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Laboratory practice No. 1: Recursion

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1) ONLINE EXERCISES (CODINGBAT)

1.a. Recursion I

```
i.
                                                           // c0
        public int countPairs(String str) {
          if (str.length() <= 2) {</pre>
                                                           // c1
            return 0;
                                                           // c2
          } else if (str.charAt(0) == str.charAt(2)) { // c3}
                                                         // c4 + T(n-1)
            return 1 + countPairs(str.substring(1));
                                                           // c4
          } else {
            return countPairs(str.substring(1));
                                                          // T(n-1)
          }
        }
```

Complexity of countPairs can be writen as:

$$T(n) = \begin{cases} c_0 + c_1 + c_2 & n \le 2\\ c_3 + c_4 + T(n-1) & n > 2 \end{cases}$$

Solving the recursive equation yields:

$$T(n) = (c_3 + c_4)n + k$$

Therefore, T(n) is O(cn+k) and applying the sum and product rule T(n) is O(n).

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```
// T(n-2)
      return countHi2(str.substring(2));
    } else {
                                                 // c5
      return countHi2(str.substring(1));
                                                 // T(n-1)
  } else if (str.charAt(0) == 'h'
    && str.charAt(1) == 'i') {
                                                 // c5
                                                 // c5
    return 1 + countHi2(str.substring(1));
                                                 // c6
  } else {
                                                 // T(n-1)
    return countHi2(str.substring(1));
  }
}
```

The complexity of countHi2 can be writen as:

$$T(n) = \begin{cases} c_0 + c_1 + c_2 & n \le 1 \\ c_5 + T(n-1) & n > 1 \end{cases}$$

Solving the recursive equation for this algorithm, yields:

$$T\left(n\right) = c_5 n + k$$

Then, T(n) is $O(c_5n + k)$ and applying the sum and product rule T(n) is O(n).

```
iii.
         public int countAbc(String str) {
                                                           // c0
            if (str.length() == 0 || str.length() == 1
            || str.length() == 2) {
                                                           // c1
                                                           // c2
             return 0;
            } else if (str.charAt(0) == 'a'
              && str.charAt(1) == 'b'
              && (str.charAt(2) == 'c'
              || str.charAt(2) == 'a')) {
                                                           // c3
                                                          // c4 + T(n-1)
              return 1 + countAbc(str.substring(1));
                                                           // c5
           } else {
                                                           // T(n-1)
              return countAbc(str.substring(1));
            }
```

The complexity of countAbc can be writen as:

$$T(n) = \begin{cases} c_0 + c_1 + c_2 & n \le 2 \\ c_3 + c_4 + T(n-1) & n > 2 \end{cases} 1$$

The solution to this recursive equation yields:

$$T(n) = (c_3 + c_4)n + k$$

Therefore, T(n) is $O((c_3+c_4)n+k)$ and applying the sum and product rule T(n) is O(n).

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```
// c0
iv.
         public String parenBit(String str) {
           int a = str.length();
                                                           // c1
           if (a <= 1) {
                                                           // c2
               return "";
                                                           // c3
           }
           if (str.substring(a - 1).equals(")")) {
                                                          // c4
                                                          // c5
             int paren = str.indexOf("(");
                                                          // T(n-k)
             return str.substring(paren);
           }
           return parenBit(str.substring(0,a - 1));
                                                      // T(n-1)
         }
```

The complexity of parenBit can be writen as:

$$T(n) = \begin{cases} c_0 + c_1 + c_2 + c_3 & n \le 1 \\ c_4 + T(n-1) & n > 1 \end{cases}$$

Solving the recursive equation yields:

$$T(n) = c_4 n + k$$

Then T(n) is $O(c_4n + k)$ and applying the product and sum rules, we obtain that T(n) is O(n).

```
v. public int strCount(String str, String sub) {
    int a = str.length();
    int b = sub.length();
    if (a < b || b == 0){
        return 0;
    }
    if (str.substring(a - b).equals(sub)) {
        return 1 + strCount(str.substring(0,a - b),sub);
    }
    return strCount(str.substring(0,a - 1), sub);
}</pre>
```

1.b. Recursion II

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Complexity of splitArray can be writen as:

$$T(n) = \begin{cases} c_1 + c_2 + c_3 + c_4 & n = 0 \\ c_5 + 2T(n-1) & n \neq 0 \end{cases}$$

The solution to this recursive equation is:

$$T(n) = k2^{n-1} + (2^n - 1)(c1 + c2 + c3 + c4 + c5)$$

Then, T(n) is $O(k2^{n-1} + (2^n - 1)(c_1 + c_2 + c_3 + c_4 + c_5))$. Therefore, applying the sum and product rule T(n) is $O(2^n)$.

```
public boolean splitOdd10(int[] nums) {
ii.
           return splitOdd10Aux(nums, 0, 0, 0);
         public boolean splitOdd10Aux(int [] nums, int start,
                                                              // c1
           int first, int second) {
           if (start == nums.length) {
                                                              // c2
             return (first % 10 == 0) && (second % 2 != 0); // c3
           } else {
                                                               // c4
             return splitOdd10Aux(nums, start + 1;
               first + nums[start], second) ||
             splitOdd10Aux(nums, start + 1,
               first, second + nums[start]);
                                                              // c5 + 2T(n-1)
           }
         }
```

Complexity of split0dd10 can be writen as:

$$T(n) = \begin{cases} c_1 + c_2 + c_3 + c_4 & n = start \\ c_5 + 2T(n-1) & n \neq start \end{cases}$$

The solution to this recursive equation is:

$$T(n) = k2^{n-1} + (2^n - 1)(c1 + c2 + c3 + c4 + c5)$$

Then, T(n) is $O(k2^{n-1} + (2^n - 1)(c1 + c2 + c3 + c4 + c5))$. Therefore, applying the sum and product rule T(n) is $O(2^n)$.

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```
iii.
           public boolean groupSumClump(int start, int[] nums,
             int target) {
                                                                        // c1
             if (start >= nums.length) {
                                                                         // c2
                return target == 0;
                                                                         // c3
             }
             int sum = 0;
                                                                         // c4
                                                                         // c5
             int i;
             for (i = start; i < nums.length; i++) {</pre>
                                                                        // c6 * n
                if (nums[i] == nums[start]) {
                                                                        // c7 * n
                  sum += nums[start];
                                                                        // c8 * n
                } else {
                                                                         // c9 * n
                                                                         // c10 * n
                  break:
                }
             }
             return groupSumClump(i, nums, target - sum)
                                                                        // c12 + 2T(n-1)
             || groupSumClump(i, nums, target);
           }
    Can be writen as:
    T(n) = \begin{cases} c_3 & n \leq \text{start} \\ c_1 + c_2 + c_4 + c_5 + c_{12} + (c_6 + c_7 + c_8 + c_9 + c_{10}) n + 2T(n-1) & n > start \end{cases}
    The solution to this recursive equation is:
                        T(n) = 2^{n-1}(c+4c_1) + c_2(2^n-1) - c_1(n+2).
    Then, T(n) is O(2^{n-1}(c+4c_1)+c_2(2^n-1)-c_1(n+2))
    Therefore, applying the sum and product rule T(n) is O(2^n).
```

```
public boolean groupSum5(int start, int[] nums, int target) {
iv.
                                                     // c1
          if (start == nums.length) {
           return target == 0;
                                                     // c2
                                                     // c3
          } else {
            if (nums[start] % 5 == 0) {
                                                     // c4
             return groupSum5(start + 1, nums,
             target - nums[start]);
                                                     // c5 + T(n-1)
            } else if (start > 0 && nums[start] == 1
             && nums[start - 1] % 5 == 0) {
                                                     // c6
             return groupSum5(start + 1, nums, target); // c7 + T(n-1)
                                                     // c8
            } else {
             return groupSum5(start + 1, nums,
             target - nums[start])
             }
```



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} }

Taking into account that the case $c_9 + 2T(n-1)$ is the worst out of all, we can write the recursive equation as:

$$T(n) = \begin{cases} c_2 & n = start \\ c_1 + c_3 + c_4 + c_6 + c_8 + c_9 + 2T(n-1) & n \neq start \end{cases}$$

The solution to this recursive equation is:

$$T(n) = (c_1 + c_3 + c_4 + c_6 + c_8 + c_9)(2^n - 1) + c2^{n-1}$$

```
public boolean split53(int[] nums) {
\mathbf{v}.
           return split53Aux(nums, 0, 0, 0);
         }
        public boolean split53Aux(int [] nums, int start,
           int first, int second) {
           if (start == nums.length) {
             return first == second;
           } else {
             if (nums[start] % 5 == 0) {
               return split53Aux(nums, start + 1, first + nums[start], second);
             } else if (nums[start] % 3 == 0) {
               return split53Aux(nums, start + 1, first, second + nums[start]);
             } else {
               return split53Aux(nums, start + 1, first + nums[start], second)
               || split53Aux(nums, start + 1, first, second + nums[start]);
             }
          }
         }
```

[3]

2) What did you learn about Stack Overflow?

The Stack Overflow error is caused by a bad recursive call -for example you do not make the problem simpler every time you make a recursive call- or when you do not have a stopping condition.[2] Java Stack memory is used for execution of a thread. Whenever a method is invoked, a new block is created in the stack memory for the method to hold local primitive values and reference to other objects in the method.[1]



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References

- [1] Pankaj. Java heap space vs. stack memory allocation in java. http://www.journaldev.com/4098/java-heap-space-vs-stack-memory, 2017.
- [2] Sean. What is a stackoverflowerror? https://stackoverflow.com/questions/214741/what-is-a-stackoverflowerror, 2008.
- [3] WolframAlpha. https://www.wolframalpha.com/.