Path-based depth-first search for strong and biconnected components

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Outline

Introduction

- Strong Components
 - Purdom and Munro's high-level algorithm
 - Contribution





Several Questions

- One-pass or two-pass?
- LOWPOINT?
- Ear decomposition?
- Compele version?
- Robbin's Theorem?





Questions

 "Equivalently the strong component graph is the acyclic digraph, formed by contracting vertices of G, that has an many vertices as possible." What is the meanings of this sentence?



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Pseudo-Code

```
\mathbf{H} = \mathbf{G};
   while H still has a vertex v
       start a new path P = (v);
4
       while P is not empty
5
           if the last vertex of P has an edge (v_k, w)
               if w belongs to P
6
                   find \mathbf{v} i in \mathbf{P}, which \mathbf{w} and \mathbf{v} i are
                        identical;
                   contract the cycle \mathbf{v_i}, ..., \mathbf{v_k}, both in
8
                        H and in P;
               else
9
                   add w to P, as the new last vertex of P;
10
               end if
11
```





Pseudo-Code (Continue.)

12

13

14

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16

```
else
    output v_k as a vertex of the strong component
        graph;
    {* v_k may be a set of multiple vetices in the
        original graph *}
    end if
    end
end
```



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His Contribution

 He gave a simple list-based implementation that achieves linear time.





Summary

- The first main message of your talk in one or two lines.
- The second main message of your talk in one or two lines.
- Perhaps a third message, but not more than that.

- Outlook
 - Something you haven't solved.
 - Something else you haven't solved.





For Further Reading I



A. Author.

Handbook of Everything.

Some Press, 1990.



S. Someone.

On this and that.

Journal of This and That, 2(1):50-100, 2000.



