



# Importance of Branch Instr. & its Penalty

Branch penalty –

- Intel core i7 - **14 cycles**
- ARM Cortex – A8 - **13 cycles**
- AMD – **19 cycles**
- MIPS – 5-stage pipeline - ?

Can you imagine a useful program without any branch instructions or if-else or loop?

Branchless programming

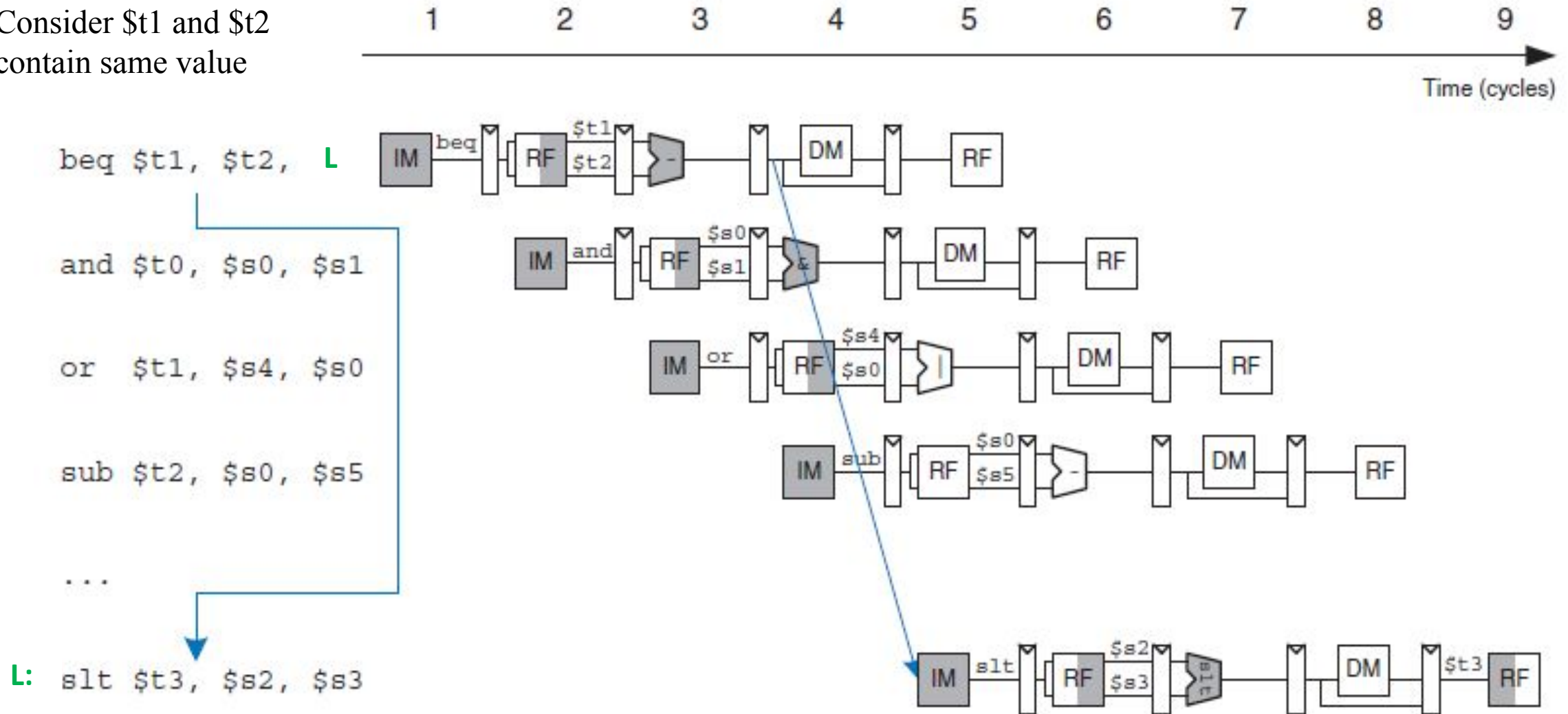
Program contains **15% to 25% branch instructions** among all instructions

# Objectives

- Minimize the penalty for control hazard
- Methods for the minimization
  - Appropriate time to take the branch decision
  - Filling the instruction the delayed branch slot
  - Branch prediction
    - Static [Compile time]
    - Dynamic [Execution time]
  - Branchless programming

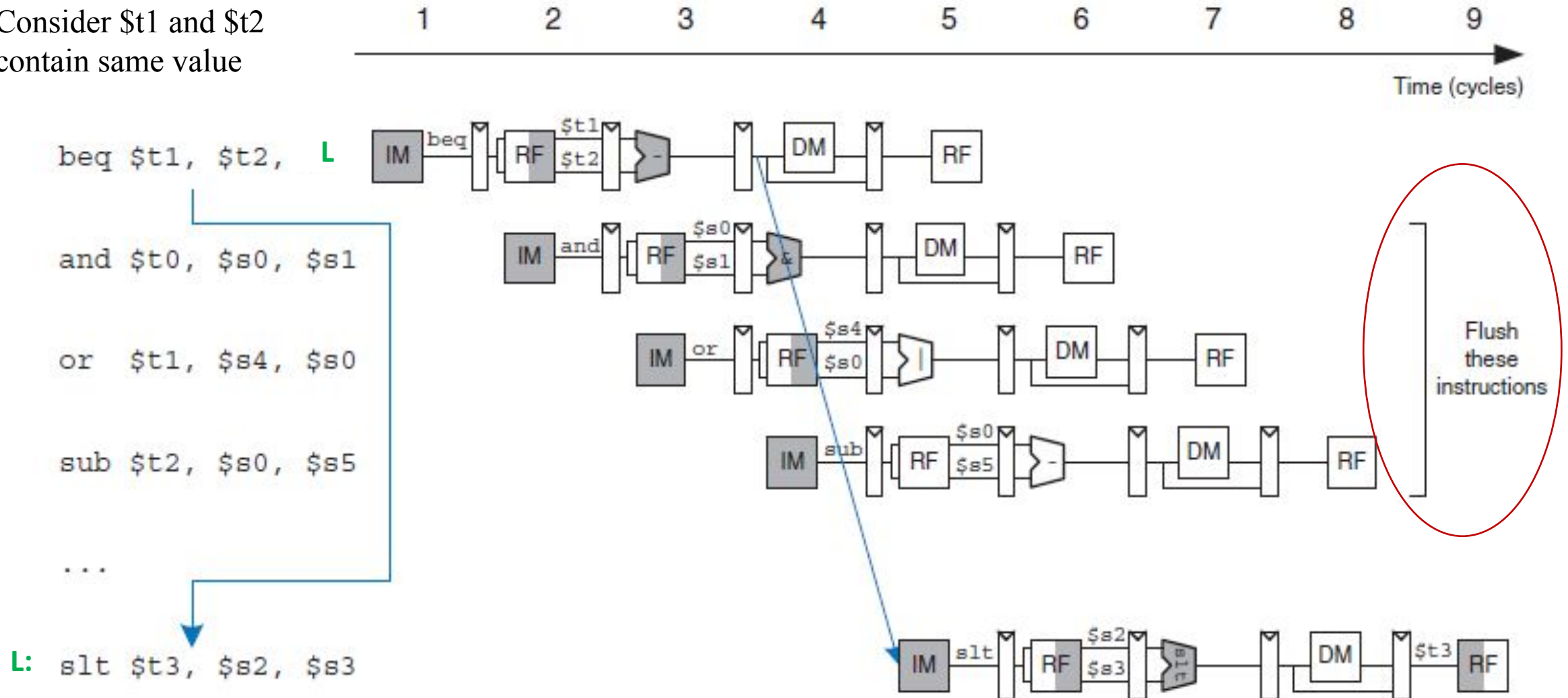
# What is this?

Consider \$t1 and \$t2  
contain same value



# An example of Control Hazards

Consider \$t1 and \$t2  
contain same value



# Control Hazards

- **EX-stage computes** the branch target address
- Cause higher performance penalty as compared to data hazards
- How does one reduce such penalty?
  - Take the branch decision early
    - ID and/or IF
    - IF-stage
      - Can we predict the next PC value from the current PC value?
        - $PC_{next} = g(PC_{current})$

# Control Hazards

- What if branch target address is computed at the **end of ID-stage**

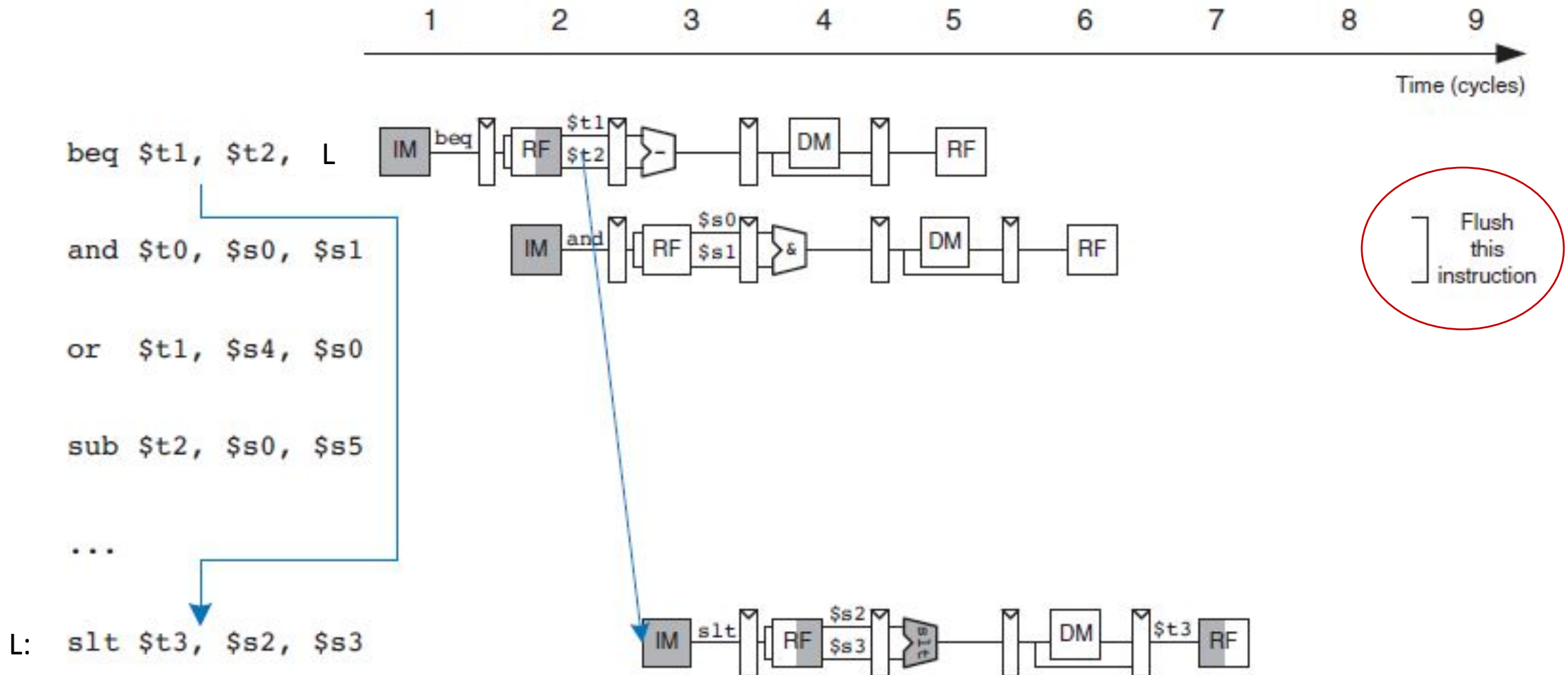
Branch instr.	IF	ID	EXE	MEM	WB		
Branch succ.		<b>IF</b>	<b>IF</b>	ID	EXE	MEM	WB
Branch succ + 1				IF	ID	EXE	MEM
Branch succ + 2					IF	ID	EX

$$\begin{aligned}
 \text{Speedup} &= \frac{CPI_{\text{unpipelined}}}{1 + \text{pipeline stall cycle from branches}} \\
 &= \frac{\text{Pipeline depth}}{1 + \text{Branch frequency} \times \text{Branch penalty}}
 \end{aligned}$$



# Control Hazards

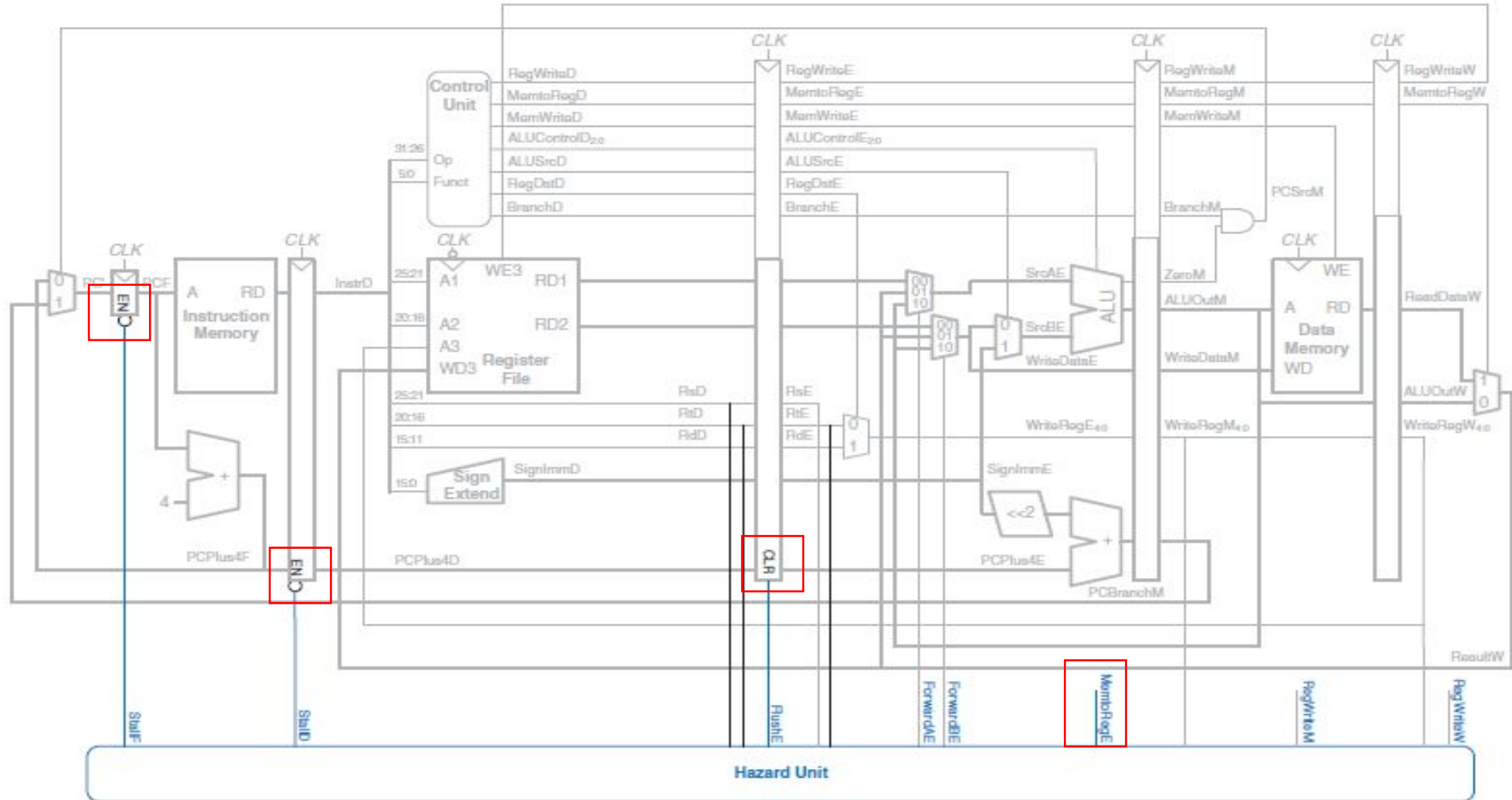
- Branch target address is computed at the end of ID-stage



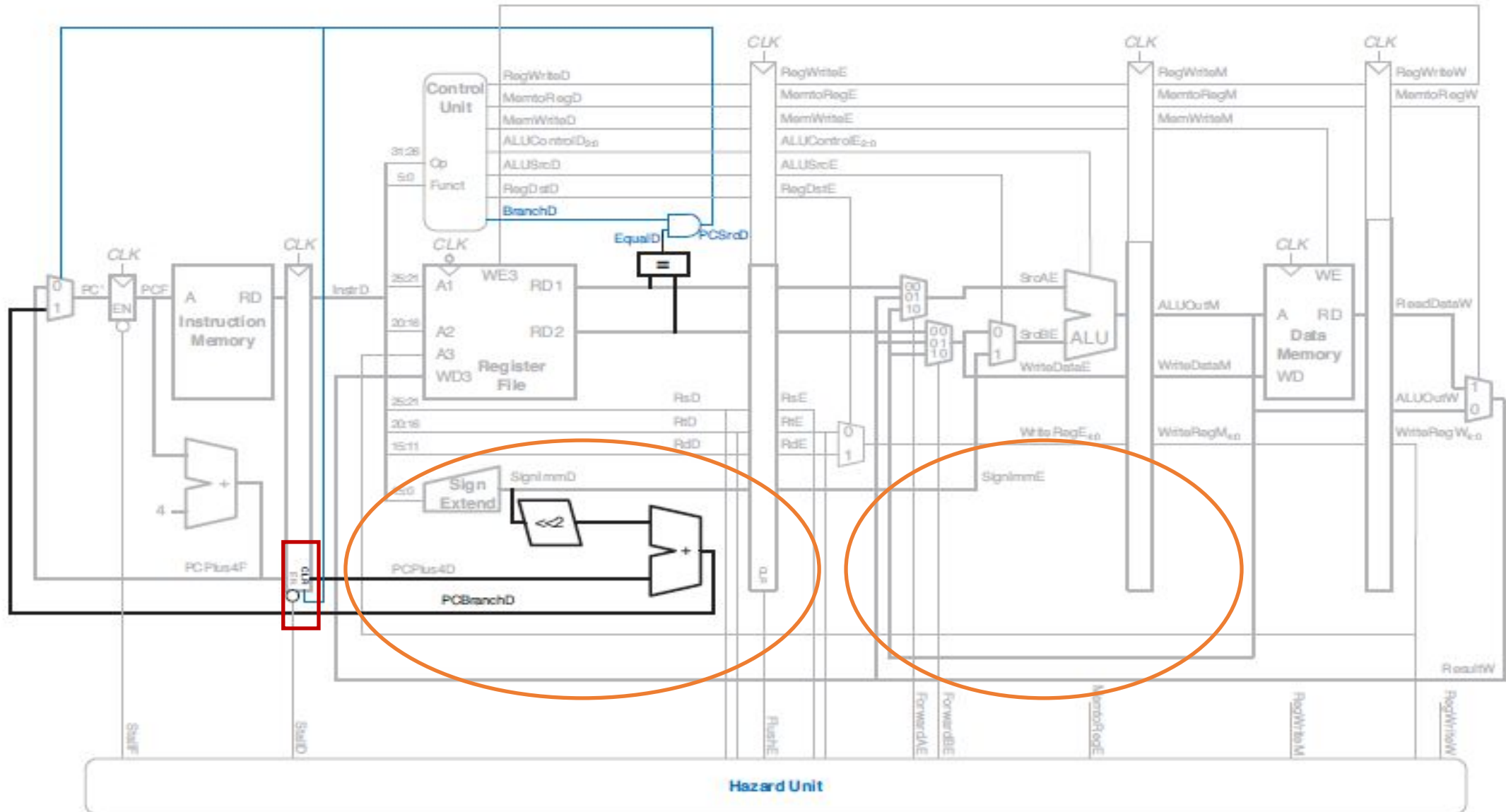


# Control Hazards

- Branch target address is computed at the end of ID-stage
- What modifications are needed in the pipelined datapath & controlpath?



# Control Hazards: Modified Pipeline

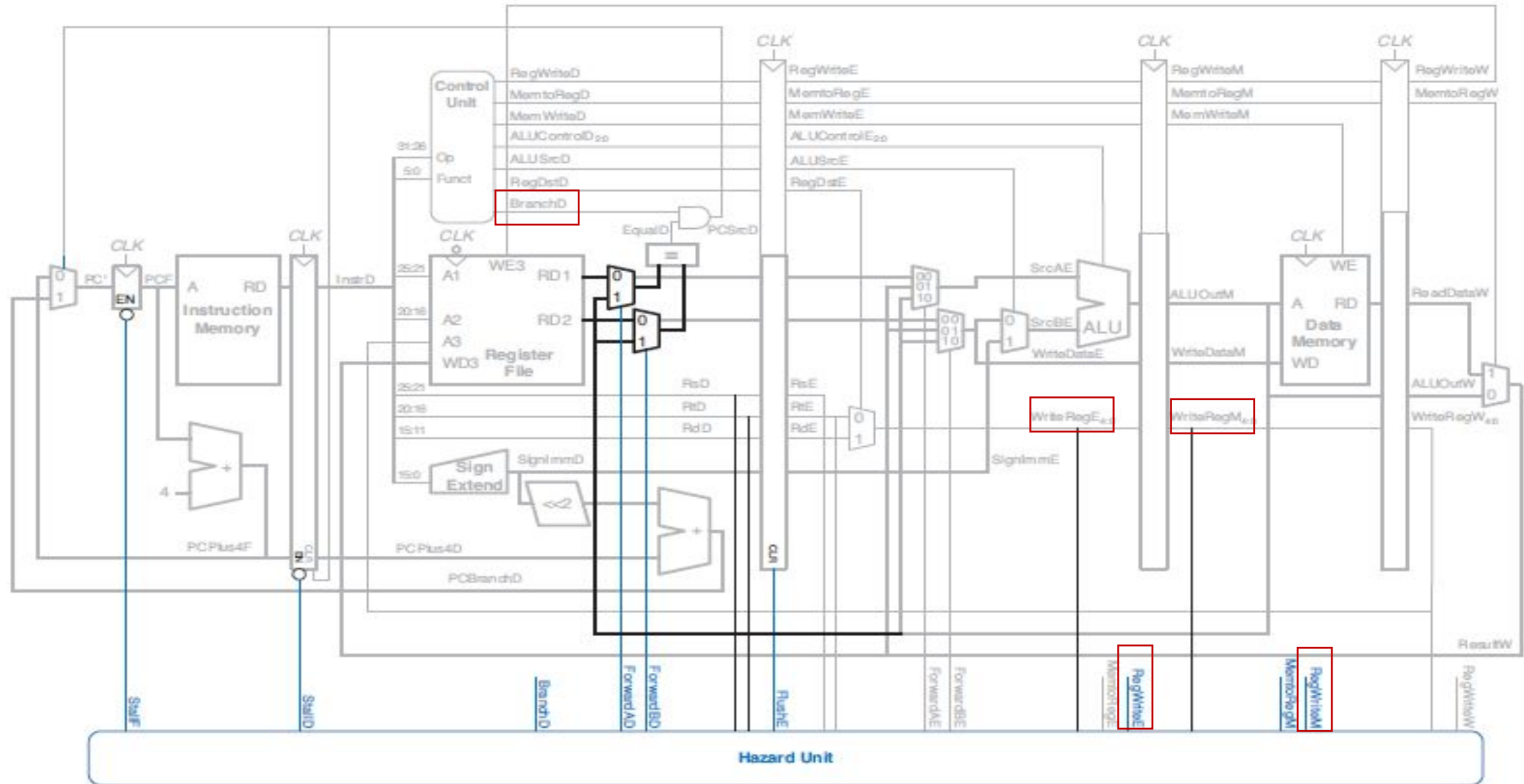


# Control Hazards: Modified Pipeline

- What if one source operand of branch instruction was computed by a previous instruction and has not yet been updated into register file?
- One can use forwarding techniques
- Stalling technique can be used (lw-type)

# Control Hazards & H/W-based solutions

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# Control Hazards & H/W-based solutions

- The function of the decode stage & forwarding logic
- $\text{FowardAD} = (\text{rsD} \neq 0) \text{ AND } (\text{rsD} == \text{WriteRegM}) \text{ AND } \text{RegWriteM}$
- $\text{FowardBD} = (\text{rtD} \neq 0) \text{ AND } (\text{rtD} == \text{WriteRegM}) \text{ AND } \text{RegWriteM}$

**E**: EXE/MEM, **D**: ID/EXE, **M**: MEM/WB

# Control Hazards & H/W-based solutions

- The function of the stall detection logic for a branch instruction
  - What if one of the source operands is in Execute stage and R-type instr. **or**
  - What if one of the source operands is in the Memory stage for a lw-type instruction?
- Branchstall=

BranchD AND RegWriteE AND (WriteRegE == rsD OR WriteRegE == rtD)

OR

BranchD AND MemtoRegM AND (WriteRegM == rsD OR WriteRegM == rtD)

**E**: EXE/MEM, **D**: ID/EXE, **M**: MEM/WB

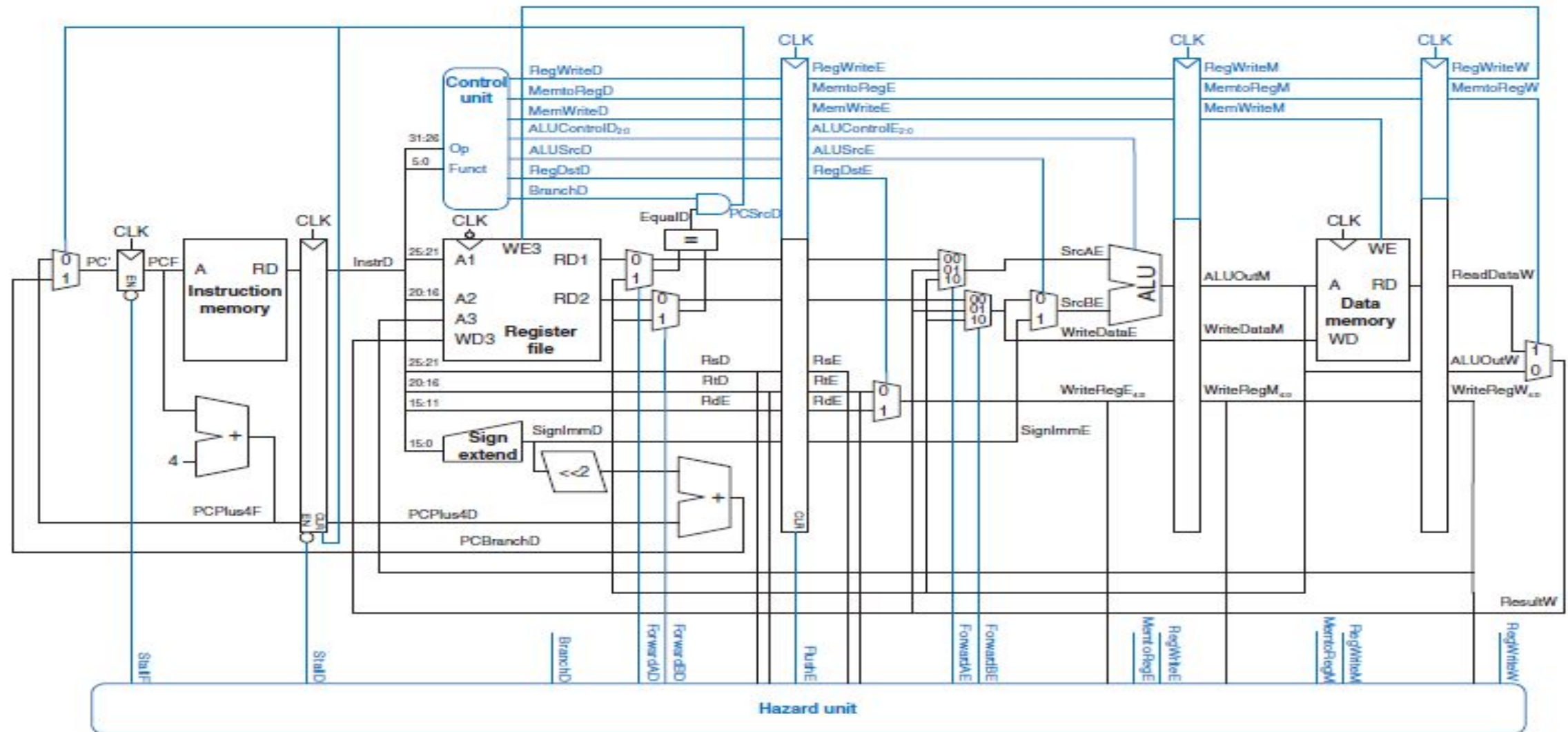
# Control Hazards & H/W-based solutions

- Now the pipelined processor stall due to either a load or a branch hazard
- $\text{StallF} = \text{StallD} = \text{FlushE} = \text{lwstall OR branchstall}$



# Pipelined processor with full hazard handling unit

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# Pipelined processor with full hazard handling unit

- Determine the cycle time
  - consider the critical path
  - five pipeline stages
- Register file is written in the first half of the Writeback cycle and read in the second half of the Decode cycle
- The cycle time of the Decode and Writeback stages is twice the time necessary to do the half-cycle of work

$$\bullet \text{ Cycle period, } T_c = \max \left( \begin{array}{c} t_{pcq} + t_{mem} + t_{setup} \\ 2(t_{RFread} + t_{mux} + t_{eq} + t_{AND} + t_{mux} + t_{setup}) \\ t_{pcq} + t_{mux} + t_{mux} + t_{ALU} + t_{setup} \\ t_{pcq} + t_{memwrite} + t_{setup} \\ 2(t_{pcq} + t_{mux} + t_{RFWrite}) \end{array} \right)$$

# Pipelined processor with full hazard handling unit

- XYZ needs to compare the pipelined processor performance to that of the single-cycle and multicycle processors considered in earlier. Most of the logic delays is given in Table. The other element delays are 40 ps for an equality comparator, 15 ps for an AND gate, 100 ps for a register file write, and 220 ps for a memory write. Help XYZ compare the execution time of 100 billion instructions of the program for each processor.

Parameter	Delay (ps)
	30
	250
	20
	200
	25
	20
	20

# Characteristics of the Program and Avg. CPI

Instruction type	%
Load	25
Store	10
Branch	11
Jump	2
R-type	52

Additional information:

40% loads are immediately followed by an instruction that uses the result, required a stall.

25% of branches are mispredicted, required a flush.

Jumps always flush the subsequent instructions.

Ignore other hazards.

Loads take 1-clock cycle when there is no dependency

2-clock cycle when there is a dependency

$$0.6 * (1) + 0.4 * (2)$$

Branches take 1-clock cycle for correct prediction

2-clock cycle for misprediction

$$0.75 * (1) + 0.25 * (2)$$

Jumps always have a CPI of 2

Other instructions have a CPI of 1

Average CPI=

$$0.25 [0.6 * (1) + 0.4 * (2)] +$$

$$0.1 [1] +$$

$$0.11 [0.75 * (1) + 0.25 * (2)] +$$

$$0.02 [2] +$$

$$0.52 [1]$$

$$=1.15$$

# Pipelined processor with full hazard handling unit

- According to Equation on slide 15, the cycle time of the pipelined processor is

$$T_{c3} = \max[30 + 250 + 20, 2(150 + 25 + 40 + 15 + 25 + 20), 30 + 25 + 25 + 200 + 20, 30 + 220 + 20, 2(30 + 25 + 100)] = 550 \text{ ps.}$$

- According to Equation of CPI, the total execution time is  $T_3 = (100 \times 10^9 \text{ instructions})(1.15 \text{ cycles/instruction}) (550 \times 10^{-12} \text{ s / cycle}) = 63.3 \text{ seconds.}$
- For the single-cycle processor it is 92.5 seconds and 133.9 seconds for the multicycle processor.
- What can be observed?

# Static branch prediction

# Control Hazards & Software-based solutions

- Assumption: predict-not-taken or predict-untaken
- Where does this assumption come from?
- Compiler rearranges the code
- Control flow will change only when prediction is wrong
- Example:

Untaken branch instruction	IF	ID	EX	MEM	WB				
Instruction i+1		IF	ID	EX	MEM	WB			
Instruction i+2			IF	ID	EX	MEM	WB		
Instruction i+3				IF	ID	EX	MEM	WB	
Instruction i+4					IF	ID	EX	MEM	WB



# Control Hazards & Software-based solutions

- Assumption: predict-not-taken or predict-untaken
- Where does this assumption come from?
- Compiler rearranges the code
- Control flow will change only when prediction is wrong
- Example:

Prediction goes wrong

Taken branch instruction	IF	ID	EX	MEM	WB				
Instruction i+1		IF	idle	idle	idle	idle			
Branch target			IF	ID	EX	MEM	WB		
Branch target +1				IF	ID	EX	MEM	WB	
Branch target +2					IF	ID	EX	MEM	WB

# Control Hazards & Software-based solutions

- Assumption: predict-taken
- Compiler rearranges the code, for both the assumptions, so that the most frequent path matches the hardware's choice

# Control Hazards & Software-based solutions

- Which assumption is suitable for pipelined MIPS-based processor?
- Predict-untaken

# Control Hazards & Software-based solutions

- Prediction based on control flow
- How many types of branch are possible?
  - Forward branch
  - Backward branch
- For backward-type branch, predict-taken is suitable
- For forward-type branch, predict-untaken is suitable

# Control Hazards & Software-based solutions

- Is there another way to specify predict-taken or predict-untaken in the branch instruction?
- A bit in the branch opcode
  - Bit set means predict-taken
  - Bit not set means predict-untaken
- Who will set or reset such bit?
  - Compiler

# Control Hazards & Software-based solutions

- Can we eliminate one cycle delay associated in branch prediction?
- Delayed branch technique

# Control Hazards & Delayed branch (S/W-based approach)

- Delayed branch technique
- Examples
- Find useful & independent instruction
- How many delay slots?

<b>Untaken</b> branch instruction	IF	ID	EX	MEM	WB				
Branch Delay Instruction i+1		IF	ID	EX	MEM	WB			
Instruction i+2			IF	ID	EX	MEM	WB		
Instruction i+3				IF	ID	EX	MEM	WB	
Instruction i+4					IF	ID	EX	MEM	WB
<b>Taken</b> branch instruction	IF	ID	EX	MEM	WB				
Branch Delay Instruction i+1		IF	ID	EX	MEM	WB			
Instruction i+2			IF	ID	EX	MEM	WB		
Instruction i+3				IF	ID	EX	MEM	WB	
Instruction i+4					IF	ID	EX	MEM	WB

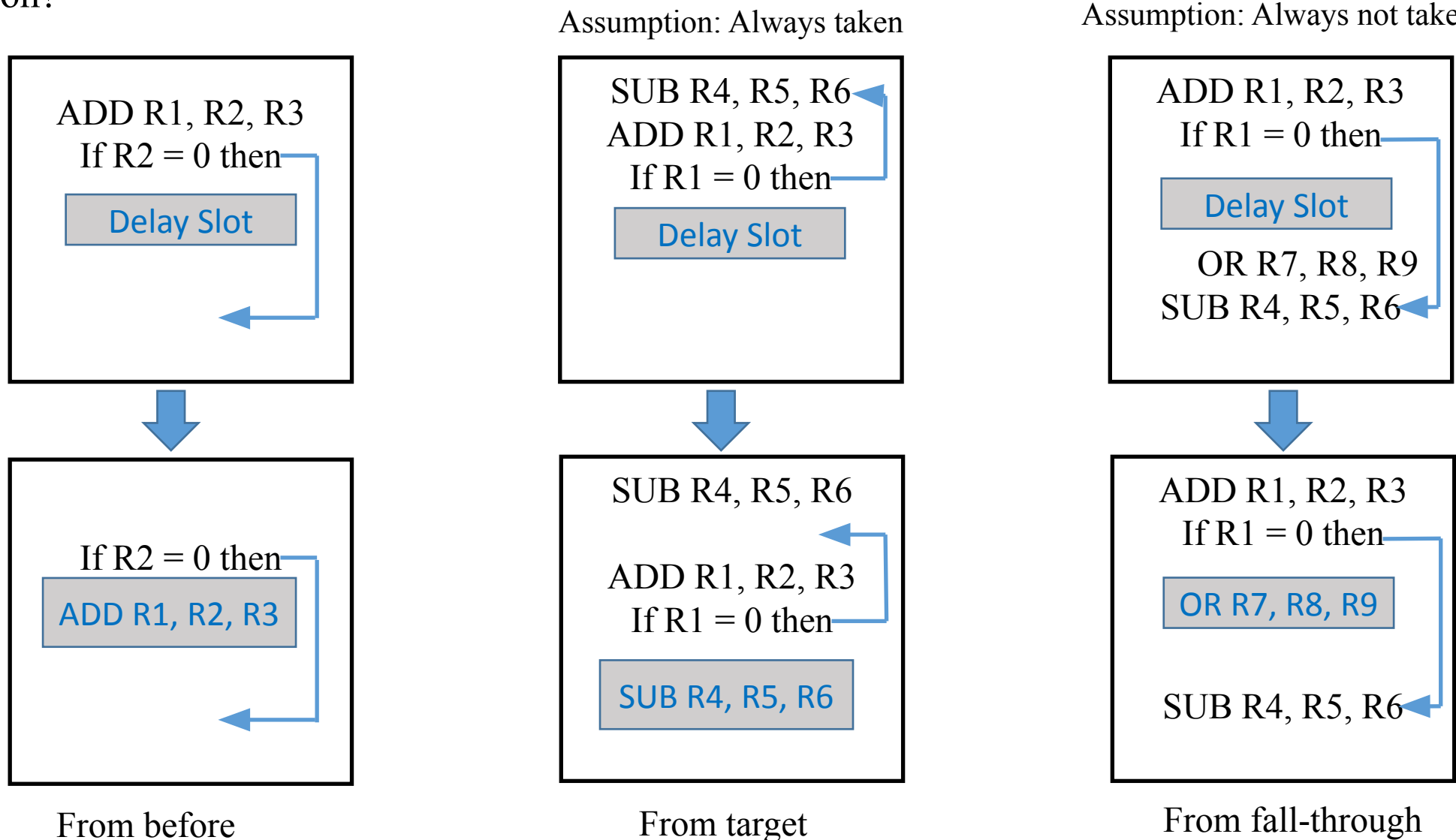


## Control Hazards & Delayed branch (S/W-based approach)

- How does compiler find useful & independent instruction?
- Can compiler always find such instruction?

# Control Hazards & Delayed branch (S/W-based approach)

- How does compiler find useful & independent instruction?
- Can we put a branch instruction in the delay slot?



# Control Hazards, static analysis & software-based solution

- Previous software-based approaches are based on static analysis
  - Assumption on Processor Design
    - Predict-not-taken
    - Predict-taken
  - Assumption on Control flow
    - Forward
    - Backward
  - Delayed branch
- Can we take decision during execution of the program?

# Dynamic branch prediction

# Control Hazards and Dynamic Branch Prediction

- Previous software-based approaches are based on static analysis
- Equal priority given to each branch instruction, however reality may differ
  - Branch prediction change if inputs of the program change
- We need to predict the branch behavior during runtime

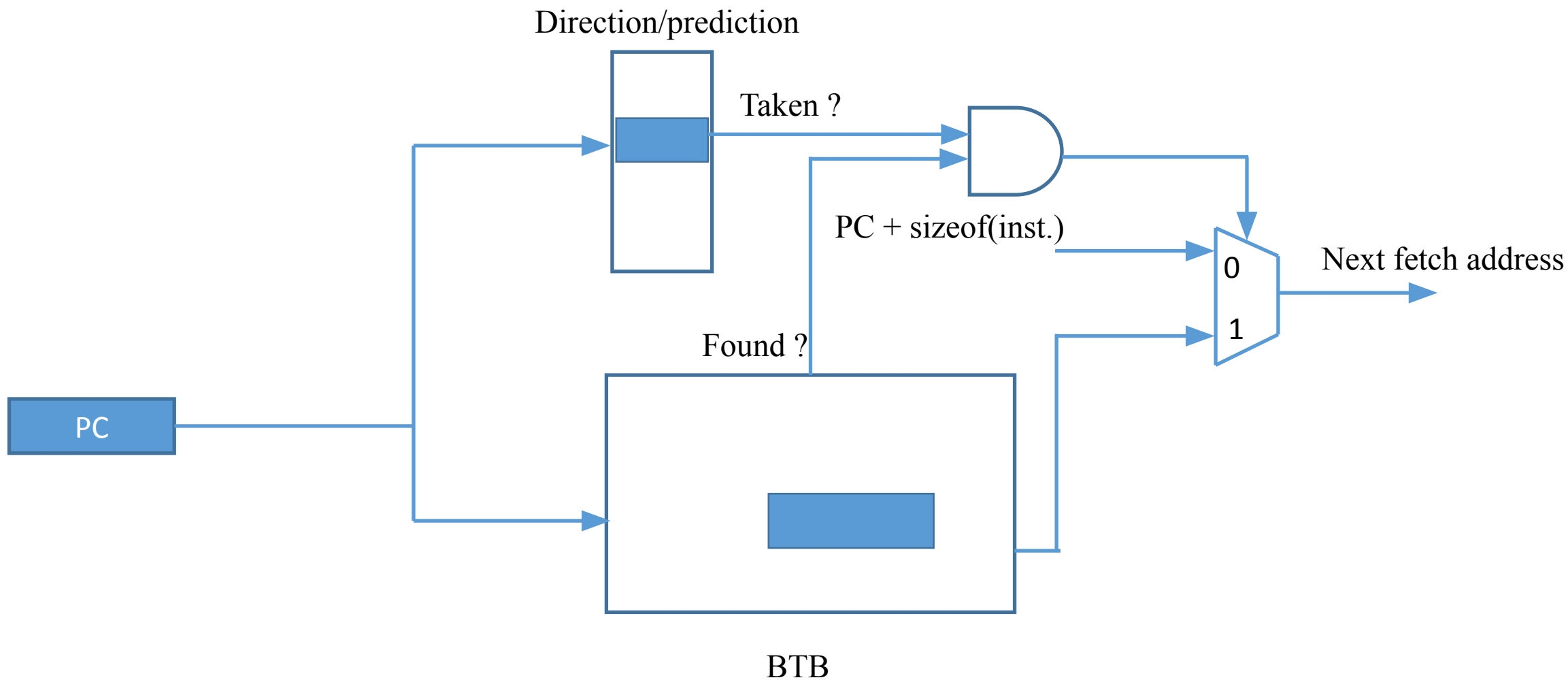
# Control Hazards and Dynamic Branch Prediction

- How does one predict the branch behavior during execution?
- Exploit the previous execution history of the instruction
- What are the components needed to do such thing?
- Component to make prediction & store target address
- Which stage of the pipeline is suitable for that?
- IF-stage

# Control Hazards and Dynamic Branch Prediction

- Three items are needed in IF-stage
  - Is it a branch instruction?
  - What is the branch direction?
    - Conditional
    - Unconditional
  - What is the target address (if taken)?
- Is the target address fixed or changed?

# Dynamic Branch Prediction: BTB





# Control Hazards and Dynamic Branch Prediction

- The *branch-target buffer* (BTB) or *branch-target (address) cache* (BTAC) is a branch-prediction cache that stores the predicted address for the next instruction after a branch

Consider \$t1 and \$t2 contain same value

$$\text{PC} = (\text{PC} + 4) + \text{signExtn}(40)$$

```
20    beq $t1, $t2, 40
```

24 and \$t0, \$s0, \$s1

28 or \$t1, \$s4, \$s0

```
2C    sub $t2, $s0, $s5
```

30 . . .

```
64    slt $t3, $s2, $s3
```

## Address

[illegible]

# Control Hazards and Dynamic Branch Prediction

- The BTB is accessed during the **IF-stage**
- A table with branch addresses, the corresponding target addresses, and prediction information
- The PC for the next instruction to fetch is compared with the entries in the BTB. If a matching entry is found in the BTB, fetching can start immediately at the target address

# Control Hazards and Dynamic Branch Prediction

- What is this prediction bit in the BTB?
- How many bits are needed?

# Control Hazards and Dynamic Branch Prediction

- Example: branch outcome sequence (T – Taken & N – Not Taken)
  - T N T N T N T N T N
- How does one design such a predictor?

# Control Hazards and Dynamic Branch Prediction

- One bit predictor

- If the bit is set, the branch is predicted taken
- If the bit is not set, the branch is predicted not taken
- In the case of a misprediction, the bit state is reversed and stored back and so is the prediction direction

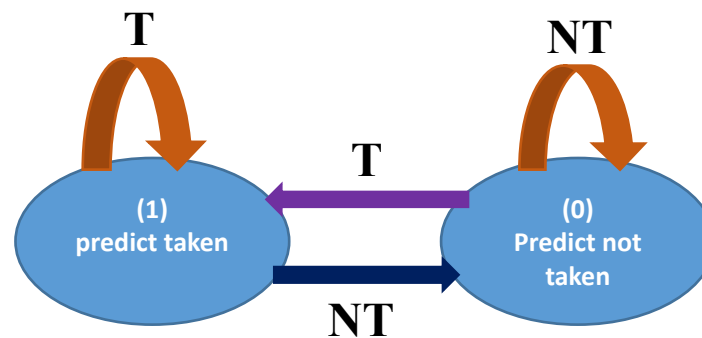
- How does one design such predictor?

- Encode the states
- Relation among the states
- Finite State Machine (FSM)

# Control Hazards and Dynamic Branch Prediction

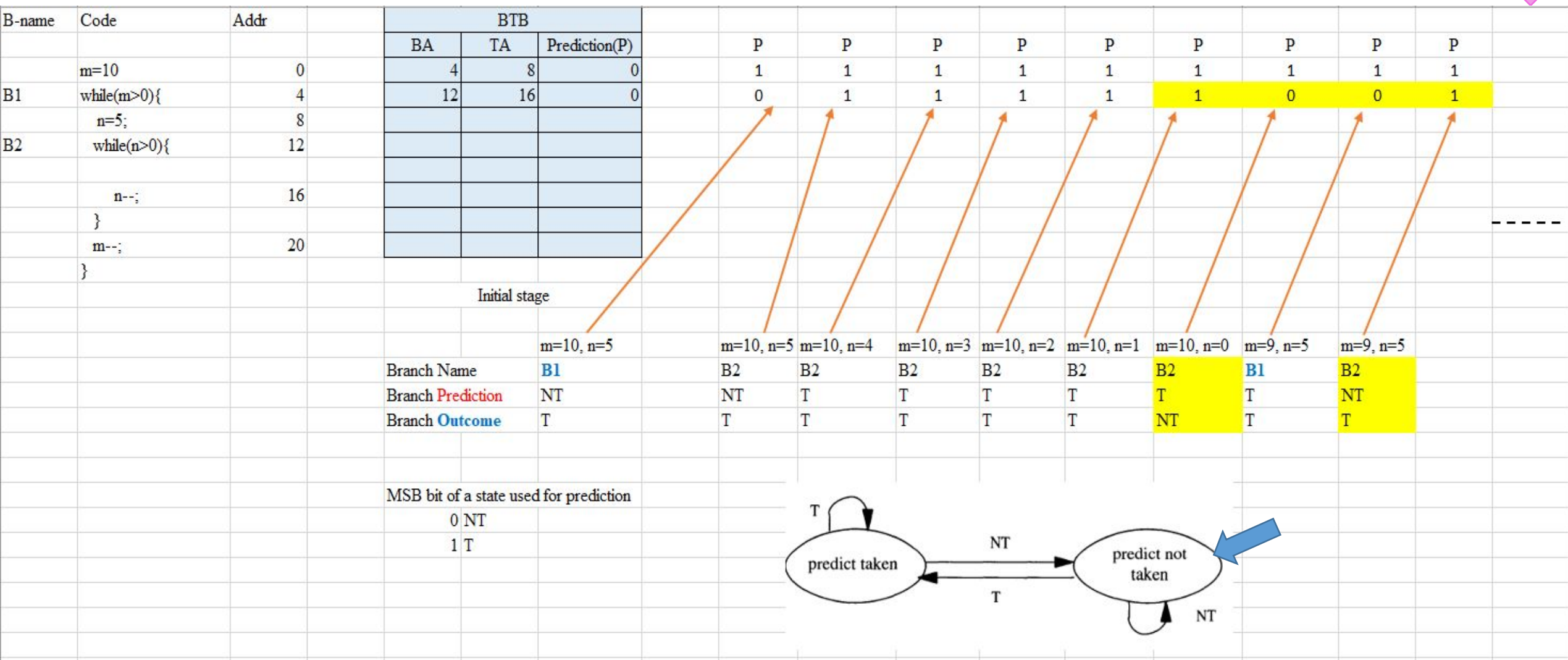
- One bit predictor

- If the bit is set, the branch is predicted taken
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- In the case of a misprediction, the bit state is reversed and stored back and so is the prediction direction



**T** for Taken  
**NT** for Not Taken

# Example



Is there any shortcoming of this approach?

# Control Hazards and Dynamic Branch Prediction

- Shortcoming of one bit predictor
- Predict taken always
- Predict incorrectly twice (why?), rather than once, when it is not taken
- What if we have the nested loops
  - Two misprediction for inner loop
    - Entry in the loop
    - Exit from the loop
  - For a loop with N-iteration the accuracy is  $\frac{N-2}{N}$
  - How does one avoid such double misprediction?

TTTTTNNNNN...

What is the accuracy?

80%

TNTNTNTNTN...

What is the accuracy?

0%



# Control Hazards and Dynamic Branch Prediction

## Two-bit predictor:

- Two-bits are in each entry in the BHT
- The two bits stand for the prediction states:
  - “predict strongly taken”
  - “predict weakly taken”
  - “predict strongly not taken”
  - “predict weakly not taken”
- For a misprediction in the “strongly” state cases, the prediction direction is not changed, rather the prediction goes into the respective “weakly” state
- A prediction must miss twice, before changing the state

# Control Hazards and Dynamic Branch Prediction

- How does one design such 2-bits predictor?

# Control Hazards and Dynamic Branch Prediction

- How does one design such 2-bits predictor?
  - Encode the different states
  - Relation among the states
  - Finite State Machine (FSM)

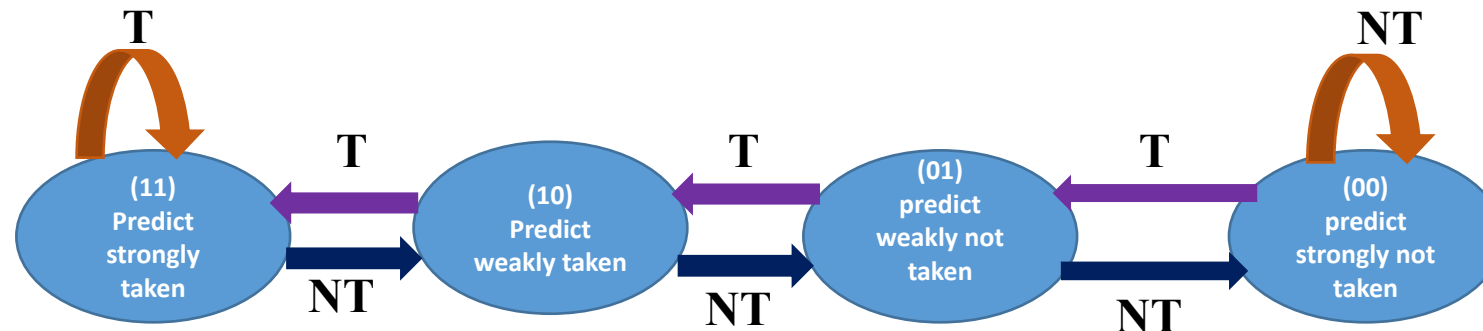
# Control Hazards and Dynamic Branch Prediction

- Two kinds of 2-bits prediction methodology
  - The saturation up-down counter
  - Others

# Control Hazards and Dynamic Branch Prediction

- The saturation up-down counter
  - Taken branch
    - Increment
  - Not taken
    - Decrement
  - Saturation
  - MSB of a state determine the prediction

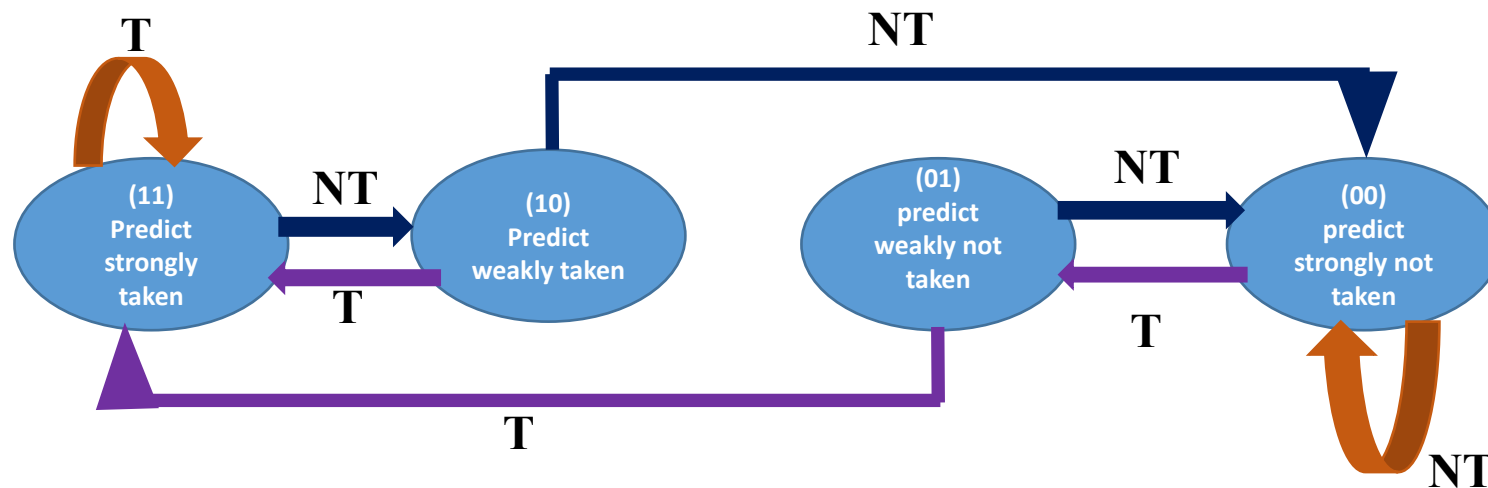
T for Taken  
NT for Not Taken



# Control Hazards and Dynamic Branch Prediction

- Other methodology

- It differs from the saturation up-down counter method by changing directly from the “weakly” to the “strongly” states, in case of misprediction
- Minimize the switching (or power consumption)



T for Taken  
NT for Not Taken

# Example

B-name	Code	Addr	BTB			P	P	P	P	P	P	P	P	P
			BA	TA	Prediction(P)									
B1	m=10	0	4	8	00	01	01	01	01	01	01	01	11	11
	while(m>0){	4	12	16	00	00	01	11	11	11	11	10	10	11
	n=5;	8												
B2	while(n>0){	12												
	n--;	16												
	}	20												
	m--;													
	}													

Initial stage			m=10, n=5	m=10, n=5	m=10, n=4	m=10, n=3	m=10, n=2	m=10, n=1	m=10, n=0	m=9, n=0	m=9, n=5
Branch Name	B1		B2	B2	B2	B2	B2	B2	B2	B1	B2
Branch Prediction	NT		NT	NT	T	T	T	T	T	NT	T
Branch Outcome	T		T	T	T	T	T	T	NT	T	T

MSB bit of a state used for prediction			0 NT
			1 T

```

graph LR
    S11((11)  
predict strongly  
taken)) -- T --> S11
    S11 -- NT --> S10((10)  
predict weakly  
taken))
    S10 -- T --> S11
    S10 -- NT --> S01((01)  
predict weakly  
not taken))
    S01 -- T --> S11
    S01 -- NT --> S00((00)  
predict strongly  
not taken))
    S00 -- T --> S11
    S00 -- NT --> S00
  
```

# Control Hazards and Dynamic Branch Prediction

- n-bits predictor

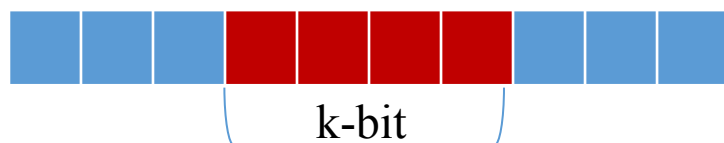
- n-bit counter (0 to  $2^n - 1$ )
- Taken when counter value is one-half of the max. value ( $2^n - 1$ )
- Otherwise, Not taken
- Studies of n-bits predictor have shown that 2-bits predictor do almost well, thus most systems rely on 2-bits predictor



# Bimodal Predictor

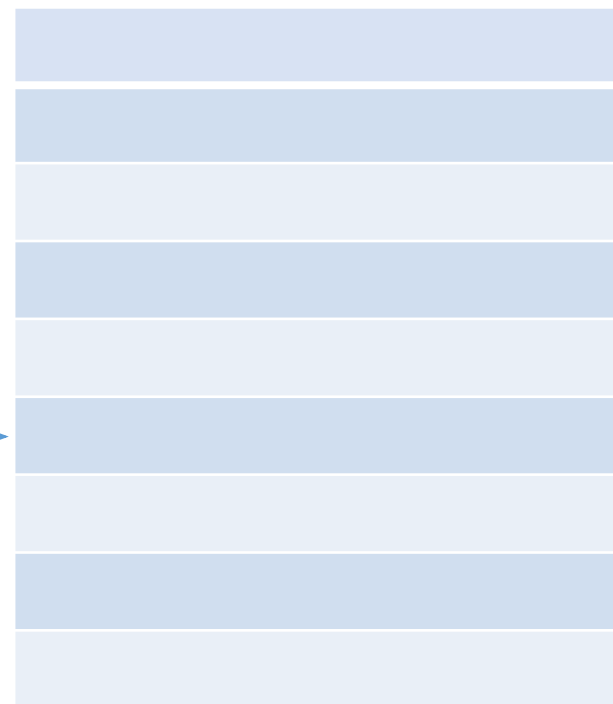
- Prediction data are not stored with BTB
- Prediction data are stored in the Pattern History Table (PHT), which is separated from BTB. Why?

PC



k-bit

Pattern History Table (PHT)



$2^k$  predictors/counters

BTB

How does size of the table  
affect the performance?

# Control Hazards and Dynamic Branch Prediction

- The *branch-target buffer* (BTB) or *branch-target (address) cache* (BTAC) is a branch-prediction cache that stores the predicted address for the next instruction after a branch

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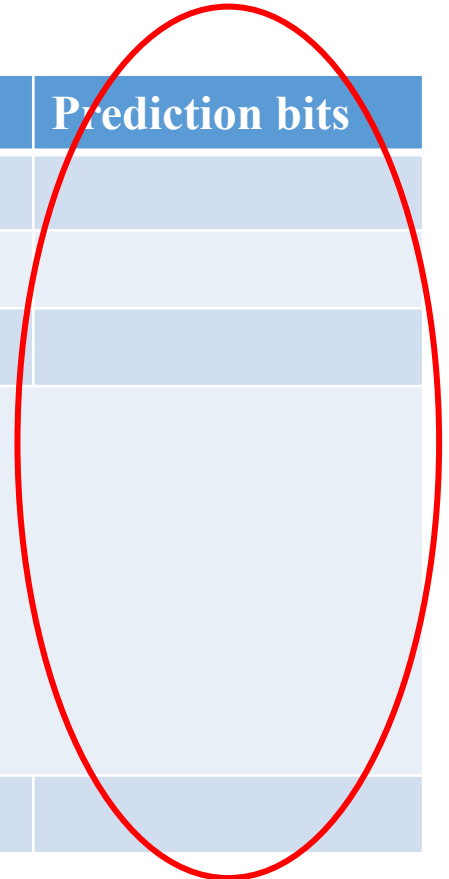
```
2C    sub $t2, $s0, $s5
```

30 . . .

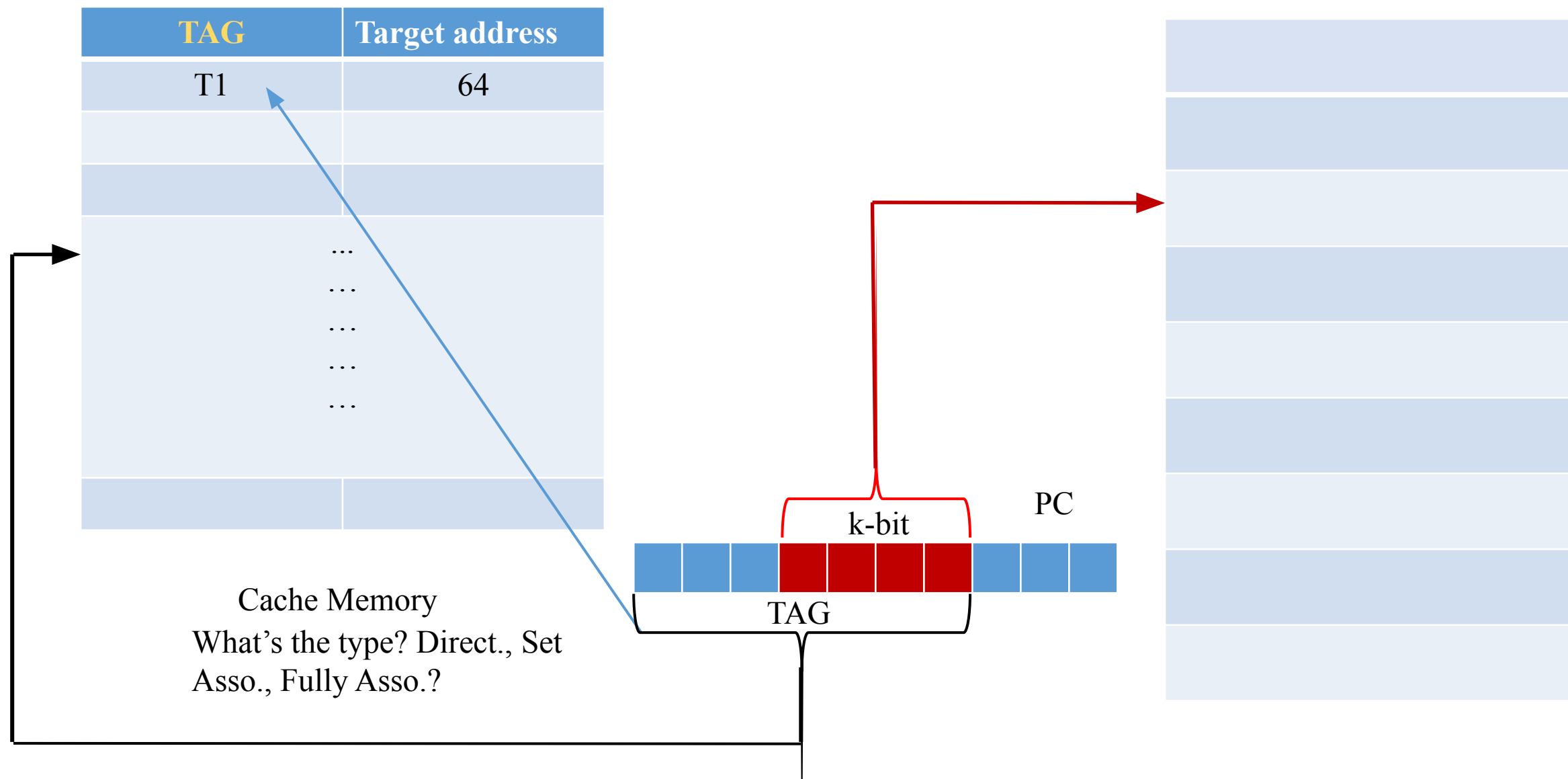
```
64    slt $t3, $s2, $s3
```

## Address

## Integrated BTB-PHT

[illegible]

# Decoupled BTB-PHT



# Homework

- Write a Verilog and C++ code for pipelined with full hazard detection unit
  - Incorporate the dynamic branch prediction
- Write a Verilog and C++ code for generalized N-bit branch predictor
- Is there any effect on the branch prediction for the starting state?

# Homework:

## Control Hazards: Performance Analysis

- No penalty for correct prediction
- 3 bubbles for incorrect prediction
- No data dependency among the instructions
- 20% instructions are branch
- 70% of branches are taken
- What is the CPI?
- What is the probability of wrong guess?
- What is the penalty of wrong guess?

# Summary

- Control hazard
- Performance analysis
- Flush the pipeline
- Hardware-based solution technique
  - Take decision at ID stage
- Software-based solution technique
  - Predict-taken
  - Predict-untaken
  - Delayed branch
- Dynamic branch prediction techniques
  - N-bit FSM