

Hypotheses testing

Q The mean life time of 81 glucometer produced by a company is found to be 59 months with S.D. of 10 months. Company claims that the mean life time is 60 months. Test hypotheses at 5% level of sig., whether 58 months lifetime is acceptable or not?

Null Hyp. H_0 : There is no significant difference betⁿ lifetime of sample & populations

Alt. Hyp. H_1 : There is sig. diff. betⁿ life of sample & pop.

$$\text{Add SEM} = \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{81}} = \frac{10}{9} = 1.11 \\ (\text{Standard error}) \quad \text{of mean}$$

$$\frac{\text{Diff.}}{\text{SEM}} = \frac{|58 - 60|}{1.11} = \frac{2}{1.11} = 1.80$$

Procedure for Hyp. Testing

- 1) Set up a Hyp. (H_0, H_1)
- 2) Set up a signif. level (0.1%, 1%, 5%, 10%)
- 3) Set a test criterion (Z-test, t-test, χ^2 test, f-test)
- 4) Do computation

Date: 11/11

5) Make decision

	Acc: H_0	Reject H_0
H_0 true corr. dec.	Type I (α)	
H_0 false Type-II (β)	Correct	

S-2: Set a sig. level

$$p + q = 1 \quad p = \text{Prob. of Acc.}$$

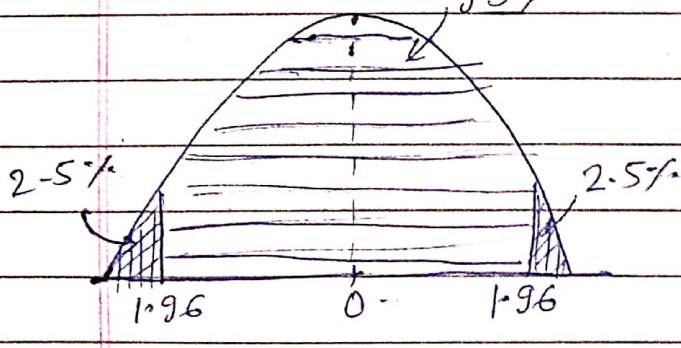
$q = H_1$ — non-Acc.

p	Signif.	Confid.	Two-tail	One-tail
0.1	10%	90%	1.65	1.28
0.05	5%	95%	1.96	1.64
0.01	1%	99%	2.58	2.33
0.001	0.1%	99.9%	3.29	3.10

As 1.80 lies betw -1.96 to 1.96 our H_0 is correct.

Give Two-tail

95%



One-tailed test:

H_0 : Life is not less than 60

H_1 : Life is less than 60

As $Z = 1.80$ does not lie in -1.64 to 1.64

- 1.64 to 1.64

∴ We reject null hypotheses

Hypotheses testing

→ Statistical tech. to test some hyp. about the parent pop. from which the sample is actually drawn.

Population → complete collec. of all elements under study

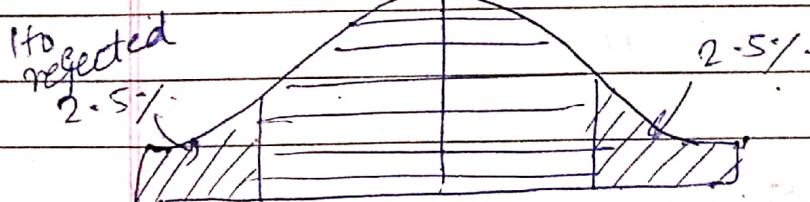
sample: sub-collec. of elements drawn from population

Estimation: Use the stats obtained from sample as estimate of unknown param. of the pop. from which the sample is drawn.

A Hyp. in stat. is simply a quantitative statement about population

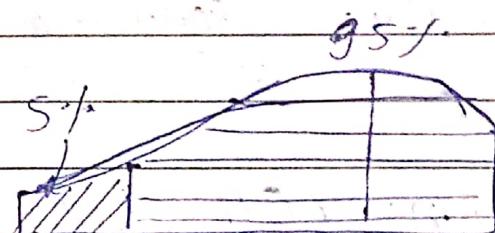
Two tailed test

H_0 accepted
95%



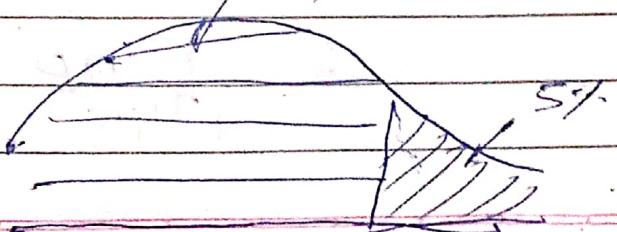
One tailed test

Left - side



Right - side

95%



Z-value: Standardized score that describes how many S.D. (σ) an element is from mean.

Test for no. of succ.

$$Z = \frac{x - \mu}{\sqrt{npq}} = \frac{x - np}{\sqrt{npq}}$$

Z = calc. critical value

x = Obs. succ.

n = size of samples

p = prob. of succ.

$q = 1 - p$ = failure

Q: A coin was tossed 484 times.

Head turned up 265 times. Test the Hyp. that coin is unbiased

Soln:

H_0 : No. of Head = No. of Tail

H_a : Head \neq Tail

$\leftarrow 1 - 1 - \neq - 1 - \rightarrow$

$$n = 484 \quad x = 265$$

$$p = \frac{1}{2} \quad q = \frac{1}{2}$$

$$Z = \frac{x - np}{\sqrt{npq}} = \frac{265 - 484 \times \frac{1}{2}}{\sqrt{484 \times \frac{1}{2} \times \frac{1}{2}}}$$

$$Z = \frac{23}{\sqrt{12}} = \frac{23}{11}$$

$$Z_{cal} = 2.09$$

$$Z_{tab} = 1.96$$

-1.96 so +1.96

∴ Z cal. do not lie in $|1.96|$

$\therefore H_0$ is rejected \because cal. value exceeds the limit.

Decision: Con'tg based

- 2) In a chesp. 960 females & 1040 males were born in a year. Does this figures confirm the hyp. that males & females are born in equal nos? (5% level of signif.)

H_0 : Male babies = female babies

H_a : \neq

Given: $n = 1040 + 960 = 2000$

$x = 1040$ or $960 \therefore$ of $\pm 1(n - \bar{x})$ ans.

would be same

$$p = \frac{1}{2} \text{ & } q = \frac{1}{2}$$

$$Z = \frac{x - np}{\sqrt{npq}} = \frac{|1040 - 2000 \times \frac{1}{2}|}{\sqrt{2000 \times \frac{1}{2} \times \frac{1}{2}}} = \frac{40}{\sqrt{500}} = 1.79$$

H₀ is accp. as 1.79 less feet² = 7.96 ft + 1.96

i.e. H₀: Males Male babies = Female babies

Test for prop. of Success:

$$\text{S.E. (prop.)} = \sqrt{\frac{pq}{n}} \quad \begin{aligned} p &= \text{prob. of succ.} \\ q &= 1 - \text{fail.} \\ n &= \text{size of sample} \end{aligned}$$

For det. limit in prop. of success:

$$= p \pm Z \times \text{S.E. (prop.)}$$

$$= \boxed{p \pm Z \times \sqrt{\frac{pq}{n}}}$$

Q1) 1000 apples are taken at random from a large basket & 100 are found to be bad. Estimate the prop. of bad apples in the basket & assign limits within which ~~prop.~~ percentage most prob. lies.

$$n = 1000 \quad p = \frac{100}{1000} = 0.1 \quad q = 0.9$$

$$\therefore \text{limit} = p \pm Z \times \text{S.E.}$$

$$= 0.1 \pm 1.96 \times \sqrt{\frac{0.1 \times 0.9}{1000}}$$

$$= 0.1 \pm 1.96 \times 0.0095$$

Limits:

$$0.1 - 0.0186 = 0.0814 \times 100 = 8.14\%$$

$$0.1 + 0.0186 = 0.1186 \times 100 = 11.86\%$$

i.e. % of bad apples goes from 8.14% to 11.86%.

- 2) A drug company claims that only 3% tablets manufactured by them are defected. A random sample of 600 tablets contained 25 defected tablets. Test the claim of company at 5% level of significance

$$H_0: \text{Def. tablet} = 3\%$$

$$H_a: \text{Def. tablet} \neq 3\%$$

Given: $n = 600, p = 0.03, q = 0.097$

$$\text{Limits} = 0.03 \pm 1.96 \sqrt{\frac{0.03 \times 0.097}{600}}$$

$$= 0.03 \pm 1.96 \sqrt{\frac{0.0291}{600}}$$

$$= 0.03 \pm 1.96 \sqrt{0.000485}$$

$$= 0.03 \pm 0.014$$

Limits: 0.016 to 0.044

$$= 9.6 \text{ to } 26.4$$

25 def. tablets come in the range
 H_0 is correct & accepted

Test for diff. defⁿ prop.

$$Z = \frac{P_1 - P_2}{\sqrt{pq \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

p = prob. of success
 $pq = 1 -$ failure

P_1 = Prob. of success of sample A

P_2 = - 11 - 11 - 11 - B

n_1 = Sample size of A

n_2 = - 11 - B

$$p = \frac{x_1 + x_2}{n_1 + n_2} \quad \text{OR} \quad n_1 p_1 + n_2 p_2 \\ n_1 + n_2$$

x_1 = no. of occ. in sample A

x_2 = - 11 - B

- Q) In a random sample of 1000 persons from Delhi 500 are found to be cons. of rice. In another random sample from Mumbai 650 out of 1200 are found to be consumers of rice. Do these data reveal a significant diff. betⁿ these cities so far as the prop. of rice conso. at 5% level of significance.

Calc: $H_0: P_1 = P_2$ $H_a: P_1 \neq P_2$

$$n_1 = 1000, x_1 = 500, p_1 = 500/1000 = 0.5$$

$$n_2 = 1200, x_2 = 650, p_2 = 650/1200 = 0.541666\ldots$$

$$z = \frac{p_1 - p_2}{\sqrt{pq \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}} \quad z, p = 500 + 650 \\ 2200 \\ p = 0.52 \\ q = 0.48$$

$$z = 0.5 - 0.46$$

$$\sqrt{0.52 \times 0.48 \left(\frac{1}{1000} + \frac{1}{1200} \right)}$$

$$= \frac{0.04}{\sqrt{0.2496 \left(\frac{11}{6000} \right)}} = \frac{0.04}{\sqrt{0.2496 \times 0.0018}}$$

$$= \frac{0.04}{\sqrt{0.00045}} = \frac{0.04}{0.0212} = 1.887 \text{ (z value)}$$

$$Z_{\text{table}} = -1.96 \text{ to } 1.96$$

$\therefore H_0$ is passed & accp'. There is no diff.
betw in eating habits of rice eaters & others