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### Laboratory practice No. 2: Big O Notation

Juan S. Cárdenas Rodríguez

Universidad EAFIT Medellín, Colombia jscardenar@eafit.edu.co David Plazas Escudero

Universidad EAFIT Medellín, Colombia dplazas@eafit.edu.co

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### 1) CODE FOF ARRAYSUM, ARRAYMAX, INSERTIONSORT, MERGESORT WITH RANDOM ARRAYS

The .py file can be found in the "codigo" folder.

#### 2) ONLINE EXERCISES (CODINGBAT)

The source code for all 10 exercises can be found in a .java file in "ejercicioenlinea" folder.

#### 3) SIMULATION OF PROJECT PRESENTATION QUESTIONS

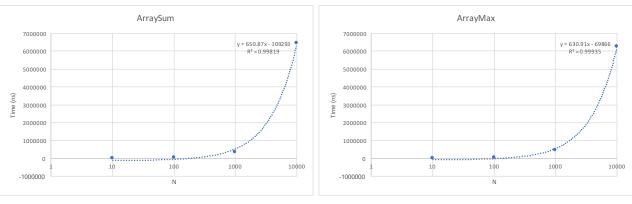
#### 3.a. Time for algorithms

$\overline{ ext{Input/Time(ns)}}$	10	100	1000	100000
ArrayMax	5000	25000	450000	6250000
ArraySum	6000	22000	348000	6410000
${f MergeSort}$	31000	291000	3734000	45673000
InsertionSort	10000	445000	47573000	4655923000

Table 1: Execution time for algorithms in nanoseconds.

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#### 3.b. Plots for execution time



(a) Time vs N for ArraySum

(b) Time vs N for ArrayMax

Figure 1: Array algorithms

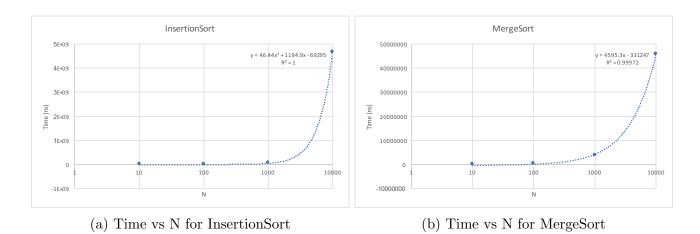


Figure 2: Sort algorithms

### 3.c. What can you say between the results obtained and the theoretical Big-O results?

According to the plots and the value of R, we can say that all of the algorithms execute within the interval of expected results; this is because all the results for R are really close to 1 (even one of them is exactly one), which allow us to affirm that the curve does indeed fit the data.

#### 3.d. What happens to insertionSort for large N?

As we see in the graphics and the values, insertion sort has a asymptotical complexity of  $n^2$ . In this manner, we can see that if we use insertion sort for big numbers it will take a enourmous amount of time, so it will not be efficient in any shape or form.



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### 3.e. What happens to arraySum for large N? Why does insertionSort increase faster?

As we know, the Big-O notation tells us how does the function behave for large values of N. arraySum only makes one simple recursive call, thus arraySum is O(n). This tells us that the execution time for arraySum increases linearly, proportional to the value of N. On the other hand, insertionSort is  $O(n^2)$ , which makes arraySum n times more efficient for the worst-case scenario.

#### 3.f. How efficient is mergeSort with respect to insertionSort for large arrays?

The asymptotic complexity of insertionSort is  $O(n^2)$ , whereas for mergeSort is  $O(n\log(n))$ ; it can be proved that  $n\log(n) < n^2, \forall n \geq 0$ , therefore, mergeSort is more efficient than mergeSort.

#### 3.g. How does maxSpan work?

```
def maxSpan(array):
    arr = []
    max = 0
    for i in range(len(array)):
        for j in range(i,len(array)):
            if array[i] == array[j]:
                 c = j-i+1
                arr.append(c)
    for i in range(len(arr)):
        if arr[i] > max:
        max = arr[i]
    return max
```

It works fairly easy. First for every data in the array of integers it moves through the same array to the same index through the end of the array searching for the number again. If it finds it again it sets the variable "c" to the numbers it has between them; it does this until the array ends. Then, it searches the array to find the biggest span and returns that number.

#### 3.h. Array II

```
i.
        public int[] zeroFront(int[] nums) {
                                                            // c0
             boolean [] used = new boolean [nums.length]; // c1
             int cont = 0;
                                                            // c2
             for (int i = 0; i < nums.length; i++) {</pre>
                                                            // c3*n
               if(nums[i] == 0) {
                                                            // c4*n
                 if (i != cont) {
                                                            // c5*n
                   nums[i] = nums[cont];
                                                            // c6+n
                   nums[cont] = 0;
                                                             // c7*n
```



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Therefore, zeroFront is  $O(c_0 + c_1 + c_2 + c_9 + (c_3 + c_4 + c_5 + c_6 + c_7 + c_8)n)$ , where n is the length of nums. Applying the sum and product properties, zeroFont is O(n).

```
ii.
                                                             // c0
       public int[] notAlone(int[] nums, int val) {
           for(int i = 1; i < nums.length-1; i++) {</pre>
                                                             // c1*n
             if(nums[i] == val && nums[i-1] != val
               && nums[i+1] != val) {
                                                             // c2*n
               if (nums[i-1] > nums[i+1])
                                                             // c3*n
                                                             // c4*n
                 nums[i] = nums[i-1];
               else
                                                             // c5*n
                 nums[i] = nums[i+1];
                                                             // c6*n
             }
           }
                                                             // c7
           return nums;
```

Therefore, notAlone is  $O(c_0 + c_7 + (c_1 + c_2 + c_3 + c_4 + c_5 + c_6)n)$ , where n is the length of nums. Applying the sum and product properties, notAlone is O(n).

tripleUp is  $O(c_0 + c_3 + (c_1 + c_2)(n-2))$ , where n is the size of nums. When we apply the product and sum properties, tripleUp is O(n).

```
// c0
iv.
     public int[] tenRun(int[] nums) {
                                                             // c1
       int tempMult = 0;
       boolean used = false;
                                                             // c2
       for(int i = 0; i < nums.length; i++) {</pre>
                                                             // c3*n
          if (nums[i] % 10 == 0) {
                                                             // c4*n
            used = true;
                                                             // c5*n
                                                             // c6*n
            tempMult = nums[i];
          }
```



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tenRun is  $O(c_0 + c_1 + c_2 + c_9 + (c_3 + c_4 + c_5 + c_6 + c_7 + c_8)n)$ , where n is the length of nums. When we apply the product and sum properties of the big-O notation, yields that tenRun is O(n).

```
public int[] shiftLeft(int[] nums) {
                                                              // c0
\mathbf{v}.
       int [] mod = new int[nums.length];
                                                              // c1
       if (nums.length==1) return nums;
                                                              // c2
       for (int i=1; i<nums.length; i++) {</pre>
                                                              // c3*n
         mod[nums.length-1]=nums[0];
                                                              // c4*n
         mod[i-1] = nums[i];
                                                              // c5*n
       }
                                                              // c6
       return mod;
     }
```

shiftleft is  $O(c_0 + c_1 + c_2 + c_6 + (c_3 + c_4 + c_5)n)$ , where n is the size of nums; which implies that shiftLeft is O(n).

#### 3.i. Array III

```
public int[] seriesUp(int n) {
                                                           // c0
i.
        int no = n*(n+1)/2;
                                                           // c2
                                                           // c3
        int [] nums = new int [no];
        int a = 0;
                                                           // c4
        for (int i = 1; i <= n; i++) {
                                                           // c5*n
          for (int j = 1; j \le i; j++) {
                                                           // c6*n*n
            nums[a] = j;
                                                           // c7*n*n
                                                           // c8*n*n
             a++;
          }
        }
                                                           // c9
        return nums;
      }
```

seriesUp is  $O(c_0 + c_1 + c_2 + c_3 + c_4 + c_9 + c_5 n + (c_6 + c_7 + c_8)n^2)$ , then seriesUp is  $O(n^2)$ .



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```
if (nums[j] != nums[i]) {
                                                     // c5*n*n
                                                     // c6*n*n
          i = j;
          C++;
                                                     // c7*n*n
        }
        if (c == 0 \&\& j == nums.length-1) {
                                                     // c8*n*n
                                                     // c9*n*n
        }
      }
    }
  }
 return c;
                                                     // c10
}
```

countClumps is  $O(c_0 + c_1 + c_10 + (c_2 + c_3)n + (c_4 + c_5 + c_6 + c_7 + c_8 + c_9)n^2)$ , where n is the length of nums; then countClumps is  $O(n^2)$ .

iii.

```
public boolean linearIn(int[] outer,
  int[] inner) {
                                                     // c1
  int j = 0;
                                                     // c2
                                                     // c3
  int c = 0;
                                                     // c4
  if (inner.length == 0) return true;
  for (int i = 0; i < outer.length; i++) {</pre>
                                                     // c5*n
                                                     // c6*n
    if (inner[j] == outer[i]) {
                                                     // c7*n
                                                     // c8*n
      if (j==inner.length) {
        return true;
                                                     // c9*n
      }
    }
  }
                                                     // c10
  return false;
}
```

linearIn is  $O(c_1 + c_2 + c_3 + c_4 + c_10 + (c_5 + c_6 + c_7 + c_8 + c_9)n)$ , where n is the size of outer; this implies that linearIn is O(n).

```
iv.
       public int[] fix45(int[] nums) {
                                                           // c1
         boolean [] arr = new boolean[nums.length];
                                                           // c2
         for (int i = 0; i < nums.length-1; i++) {
                                                          // c3*n
           if (nums[i] == 4 && nums[i+1] == 5) {
                                                          // c4*n
             arr[i+1] = true:
                                                          // c5*n
           } else if (nums[i] == 4 \&\& nums[i+1] != 5) { // c6*n}
             for (int j = 0; j < nums.length; j++) {</pre>
                                                         // c7*n*n
                if (nums[j] == 5 && arr[j] == false) {
                                                          // c8*n*n
```

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fix45 is  $O(c_1 + c_2 + c_1 3 + (c_3 + c_4 + c_5 + c_6)n + (c_7 + c_8 + c_9 + c_1 0 + c_1 1 + c_1 2)n^2)$ , where n represents the length of nums; this implies that fix45 is  $O(n^2)$ .

```
public boolean canBalance(int[] nums) {
                                                            // c0
\mathbf{v}.
                                                            // c1
         int sumRight;
         int sumLeft;
                                                            // c2
         for (int i = 1; i < nums.length; i++) {
                                                            // c3*n
                                                            // c4*n
           sumLeft = 0;
           sumRight = 0;
                                                            // c5*n
                                                            // c6*n*n
           for (int j = 0; j < i; j++) {
             sumLeft += nums[j];
                                                            // c7*n*n
           }
           for (int j = i; j < nums.length; j++) {
                                                            // c8*n*n
             sumRight += nums[j];
                                                            // c9*n*n
           }
           if (sumRight == sumLeft) {
                                                            // c10*n
             return true;
                                                            // c11*n
           }
                                                            // c12
         return false;
       }
```

canBalance is  $O(c_0 + c_1 + c_2 + (c_3 + c_4 + c_5 + c_10 + c_11)n + (c_6 + c_7 + c_8 + c_9)n^2)$ , where n is the size of nums; therefore canBalance is  $O(n^2)$ .

#### 4) EXAM SIMULATION

```
i. c) O(n+m)
```

ii. d) O(n\*m)

iii. b) O(ancho)

**iv.** b)  $O(n^3)$ 



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**v.** d)  $O(n^2)$