# Abstract Data Types II - Stacks & Queues

#### Doan Nhat Quang

doan-nhat.quang@usth.edu.vn University of Science and Technology of Hanoi ICT department

### Linked Lists

#### Linear Abstract Data Types:

- Lists
  - Definition: is a collection with finite number of data objects (same type) and has a finite size.
  - List ADT: Array-based Lists, Linked Lists
  - List Operations
- Stacks
- Queues

## **Today Objectives**

- Introduce the basic of Stacks and Queues: declaration, initialization, and use.
- Learn different functions, operations with Stacks and Queues: add, remove, search, etc.
- Implement examples in C/C++.

## Plan

Stacks

Queues





Stack of books



Stack of coins

#### General Definition

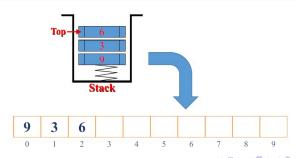
A stack is a pile of objects, typically one that is neatly arranged.

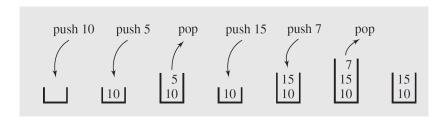
### Programming Definition

A **stack** is a container of objects that are inserted and removed according to the First In Last Out (FILO) principle.

#### **ADT Stacks**

- A linear data structure used to store data in a particular order.
- Storing and retrieving data are performed only on the top: Push inserts an element; Pop removes the last element that was added.
- Access of items in a stack is restricted, it follows First In Last Out (FILO) order.





Push and pop operations follows FILO order.

#### Stack Application

- Expression evaluation: calculate arithmetic expression.
- Backtracking: This is a process when you need to access the most recent data element in a series of elements
  - Find your way through a maze.
  - Find a path from one point in a graph (roadmap) to another point.
  - Play a game in which there are moves to be made (checkers, chess, sudoku).
- undo-mechanism in an editor



### Stack Application

#### Aerithmetic Expression:

• infix - operation between operands

$$(3+5)*10$$

• prefix - operation before operands

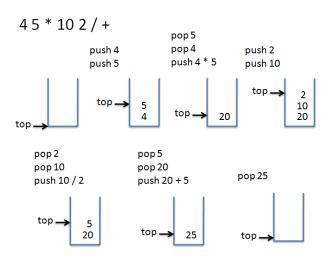
• postfix - operation after operands



### Stack Application

Aerithmetic Expression: evaluating postfix

- repeat
  - find the first operation preceded by two operands
  - evaluate and replace
- Example:



Stacks implementation may offer the possible operations:

- init(): create an empty stack.
- isEmpty(): check if the stack is empty.
- push(): add a new item at the top of a stack.
- pop(): remove the top item of a stack.
- top(): retrieve the top item of a stack.

#### Other operations can be possibly defined:

- size(): return the size of a stack.
- isFull(): check if the stack is full.
- display(): display the content of a stack.
- etc.



#### **ADT Stacks**

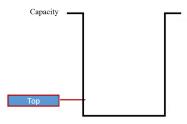
There are several solutions to the stack implementation using different declaration.

- Static array-based stack: arrays can be simply used to manipulate collections of items.
- Dynamic array-based stack: malloc() is capable of representing a stack.
- Linked stack: A very flexible mechanism for dynamic memory management is provided by pointers.

The idea is to store a stack in a fixed size static array for simple implementation.

```
• init(): this function allows to create an empty stack.

1 void init (Stack *s) {
2     I->top = -1;
3 }
```



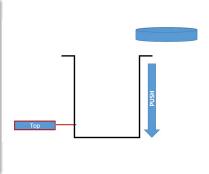
```
isEmpty(): this action allows to check if a stack is empty.
int isEmpty(Stack st){
  return (st.top < 0);
}</pre>
```

```
• size(): this function returns the stack size.

1 int size(Stack st){
2  return st.top+1;
3 }
```

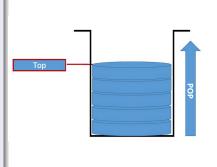
 push(): this function allows to add new item into a stack.

```
1  void push(Stack *s, int val){
2   if (isFull(*s))
3     printf(''Stack is full!'');
4   else{
5     s->top ++;
6     s->data[s->top] = val;
7   }
8 }
```



 pop(): this function allows to remove the top item from a stack,

```
1  void pop(Stack *s){
2   if (isEmpty(*s))
3     printf(''Stack empty!'');
4   else{
5     s->top --;
6   }
7  }
```



## Dynamic Array-Based Stacks

The idea is to perform the stack implementation with a dynamic array.

## Dynamic Array-Based Stacks

```
init(): this function allows to create an empty stack.

void init (Stack *s, int N) {
    s->top = 0;
    s->capacity = N;
    s->array = malloc(sizeof(<DataType>)*s->capacity);
}
```

# Array-Based Stacks

Array-based stack implementation:

#### Pros

- Simple to understand and to implement.
- Stack is assserted at the top without changing other elements.

#### Cons

• Stack size has to be manipulated.

# Stack Implementation with Linked Lists

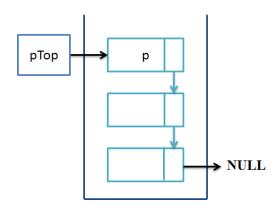
#### Definition

In this implementation, each item is placed together with the link to the next item, resulting in a simple component called a node:

- A data part stores an element value of the stack.
- A next part contains a link (or pointer) that indicates the location of the node containing the next element.

## Stack Implementation with Linked Lists

```
Implementing a stack as a linked list:
   struct _Node{
       <DataType> data;
3
        struct _Node *next;
   typedef struct _Node Node;
   struct _Stack{
        int size;
8
        Node *pTop;
9
   };
10
   typedef struct _Stack Stack;
```



# Stack Implementation with Linked Lists

```
Push operation is adapted to the new declaration:
    int Push(<DataType> newData, Stack *st){
        Node *p:
        p=(Node *) malloc(size of (Node));
4
        if (p = NULL)
 5
           return 0:
6
        p->data = newData;
        //insert at the begining of the list
8
        p\rightarrow next = st \rightarrow pTop \rightarrow next;
        st \rightarrow pTop = p;
10
        st \rightarrow size ++:
        return 1:
11
12
```

## Stack Implementation with Linked Lists

Pop operation is adapted to the new declaration:

```
1 int Pop(stack *st){
2   Node *p;
3   if (isEmpty(*st))
4       return 0; // fail to pop
5   p = st->pTop;
6   st->pTop = st->pTop->next;
7   st->size--;
8   free(p);
9   return 1;
10 }
```

# Complexity

Comparisons of complexity for different stack implementations

	push()	pop()	top()
Array-based Stacks	O(1)	O(1)	O(1)
Stacks with Linked List	O(1)	O(1)	O(1)

## Stack Implementation with Linked Lists

#### Pros

 Stack implementation with linked lists is flexible to the size and memory.

#### Cons

• If the top element is not used in the implementation, to find the top, we have to traverse all the elements in the stack.



#### General Definition

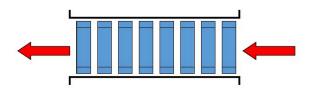
A **queue** is a line or sequence of people or vehicles awaiting their turn to be attended to or to proceed.

### Programming Definition

A **queue** is a container of objects (a linear collection) that are inserted and removed according to the first-in first-out (FIFO) principle.

#### **ADT Queues**

- A special data structure of lists used to store data in a particular order.
- Basic operations are done in both end: insert at one end (back/rear) and remove at the other end (front/head).
- Access of items in a Queue is restricted, it follows First In First Out (FIFO) order.



#### Queue Application

Typical uses of queues are in simulations and operating systems.

- Operating systems often maintain a queue of processes that are ready to execute or that are waiting for a particular event to occur.
- Anything that involves "waiting in line": printing on the computer, seating customers at a restaurant, etc.

Queues are an abstract data structure and its implementation may offer the possible operations:

- init(): initialize an empty queue.
- isEmpty(): check if the queue is empty.
- enqueue(): add a new item at the back of the queue.
- dequeue(): remove the front item of the queue.

#### Other operations can be possibly defined:

- length(): return the size of a queue.
- front(): retrieve the front item of the queue.
- isFull(): check if the queue is full.
- display(): display the content of a queue.



#### ADT Queues

There are several solutions to the queue implementation using different declaration.

- Static array-based queue: arrays can be simply used to manipulate collections of items.
- Dynamic array-based queue: malloc() is capable of representing a queue.
- Linked queue: A very flexible mechanism for dynamic memory management is provided by pointers.

# Static Array-Based Queues

The idea is to store a queue in a fixed size static array for simple implementation.

• init(): this function allows to create an empty queue.

```
1  void init(Queue *q){
2   q->front = 0;
3   q->back = 0;
4 }
```

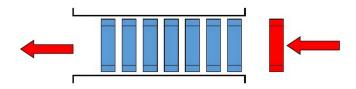
• isEmpty(): this operation verifies that a queue is empty.

```
int isEmpty(Queue *q){
    return (q->back ==0);
}
```

• length(): this operation returns the size of a queue.

```
int length(Queue *q){
    int l = q->back-q->front;
    return l;
}
```

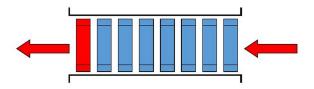
Due to the FIFO order, new items are inserted at the back of the queue. The function enqueue() allows to add new item into a queue.



There are three cases to be proceeded for enqueue(): the queue is full, empty and has at least one item.

```
int enqueue(Queue *q, <DataType> newData){
        if (length(q) = CAPACITY){
 3
            printf("Queue_is_full!");
4
            return 0;
 5
6
        if (isEmpty(q)){
           q \rightarrow val[0] = newData;
        } else {
9
               int idx = q -> back;
10
               q \rightarrow val[idx] = newData;
11
12
       q \rightarrow back++;
13
        return 1:
14
```

Due to the FIFO order, if we want to remove items from a queue, this action will be proceeded at the front of the queue. The function dequeue() asserts the deletion.



Two possible cases for dequeue() must be manipulated: when the queue is empty or not empty.

```
int dequeue(Queue *q){
        if (isEmpty(q))
 3
           return 0:
4
        else {
 5
            if (length(q) > 1){
6
               for (int i = 1; i < length(q); i++)
 7
                    q \rightarrow val[i-1] = q \rightarrow val[i];
8
9
           q->back = q->back-1;
10
11
        return 1:
12
```

## Dynamic Array-Based Queues

Dynamic array-based Queue improves the static array-based implementation.

```
1 struct _Queue{
2    int front, back;
3    int capacity;
4    <DataType> *val;
5    };
6 typedef struct _Queue Queue;
```

# Dynamic Array-Based Queues

• init(): this function allows to create an empty queue.

```
1  void init(Queue *q, int N){
2    q->back = 0;
3    q->front = 0;
4    q->capacity = N;
5    q->val = (int *) malloc(q->capacity);
6 }
```

#### Array-Based Queues

Array-based queue implementation:

#### Pros

- Simple to understand and to implement.
- Enqueue is assserted at the back without shifting elements.

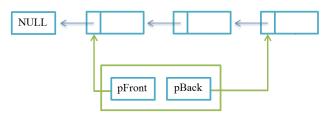
#### Cons

- Only the first element is accessible.
- All the elements have to be shifted (O(n) time for a queue with n elements) after a dequeue.

#### Definition

In this implementation, each item is placed together with the link to the next item, resulting in a simple component called a node:

- A data part stores an element value of the queue.
- A next part contains a link (or pointer) that indicates the location of the node containing the next element.
- The front element points to NULL.



3

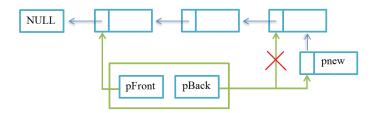
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Several basic operations are re-written to adapt to the new use of queue implementation.

```
void init(Queue *q){
q->size = 0;
q->pFront = q->pBack = NULL;
}
int isEmpty(Queue q){
return (q->qFront == NULL);
}
```

#### Enqueue opertation:

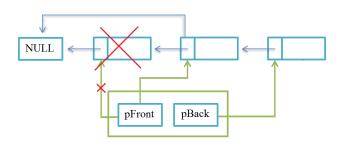
- New items are enqueued at the back of the queue.
- The back node points to new items.



```
void enqueue (Queue *q, <DataType> val){
       Node *p = (Node *) malloc(size of(Node));
3
       p->name = val;
4
       p->next = NULL;
5
       if (q \rightarrow pFront = NULL)
6
           q \rightarrow pFront = q \rightarrow pBack = p;
7
8
       else {
9
           p\rightarrow next = q\rightarrow pBack;
10
           q->pBack = p;
11
12
13
       q \rightarrow size++;
14
```

#### Dequeue opteration:

- The list should have at least one element.
- The front node points to the node that points to the first one.
- The pointer of this node points to NULL.



```
void dequeue(Queue *q){
     if (isEmpty(*q))
              return 0:
 4
          else {
 5
               if (q\rightarrow size = 1){
 6
                   q \rightarrow pFront = q \rightarrow pBack = NULL;
 7
                   q \rightarrow size --;
 8
 9
               else{
10
                   Node *p = q \rightarrow pBack;
11
                   while (p\rightarrow next !=q\rightarrow pFront)
12
                             p = p -> next;
13
                   q \rightarrow pFront = p;
14
                   q \rightarrow pFront \rightarrow next = NULL;
15
                   q \rightarrow size --;
16
17
18
          return 1;
10
```

## Complexity

Comparisons of complexity for different queue implementations

	enqueue()	dequeue()	front()
Array-based Queues	O(1)	O(n)	O(1)
Queues wLL (with pFront, pBack)	O(1)	O(n)	O(1)
Queues wLL (without pFront)	O(1)	O(n)	O(n)

#### Pros

- Flexible to the size and memory.
- Enqueue can be done without shifting elements.

#### Cons

 Have to traverse all the way to find the second element for the dequeue