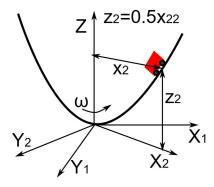
```
In [ ]: import numpy as np
    from numpy import sin,cos,pi
    import matplotlib.pyplot as plt
    from scipy.integrate import solve_ivp # import the ordinary differential equation i
    plt.style.use('fivethirtyeight')
```

## Homework #5



A roller coaster is being designed on a parabolic track that rotates at a constant speed as seen in the figure above. Assume the cart rolls on the track as a frictionless point-mass of 100-kg. Determine the equations of motion in terms of the distance from the lowest point,  $q_1=x_2$ .

- a. What is the kinetic energy of the cart?
- b. What is the potential energy of the cart?
- c. What is the equation of motion for the cart?
- 1. Create a function, cart\_ode , that represents the equation of motion for the car in terms of  $x_2$

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2. Solve the cart\_ode initial value problem for x(0)=10 m, dx/dt(0)=0 m/s and  $\omega=0$  rad/s

```
In [ ]: x0=10
v0=0
w=0 # rad/s
end_time=10 # choose an end time that displays one full period

r0 = solve_ivp(lambda t,r: cart_ode(t,r,w),[0, end_time],[x0,v0])
```

3. Solve the cart\_ode initial value problem for x(0)=3 m, dx/dt(0)=0 m/s and  $\omega=1$  rad/s

```
In [ ]: x0=10
    v0=0
    w=3
    end_time=10 # choose an end time that displays one full period

r1 = solve_ivp(lambda t,r: cart_ode(t,r,w),[0, end_time],[x0,v0])
```

4. Solve the cart\_ode initial value problem for x(0)=3 m, dx/dt(0)=0 m/s and  $\omega=2$  rad/s

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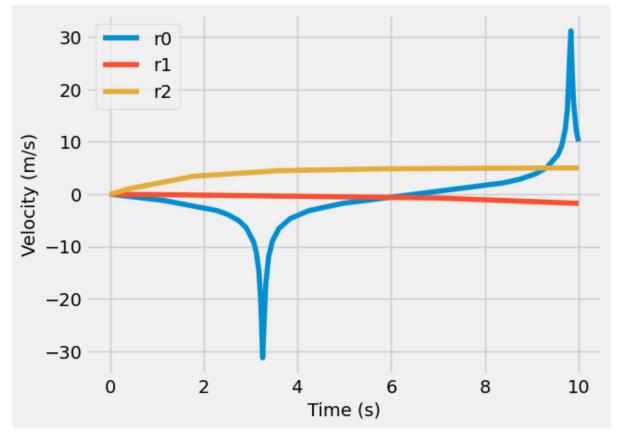
```
In [ ]: x0=10
v0=0
w=6
end_time=10 # choose an end time that displays one full period

r2 = solve_ivp(lambda t,r: cart_ode(t,r,w),[0, end_time],[x0,v0])
```

## 5. Plot the three solutions together

```
In [ ]: plt.plot(r0.t,r0.y[1],label='r0')
    plt.plot(r1.t,r1.y[1],label='r1')
    plt.plot(r2.t,r2.y[1],label='r2')
    plt.xlabel('Time (s)')
    plt.ylabel('Velocity (m/s)')
    plt.legend()
```

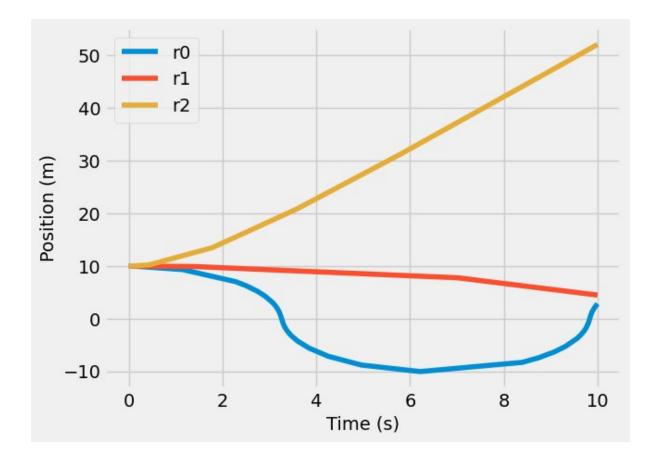
Out[ ]: <matplotlib.legend.Legend at 0x2f5f3729100>



```
In [ ]: plt.plot(r0.t,r0.y[0],label='r0')
    plt.plot(r1.t,r1.y[0],label='r1')
    plt.plot(r2.t,r2.y[0],label='r2')
    plt.xlabel('Time (s)')
    plt.ylabel('Position (m)')
    plt.legend()
```

Out[]: <matplotlib.legend.Legend at 0x2f5f4009610>

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