

Magnetic Circuits :

Current in electric ckt = Flux in magnetic ckt

Magnetomotive force : (MMF)

* In magnetic circuits, flux is present due to mmf.

mmf \propto current and no. of turns.

mmf is expressed in ampere turns.

Magnetic strength : (H)

mmf per unit length of magnetic circuit
is called magnetic field strength/intensity

$$* H = \frac{\text{mmf}}{\text{length}} = \frac{i \times N}{l}$$

(Independent of medium)

Magnetic permeability

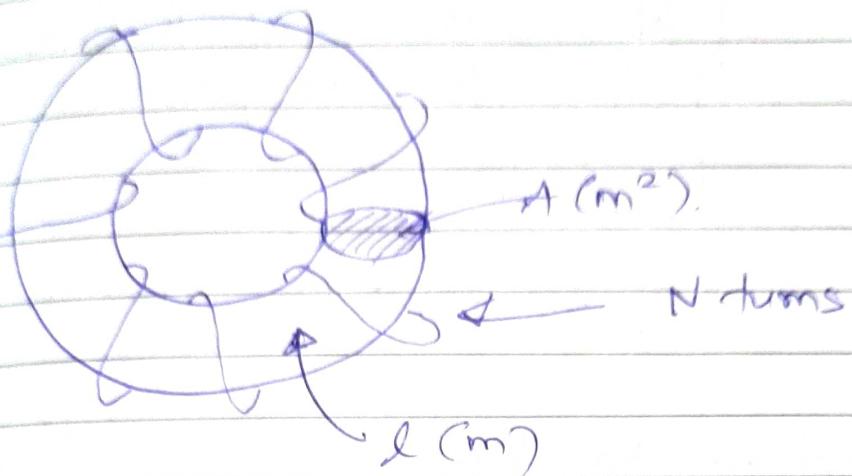
$$\mu_0 = \frac{B_0}{H_0} = 4\pi \times 10^{-7}$$

* If core is replaced by magnetic material, then flux \uparrow
hence mmf \uparrow , hence flux density \uparrow

$$T \mu_f = \frac{\mu}{\mu_0}$$

Reluctance: Measure of opposition by magnetic circuit to setting up of flux

$$R = \frac{1}{\mu} \times \frac{l}{A} = \frac{1}{\mu_r \mu_0} \cdot \frac{l}{A} \approx \frac{F}{\phi}$$



$\text{mmf} = F = N \cdot i$

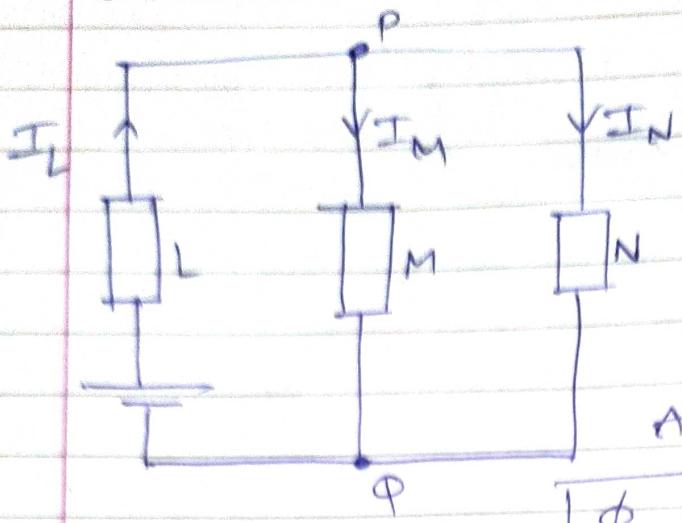
$$H = \frac{F}{l} \quad \phi = BA$$

$$\frac{\phi}{F} = \frac{BA}{Fl} = \frac{B}{F} \times \frac{A}{l} = \frac{\mu \times A}{l} = \frac{\mu_r \mu_0 A}{l}$$

$$R = \frac{l}{\mu_r \mu_0 A} \Rightarrow \frac{1}{R} = \mu_r \mu_0 \frac{A}{l}$$

Permeance = $\frac{1}{R} = \frac{\phi}{F}$

Kirchoff's flux law



Total mmf towards a junction is equal to the total flux away from the junction.

At P,

$$\boxed{\phi_L = \phi_M + \phi_N}$$

Kirchoff's magnetomotive law

In a closed magnetic ckt, the algebraic sum of the product of the field strength and length of each part of the ckt is equal to resultant mmf

$$\text{Total mmf of coil} = H_L l_L + H_M l_M$$

$$= H_L l_L + H_N l_N$$

$$\phi = H_M l_M - H_N l_N$$

Self Inductance

$$e \propto \frac{di}{dt} \quad \text{or} \quad e = L \frac{di}{dt}$$

$L \equiv$ Self Inductance

Energy stored in inductor

$$E = \frac{1}{2} Li^2$$

$$e = N \frac{d\phi}{dt} = L \frac{di}{dt}$$

$$\therefore L = N \frac{d\phi}{di}$$

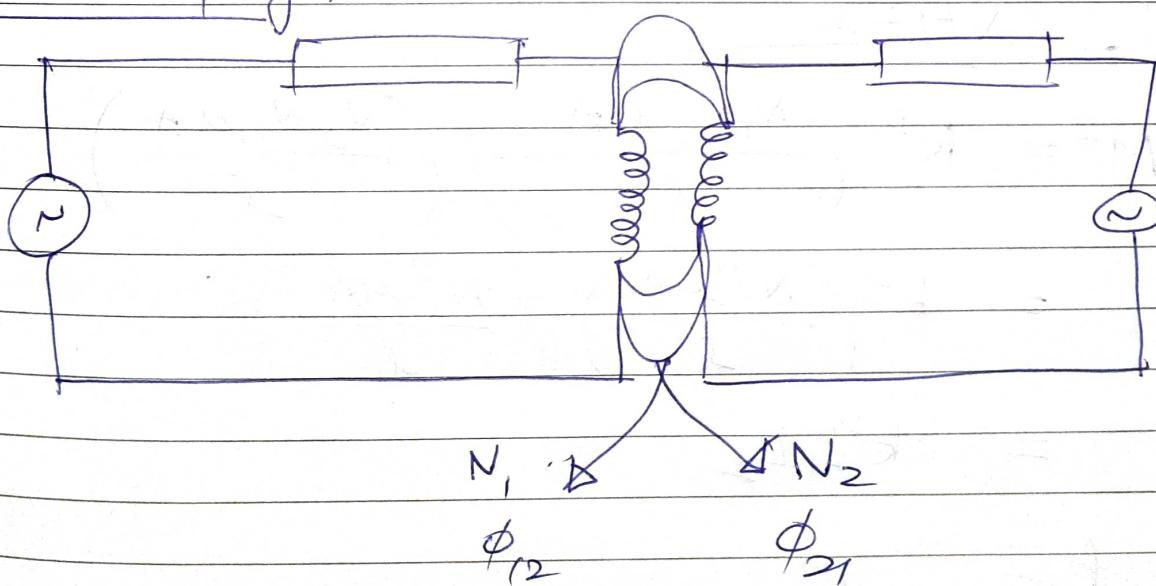
$$\phi = \frac{Ni}{R} \quad \text{and} \quad R = \frac{1}{\mu} \frac{L}{A}$$

\therefore For linear change,

$$L = \frac{N^2 \mu A}{l}$$

Mutual inductance :

EM coupling :



$$e_s = M_{12} \frac{di_1}{dt} - ①$$

$$\phi_1 = \phi_{11} + \phi_{12}$$

$$\phi_2 = \phi_{22} + \phi_{21}$$

$$M_{12} \frac{di_1}{dt} = N_2 \frac{d\phi_{12}}{dt}$$

$$\therefore \boxed{M_{12} = N_2 \frac{d\phi_{12}}{di_1}}$$

$$\boxed{M_{21} = N_1 \frac{d\phi_{21}}{di_2}}$$

$$\text{i.e. } \boxed{M_{12} = M_{21}}$$

coeff. of coupling :

$$\boxed{k = \frac{M}{\sqrt{L_1 L_2}}}$$

$$M^2 = k^2 \left(\frac{N_1 N_2 \mu A}{l} \right) \left(\frac{N_2 N_1 \mu A}{l} \right)$$

$$= k^2 \left(\frac{N_1^2 \mu A}{l} \right) \left(\frac{N_2^2 \mu A}{l} \right)$$

$$= k^2 l_1 l_2$$

$$k = \frac{M}{\sqrt{l_1 l_2}}$$

Dot Conventions :

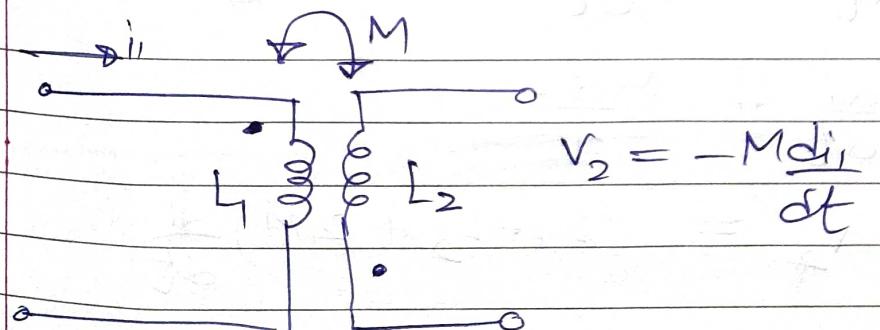
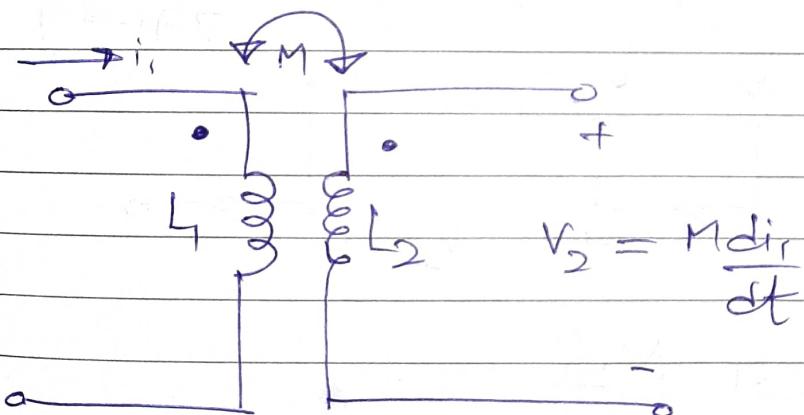
Voltage across coil 1 is

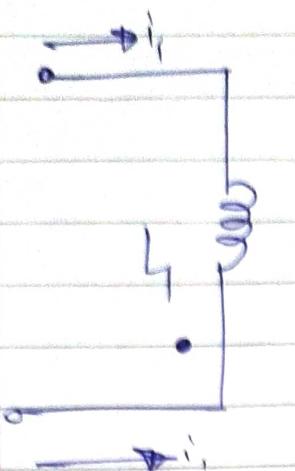
$$\boxed{V_1 = L_1 \frac{di_1}{dt} + M \frac{di_2}{dt}}$$

$$\boxed{V_2 = L_2 \frac{di_2}{dt} + M \frac{di_1}{dt}}$$

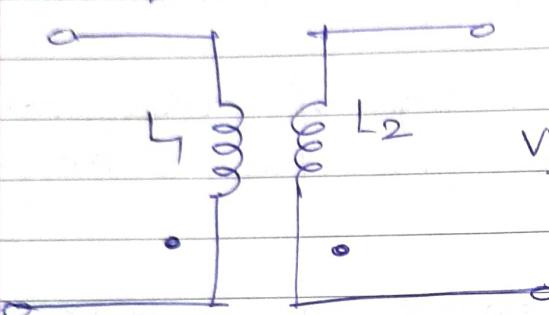
Dot convention : Determines sign of mutual voltage without going into physical construction of the coils.

A current entering the dotted terminal of one coil produces an open-circuit voltage which is positively sensed at the dotted terminal of 2nd coil.





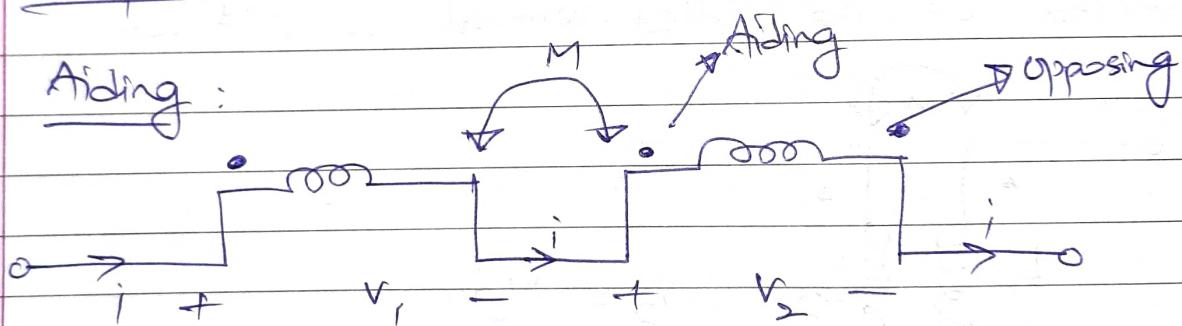
Represents positive terminal

$$L_2 \quad V_2 = -M \frac{di_1}{dt}$$


$$V_2 = M \frac{di_1}{dt}$$

Coupled coils in series

Aiding :



$$V_1 = L_1 \frac{di}{dt} + M \frac{di}{dt}$$

$$V_2 = L_2 \frac{di}{dt} + M \frac{di}{dt}$$

$$V = V_1 + V_2 = (L_1 + L_2 + 2M) \frac{di}{dt}$$

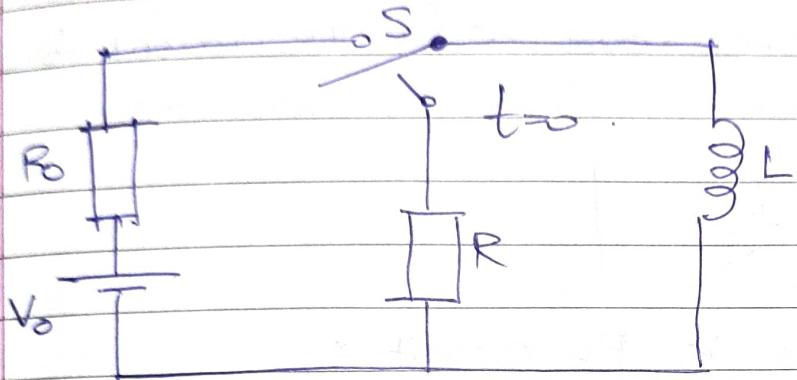
Opposing : $V_1 + V_2 = (L_1 + L_2 - 2M) \frac{di}{dt}$

DC Transients :

Time taken by a circuit from one steady state to another is known as transient time.

RL circuit :

$$i(t) = I_0 \text{ at } t=0 \text{ (Assumption)}$$

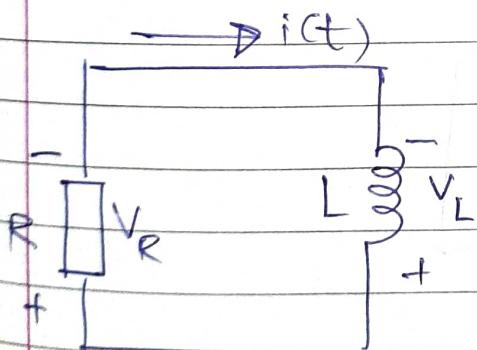


Assume that circuit is in this condition for a long time so as to achieve steady state.

Since I_0 is not changing with time,

current through inductor

$$I_0 = \frac{V_0}{R_0}$$



Applying KVL,

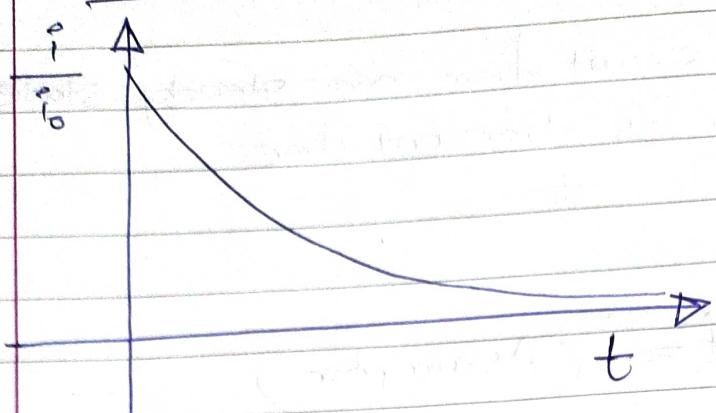
$$Ri + L \frac{di}{dt} = 0$$

$$\frac{di}{dt} + \frac{R}{L}i = 0$$

$$\Rightarrow \int_{I_0}^{i(t)} \frac{di}{i} = \int_0^t -\frac{R}{L} dt$$

$$\Rightarrow i(t) = I_0 e^{-Rt/L}$$

Nature of the response :



Time const : Time reqd for the current to drop to zero if continued to drop at initial rate

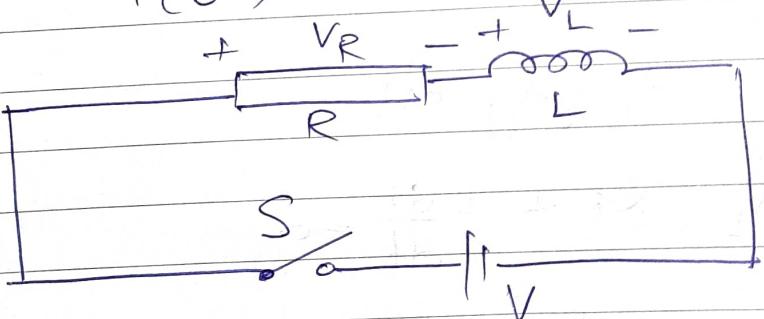
$$\boxed{\tau = \frac{L}{R}}$$

Growth of current in RL circuit :

Before closing the switch, $\text{if } i(0^-) = 0$.

Since an inductor cannot change current in zero time,

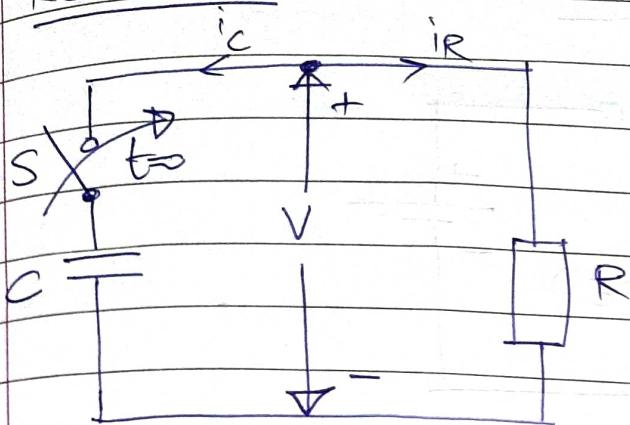
$$i(0^+) = 0.$$



$$L \frac{di}{dt} + iR = V$$

$$\boxed{i(t) = I_0 (1 - e^{-t/\tau})}$$

RC circuit :



Initial voltage V_0

$$i_C + i_R = 0$$

$$\frac{dV}{dt} + \frac{V}{R} = 0$$

$$\frac{dV}{dt} + \frac{V}{CR} = 0$$

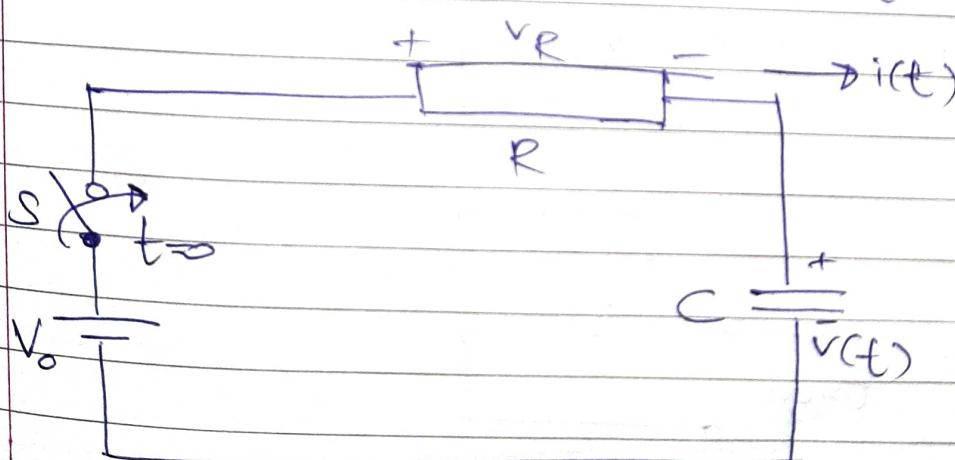
$$V = V_0 e^{-\frac{t}{RC}} = V_0 e^{-\frac{t}{CR}}$$

Charging :

Instantaneously, $V(0^+) = V(0^-) = 0$.

$$i(0^+) = \frac{V_0}{R}$$

$$V(t \rightarrow \infty) = V_0 \text{ and } i(t \rightarrow \infty) = 0$$

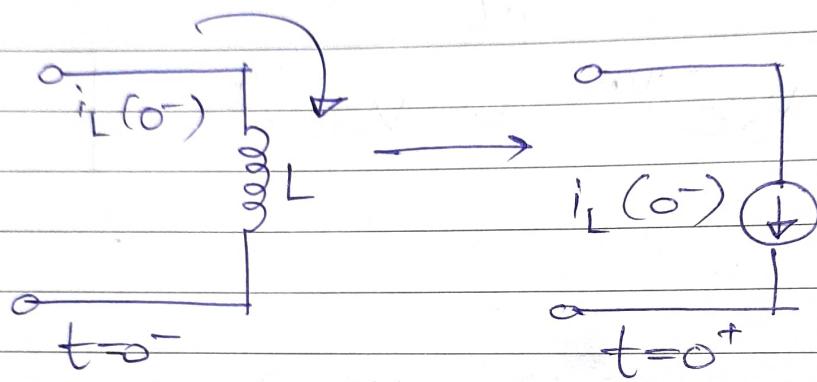
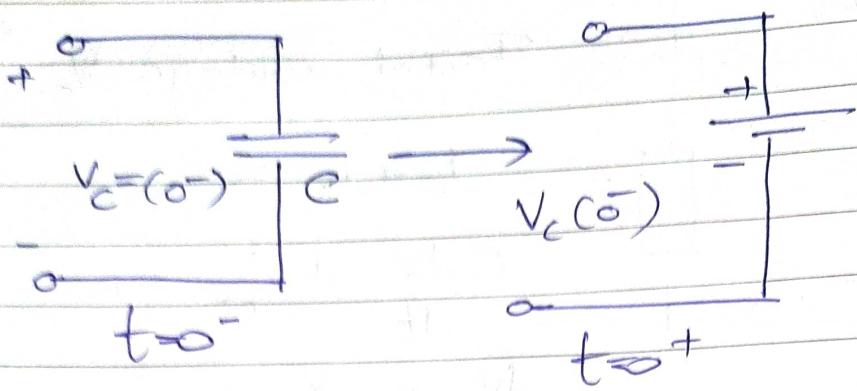


$$iR + V = V_0$$

$$i = \frac{C dV}{dt}$$

$$V = V_0 (1 - e^{-\frac{t}{RC}})$$

Determining initial values :



Determining final values :

