

## BHARATIYA VIDYA BHAVAN'S SARDAR PATEL INSTITUTE OF TECHNOLOGY MUNSHI NAGAR, ANDHERI (WEST), MUMBAI – 400 058, India

(Autonomous College Affiliated to University of Mumbai)

## Mid Semester Examination October 2023

Max. Marks: 30 Duration:1 Hour

Class: SE EXTC (A & B) Semester: III Course Code: MA201 Date: 09/10 /23

Subject :- Linear Algebra Time: 10.00 to 11.00 a.m.

Instructions: (1) All questions are compulsory.

(2) Use of scientific calculator is allowed.

Q. No.	Questions	Max. Marks	CO 1	BL
Q. 1	Show that the following system of equations is consistent if a, b, c are in arithmetic progression. $3x + 4y + 5z = a$ , $4x + 5y + 6z = b$ , $5x + 6y + 7z = c$ Find the solution when $a = 1$ , $b = 2$ , $c = 3$ .	7		2
Q. 2	Apply Gauss –Seidel Method to solve the following equations $20x + y - 2z = 17$	7	CO 2	3
	3x + 20y - z = -18 $2x - 3y + 20z = 25$ Note: - Perform 5 iterations.			
Q. 3	Is the matrix $A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ diagonalisable? If so find the diagonal matrix and the transforming matrix.	7	CO 5	3
Q. 4	Show that the Eigen values of a unitary matrix are of unit modulus.	2	CO 6	1.
Q. 5	Find the characteristic equation of the matrix $A = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix} \text{ and verify that it is satisfied by A and hence obtain A}^{-1} \text{ and } A^4$	7	CO6	2
	OR	97		

Find characteristic equation of the matrix $A = \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}$	1 1 1	1 0 2		
& find the matrix represented by				P
$A^8 - 5A^7 + 7A^6 - 3A^5 + A^4 - 5A^3 + 8A^2 - 2A + I$				

\*\*\*\*\*\* The End \*\*\*\*\*\*