# New functions for exploring multiple-QTL models

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(minor revisions 28 May 2008; further revised 18 July 2008 to discuss stepwiseqtl)

R/qtl version 1.08 included a number of new functions to simplify the exploration of multiple-QTL models. In R/qtl version 1.09, the function stepwiseqtl was added to perform a stepwise selection to identify the multiple-QTL model optimizing a penalized LOD score.

The "Brief tour of R/qtl" document contains a brief description of these functions (see Example 5 in that document); here, we provide a more thorough explanation.

### Introduction

Let us begin with a brief overview of the changes. The basic functions remain makeqt1 (for creating a QTL object), fitqt1 (for fitting a defined multiple-QTL model) and scanqt1 (for multi-dimensional scans with a multiple-QTL model).

Previously, fitqtl and scanqtl used multiple imputation exclusively. We have now implemented Haley-Knott regression as well. To use Haley-Knott regression, use the argument what="prob" in a call to makeqtl and then method="hk" in calls to fitqtl and scanqtl (and the other functions, to be described shortly).

The scanqt1 function, while completely flexible and so suitable for most purposes, is rather cumbersome to use. Our most important additions are the functions addqt1, to scan for a single QTL to be added to a multiple-QTL model, and addpair, to scan for a pair of QTL to be added to a multiple-QTL model. The output of these functions is of the forms produced by scanone and scantwo, respectively, and so one may use the corresponding plot and summary functions, making the results easier to deal with. For most purposes, these functions will be sufficient and direct calls to scanqt1 will no longer be needed. Thus, we will not discuss the use of scanqt1 further here.

The next important addition is refineqt1, which uses an iterative algorithm to refine the locations of QTL in a multiple-QTL model, with the aim of obtaining the maximum likelihood estimates of the QTL positions. If the function is called with keeplodprofile=TRUE (which is the default), one may use another new function, plotLodProfile, to plot the LOD profiles for each QTL, in the context of the multiple-QTL model, as is commonly used in multiple interval mapping.

The function addint may be used to test all possible pairwise interactions among the QTL in a multiple-QTL model.

We added several functions for manipulating a QTL object (created by makeqtl). The function addtoqtl is used to add additional QTL to an object, dropfromqtl is used to remove QTL from an object, replaceqtl is used to move a QTL to a new position, and reorderqtl is used to change the order the loci within the QTL object.

Finally, the function stepwiseqt1 may be used to perform a stepwise search for the multiple-

QTL model optimizing a penalized LOD score criterion. The function calc.penalties can be used to calculate the penalties for stepwise, using the output of a permutation test with scantwo.

## makeqtl and fitqtl

We'll look at the hyper data as an example. These data are from Sugiyama et al. (Genomics 71:70–71, 2001), and concern blood pressure in 250 male backcross mice. We'll use multiple imputation (the default), as Haley-Knott regression performs poorly in the case of selectively genotyping, which was used for the hyper data.

First we need to load the package and the data.

```
> library(qtl)
> data(hyper)
```

We will use the multiple imputation approach, and so we first run sim.geno to perform the imputations. We'll use 128 imputations; this is insufficient for the current data, which has extensive missing genotype information, but suffices to illustrate the methods. In practice, it is a good idea to repeat the analysis with independent imputations. If the results are much changed, increase the number of imputations.

```
> hyper <- sim.geno(hyper, step=2, n.draws=128, err=0.001)
```

Results of scanone and scantwo, which we won't revisit, indicated QTL on chromosomes 1, 4, 6 and 15, with an interaction between the QTL on chr 6 and 15, and the possibility of a second QTL on chr 1. We will begin by fitting this 4-QTL model. The function makeqtl is used to create a QTL object; it pulls out the imputated genotypes at the selected locations.

```
> qtl <- makeqtl(hyper, chr=c(1, 4, 6, 15), pos=c(67.3, 30, 60, 17.5))</pre>
```

Note that if you type the name of the QTL object, you get a brief summary.

```
> qtl
```

QTL object containing imputed genotypes, with 128 imputations.

Also, there is a plot function for displaying the locations of the QTL on the genetic map. See Fig. 1.

```
> plot(qtl)
```

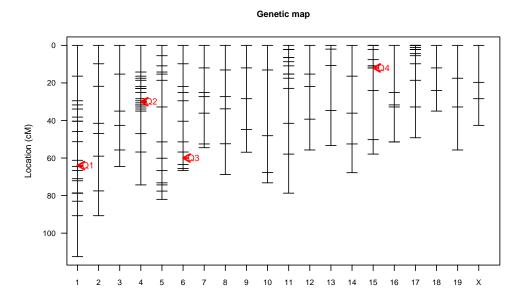


Figure 1: Locations of the QTL object qtl on the genetic map for the hyper data.

Chromosome

We may now use fitqtl to fit the model (with QTL in fixed positions). (In previous versions of R/qtl, fitqtl required a column of phenotypes, rather than a cross object, but this has been revised to make calls to fitqtl more like those to scanone, scantwo, and scanqtl.) Note that we use Q3\*Q4 to indicate that QTL 3 and 4 should interact. We could also have written the formula as  $y^Q1+Q2+Q3+Q4+Q3:Q4$ . See the help file for formula for more information.

```
> out.fg <- fitgtl(hyper, gtl=gtl, formula=y~Q1+Q2+Q3*Q4)</pre>
> summary(out.fq)
                 fitqtl summary
Method: multiple imputation
Number of observations: 250
Full model result
Model formula: y \sim Q1 + Q2 + Q3 + Q4 + Q3:Q4
           SS MS LOD %var Pvalue(Chi2) Pvalue(F) 5842 1168.5 21.8 33.1 0 0
       df
Model
        5
Error 244 11827
                   48.5
Total 249 17669
Drop one QTL at a time ANOVA table:
             df Type III SS
                                   LOD
                                           %var
                                                 F value Pvalue(Chi2) Pvalue(F)
                    1291.876
                                5.628
                                                               3.56e-07 5.05e-07
1@67.3
                                          7.312
                                                   26.653
              1
4@30
                    2949.013
                               12.086
                                         16.690
                                                   60.842
                                                               8.63e-14 1.80e-13
```

6@60	2	1635.264	7.031	9.255	16.869	9.32e-08	1.37e-07
15@17.5	2	1473.998	6.376	8.342	15.205	4.20e-07	5.98e-07
6@60:15@17.5	1	1187.869	5.196	6.723	24.507	1.00e-06	1.38e-06

The initial table indicates the overall fit of the model; the LOD score of 21.8 is relative to the null model (with no QTL). In the second table, each locus is dropped from the model, one at a time, and a comparison is made between the full model and the model with the term omitted. If a QTL is dropped, any interactions it is involved in are also dropped, and so the loci on chr 6 and 15 are associated with 2 degrees of freedom, as the 6×15 interaction is dropped when either of these QTL is dropped. The results indicate strong evidence for all of these loci as well as the interaction.

# refineqtl and plotLodProfile

Let us explore the use of refineqt1, which allows us to get improved estimates of the locations of the QTL. We use verbose=FALSE to suppress the display of tracing information.

```
> rqtl <- refineqtl(hyper, qtl=qtl, formula=y~Q1+Q2+Q3*Q4, verbose=FALSE)</pre>
```

The output is a modified QTL object, with loci in new positions. We can type the name of the new QTL object to see the new locations.

> rqtl

QTL object containing imputed genotypes, with 128 imputations.

The loci on chr 1 and 4 changed position very slightly. Let us use fitqtl to assess the improvement in fit; we'll skip the drop-one analysis.

```
Model formula: y \sim Q1 + Q2 + Q3 + Q4 + Q3:Q4
```

```
df SS MS LOD %var Pvalue(Chi2) Pvalue(F)
Model 5 5893 1178.6 22.0 33.4 0 0
Error 244 11776 48.3
Total 249 17669
```

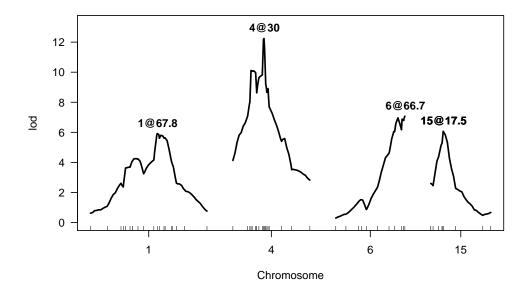


Figure 2: LOD profiles for a 4-QTL model with the hyper data.

The LOD score comparing the full model to the null model has increased by 0.2, from 21.8 to 22.0.

If refineqt1 is run with the argument keeplodprofile=TRUE (which is the default), the LOD traces at that last iteration are saved, which can then be plotted with plotLodProfile, as follows. See Fig. 2.

### > plotLodProfile(rqtl)

The LOD profiles in Fig. 2 are similar to the usual LOD curves, but instead of comparing a model with a single QTL at a particular position to the null model, we compare, at each position for a given QTL, the model with the QTL of interest at that particular position (and with the positions of all other QTL fixed at their maximum likelihood estimates) to the model with the QTL of interest omitted (and, again, with the positions of all other QTL fixed at their maximum likelihood estimates). For the loci on chromosomes 6 and 15, the 6×15 interaction is omitted when either of the two loci is omitted. Note that maximum LOD for each of the LOD profiles should be the value observed in the drop-one analysis from fitqt1.

These profile LOD curves are useful for the assessment of both the evidence for the individual QTL and the precision of localization of each QTL, but note that they fail to take account of the uncertainty in the location of the other QTL in the model.

### addint

The function addint is used to test, one at a time, all possible pairwise interactions between QTL that are not already included in a model. For our model with loci on chr 1, 4, 6 and 15, and with a  $6\times15$  interaction, we will consider each of the 5 other possible pairwise interactions, and will compare the base model (with the four QTL and just the  $6\times15$  interaction) to the model with the additional interaction included.

The syntax of the function is similar to that of fitqtl. The output is a table of results similar to that provided by the drop-one analysis of fitqtl.

> addint(hyper, qtl=rqtl, formula=y~Q1+Q2+Q3\*Q4)

Model formula:  $y \sim Q1 + Q2 + Q3 + Q4 + Q3:Q4$ 

### Add one pairwise interaction at a time table:

	df	Type III SS	LOD	%var	F value	Pvalue(Chi2)	Pvalue(F)
1067.8:4030	1	61.380843	0.283709	0.347394	1.273270	0.253	0.260
1067.8:6066.7	1	1.402998	0.006468	0.007940	0.028955	0.863	0.865
1067.8:15017.5	1	71.144546	0.328975	0.402653	1.477037	0.218	0.225
4@30:6@66.7	1	64.916064	0.300094	0.367402	1.347010	0.240	0.247
4@30:15@17.5	1	16.225653	0.074853	0.091832	0.335289	0.557	0.563

None of the interactions is particularly interesting.

Note the difference in the results if we use as the formula y Q1+Q2+Q3+Q4 (that is, omitting the  $6\times15$  interaction).

> addint(hyper, qtl=rqtl, formula=y~Q1+Q2+Q3+Q4)

Model formula:  $y \sim Q1 + Q2 + Q3 + Q4$ 

### Add one pairwise interaction at a time table:

	df	Type III SS	LOD	%var	F value	Pvalue(Chi2)	Pvalue(F)
1067.8:4030	1	60.30574	0.25455	0.34131	1.14681	0.279	0.285
1067.8:6066.7	1	11.62534	0.04898	0.06580	0.22024	0.635	0.639
1067.8:15017.5	1	86.59440	0.36589	0.49009	1.65011	0.194	0.200
4@30:6@66.7	1	39.81677	0.16793	0.22535	0.75597	0.379	0.385
4@30:15@17.5	1	58.92350	0.24870	0.33349	1.12040	0.285	0.291
6@66.7:15@17.5	1	1115.46429	4.91316	6.31314	23.11304	0.00000197	0.00000264

The  $6\times15$  interaction is also tested, and the LOD scores for the other interactions are somewhat different, as they concern comparisons between the 4-locus additive model and the model with that one interaction added.

### addqtl

We may use the addqt1 function to scan for an additional QTL, to be added to the model. By default, the new QTL is strictly additive.

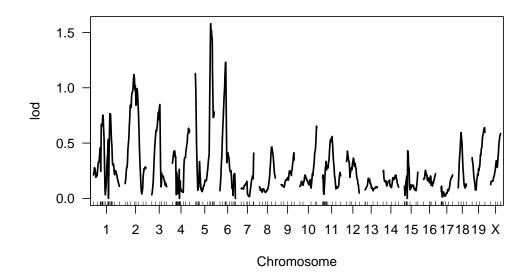


Figure 3: LOD curves for adding one QTL to the 4-QTL model, with the hyper data.

```
> out.aq <- addqtl(hyper, qtl=rqtl, formula=y~Q1+Q2+Q3*Q4)</pre>
```

The output of addqtl has the same form as that from scanone, and so we may use the same summary and plot functions. For example, we can identify the genome-wide maximum LOD score with max.scanone.

```
> max(out.aq)
```

chr pos lod D5Mit31 5 66.7 1.58

And we may plot the results with plot.scanone; see Fig. 3.

> plot(out.aq)

We may also use addqtl to scan for an additional QTL, interacting with one of the current loci. This is done by including the additional QTL in the model formula, with the relevant interaction term. For example, let's scan for an additional QTL interacting with the chr 15 locus.

> out.aqi <- addqtl(hyper, qtl=rqtl, formula=y~Q1+Q2+Q3\*Q4+Q4\*Q5)</pre>

We plot the results as follows; see Fig. 4.

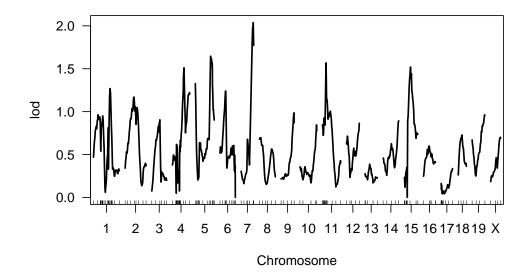


Figure 4: LOD curves for adding one QTL, interacting with the chromosome 15 locus, to the 4-QTL model, with the hyper data.

> plot(out.aqi)

Also of interest are the LOD scores for the interaction between the chr 15 locus and the new locus being scanned, which are the differences between the LOD scores in out.aqi and out.aq. See Fig. 5.

> plot(out.aqi - out.aq)

There is nothing particularly exciting in either of these plots.

## addpair

The function addpair is similar to addqt1, but performs a two-dimensional scan to seek a pair of QTL to add. By default, addpair performs a two-dimensional scan analogous to that of scantwo: for each pair of positions for the two putative QTL, we fit both an additive model and a model including an interaction between the two QTL.

Recall that in the single-QTL analysis with the hyper data, there were two peaks in the LOD curve on chromosome 1, which indicates that there may be two QTL on that chromosome. In the context of our multiple-QTL model, the LOD profile on chromosome 1 (see Fig. 2) still shows two peaks, though the distal one is more prominent.

We may use addpair to investigate the possibility of a second QTL on chromosome 1. To

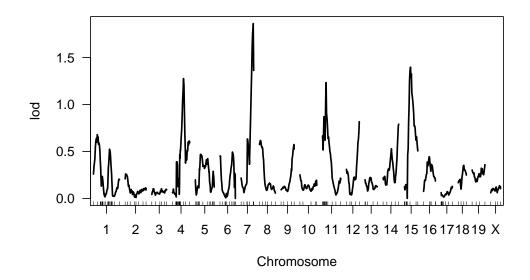


Figure 5: Interaction LOD curves in the scan for an additional QTL, interacting with the chromosome 15 locus, to the 4-QTL model, with the hyper data.

do so, we omit the chr 1 locus from our formula, and perform a two-dimensional scan just on chromosome 1.

```
> out.ap <- addpair(hyper, qtl=rqtl, chr=1, formula=y~Q2+Q3*Q4, verbose=FALSE)
```

The output is of the same form as that produced by **scantwo**, and so we may use the same summary and plot functions.

```
> summary(out.ap)
```

```
pos1f pos2f lod.full lod.fv1 lod.int pos1a pos2a lod.add lod.av1 c1:c1 43.3 73.3 7.83 1.98 0.458 45.3 77.3 7.37 1.52
```

There is little evidence for an interaction, and the LOD score comparing the model with two additive QTL on chr 1 to that with a single QTL on chr 1 is 1.52, indicating relatively weak evidence for a second QTL on chr 1.

Let us also plot the results. We'll focus on the evidence for a second QTL on the chromosome, displaying  $LOD_{fv1}$  (evidence for a second QTL, allowing for an interaction) and  $LOD_{av1}$  (evidence for a second QTL, assuming to two are additive). See Fig 6.

```
> plot(out.ap, lower="cond-int", upper="cond-add")
```

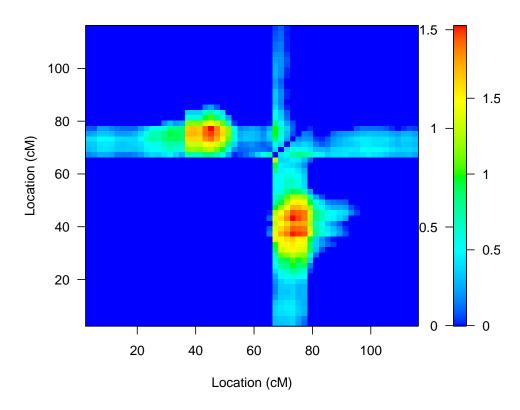


Figure 6: Results of a two-dimensional, two-QTL scan on chromosome 1, in the context of a model with additional QTL on chr 4, 6 and 15, and a  $6\times15$  interaction, with the hyper data. LOD<sub>fv1</sub> is in the lower-right triangle, and LOD<sub>av1</sub> is in the upper-left triangle.

There is a good deal of flexibility in the way that addpair may be used. As in addqt1, where one can scan for loci that interact with a particular locus in the model, we can use addpair to scan for an additional pair, with any prespecified set of interactions.

For example, we may retain the loci on chromosomes 1, 4 and 6, and scan for an additional pair of interacting loci, one of which also interacts with chromosome 6. This would be useful for assessing evidence for an additional QTL interacting with the chromosome 15 locus, but allowing the location of the locus on chromosome 15 to vary. We use the formula y~Q1+Q2+Q3+Q5\*Q6+Q3:Q5, as we will omit the chr 15 locus (Q4), scan for an additional interacting pair (Q5\*Q6), and allow the first QTL in the additional pair to interact with the chr 6 locus (Q3). Note that the positions of the chr 1, 4 and 6 loci are assumed known. A three-dimensional scan could be performed with the scanqt1 function, but we won't try that here.

To save time, we will focus just on chromosomes 7 and 15.

Because we are using a special formula here, with one of the new QTL interacting with the chr 6 locus, the results are similar to, but not quite the same as, those from scantwo. Rather than fitting an additive and an interactive model at each pair of positions, we fit just the single model specified in the formula. And note that as the formula is not symmetric in Q5 and Q6, we must do a full 2-dimensional scan, and not just on the triangle. (That is, we need Q5 and Q6 assigned to chromosomes (7,15) as well as (15,7).)

The summary of the results are somewhat different here. For each pair of chromosomes, a set of three LOD scores are presented. lod.2v0 compares the full model to the model with neither of the two new QTL included, lod.2v1b compares the full model to the model with the first of the two new QTL omitted, and lod.2v1a compares the full model to the model with the second QTL omitted. When a QTL is omitted, any interactions involving that QTL is also omitted.

### > summary(out.ap2)

```
pos1a pos2a lod.2v0 lod.2v1b lod.2v1a
c7 :c7
         29.1 25.1
                       2.89
                                2.54
                                          1.55
c7 :c15 51.1 15.5
                       3.84
                                2.51
                                          2.51
                                 7.72
         17.5
               53.1
                       8.08
                                          2.01
c15:c7
               31.5
c15:c15
        17.5
                       7.59
                                6.26
                                          1.52
```

Note that, because of the lack of symmetry in the formula we used in addpair, separate results are provided for the two cases c7:c15 (in which the chr 7 locus interacts with the chr 6 locus) and c15:c7 (in which the chr 15 locus interacts with the chr 6 locus). The c15:c7 row is most interesting, but lod.2v1a is 2.01, indicating little evidence for a chr 7 locus. (Note that lod.2v1a here concerns both the chr 7 locus and the 7×15 interaction.)

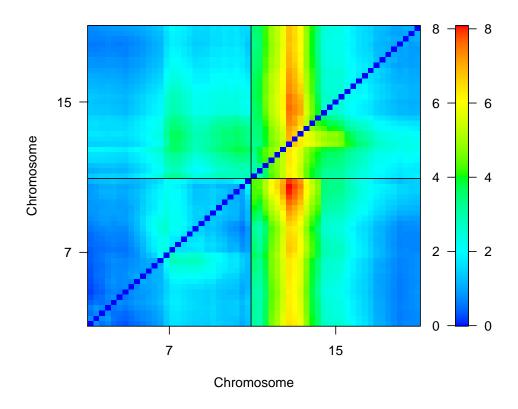


Figure 7: Results of a two-dimensional, two-QTL scan on chr 7 and 15, in the context of a model with additional QTL on chr 1, 4, and 6, with the hyper data. The two QTL being scanned were allowed to interact, and the first of them interacts with the chr 6 locus. The LOD scores displayed are for the 5-QTL model relative to the 3-QTL model. The x-axis corresponds to the first of the new QTL (which interacts with the chr 6 locus); the y-axis corresponds to the second of the new QTL.

With this sort of addpair output, the thresholds argument should have length just 1 or 2 (which is different from the usual case for summary.scantwo). Rows will be retained if lod.2v0 is greater than thresholds[1] and either of lod.2v1a or lod.2v1b is greater than thresholds[2]. (If a single thresholds is given, we assume that thresholds[2] ==0.) Note that, of the other arguments to summary.scantwo, all but allpairs is ignored.

The plot of the output from addpair, in the case of a special formula, is also different from the usual scantwo plot.

#### > plot(out.ap2)

The plot, shown in Fig. 7, contains LOD scores comparing the full 5-QTL model to the 3-QTL model (having loci on chr 1, 4 and 6). The x-axis corresponds to the first of the new QTL (Q5), which is the one that interacts with the chr 6 locus. The y-axis corresponds to the second of the new QTL (Q6). Clearly, the QTL interacting with the chr 6 locus wants to be on chr 15.

Note that the lower and upper arguments to plot.scantwo are ignored in this case.

# addtoqtl, dropfromqtl, and replaceqtl

Our analysis of the hyper data, above, did not indicate much evidence for any further QTL. If we had seen evidence for additional loci, we would want to add them to the QTL object and repeat our explorations with fitqtl, addint, addqtl, and addpair.

The functions addtoqt1, dropfromqt1 and replaceqt1 can be used to facilitate such analyses. Rather than re-creating the QTL object from scratch with makeqt1, one can use addtoqt1 to add an additional locus to a QTL object that was previously created. For example, if we were satisfied with the evidence for an additional QTL on chr 1, it could be added to the QTL object rqt1 as follows.

```
> rqtl <- addtoqtl(hyper, rqtl, 1, 43.3)
> rqtl
```

QTL object containing imputed genotypes, with 128 imputations.

```
name chr pos n.gen
Q1 1067.8 1 67.8 2
Q2 4030 4 30.0 2
Q3 6066.7 6 66.7 2
Q4 15017.5 15 17.5 2
Q5 1043.3 1 43.3 2
```

The syntax of addtoqtl is much like that of makeqtl, though one also provides the QTL object to which additional QTL are to be added.

If we want to move the first QTL on chromosome 1 to a different position (say to 73.3 cM rather than 67.8 cM), we may use replaceqt1, as follows.

```
> rqtl <- replaceqtl(hyper, rqtl, 1, 1, 73.3)
> rqtl
```

QTL object containing imputed genotypes, with 128 imputations.

```
name chr pos n.gen
Q1 1073.3 1 73.3 2
Q2 4030 4 30.0 2
Q3 6066.7 6 66.7 2
Q4 15017.5 15 17.5 2
Q5 1043.3 1 43.3 2
```

If we wish to reorder the QTL (e.g., according to their map positions), we may use reorderqt1, as follows. The argument neworder is to indicate the new order for the QTL. If missing, the QTL will be ordered by chromosome and position within a chromosome.

```
> rqtl <- reorderqtl(rqtl, c(5,1:4))
> rqtl
```

QTL object containing imputed genotypes, with 128 imputations.

```
name chr pos n.gen
Q1 1043.3 1 43.3 2
Q2 1073.3 1 73.3 2
Q3 4030 4 30.0 2
Q4 6066.7 6 66.7 2
Q5 15017.5 15 17.5 2
```

Finally, dropfromqtl is used to drop a locus from a QTL object.

```
> rqtl <- dropfromqtl(rqtl, 2)
> rqtl
```

QTL object containing imputed genotypes, with 128 imputations.

```
name chr pos n.gen
Q1 1043.3 1 43.3 2
Q2 4030 4 30.0 2
Q3 6066.7 6 66.7 2
Q4 15017.5 15 17.5 2
```

## stepwiseqtl

With the function stepwiseqt1, one may perform a forward/backward stepwise search algorithm find the multiple-QTL model optimizing a penalized LOD score criterion. The penalized LOD score for a model is the LOD score comparing the model to the null model (with no QTL), with a penalty subtracted for each main effect and separate penalties subtracted for each pairwise interactions among QTL.

We consider models with possible pairwise interactions among QTL but no higher-order interactions allowed. A hierarchy is enforced in which the inclusion of an interaction requires the inclusion of each of the corresponding main effects. Such a model may be represented by a graph in which vertices (dots) represent QTL and edges (line segments between the dots) represent interactions between QTL.

In the penalized LOD score considered by **stepwiseqt1**, we allow two penalties on interactions, a light penalty and a heavy penalty. Each disconnected component of a model is allowed one light interaction penalty; all other interactions are assigned the heavy penalty.

The three penalties may be calculed from permutation results with scantwo, using the function calc.penalties. We will use default penalties derived by computer simulation: (2.69, 2.62, 1.19) for a mouse backcross, or (3.52, 4.28, 2.69) for a mouse intercross. (The penalties are in the order (main, heavy interaction, light interaction).)

First, let us apply stepwiseqt1, considering only additive QTL models (with additive.only=TRUE. The algorithm performs forward selection up to a model with a given number of QTL (specified by the argument max.qtl; we'll use 6), followed by backward elimination.

The output is a QTL object; type the name to view the chosen model.

### > stepout1

QTL object containing imputed genotypes, with 128 imputations.

We obtain a model with two QTL, with one on each of chr 1 and 4.

Now let's re-run the analysis, allowing for the possibility of interactions among the QTL. If stepwiseqtl is called with keeptrace=TRUE, the sequence of models from the stepwise selection is retatined as an attribute.

```
> stepout2 <- stepwiseqtl(hyper, max.qtl=6, keeptrace=TRUE,
+ verbose=FALSE)</pre>
```

The chosen model contains QTL on chr 1, 4, 6 and 15, with the QTL on 6 and 15 interacting.

#### > stepout2

QTL object containing imputed genotypes, with 128 imputations.

```
name chr pos n.gen
Q1 1067.8 1 67.8 2
Q2 4030 4 30.0 2
Q3 6066.7 6 66.7 2
Q4 15017.5 15 17.5 2
Formula: y~Q1 + Q2 + Q3 + Q4 + Q3:Q4
pLOD: 10.1
```

Since we called stepwiseqt1 with the argument keeptrace=TRUE, the sequence of models visited by stepwiseqt1 are retained as an attribute (called "trace") of the output, stepout2. Attributes are a way of hiding additional information within an object. The entire set of attributes for an object may be obtained with the attributes function. It is often useful to just look at the names of the attributes.

```
> names(attributes(stepout2))
[1] "names" "class" "map" "formula" "pLOD" "trace"
```

Individual attributes may be obtained with the attr function. So we can pull out the trace of models with the following. This is a long list, with each component being a compact representation of a QTL model, and so we will print just the first of them.

It is nicer to look at a sequence of pictures rather than a long list of models. The function plotModel may be used to plot a graphical representation of a model, with nodes (i.e., dots) representing QTL and edges (i.e., line segments connecting two nodes) representing pairwise interactions among QTL. The argument chronly is used to print just the chromosome ID for each QTL (rather than chromosome and position). The penalized LOD score for each model is saved as an attribute, "pLOD"; we include them in the title of each subplot, but this requires another call to attr.

As seen in Fig. 8, our chosen model is identified immediately (at step 4). Note that the model at step 3 (with additive QTL on chr 1, 4 and 6) has a lower penalized LOD score than the model at step 2 (with just the chr 1 and 4 QTL), but then the inclusion of the chr 15 QTL and the  $6 \times 15$  interaction gave the largest penalized LOD score, among all models visited. With the addition of a QTL on chr 5 (at step 5), the pLOD decreased somewhat; the LOD score for the model increased, but not as much as the main effect penalty.

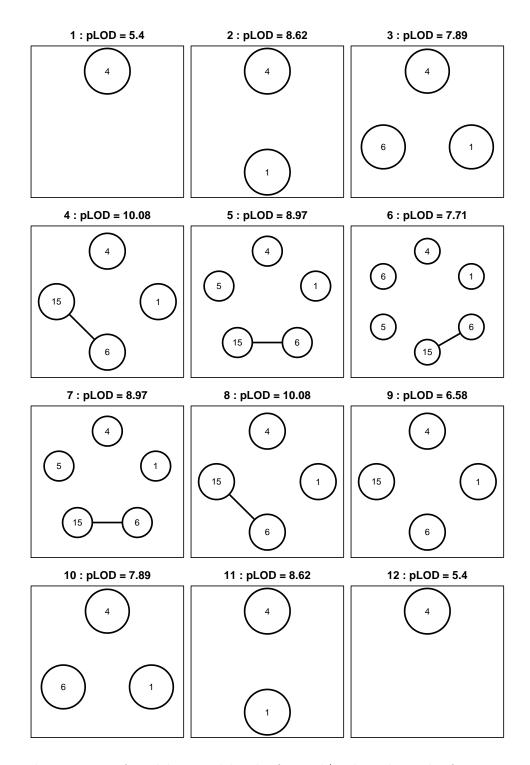


Figure 8: The sequence of models visited by the forward/backward search of stepwiseqtl, with the hyper data.