

Sardar Patel Institute of Technology

Bhavan's Campus, Munshi Nagar, Andheri (West), Mumbai-400058, India (Autonomous College Affiliated to University of Mumbai)

END SEMESTER EXAMINATION SECTION-I

Total Marks: 60 Duration: 2 Hrs Class: SE Semester: III

Name of the Course: Linear Algebra Branch: ETRX/EXTC

Instructions:

- (1) All questions are compulsory
- (2) Assume suitable data if necessary
- (3) All steps to be shown for full credit
- (4) Marks and time are inclusive of section I and II

(4) IVIa	(4) Marks and time are inclusive of section I and II				
Q NO.		Max Marks	СО		
Q.1	Find the rank of the following matrix by converting first into row echelon form and then to reduced row echelon form. $A = \begin{bmatrix} 2 & -1 & 3 & 4 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 4 \\ 2 & 5 & 11 & 6 \end{bmatrix}$	07	CO1		
Q.2	Solve following equations by Gauss Jacobi iteration method,	07	CO2		
	Take 5 iterations, show working for first 2 iterations. Take answer correct up to 4 decimals.				
	2x - 14y + 3z = 19				
	x - 3y + 16z = 20				
	14x - y + 3z = 18				
Q.3	Decode the following message:	08	CO3		
	26,4,5,8,14,19,3,12,9,25,26,27,14,26,19,9,22,14,13,24,27				
	under modulo 27, using key matrix A,				
	where $A = \begin{bmatrix} 1 & 2 & 1 \\ -1 & 0 & 3 \\ 0 & 0 & 1 \end{bmatrix}$				

Q.4	Find the characteristic equation of the matrix A where	08	CO5
	$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}$		
	Show that the matrix A satisfies its characteristic equation and hence find (a) A^{-1} (b) A^4		
	OR		
	If $A = \begin{bmatrix} 8 & -8 & -2 \\ 4 & -3 & -2 \\ 3 & -4 & 1 \end{bmatrix}$ Show that A is diagonalizable. Find diagonal matrix D and transforming matrix M		

