

Assign 4

Q.1

$$F = \begin{bmatrix} 6 & 5 & 10 \\ 100 & 100 & 100 \\ 4 & 20 & 10 \end{bmatrix}$$

$$F = \begin{bmatrix} 6 & 6 & 5 & 10 & 10 \\ 6 & 6 & 5 & 10 & 10 \\ 100 & 100 & 100 & 100 & 100 \\ 4 & 4 & 20 & 10 & 10 \\ 4 & 4 & 20 & 10 & 10 \end{bmatrix}$$

Horizontal

line

$$\begin{bmatrix} -1 & -1 & -1 \\ 2 & 2 & 2 \\ -1 & -1 & -1 \end{bmatrix}$$

Vertical

line

$$\begin{bmatrix} -1 & 2 & -1 \\ -1 & 2 & -1 \\ -1 & 2 & -1 \end{bmatrix}$$

$$A = \begin{bmatrix} -283 & -279 & -275 \\ 555 & 541 & 531 \\ -272 & -266 & -269 \end{bmatrix}$$

$$A = \begin{bmatrix} 122 & -12 & 10 \\ -15 & 20 & -5 \\ -32 & 52 & -20 \end{bmatrix}$$

$$Q.2 \quad F = \begin{bmatrix} 50 & 60 & 70 \\ 5 & 50 & 80 \\ 7 & 9 & 50 \end{bmatrix}$$

Prewitt's filter

$$G_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$$

$$G_y = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

$$\text{For } f(x, y) = 50$$

$$A_x = 138$$

$$A_y = 114$$

$$\alpha = \tan^{-1} \left(\frac{114}{138} \right) = 39.56^\circ$$

$$Q.3 \quad F = \begin{bmatrix} 1 & 6 & 5 \\ 0 & 7 & 6 \\ 3 & 1 & 7 \end{bmatrix}$$

$$I_{\max} = 7$$

$$A \downarrow B$$

$$\text{cost}(A, B) = I_{\max} - |A - B|$$

① Edge 1

$$\begin{array}{c|cc} 1^{C1} & 6 & 5 \\ 0^{C2} & 7 & 6 \\ 3^{C3} & 1 & 7 \end{array}$$

$$C1 = 7 - |1 - 6| = 7 - 5 = 2$$

$$C2 = 7 - |7 - 0| = 7 - 7 = 0$$

$$C3 = 7 - |3 - 1| = 7 - 2 = 5$$

$$\text{cost}(E1) = 7$$

② Edge 2

$$\begin{array}{c|cc} 1^{C1} & 6 & 7 \\ 0^{C2} & 7 & 6 \\ 3^{C3} & 1 & 7 \end{array}$$

$$C1 = 7 - |6 - 1| = 7 - 5 = 2$$

$$C2 = 7 - |7 - 6| = 7 - 1 = 6$$

$$C3 = 7 - |7 - 6| = 7 - 1 = 6$$

$$C4 = 7 - |7 - 1| = 7 - 6 = 1$$

$$\text{cost}(E2) = 15$$

③ Edge 3

1	c1	6	7
0	c2	7	6
3	c3	7	

$$\begin{aligned} \text{Cost}(E3) &= (7-5) + (7-7) + (7-6) \\ &= 2 + 0 + 1 + 1 \\ &= 4 \end{aligned}$$

④ Edge 4

1	c1	6	7
0	c2	7	6
3	c3	1	7

$$\begin{aligned} \text{Cost}(E4) &= (7-5) + (7-1) \\ &\quad + (7-1) + (7-6) + (7-2) \\ &= 2 + 6 + 6 + 1 + 5 \\ &= 20 \end{aligned}$$

⑤ ES

1	6	c1	5
0	7	c2	6
3	1	c3	7

$$\begin{aligned} \text{Cost}(ES) &= 7 \times 3 - (1 + 1 + 6) \\ &= 21 - 8 \\ &= 13 \end{aligned}$$

⑥ EG

1	6	c1	5
0	7	c2	6
3	1	c3	7

$$\begin{aligned} \text{Cost}(EG) &= 7 \times 4 - (1 + 5 + 1 + 2) \\ &= 28 - 9 \\ &= 19 \end{aligned}$$

⑦ E7

1	6	5
0	7	6
3	1	7

$$\begin{aligned} \text{Cost}(E7) &= 7 \times 4 - (1 + 1 + 6 + 2) \\ &= 28 - 10 \\ &= 18 \end{aligned}$$

$$\begin{aligned} &= (7-1) + (7-1) + (7-6) + (7-2) \\ &= 18 \end{aligned}$$

⑧ E8

1	6	5
0	7	6
3	1	7

$$\begin{aligned} \text{Cost}(E8) &= 7 \times 5 - (1 + 1 + 7 + 6 + 6) \\ &= 35 - 21 \\ &= 14 \end{aligned}$$

Edge 3 has minimum cost of 4.

q.5

$$R = \begin{bmatrix} 10 & 9 & 30 & 4 \\ 7 & 6 & 33 & 37 \\ 51 & 52 & 54 & 53 \\ 55 & 57 & 56 & 58 \end{bmatrix}$$

$$\text{Max-Min} \\ = |58 - 4| \geq 30$$

	R1		R2		
	10	9	30	4	
	7	6	33	37	
R3	51	52	54	53	R4
	55	57	56	58	

R1,

$$I_{\max} - I_{\min} = 10 - 6 = 4 \\ \not\geq 30$$

R2,

$$I_{\max} - I_{\min} = 37 - 4 = 33 \\ \geq 30$$

	R21	R22
R2	30	4
	33	37
R23		R24

R3,

$$I_{\max} - I_{\min} = 55 - 51 \\ = 4$$

$$\not\geq 30$$

$$\begin{aligned}
 R_4, I_{\max} - I_{\min} \\
 &= 58 - 53 \\
 &= 5 \\
 &\neq 30
 \end{aligned}$$

If $|I_{\max} - I_{\min}| < 8$ merge

$$R_{21} \& R_{22} \quad 33 - 30 = 3 < 8$$

$$\text{Merge } M_1 = \{R_{21} \cup R_{22}\}$$

$$M_1 \& R_{24}, \quad 37 - 30 = 7 < 8$$

$$\text{Merge } M_2 = \{M_1 \cup R_{24}\}$$

$$R_3 \& R_4, \quad 58 - 51 = 7 < 8$$

$$M_3 = \{R_3 \cup R_4\}$$

R_1	M_2	R_{22}
M_3		

10	9	30	4
7	6	33	37
51	52	54	53
55	57	56	58

Q.4

$$F = \begin{bmatrix} 7 & 5 & 6 & 4 & 5 \\ 7 & 4 & 5 & 7 & 4 \\ 5 & 5 & 6 & 2 & 3 \\ 0 & 3 & 1 & 0 & 4 \\ 2 & 1 & 0 & 2 & 3 \end{bmatrix}$$

Range 0-7

Threshold = 3

① Seed point $S_1(0,0)=7$ & $T=3$

$$\text{If } |F(x,y) - 7| \leq 3$$

i.e. $F(x,y) = \{4, 5, 6, 7\}$
 then $F(x,y) = A$

$$F = \begin{bmatrix} 0 & A & A & A & A & A \\ 1 & A & A & A & A & A \\ 2 & A & A & A & 2 & 3 \\ 3 & 0 & 3 & 1 & 0 & 4 \\ 4 & 2 & 1 & 0 & 2 & 3 \end{bmatrix}$$
 $R_1 = \{A\}$ ② Seed pt. $S_2(2,3)=2$

$$\text{If } |F(x,y) - 2| \leq 3$$

i.e. $F(x,y) = \{1, 2, 3, 4, 5\}$
 then $F(x,y) = B$

$$F = \begin{bmatrix} A & A & A & A & A \\ A & A & A & A & A \\ A & A & A & B & B \\ B & B & B & B & B \\ B & B & B & B & B \end{bmatrix}$$
 $R_2 = \{B\}$ $R = \{R_1 \cup R_2 \cup R_3\}$

Q.6

- (a) Laplacian is not a good edge operator - False
- (b) Laplacian is better than gradient for detection of edges - False
- (c) Image resulting from poor illumination can't be segmented easily - True
- (d) Segmentation algg. for monochrome images generally based on 2 basic properties of gray level values - True
- (e) First order derivative operators can detect any edge in gray image - False
- (f) Hough transform is not suitable for vertical lines. - False

Q.2

S_1	S_2	S_3	S_4	S_5	S_6	S_7	S_8
0.25	0.15	0.06	0.08	0.21	0.14	0.07	0.04

 S_1 0.25 S_8 0.04 S_5 0.21 S_2 0.15 S_6 0.14 S_4 0.08 S_3 0.06