spaces.
- *WrapBlock*(*b*₁, *b*₂, . . . , *b*_{*n*}): Fit as many blocks on each line as possible, break when the column limit is exceeded and align by the first character in *b*₁.

We’ll use an example to show how these relatively few combinators allow an impressive amount of flexibility. Listings 17 and 18 shows two different layouts to format an argument list.

Listing 17: Line block		Listing 18: Stack block	
1	<code>// Column 35</code>	1	<code>// Column 35</code>
2	<code>function(argument1, argument2,</code>	2	<code>function(</code>
3	<code> argument3, argument4,</code>	3	<code> argument1, argument2, argument3,</code>
4	<code> argument5, argument6)</code>	4	<code> argument4, argument5, argument6</code>
5		5	<code>)</code>

In this case, we prefer the line block from listing 17 since it requires fewer lines. However, our preference changes if the function name is longer as is shown in listings 19 and 20.

Listing 21: Formatting layout for argument lists

```
ChoiceBlock(LineBlock(LineBlock(TextBlock(f), TextBlock("("))),
            WrapBlock(a1, ... , am),
            TextBlock(")"),
            StackBlock(LineBlock(TextBlock(f), TextBlock("("))),
            IndentBlock(4, WrapBlock(a1, ... , am)),
            TextBlock(")")).
```

Listing 19: Line block

```
1 // Column 35
2 functionNameIsLonger(argument1,
3     argument2,
4     argument3,
5     argument4,
6     argument5,
7     argument6)
8
```

Listing 20: Stack block

```
1 // Column 35
2 functionNameIsLonger(
3     argument1, argument2, argument3,
4     argument4, argument5, argument6
5 )
6
7
8
```

Here, we clearly prefer the stack block in listing 20. Listing 21 shows how we use the 6 fundamental blocks in the `rfmt` combinator algebra to express the choice between these formatting layouts. The variable f denotes the function name and a_1, \dots, a_m denote the argument list. Observe that listing 21 does not express how to find the optimal layout.

To find an optimal layout, `rfmt` employs a smart dynamic programming trick. First, it is possible to enumerate all layout combinations like the re-predictor algorithm does in section 2.3.3. This leads to exponential growth which turns out to be a problem for some cases. Dynamic programming comes to the rescue by allowing us to reuse partial solutions. Instead of re-calculating the layout cost at each (starting column, block) pair, we store the result in an associative array keyed by the starting column. However, it turns out that this can still be inefficient in terms of memory and speed². To overcome this limitation, Yelland – the `rfmt` author – presents an indexing scheme that makes it possible to extrapolate the layout cost even for missing keys. We refer to the original paper[43] for details. This novel approach enables `rfmt` to format even the most pathologically nested code in near instant time.

² In fact, ClangFormat started with a similar approach, as explained in this[6] video recording, but then switched to Dijkstra’s shortest path algorithms (which in itself is another form of dynamic programming).

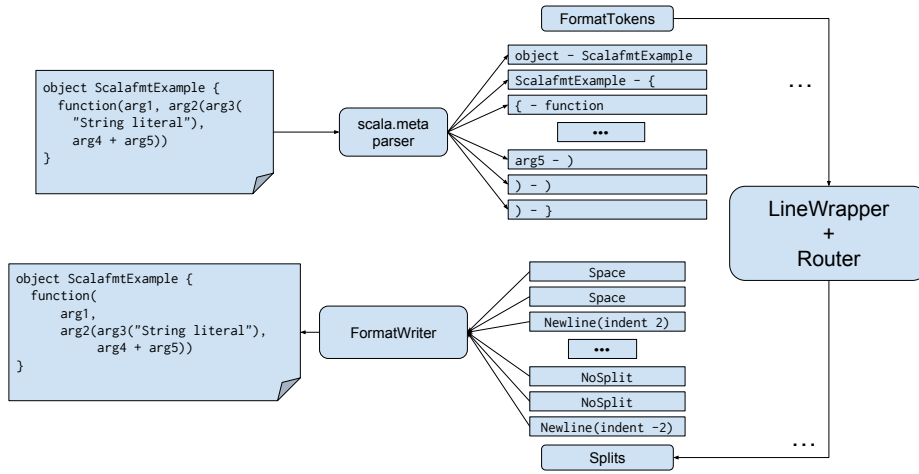


Figure 2: Scalafmt architecture

3 Algorithms

This chapter describes how scalafmt formats Scala code. We will see that scalafmt’s design is inspired by ClangFormat and dartfmt. However, we believe our design makes a valuable contribution in that it leverages functional programming principles to maximise code reuse and extensibility.

3.1 Design

Figure 2 shows a broad architectural overview of scalafmt. First, scalafmt parses a source file using `scala.meta`. Next, we feed a sequence of *FormatToken* data types into a *LineWrapper*. The *LineWrapper* uses a *Router* to construct a weighted directed graph and run a best-first search to find an optimal formatting layout for the whole file. Finally, the *LineWrapper* feeds a sequence of *Split* data types into the *FormatWriter*, which constructs a new reformatted source file. The following sections explain these data types and abstractions in detail.

3.2 Data structures

Scalafmt leverages a few carefully designed data structure to allow an implementation that emphasizes correctness and maintainability.

3.2.1 FormatToken

A *FormatToken* is a pair of two non-whitespace tokens. Listing 22 shows the definition of the *FormatToken* data type.

Listing 22: *FormatToken* definition

```
1 case class FormatToken(left: Token, right: Token, between: Vector[Whitespace])
```

As shown in the architecture overview in figure 2, each token except the beginning and end of file tokens appear twice in the sequence of *FormatTokens*: once as the *left* member and once as the *right* member. In a nutshell, the job of the *LineWrapper* is to convert each *FormatToken* into a *Split*

3.2.2 Decision

A *Decision* is a pair of a *FormatToken* and a sequence of *Splits*. Listing 23 shows the Definition of decision.

Listing 23: *Decision* definition

```
1 case class Decision(formatToken: FormatToken, splits: Seq[Split])
```

The *splits* member represents the possible splits that we can take at *formatToken*.

3.2.3 Policy

A *Policy* is an enforced formatting layout over a region. Listing 24 shows the definition of *Policy*.

Listing 24: Policy definition

```
1 case class Policy(f: PartialFunction[Decision, Decision], expire: Token)
```

A Policy is a partial function that should be applied to future Decisions up until the *expire* token. Policies easily compose using the Scala standard library `orElse` and `andThen` methods on `PartialFunction`³. This enables a high-level way to express arbitrary formatting layouts over a region of code.

3.2.4 Indent

An *Indent* describes indentation over a region of code.

Listing 25: Indent definition

```
1 sealed abstract class Length
2 case class Num(n: Int) extends Length
3 case object StateColumn extends Length
4
5 case class Indent[T <: Length](length: T, expire: Token, inclusive: Boolean)
```

Listing 25 shows the definition of *Indent* along with the algebraic data type *Length*. *Length* can either be *Num(n)* where *n* represents an explicit number of spaces to indent by or *StateColumn* which is a placeholder the number of spaces required to vertically align by the current column. *Indent* is type parameterized by *Length* so that, at some point, we can replace *StateColumn* placeholders with *Nums* to obtain a concrete number. For example, given a `scala.meta` tree `expr`, the definition `Indent(Num(2), expr.tokens.last, inclusive=true)` increases the indentation level by 2 spaces up to and including the last token of `expr`. The `inclusive` member is set to false when the indentation should expire before the expire token, for example in a block wrapped by curly braces, since the closing curly brace should not be indented by 2 spaces. The *StateColumn* placeholder is required to allow memoization of *Splits*, which is critical for performance reason as explained in section 3.3.1 on the *Router*.

³ Careful eyes will observe that *Policy* is in fact a monoid with the empty partial function as identity and function composition as associative operator.

3.2.5 Split

A *Split* represents a (possibly empty) whitespace character to be inserted between two non-whitespace tokens. Listing 26 shows the rather intricate definition of the Split data type⁴.

Listing 26: Split definition

```
1 case class Split(modification: Modification,  
2                 cost: Int,  
3                 policy: Policy,  
4                 optimalAt: Option[OptimalToken],  
5                 indents: Vector[Indent[Length]])(  
6   implicit val line: sourcecode.Line)
```

The Split data type went through several generations of design before reaching its current structure. Each member serves an important role. The most important member of the Split type is the *modification*. A modification must be one of `NoSplit`, `Space` and `Newline`. The *cost* member represents the penalty for choosing this split. The *optimalToken* member enables an optimization explained in section 3.4.1. The *indents* member contains the indentation layers that this splits adds. The *line* member allows a powerful debugging technique explained in section 3.3.1. The *policy* and *indents* members are explained in sections 3.2.3 and 3.2.4, respectively.

3.2.6 State

A *State* is a partial formatting solution during by the best-first search. Listing 27 shows the definition of the State class and companion object.

⁴ For clarity reasons, a few less important members have been removed from the actual Split definition.

Listing 27: State definition

```
1 case class State(splits: Vector[Split],
2                 totalCost: Int,
3                 policies: Vector[Policy],
4                 indents: Vector[Indent[Num]],
5                 indentation: Int,
6                 column: Int,
7                 formatOff: Boolean) extends Ordered[State] {
8
9   def compare(that: State): Int
10 }
11
12 object State {
13   def nextState(currentState: State, formatToken: FormatToken, split: Split): State
14 }
```

Observe the similarity of `State` and `Split`. A `State` contains various summaries calculated from the `splits` member. The summaries are necessary for performance reasons in the best-first search. Observe that the indents are type parameterized by `Num`, meaning they only contain concrete indentations and no `StateColumn` indents. The `indentation` member is the sum of all currently active indents and `column` represents how many characters have been consumed since the last newline. The `State` class extends the `Ordered` trait to allow for efficient polling from a priority queue. The `compare` method orders `States` firstly by their `totalCost` member, secondly by `splits.length` – how many `FormatTokens` have been formatted – and finally breaking ties by the `indentation`. The method `nextState` recalculates new summaries as efficiently as possible since the method is on a hot path in the best-first search.

3.3 LineWrapper

The `LineWrapper` is responsible for turning `FormatTokens` into `Splits`. To accomplish this, the `LineWrapper` employs a *Router* and a best-first search.

3.3.1 Router

The `Router`'s role is to produce a `Decision` given a `FormatToken`. Figure 3 shows all possible formatting layout for the small input `val x = y + z`. The `Router` must in this case figure out the correct combination of modifications and costs to associate with each `FormatToken`. This is no

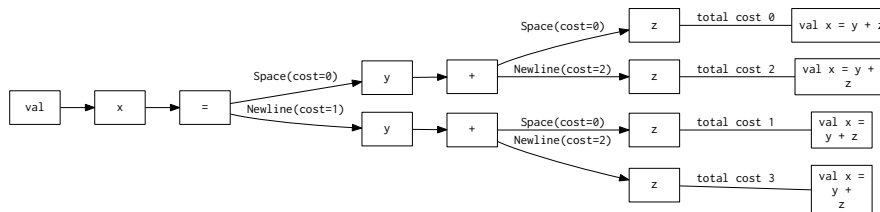


Figure 3: Example graph produced by Router

easy task since a `FormatToken` can be any pair of two tokens. How do we go about implementing a Router?

The Router is implemented as one single large pattern match on a `FormatToken`. Listing 28 shows how to pattern match on a `FormatToken`.

Listing 28: Pattern matching on `FormatToken`

```
1 formatToken match {
2   case FormatToken(_: Keyword, _) => Seq(Split(Space, 0))
3   case FormatToken(_, _: '=')    => Seq(Split(Space, 0))
4   case FormatToken(_: '=', _)    => Seq(Split(Space, 0)
5                                     Split(Newline, 1))
6   // ...
7 }
```

The pattern `_: '='` matches a `scala.meta` token of type `'='`. The underscore `_` ignores the underlying value. `Keyword` is a super-class of all `scala.meta` keyword token types. Now this pattern match quickly grows unwieldy long. How does this solution scale? Also, once the match grows bigger how can we know from which case each `Split` origins? It turns out that Scala's pattern matching and `scala.meta`'s algebraically typed tokens are able to help us.

The Scala compiler can statically detect unreachable code. If we add a case that is already covered higher up in the pattern match, the Scala compiler issues a warning. For example, listing 29 shows an example where the compiler issues a warning.

Listing 29: Unreachable code

```
1 formatToken match {
2   case FormatToken(_, _: Keyword) => Seq(Split(Space, 0))
3   // ...
4   case FormatToken(_, _: 'else')  => Seq(Newline(, 0)) // Unreachable code!
```

5 }

Here, we accidentally match on a `FormatToken` with an `else` keyword on the right which will never match because we have a broader match on a `Keyword` higher up. In this small example, the bug may seem obvious but once the Router grows bigger such issues the compiler becomes an invaluable companion. However, this still leaves us with the second question of finding the origin of each `Split`. Scala macros and implicits come to the rescue.

The origin line number of `Split` is automatically attached with each `Split`. Remember in listing 26 that the `Split` case class had an implicit member of type `sourcecode.Line`. `Sourcecode`[36] is a Scala library to extract source code metadata from your programs. The library leverages Scala macros and implicits to unobtrusively surface useful information such as line number of the origin call site. Listing 30 shows the instantiation of a `Split`.

Listing 30: Extracting line number from call site

```
1 Split(Space, 0) /* expands into */ Split(Space, 0)(sourcecode.Line(1))
```

Since there is a missing implicit `sourcecode.Line`, the Scala compiler's implicit search will invoke an implicit macro that extracts the call site line number to instantiate a `sourcecode.Line` instance. The `scalafmt` router implementation contains 88 cases and spans over 1.000 lines of code. The ability to trace the origin of each `Split` has been indispensable in the development of the Router. Once the Router can produce Decisions, we can run a best-first search to choose the optimal splits.

3.3.2 Best-first search

The Decisions from the Router produce a directed weighted graph, as demonstrated in figure 3. To find the optimal formatting layout, our challenge is to find the cheapest path from the root node to a final node. The best-first[29] algorithm is an excellent fit for the task.

Best-first search is a graph search algorithm to efficiently traverse a directed weighted graph. The objective for `scalafmt` is to choose Algorithm 1 show how a basic best-first search algorithm can be applied to finding an optimal formatting layout in `scalafmt`.

Algorithm 1: Scalafmt best-first search, v1

Input: formatTokens: List[FormatTokens], router: Router

Output: List of Splits which represent an optimal formatting layout.

```
1  /** @returns Splits that produce and optimal formatting layout */
2  def bestFirstSearch(formatTokens: FormatTokens, router: Router): List[Split] = {
3    val lastFormatToken = formatTokens.last
4    val Q = PriorityQueue(State(formatTokens.head))
5    while (Q.nonEmpty) {
6      val currentState = Q.pop
7      if (currentState.formatToken == lastFormatToken) {
8        return currentState.splits // reached the final state.
9      } else {
10       val decisions = router.getSplits(currentState.formatToken)
11       for (decision <- decisions) {
12         Q += State.nextState(currentState, decision)
13       }
14     }
15   }
16   // Error: No formatting solution found.
17   ???
18 }
```

The Router constructs a weighted directed graph that represents all possible formatting layouts for an input source code. For clarity reasons, the figure excludes trivial splits, policies and indents.

Observe that graph in listing 3 grows exponentially at every FormatToken where we have more than one Split options. If we implement the best first search naïvely Like with ClangFormat and dartfmt, a few domain-specific optimisations. This must be handled intelligently by the best-first search.

3.4 Optimizations

3.4.1 OptimalToken

3.4.2 dequeueOnNewStatements

3.4.3 recurseOnBlocks

3.4.4 escapeInPathologicalCases

3.4.5 escapeInPathologicalCases

3.4.6 pruneSlowStates

3.4.7 FormatWriter

- vertical alignment
- comment formatting
- stripMargin alignment

4 Tooling

4.1 Heatmaps

4.2 Traceability

4.3 Configuration

4.3.1 maxColumn

4.3.2 binPacking

4.3.3 vertical alignment

4.4 Unit tests

4.5 Property based tests

4.5.1 AST Integrity

4.5.2 Idempotency

4.6 Regressions tests

5 Evaluation

5.1 Micro benchmarks

5.2 Adoption

6 Discussion

6.1 Future work

6.2 Conclusion

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