2NF Example

Condition: 1) Relation should be in 1NF.

2) No partial dependencies.

Partial Dependencies: Proper subset of CK --> Non prime attributes. Example: ABC is CK and Proper subset of CK are {A, B, C, AB, BC, AC}

Example 1:

Consider a Relation
$$R(A,B,C,D,E,F)$$
 and $FD = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow E \}$ Is this relation in $2NF$?

Answer:

- 1) It is in 1NF.
- 2) To find all CK for above relation.

Is AF candidate key:

$$A + = \{ABCDE\}$$

$$F^+ = \{F\}$$

Hence AF is CK

Prime attributes : A and F. Non Prime attributes : B, C, D, E

More CK?? No because A and F are not on RHS of FD. Hence only one CK AF.

Partial dependencies is there as A --> B.

Hence it is not in 2NF.

Example 2:

Consider a relation
$$R(A,B,C,D)$$
 and

$$FD = \{AB \longrightarrow CD, C \longrightarrow A, D \longrightarrow B\}$$
 Is this relation in 2NF?

Answer:

- 1) It is in 1NF.
- 2) To find all CK for above relation.

AB is CK?

$$A + = \{A\}$$

$$B+=\{B\}$$

AB is a CK

Prime attributes : A and B Non Prime attributes : C and D

More CK?? Yes because prime attribute A and B are present in RHS of FD.

Replace A with C. Hence BC

$$B+=\{B\}$$

$$C+ = \{CA\}$$

BC is CK

Prime attributes: A, B and C

Replace B with D, hence AD

$$A + = \{A\}$$

$$D+ = \{DB\}$$

AD is CK

Prime attributes : A, B, C and D

C and D both are on RHS of FD. But here AB is already candidate key

Hence for above relation CK are = $\{AB, BC, AD\}$

Since all are prime attributes, hence above relation is in 2NF.

Example 3:

Consider a relation R (A,B,C,D) and $FD = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D \}$ Is this relation in 2NF?

Answer:

- 1) It is in 1NF.
- 2) To find all CK for above relation.

A is CK.

Prime Attribute A

Non Prime attribute B, C and D

This is in 2NF.