

Laboratory practice No. 2: Big O Notation

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1) CODE FOR ARRAYSUM, ARRAYMAX, INSERTIONSORT, MERGESORT WITH RANDOM ARRAYS

The .java file can be found in the “codigo” folder.

2) ONLINE EXERCISES (CODINGBAT)

The source code for all 10 exercises can be found in a .java file in “ejercicioonlinea” folder.

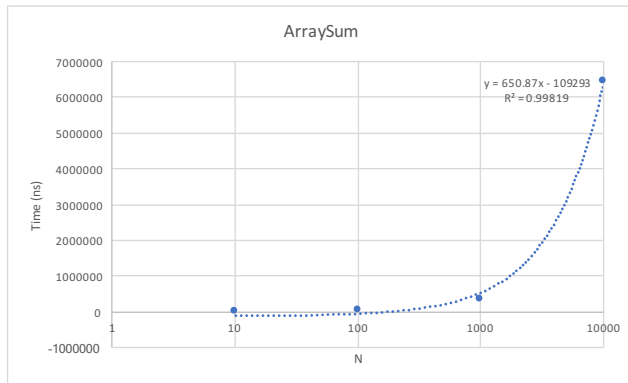
3) SIMULATION OF PROJECT PRESENTATION QUESTIONS

3.a. Time for algorithms

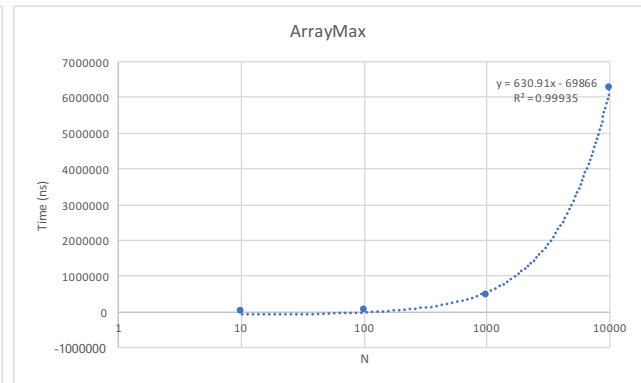
Input/Time(ns)	10	100	1000	100000
ArrayMax	5000	25000	450000	6250000
ArraySum	6000	22000	348000	6410000
MergeSort	31000	291000	3734000	45673000
InsertionSort	10000	445000	47573000	4655923000

Table 1: My caption

3.b. Plots for execution time

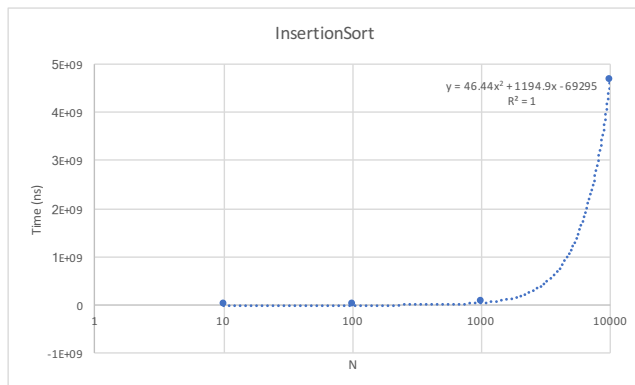


(a) Time vs N for ArraySum

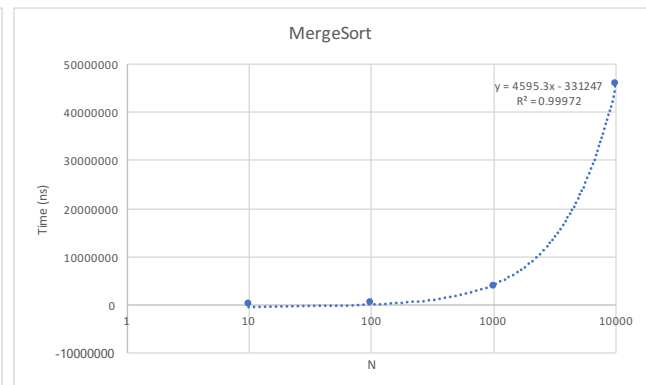


(b) Time vs N for ArrayMax

Figure 1: Array algorithms



(a) Time vs N for InsertionSort



(b) Time vs N for MergeSort

Figure 2: Sort algorithms

3.c. What can you say between the results obtained and the theoretical Big-O results?

According to the plots and the value of R, we can say that all of the algorithms execute within the interval of expected results; this is because all the results for R are really close to 1 (even one of them is exactly one), which allow us to affirm that the curve does indeed fit the data.

3.d. What happens to insertionSort for large N?

As we see in the graphics and the values, insertion sort has a asymptotical complexity of n^2 . In this manner, we can see that if we use insertion sort for big numbers it will take a enormous amount of time, so it will not be efficient in any shape or form.

3.e. How does *maxSpan* work?

```
def maxSpan(array):
    arr = []
    max = 0
    for i in range(len(array)):
        for j in range(i, len(array)):
            if array[i] == array[j]:
                c = j-i+1
            arr.append(c)
    for i in range(len(arr)):
        if arr[i] > max:
            max = arr[i]
    return max
```

It works fairly easy. First for every data in the array of integers it moves through the same array to the same index through the end of the array searching for the number again. If it finds it again it sets the variable “c” to the numbers it has between them; it does this until the array ends. Then, it searches the array to find the biggest span and returns that number.

3.f. Array II

```
i.    public int[] zeroFront(int[] nums) {           // c0
        boolean [] used = new boolean [nums.length]; // c1
        int cont = 0;                               // c2
        for (int i = 0; i < nums.length; i++) {      // c3*n
            if(nums[i] == 0) {                       // c4*n
                if (i != cont) {                     // c5*n
                    nums[i] = nums[cont];            // c6+n
                    nums[cont] = 0;                  // c7*n
                }
                cont++;                               // c8*n
            }
        }
        return nums;                                // c9
    }
```

Therefore, **zeroFront** is $O(c_0 + c_1 + c_2 + c_9 + (c_3 + c_4 + c_5 + c_6 + c_7 + c_8)n)$, where n is the length of **nums**. Applying the sum and product properties, **zeroFont** is $O(n)$.

```
ii.   public int[] notAlone(int[] nums, int val) {   // c0
        for(int i = 1; i < nums.length-1; i++) {    // c1*n
            if(nums[i] == val && nums[i-1] != val
                && nums[i+1] != val) {               // c2*n
                if (nums[i-1] > nums[i+1])           // c3*n
```

```

        nums[i] = nums[i-1];           // c4*n
    else                               // c5*n
        nums[i] = nums[i+1];           // c6*n
    }
}
return nums;                           // c7
}

```

Therefore, `notAlone` is $O(c_0 + c_7 + (c_1 + c_2 + c_3 + c_4 + c_5 + c_6)n)$, where n is the length of `nums`. Applying the sum and product properties, `notAlone` is $O(n)$.

```

iii. public boolean tripleUp(int[] nums) {           // c0
    for (int i = 0; i < nums.length - 2; i++) {      // c1*(n-2)
        if(nums[i] + 1 == nums[i+1] && nums[i]
            + 2 == nums[i+2]) return true;           // c2*(n-2)
    }
    return false;                                    // c3
}

```

`tripleUp` is $O(c_0 + c_3 + (c_1 + c_2)(n - 2))$, where n is the size of `nums`. When we apply the product and sum properties, `tripleUp` is $O(n)$.

```

iv. public int[] tenRun(int[] nums) {                // c0
    int tempMult = 0;                                // c1
    boolean used = false;                             // c2
    for(int i = 0; i < nums.length; i++) {            // c3*n
        if (nums[i] % 10 == 0) {                      // c4*n
            used = true;                               // c5*n
            tempMult = nums[i];                        // c6*n
        }
        if(used)                                       // c7*n
            nums[i] = tempMult;                       // c8*n
    }
    return nums;                                       // c9
}

```

`tenRun` is $O(c_0 + c_1 + c_2 + c_9 + (c_3 + c_4 + c_5 + c_6 + c_7 + c_8)n)$, where n is the length of `nums`. When we apply the product and sum properties of the *big - O* notation, yields that `tenRun` is $O(n)$.

```

v. public int[] shiftLeft(int[] nums) {              // c0
    int [] mod = new int[nums.length];               // c1
    if (nums.length==1) return nums;                 // c2
    for (int i=1; i<nums.length; i++) {              // c3*n
        mod[nums.length-1]=nums[0];                  // c4*n
    }
}

```

```

        mod[i-1]=nums[i];           // c5*n
    }
    return mod;                     // c6
}

```

shiftleft is $O(c_0 + c_1 + c_2 + c_6 + (c_3 + c_4 + c_5)n)$, where n is the size of `nums`; which implies that `shiftLeft` is $O(n)$.

3.g. Array III

```

i.    public int[] seriesUp(int n) {           // c0
        int no = n*(n+1)/2;                   // c2
        int [] nums = new int [no];          // c3
        int a = 0;                           // c4
        for (int i = 1; i <= n; i++) {        // c5*n
            for (int j = 1; j <= i; j++) {      // c6*n*n
                nums[a] = j;                   // c7*n*n
                a++;                           // c8*n*n
            }
        }
        return nums;                         // c9
    }

```

`seriesUp` is $O(c_0 + c_1 + c_2 + c_3 + c_4 + c_9 + c_5n + (c_6 + c_7 + c_8)n^2)$, where n is the length of `seriesUp`; then `seriesUp` is $O(n^2)$.

```

ii.   public int countClumps(int[] nums) {     // c0
        int c = 0;                             // c1
        for (int i = 0; i < nums.length-1; i++) { // c2*n
            if (nums[i] == nums[i+1]) {          // c3*n
                for (int j = i; j < nums.length; j++) { // c4*n*n
                    if (nums[j] != nums[i]) {      // c5*n*n
                        i = j;                     // c6*n*n
                        c++;                       // c7*n*n
                    }
                    if (c == 0 && j == nums.length-1) { // c8*n*n
                        c++;                       // c9*n*n
                    }
                }
            }
        }
        return c;                             // c10
    }

```

countClumps is $O(c_0 + c_1 + c_1 0 + (c_2 + c_3)n + (c_4 + c_5 + c_6 + c_7 + c_8 + c_9)n^2)$, where n is the length of countClumps; then countClumps is $O(n^2)$.

iii.

```
public boolean linearIn(int[] outer,
    int[] inner) {
    int j = 0;
    int c = 0;
    if (inner.length == 0) return true;
    for (int i = 0; i < outer.length; i++) {
        if (inner[j] == outer[i]) {
            j++;
            if (j==inner.length) {
                return true;
            }
        }
    }
    return false;
}
```

linearIn is $O(c_1 + c_2 + c_3 + c_4 + c_1 0 + (c_5 + c_6 + c_7 + c_8 + c_9)n)$, where n is the size of outer; this implies that linearIn is $O(n)$.

iv.

```
public int[] fix45(int[] nums) {
    boolean [] arr = new boolean[nums.length];
    for (int i = 0; i < nums.length-1; i++) {
        if (nums[i] == 4 && nums[i+1] == 5) {
            arr[i+1] = true;
        } else if (nums[i] == 4 && nums[i+1] != 5) {
            for (int j = 0; j < nums.length; j++) {
                if (nums[j] == 5 && arr[j] == false) {
                    nums[j] = nums[i+1];
                    nums[i+1] = 5;
                    arr[i+1] = true;
                    break;
                }
            }
        }
    }
    return nums;
}
```

fix45 is $O(c_1 + c_2 + c_1 3 + (c_3 + c_4 + c_5 + c_6)n + (c_7 + c_8 + c_9 + c_1 0 + c_1 1 + c_1 2)n^2)$, where n represents the length of nums; this implies that fix45 is $O(n^2)$.

```
v.    public boolean canBalance(int[] nums) {           // c0
        int sumRight;                                   // c1
        int sumLeft;                                    // c2
        for (int i = 1; i < nums.length; i++) {         // c3*n
            sumLeft = 0;                                  // c4*n
            sumRight = 0;                                 // c5*n
            for (int j = 0; j < i; j++) {                 // c6*n*n
                sumLeft += nums[j];                       // c7*n*n
            }
            for (int j = i; j < nums.length; j++) {       // c8*n*n
                sumRight += nums[j];                      // c9*n*n
            }
            if (sumRight == sumLeft) {                   // c10*n
                return true;                             // c11*n
            }
        }
        return false;                                   // c12
    }
```

`canBalance` is $O(c_0 + c_1 + c_2 + (c_3 + c_4 + c_5 + c_{10} + c_{11})n + (c_6 + c_7 + c_8 + c_9)n^2)$, where n is the size of `nums`; therefore `canBalance` is $O(n^2)$.

4) EXAM SIMULATION

- i. c) $O(n + m)$
- ii. d) $O(n * m)$
- iii. b) $O(ancho)$
- iv. b) $O(n^3)$
- v. d) $O(n^2)$

References