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Assignment Lesson 7

1) Find encoder and decoder of LZ77? If we have:

Input string: “ abdcaedbdcecabbbdeacb” (first block = 7 and second block = 5)

2) Find encoder and decoder of LZ77? If we have:

Input string: “ daddacabeacaebccdaabbdeacb” (first block = 8 and second block = 6)

Answers:

1). Find encoder and decoder of LZ77

We have Input string: “abdcaedbdcecabbbdeacb”

⇒ abdcaedbdcecabbbdeacb

❖ step 1: compare 5 from first block with second block

- abdcaedbdcecabbbdeacb
- + abdca ≠ bdcec → move 1 character from first block
- + bdcae ≠ bdcec → move 1 character from first block
- + dcae ≠ bdcec → no more character from first block
- + So, remove 1 character at the end from second block
- + it rests 4 characters from the second block: “bdce”.

❖ Step 1 (cont): compare 4 from first block with second block:

- abdcaedbdcecabbbdeacb
- + abdc ≠ bdce → move 1 character from first block
- + bdca ≠ bdce → move 1 character from first block
- + dcae ≠ bdce → move 1 character from first block
- + caed ≠ bdce → no more character from first block
- + So, remove 1 character at the end from second block
- + it rests 3 characters from the second block: “bdc”.

❖ Step 1 (cont): compare 4 from first block with second block:

- abdcaedbdcecabbdeacb
- + abd ≠ bdc → move 1 character from first block
- + bdc = bdc → match or equal each other
- + Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.

a b d c a e d b d c e c a b b d e a c b 7 6
5 4 3 2 1

⇒ Formula **Codeword**<position, length, C(x)> (x is next character from the last matching character in second block)

➤ Therefore, we get Codeword<7, 3, C(e)> (n=length=3)

❖ Step 2: move n+1 (3+1=4) window at first block

⇒ **ab**dca**ed**bdceabbdeacb

❖ Compare 5 character from first block and second block

- **a**edbdceabbdeacb

+ aedbd ≠ cabbd → move 1 character from first block

+ edbdc ≠ cabbd → move 1 character from first block

+ dbdce ≠ cabbd → no more character from first block

+ So, remove 1 character at the end from second block

+ it rests 4 characters from the second block: “cabb”.

❖ Compare 4 character from first block and second block

- **a**edbdceabbdeacb

+ aedb ≠ cabb → move 1 character from first block.

+ edbd ≠ cabb → move 1 character from first block.

+ dbdc ≠ cabb → move 1 character from first block.

+ bdce ≠ cabb → no more character from first block.

+ So, remove 1 character at the end from second block.

+ it rests 3 characters from the second block: “cab”.

❖ Compare 3 character from first block and second block

- **a**edbdceabbdeacb

+ aed ≠ cab → move 1 character from first block.

+ edb ≠ cab → move 1 character from first block.

+ dbd ≠ cab → move 1 character from first block.

+ bdc ≠ cab → move 1 character from first block.

+ dce ≠ cab → no more character from first block.

+ So, remove 1 character at the end from second block.

+ it rests 3 characters from the second block: “ca”.

❖ Compare 2 character from first block and second block

- **a**edbdceabbdeacb

+ ae ≠ ca → move 1 character from first block.

+ ed ≠ ca → move 1 character from first block.

+ db ≠ ca → move 1 character from first block.

+ bd ≠ ca → move 1 character from first block.

+ dc ≠ ca → move 1 character from first block.

+ ce ≠ ca → no more character from first block.

+ So, remove 1 character at the end from second block.

+ it rests 3 characters from the second block: “c”.

❖ Compare 1 character from first block and second block

- aedbdceabbdeacb

+ $a \neq c \rightarrow$ move 1 character from first block.

+ $e \neq c \rightarrow$ move 1 character from first block.

+ $d \neq c \rightarrow$ move 1 character from first block.

+ $b \neq c \rightarrow$ move 1 character from first block.

+ $d \neq c \rightarrow$ move 1 character from first block.

+ $c = c \rightarrow$ match or equal each other

+ Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.

a e d b d c e c a b b d e a c b 7 6

5 4 3 2 1

\Rightarrow Formula **Codeword**<position, length, C(x)> (x is next character from the last matching character in second block)

\rightarrow Therefore, we get Codeword<2, 1, C(a)> (n=length=1)

❖ Step 3: move n+1 (1+1=2) window at first block

\Rightarrow aedbdcecaabbdeacb

❖ Compare 5 character from first block and second block

- dbdcecaabbdeacb

+ dbdce \neq bbdea \rightarrow move 1 character from first block.

+ edbdc \neq bbdea \rightarrow move 1 character from first block.

+ dbdce \neq bbdea \rightarrow no more character from first block.

+ So, By the string remove 1 character at the end from second block is not possible for match and for better let skip and remove 4 characters

+ it rests 1 character from the second block: "b".

❖ Compare 1 character from first block and second block

- dbdcecaabbdeacb

+ $d \neq b \rightarrow$ move 1 character from first block

+ $b = b \rightarrow$ match or equal each other

+ Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.

d b d c e c a b b d e a c b 7 6

5 4 3 2 1

\Rightarrow Formula **Codeword**<position, length, C(x)> (x is next character from the last matching character in second block)

\rightarrow Therefore, we get Codeword<6, 1, C(b)> (n=length=1).

❖ Step 4: move n+1 (1+1=2) window at first block

\Rightarrow dbdcecaabbdeacb

❖ Compare 5 character from first block and second block

- dcecaabbdeacb

- + dceca \neq deacb \rightarrow move 1 character from first block
- + cecab \neq deacb \rightarrow move 1 character from first block
- + ecabb \neq deacb \rightarrow no more character from first block
- + So, By the string remove 1 character at the end from second block is not possible for match and for better let skip and remove 4 characters
- + it rests 1 characters from the second block: "d".

❖ Compare 1 character from first block and second block

- dcecabbd~~ea~~cb

+ d = d \rightarrow match or equal each other

+ Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.

d c e c a b b d e a c b 7 6

5 4 3 2 1

\Rightarrow Formula Codeword<position, length, C(x)> (x is next character from the last matching character in second block)

➤ Therefore, we get Codeword<7, 1, C(e)> (n=length=1).

❖ Step 5: move n+1 (1+1=2) window at first block

\Rightarrow dcecabbd~~ea~~cb

❖ Compare 3 character from first block and second block

- ecabbde~~ac~~b

+ eca \neq acb \rightarrow move 1 character from first block

+ cab \neq acb \rightarrow move 1 character from first block

+ abb \neq acb \rightarrow move 1 character from first block

+ bbd \neq acb \rightarrow move 1 character from first block

+ bde \neq acb \rightarrow no more character from first block

+ So, By the string remove 1 character at the end from second block is not possible for match and for better let skip and remove 4 characters

+ it rests 1 characters from the second block: "a".

❖ Compare 1 character from first block and second block

- ecabbde~~a~~cb

+ e \neq a \rightarrow move 1 character from first block

+ c \neq a \rightarrow move 1 character from first block

+ a = a \rightarrow match or equal each other

+ Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.

e c a b b d e a c b 7 6

5 4 3 2 1

\Rightarrow Formula Codeword<position, length, C(x)> (x is next character from the last matching character in second block)

➤ Therefore, we get Codeword<5, 1, C(c)> (n=length=1).

- ❖ Step 6: move $n+1$ ($1+1=2$) window at first block
- ⇒ **ecabbdeacb**
- ❖ Compare 1 character from first block and second block
- **abbdeacb**
- + $a \neq b \rightarrow$ move 1 character from first block
- + $b = b \rightarrow$ match or equal each other
- + Start to give index in the first block (7 character) from 1 by reversing from the end to the beginning.
- a b b d e a c b 7 6**
5 4 3 2 1
- ⇒ Formula **Codeword<position, length, C(x)>** (x is next character from the last matching character in second block)
 - Therefore, we get Codeword<6, 1, null> ($n=length=1$).
- Because there is no more character in second block, we stop here:
 - ⇒ Encode: {<7, 3, C(e)>, <2, 1, C(a)>, <6, 1, C(b)>, <7, 1, C(e)>, <5, 1, C(c)>, <6, 1, null>}
 - ⇒ Result = {"**abdcaed**", <7, 3, C(e)>, <2, 1, C(a)>, <6, 1, C(b)>, <7, 1, C(e)>, <5, 1, C(c)>, <6, 1, null>}
- Decode part:
 - ⇒ So, we get: "**abdcaed**" and
Encode: { <7, 3, C(e)>, <2, 1, C(a)>, <6, 1, C(b)>, <7, 1, C(e)>, <5, 1, C(c)>, <6, 1, null> }
 - ⇒ Give index from 1 as in encoder: <7, 3, C(e)> **a b**
d c a e d b d c e
7 6 5 4 3 2 1
 - ❖ Step 2: move $n+1$ ($3+1=4$) window **a b**
d c a e d b d c e (result from step 1) **a b d c**
a e d b d c e
 - ⇒ Use the second result of encoder: <2, 1, C(a)> **a b**
d c a e d b d c e
7 6 5 4 3 2 1
a b d c a e d b d c e c a
 - ❖ Step 3: move $n+1$ ($1+1=2$) window
a b d c a e d b d c e c a (result from step 2) **a b**
d c a e d b d c e c a
 - ⇒ Use the third result of encoder: <6, 1, C(b)> **a b**
d c a e d b d c e c a
7 6 5 4 3 2 1

a b d c a e d b d c e c a b b

❖ Step 4: move n+1 (1+1=2) window

a b d c a e d b d c e c a b b (result from step 3) a b

d c a e d b d c e c a b b

⇒ Use the fourth result of encoder: <7, 1, C(e)>a

b d c a e d b d c e c a b b

7 6 5 4 3 2 1

a b d c a e d b d c e c a b b d e

❖ Step 5: move n+1 (1+1=2) window

a b d c a e d b d c e c a b b d e (result from step 4) a b

d c a e d b d c e c a b b d e

⇒ Use the fifth result of encoder: <5, 1, C(c)>a b

d c a e d b d c e c a b b d e

7 6 5 4 3 2 1

a b d c a e d b d c e c a b b d e a c

❖ Step 6: move n+1 (1+1=2) window

a b d c a e d b d c e c a b b d e a c (result from step 5) a b

d c a e d b d c e c a b b d e a c

⇒ Use the last result of encoder: <6, 1, null>a

b d c a e d b d c e c a b b d e a c

7 6 5 4 3 2 1

a b d c a e d b d c e c a b b d e a c b EOF

⇒ Decoder: "abdcaedbdcceabbdeacb"

2). Find encoder and decoder of LZ77? If we have:

Input string: "daddacabeacaebccdaabbbeacb" (first block = 8 and second block = 6)

○ Encode part

daddacabeacaebccdaabbbeacb

❖ Step 1: Compare 6 character first block with second block

daddacabeacaebccdaabbbeacb

+ daddac ≠ eacaeb → Move 1 character from the first block

+ addaca ≠ eacaeb → Move 1 character from the first block

+ ddacab ≠ eacaeb → No more character from first block

- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → No match “e”≠“b”

⇒ Codeword <0, 0, C(e)>

- ❖ Step 2: move $n+1$ ($0+1=1$) window at first block

daddacabeacaebccdaabbbeacb

- ❖ Compare 6 character first block with second block → No match
- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → match aca = aca

a d d a c a b e a c a e b c c d a a b b e a c b 8 7
6 5 4 3 2 1

⇒ Codeword <5, 3, C(e)>

- ❖ Step 3: move $n+1$ ($3+1=4$) window at first block

addacabeacaebccdaabbbeacb

- ❖ Compare 6 character first block with second block → No match
- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → match b = b

c a b e a c a e b c c d a a b b e a c b 8 7
6 5 4 3 2 1

⇒ Codeword <6, 1, C(c)>

- ❖ Step 4: move $n+1$ ($1+1=2$) window at first block

cabecaebccdaabbbeacb

- ❖ Compare 6 character first block with second block → No match
- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → match c = c

b e a c a e b c c d a a b b e a c b 8 7

6 5 4 3 2 1

⇒ Codeword<5, 1, C(d)>

❖ Step 5: move $n+1$ ($1+1=2$) window at first block

beacae**bccda**abb**ea**cb

- ❖ Compare 6 character first block with second block → No match
- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → match $a = a$

a c a e b c c d a a b b e a c b 8 7

6 5 4 3 2 1

⇒ Codeword<8, 1, C(a)>

❖ Step 6: move $n+1$ ($1+1=2$) window at first block

a**c**aebccda**a**bbea**c**b

- ❖ Compare 6 character first block with second block → No match
- ❖ Compare 5 character first block with second block → No match
- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → match $b = b$

b c c d a a b b e a c b

8 7 6 5 4 3 2 1

⇒ Codeword<6, 1, C(b)>

❖ Step 7: move $n+1$ ($1+1=2$) window at first block

a**e**bccdaabb**e**a**c**b

- ❖ Compare 4 character first block with second block → No match
- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match
- ❖ Compare 1 character first block with second block → No match $b \neq e$

⇒ Codeword<0, 0, C(e)>

❖ Step 8: move $n+1$ ($0+1=1$) window at first block

bccdaabb**e**a**c**b

- ❖ Compare 3 character first block with second block → No match
- ❖ Compare 2 character first block with second block → No match

❖ Compare 1 character first block with second block → Match a = a

c c d a a b b e a c b 8 7
6 5 4 3 2 1

⇒ Codeword<5, 1, C(c)>

❖ Step 9: move n+1 (1+1=2) window at first block

ccdaabbbeacb

❖ Compare 1 character first block with second block → Match b = b

d a a b b e a c b 8 7
6 5 4 3 2 1

⇒ Codeword<5, 1, null>

Because there is no more character in second block, we stop here:

⇒ Encoder: {<0, 0, C(e)>, <5, 3, C(e)>, <6, 1, C(c)>, <5, 1, C(d)>, <8, 1, C(a)>, <6, 1, C(b)>, <0, 0, C(e)>, <5, 1, C(c)>, <5, 1, null>}

⇒ Result = {"daddacab", <0, 0, C(e)>, <5, 3, C(e)>, <6, 1, C(c)>, <5, 1, C(d)>, <8, 1, C(a)>, <6, 1, C(b)>, <0, 0, C(e)>, <5, 1, C(c)>, <5, 1, null>}

○ Decode part:

○ So, we get: "daddacab" and

Encoder: {<0, 0, C(e)>, <5, 3, C(e)>, <6, 1, C(c)>, <5, 1, C(d)>, <8, 1, C(a)>, <6, 1, C(b)>, <0, 0, C(e)>, <5, 1, C(c)>, <5, 1, null>}

❖ Step 1: first index encoder: <0, 0, C(e)>d a

d d a c a b e
8 7 6 5 4 3 2 1

❖ Step 2: move n+1 (0+1=1) window and 2nd index encoder: <5, 3, C(e)>d a

d d a c a b e a c a e
8 7 6 5 4 3 2 1

❖ Step 3: move n+1 (3+1=4) window and 3rd index encoder: <6, 1, C(c)>d a

d d a c a b e a c a e b c
8 7 6 5 4 3 2 1

❖ Step 4: move n+1 (1+1=2) window and 4th index encoder: <5, 1, C(d)>d a

d d a c a b e a c a e b c c d
8 7 6 5 4 3 2 1

❖ Step 5: move n+1 (1+1=2) window and 5th index encoder: <8, 1, C(a)>d a

d d a c a b e a c a e b c c d a a
8 7 6 5 4 3 2 1

❖ Step 6: move n+1 (1+1=2) window and 6th index encoder: <6, 1, C(b)>d a

d d a c a b e a c a e b c c d a a b b
8 7 6 5 4 3 2 1

❖ Step 7: move n+1 (1+1=2) window and 7th index encoder: <0, 0, C(e)>d a
d d a c a b e a c a e b c c d a a b b e
8 7 6 5 4 3 2 1

❖ Step 8: move n+1 (0+1=1) window and 8th index encoder: <5, 1, C(c)>d a
d d a c a b e a c a e b c c d a a b b e a c
8 7 6 5 4 3 2 1

❖ Step 9: move n+1 (0+1=1) window and 9th index encoder: <5, 1, null>d a
d d a c a b e a c a e b c c d a a b b e a c b EOF
8 7 6 5 4 3 2 1

⇒ Decoder: "daddacabeacaebccdaabbbeacb"