

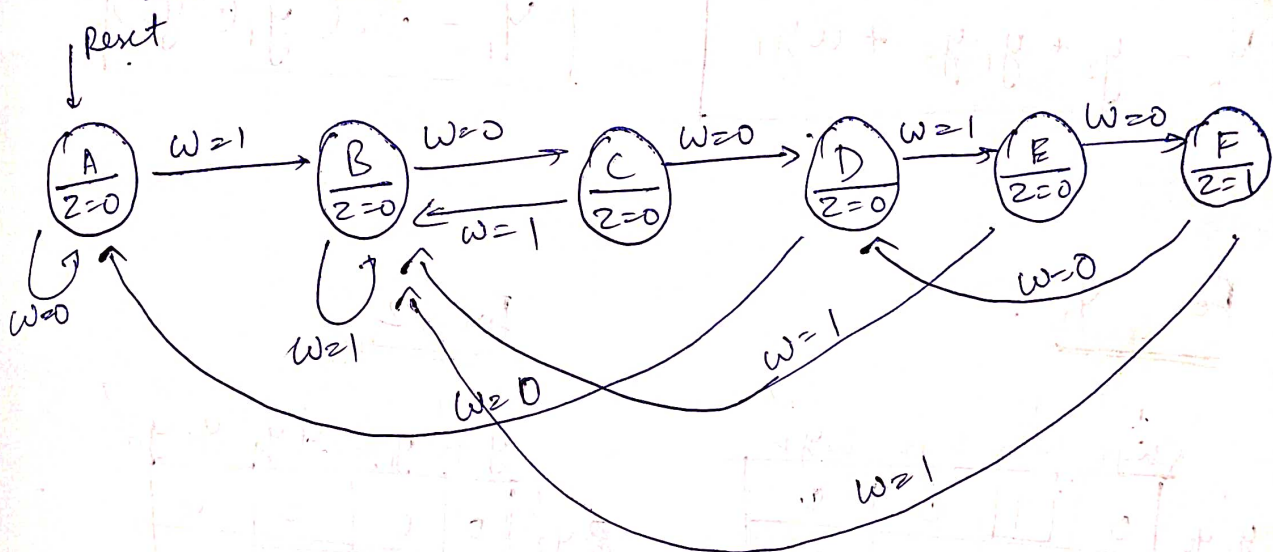
ES203 - Digital Systems

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1. i) Moore FSM : (Overlapping 10010)

* State diagram :



* State Assignment Table :

| | <u>Current State</u> | | | <u>Next State</u> | | <u>Z</u> |
|---|----------------------|----------------------|----------------------|-------------------|------------|----------|
| | <u>Y₂</u> | <u>Y₁</u> | <u>Y₀</u> | <u>W=0</u> | <u>W=1</u> | |
| A | 0 | 0 | 0 | 000(A) | 001(B) | 0 |
| B | 0 | 0 | 1 | 010(C) | 001(B) | 0 |
| C | 0 | 1 | 0 | 011(D) | 001(B) | 0 |
| D | 0 | 1 | 1 | 000(A) | 100(E) | 0 |
| E | 1 | 0 | 0 | 101(F) | 001(B) | 0 |
| F | 1 | 0 | 1 | 011(D) | 001(B) | 1 |
| G | 1 | 1 | 0 | XXX | XXX | X |
| H | 1 | 1 | 1 | XXX | XXX | X |

For Y_0 :

| | w_{y_2} | w_{y_1} | w_{y_0} | w_{y_1} |
|------------|-----------|-----------|-----------|-----------|
| y_1, y_0 | 0 | 1 | 1 | 1 |
| y_1, y_0 | 0 | 1 | 1 | 1 |
| y_1, y_0 | 0 | X | X | 0 |
| y_1, y_0 | 1 | X | X | 1 |

$$Y_0 = y_2 + y_1 \cdot y_0 + w_{y_1}$$

For Y_1 :

| | w_{y_1} | w_{y_2} | w_{y_0} | w_{y_1} |
|------------|-----------|-----------|-----------|-----------|
| y_1, y_0 | 0 | 0 | 0 | 0 |
| y_1, y_0 | 1 | 1 | 0 | 0 |
| y_1, y_0 | 0 | X | X | 0 |
| y_1, y_0 | 1 | X | X | 0 |

$$Y_1 = w_{y_1} \cdot (y_1 \oplus y_0)$$

For Y_2 :

| | w_{y_2} | w_{y_1} | w_{y_0} | w_{y_1} |
|------------|-----------|-----------|-----------|-----------|
| y_1, y_0 | 0 | 1 | 0 | 0 |
| y_1, y_0 | 0 | 0 | 0 | 0 |
| y_1, y_0 | 0 | X | X | 1 |
| y_1, y_0 | 0 | X | X | 0 |

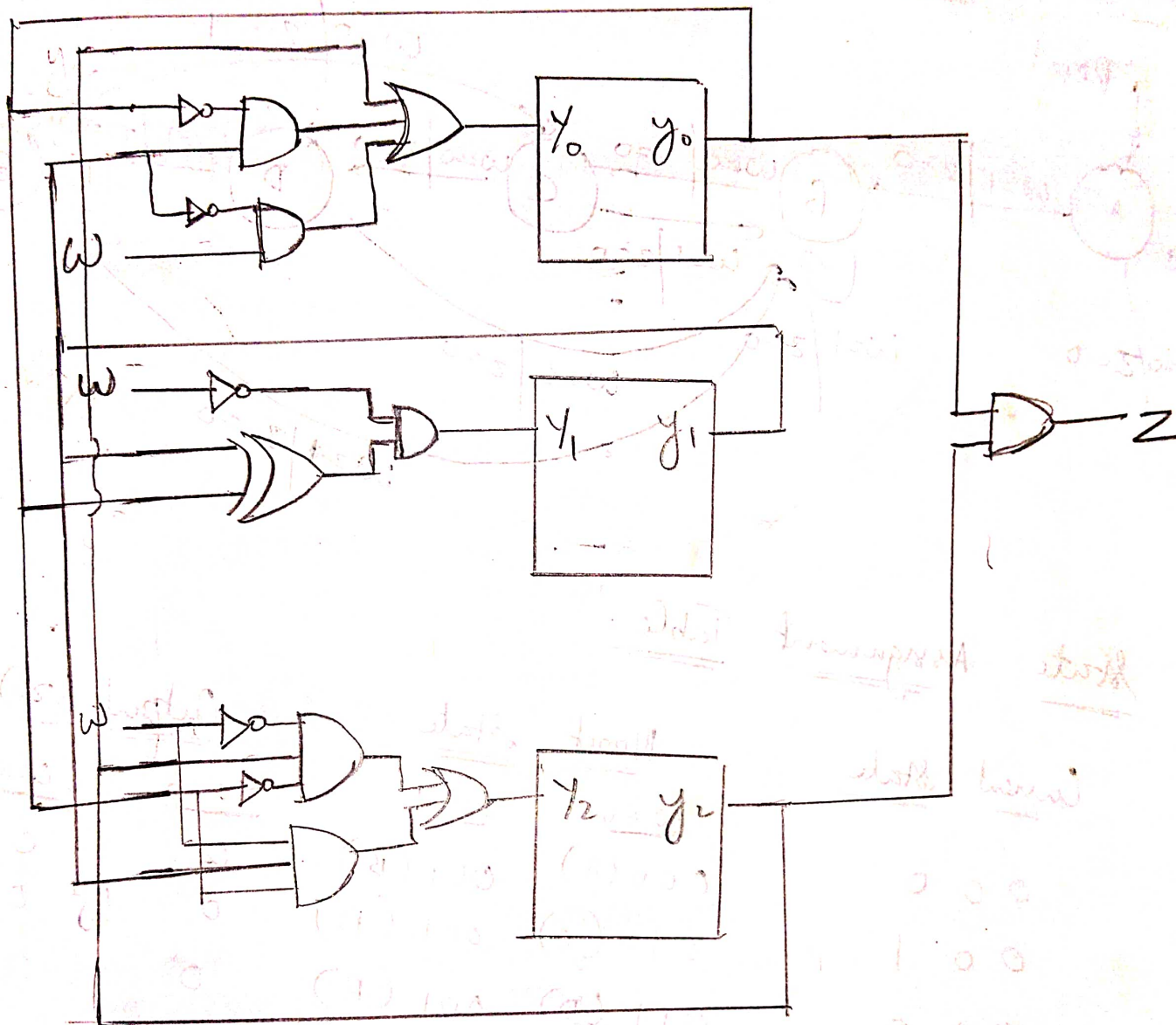
$$Y_2 = w_{y_2} \cdot y_0 + w_{y_1} \cdot y_0$$

For Z :

| | y_1, y_0 | y_1, y_0 | y_1, y_0 | y_1, y_0 |
|-------|------------|------------|------------|------------|
| y_2 | 0 | 0 | 0 | 0 |
| y_2 | 0 | 1 | X | X |

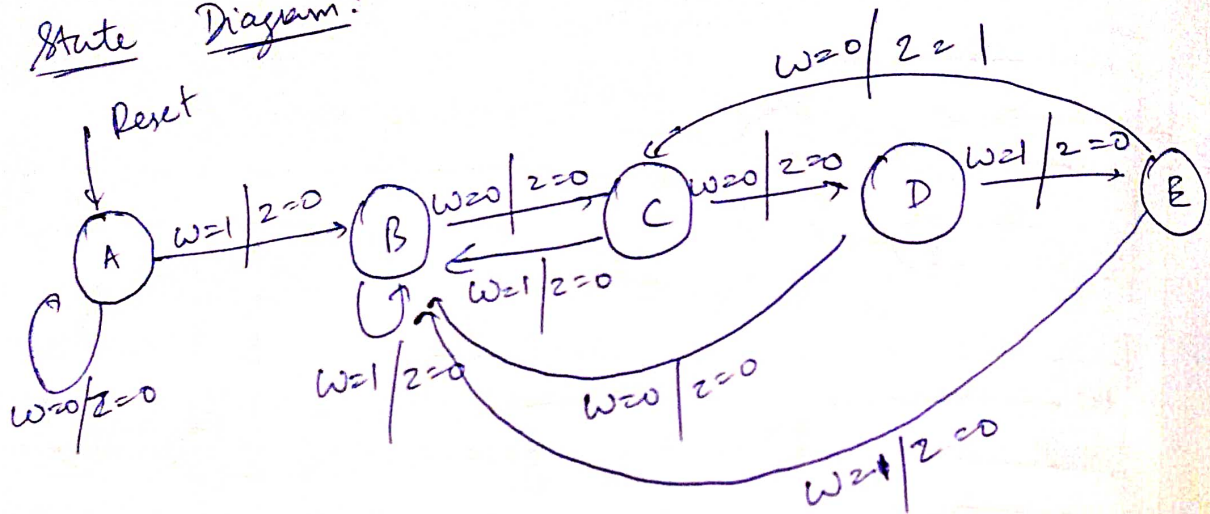
$$Z = y_2 \cdot y_0$$

* Hardware Implementation:



ii) Mealy FSM: (overlapping 10010)

* State Diagram:



* State Assignment Table:

| | <u>Current State</u> | <u>Next State</u> | | <u>Output (z)</u> | |
|---|----------------------|-------------------|------------|-------------------|------------|
| | | <u>w=0</u> | <u>w=1</u> | <u>w=0</u> | <u>w=1</u> |
| A | 0 0 0 | 0 0 0 (A) | 0 0 1 (B) | 0 | 0 |
| B | 0 0 1 | 0 1 0 (C) | 0 0 1 (B) | 0 | 0 |
| C | 0 1 0 | 0 1 1 (D) | 0 0 1 (B) | 0 | 0 |
| D | 0 1 1 | 0 0 1 (B) | 1 0 0 (E) | 0 | 0 |
| E | 1 0 0 | 0 1 0 (C) | 0 0 1 (B) | 1 | 0 |
| F | 1 0 1 | x x x | x x x | x | x |
| G | 1 1 0 | x x x | x x x | x | x |
| H | 1 1 1 | x x x | x x x | x | x |

For y_0 :

| | $w'y_2'$ | $w'y_2$ | wy_2' | wy_2 |
|------------|----------|---------|---------|--------|
| $y_1'y_0'$ | 0 | 0 | 1 | 1 |
| $y_1'y_0$ | 0 | x | x | 1 |
| y_1y_0' | 1 | x | x | 0 |
| y_1y_0 | 1 | x | x | 1 |

$$y_0 = y_1y_0' + w \cdot y_1'$$

For y_1 :

| | $w'y_2'$ | $w'y_2$ | wy_2' | wy_2 |
|------------|----------|---------|---------|--------|
| $y_1'y_0'$ | 0 | 1 | 0 | 0 |
| $y_1'y_0$ | 1 | x | x | 0 |
| y_1y_0' | 0 | x | x | 0 |
| y_1y_0 | 1 | x | x | 0 |

$$y_1 = w' \cdot (y_2 + (y_1 \oplus y_0))$$

For y_2 :

| | w_2 | w_2 | w_2 | w_2 |
|-----------|-------|-------|-------|-------|
| $y_1 y_0$ | 0 | 0 | 0 | 0 |
| $y_1 y_0$ | 0 | X | X | 0 |
| $y_1 y_0$ | 0 | X | X | 1 |
| $y_1 y_0$ | 0 | X | X | 0 |

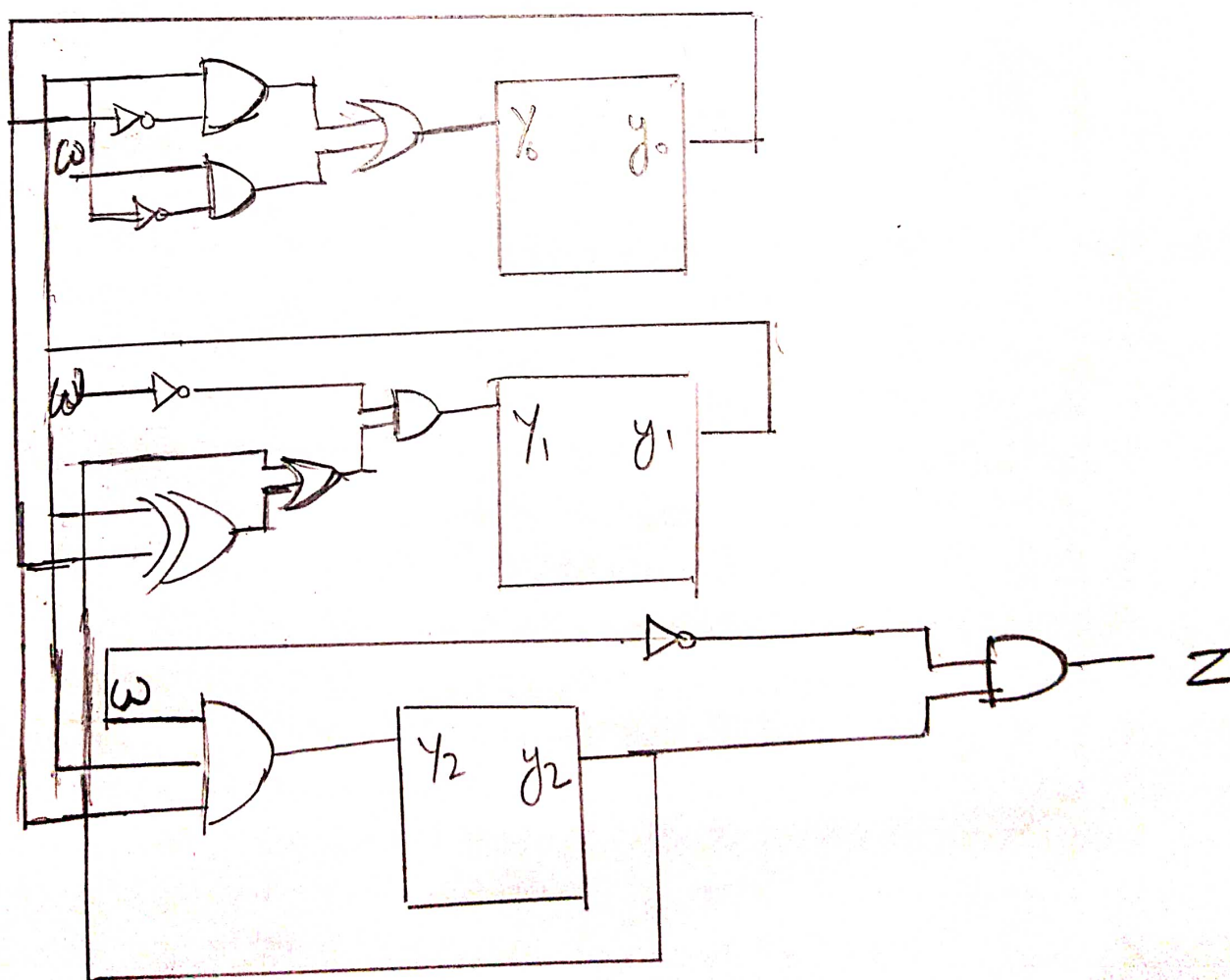
$$y_2 = w y_1 y_0$$

For z :

| | w_2 | w_2 | w_2 | w_2 |
|-----------|-------|-------|-------|-------|
| $y_1 y_0$ | 0 | 1 | 0 | 0 |
| $y_1 y_0$ | 0 | X | X | 0 |
| $y_1 y_0$ | 0 | X | X | 0 |
| $y_1 y_0$ | 0 | X | X | 0 |

$$z = w y_2$$

* Hardware Implementation:



2. Mealy FSM: State Diagram

→ (overlapping [11, 00, 11]).

