

2)

Statement: $!(A \rightarrow B) \wedge (B \rightarrow (C \rightarrow A))$								
	A	B	C	$!(A \rightarrow B)$	\wedge	$(B \rightarrow (C \rightarrow A))$		
0)	0	0	0	0	1	0	1	1
1)	0	0	1	0	1	0	1	0
2)	0	1	0	0	1	0	1	1
3)	0	1	1	0	1	0	0	0
4)	1	0	0	1	0	1	1	1
5)	1	0	1	1	0	1	1	1
6)	1	1	0	0	1	0	1	1
7)	1	1	1	0	1	0	1	1

3)

Statement: $!(A \rightarrow B) \rightarrow (B \rightarrow (C \rightarrow A))$								
	A	B	C	$!(A \rightarrow B)$	\rightarrow	$(B \rightarrow (C \rightarrow A))$		
0)	0	0	0	0	1	1	1	1
1)	0	0	1	0	1	1	1	0
2)	0	1	0	0	1	1	1	1
3)	0	1	1	0	1	0	0	0
4)	1	0	0	1	0	1	1	1
5)	1	0	1	1	0	1	1	1
6)	1	1	0	0	1	1	1	1
7)	1	1	1	0	1	1	1	1

4)

Statement: $((A \rightarrow B) \vee (B \rightarrow C)) \vee (A \rightarrow C)$								
	A	B	C	$(A \rightarrow B)$	\vee	$(B \rightarrow C)$	\vee	$(A \rightarrow C)$
0)	0	0	0	1	1	1	1	1
1)	0	0	1	1	1	1	1	1
2)	0	1	0	1	1	0	1	1
3)	0	1	1	1	1	1	1	1
4)	1	0	0	0	1	1	1	0
5)	1	0	1	0	1	1	1	1
6)	1	1	0	1	1	0	1	0
7)	1	1	1	1	1	1	1	1

5)

Statement:	$(A \vee B) \rightarrow (B \vee A)$
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	A	B	$(A \vee B)$	\rightarrow	$(B \vee A)$
0)	0	0	0	1	0
1)	0	1	1	1	1
2)	1	0	1	1	1
3)	1	1	1	1	1

6)

Statement:	$(A \vee (B \wedge C)) \rightarrow ((A \vee B) \wedge (A \vee C))$
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	A	B	C	$(A \vee (B \wedge C))$	\rightarrow	$((A \vee B) \wedge (A \vee C))$
0)	0	0	0	0	1	0
1)	0	0	1	0	1	0
2)	0	1	0	0	1	0
3)	0	1	1	1	1	1
4)	1	0	0	1	1	1
5)	1	0	1	1	1	1
6)	1	1	0	1	1	1
7)	1	1	1	1	1	1

7)

- 1: $(P \rightarrow Q) \vee (P \rightarrow R)$ premise
- 2: P assumption
- 3: $P \rightarrow Q$ assumption
- 4: Q \rightarrow elim 3,2
- 5: $Q \vee R$ \vee intro 4
- 6: $P \rightarrow R$ assumption
- 7: R \rightarrow elim 6,2
- 8: $Q \vee R$ \vee intro 7
- 9: $Q \vee R$ \vee elim 1,3-5,6-8
- 10: $P \rightarrow (Q \vee R)$ \rightarrow intro 2-9

8)

1:	$(A \rightarrow B) \wedge (A \rightarrow C)$	assumption
2:	A	assumption
3:	$A \rightarrow B$	\wedge elim 1
4:	B	\rightarrow elim 3,2
5:	$A \rightarrow C$	\wedge elim 1
6:	C	\rightarrow elim 5,2
7:	$B \wedge C$	\wedge intro 4,6
8:	$A \rightarrow (B \wedge C)$	\rightarrow intro 2-7
9:	$((A \rightarrow B) \wedge (A \rightarrow C)) \rightarrow (A \rightarrow (B \wedge C))$	\rightarrow intro 1-8

9)

1:	$E \rightarrow (F \wedge G)$	premise
2:	E	assumption
3:	$F \wedge G$	\rightarrow elim 1,2
4:	F	\wedge elim 3
5:	$E \rightarrow F$	\rightarrow intro 2-4
6:	E	assumption
7:	$F \wedge G$	\rightarrow elim 1,6
8:	G	\wedge elim 7
9:	$E \rightarrow G$	\rightarrow intro 6-8
10:	$(E \rightarrow F) \wedge (E \rightarrow G)$	\wedge intro 5,9

10)

1:	$(A \vee B) \wedge (A \vee C)$	premise
2:	$A \vee C$	\wedge elim 1
3:	A	assumption
4:	$A \vee (B \wedge C)$	\vee intro 3
5:	C	assumption
	...	
6:	B	
7:	$B \wedge C$	\wedge intro 6,5
8:	$A \vee (B \wedge C)$	\vee intro 7
9:	$(A \vee (B \wedge C))$	\vee elim 2,3-4,5-8

11)

1:	$\neg(P \wedge Q) \rightarrow (\neg P \vee \neg Q)$	premise
2:	$\neg P \vee \neg Q$	assumption
3:	$P \wedge Q$	assumption
4:	Q	\wedge elim 3
5:	P	\wedge elim 3
6:	$\neg P$	assumption
7:	\perp	\neg elim 5,6
8:	$\neg Q$	assumption
9:	\perp	\neg elim 4,8
10:	\perp	\vee elim 2,6-7,8-9
11:	$\neg(P \wedge Q)$	\neg intro 3-10
12:	$(\neg P \vee \neg Q) \rightarrow \neg(P \wedge Q)$	\rightarrow intro 2-11

12)

1:	$(P \rightarrow Q) \wedge (P \wedge \neg Q)$	premise
2:	$\neg R$	assumption
3:	$P \rightarrow Q$	\wedge elim 1
4:	$P \wedge \neg Q$	\wedge elim 1
5:	P	\wedge elim 4
6:	Q	\rightarrow elim 3,5
7:	$\neg Q$	\wedge elim 4
8:	\perp	\neg elim 6,7
9:	R	contra (classical) 2-8

13)

1:	$\neg(\neg P \vee \neg Q)$	premise
2:	$\neg(P \wedge Q)$	assumption
3:	Q	assumption
4:	P	assumption
5:	$P \wedge Q$	\wedge intro 4,3
6:	\perp	\neg elim 5,2
7:	$\neg P$	\neg intro 4-6
8:	$\neg P \vee \neg Q$	\vee intro 7
9:	\perp	\neg elim 8,1
10:	$\neg Q$	\neg intro 3-9
11:	$\neg P \vee \neg Q$	\vee intro 10
12:	\perp	\neg elim 11,1
13:	$P \wedge Q$	contra (classical) 2-12

14)

1:	$\neg(P \wedge Q)$	premise
2:	$\neg(\neg P \vee \neg Q)$	assumption
3:	P	assumption
4:	$\neg Q$	assumption
5:	$\neg P \vee \neg Q$	\vee intro 4
6:	\perp	\neg elim 5,2
7:	Q	contra (classical) 4-6
8:	$P \wedge Q$	\wedge intro 3,7
9:	\perp	\neg elim 8,1
10:	$\neg P$	\neg intro 3-9
11:	$\neg P \vee \neg Q$	\vee intro 10
12:	\perp	\neg elim 11,2
13:	$\neg P \vee \neg Q$	contra (classical) 2-12

15)

1:	$(P \wedge \neg P) \vee (Q \wedge \neg Q)$	assumption
2:	$P \wedge \neg P$	assumption
3:	P	\wedge elim 2
4:	$\neg P$	\wedge elim 2
5:	\perp	\neg elim 3,4
6:	$Q \wedge \neg Q$	assumption
7:	Q	\wedge elim 6
8:	$\neg Q$	\wedge elim 6
9:	\perp	\neg elim 7,8
10:	\perp	\vee elim 1,2-5,6-9
11:	$\neg((P \wedge \neg P) \vee (Q \wedge \neg Q))$	\neg intro 1-10

16)