

$$u(t) = U\sqrt{2} \sin(\omega t)$$

$$U_m \Rightarrow U = \frac{U_m}{\sqrt{2}}$$

$$A(t) = A \sin(\omega t)$$

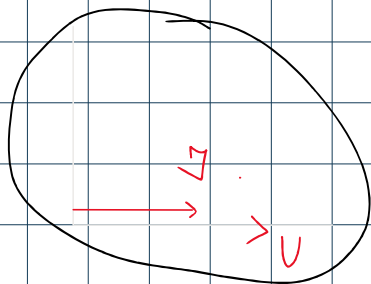
R

$$i(t) = \frac{u(t)}{R} = \frac{U\sqrt{2}}{R} \sin(\omega t) = I_m \sin(\omega t)$$

$$\omega = 2\pi f = \frac{2\pi}{T}$$

$$f = \frac{1}{T}$$

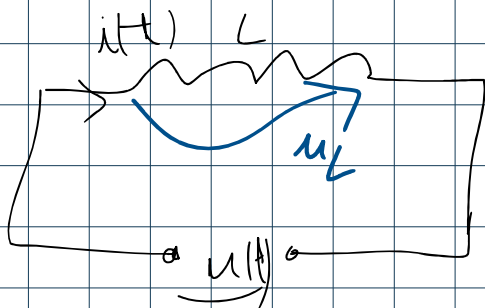
f - frecvență [Hz]  
T - perioadă [s]



L

$$X_L = \omega L$$

[Ω] inductivitate



$$u_L = L \frac{di}{dt}$$

$$i(t) = I_m \sin(\omega t + \varphi)$$

$$\Rightarrow \frac{di}{dt} = \omega I_m \cos(\omega t + \varphi)$$

$$\Rightarrow \frac{di}{dt} = u \sin(\omega t + \varphi)$$

$$u = u_L = U_m \sin(\omega t)$$

currentul care trece prin  $L$   
defazat în urmă față de tensiune  
cu  $\frac{\pi}{2}$

~~ex. 3.3.3~~

~~$R \rightarrow R$~~

~~$$L \rightarrow jX_L = j\omega L$$~~

~~$$C \rightarrow -jX_C = \frac{1}{j\omega C}$$~~

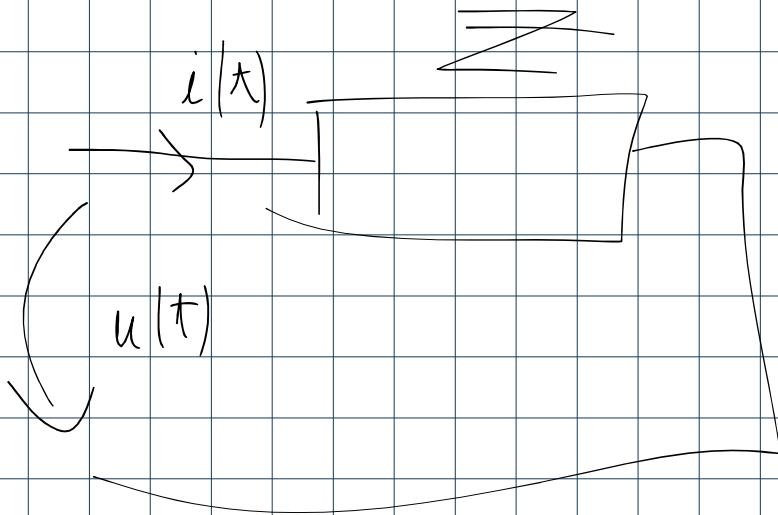
$$u(t) = 100\sqrt{2} \sin(100\pi t - 60^\circ) \text{ V.}$$

$$X_L = \omega L = 100\pi \cdot \frac{6}{10\pi} = 60 \, \Omega$$

$$X_C = \frac{1}{\omega C} = \frac{1}{100\pi \cdot \frac{1}{3\pi} \cdot 10^{-3}} = 30 \, \Omega$$

$$Z = \sqrt{R^2 + (\underbrace{x_L - x_C}_{\text{X}})^2} =$$

$$= 50 \Omega$$



$$U = I \cdot Z$$

$$\Rightarrow I = \frac{U}{Z} = \frac{100}{50} = 2 \text{ A}$$

$$x_L > x_C \Rightarrow \text{c. ind.}$$

$$\varphi = \arctg \frac{x}{R} = \arctg \frac{x_L - x_C}{R}$$

$$\varphi = \arctg \frac{3\Omega}{4\Omega} = 37^\circ$$

$$I = \frac{V_{rms}}{Z} = \frac{100}{40} = 2.5$$

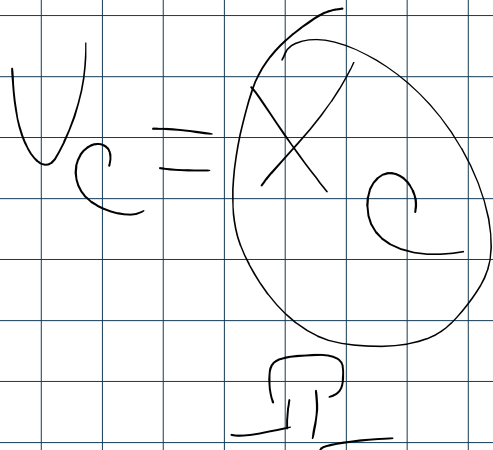
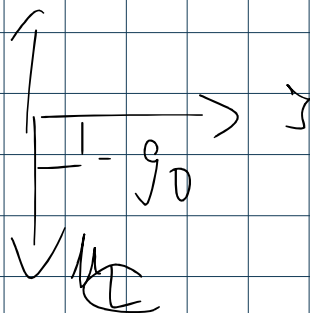
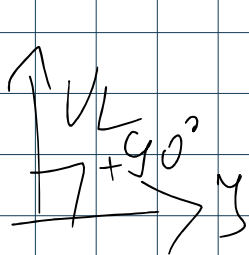
$$i(t) = \sqrt{2} \sin(\omega t + \phi) = 2\sqrt{2} \sin(100\pi t - 60^\circ - 37^\circ) = 2\sqrt{2} \sin(100\pi t - 97^\circ) \quad (A)$$

$$V_R = I \cdot R = 2.5 \cdot 40 = 100V$$

$$u_R(t) = 100\sqrt{2} \sin(100\pi t - 97^\circ)$$

$$V_L = I \cdot X_L = 120V$$

$$u_L(t) = 120\sqrt{2} \sin(100\pi t - 97^\circ + 90^\circ)$$



$$V_C = I \cdot X_C = 30 \cdot 2 = 60V$$

$$u_c(t) = 60\sqrt{2} \sin(100\pi t - 94^\circ - 90^\circ)$$

- - - -

$$\cos x = \sin\left(x + \frac{\pi}{2}\right)$$

$$- \cos x = \sin\left(x - \frac{\pi}{2}\right)$$

$$\begin{aligned} u_1(t) &= 2\sqrt{2} \cos(\omega t + 30^\circ) = \\ &= 2\sqrt{2} \sin(\omega t + 30^\circ + 90^\circ) = \\ &= 2\sqrt{2} \sin(\omega t + 120^\circ) \end{aligned}$$

$$u_2(t) = 5\sqrt{2} \sin(\omega t + 30^\circ)$$

$$\Rightarrow \underline{U_1} = \frac{U_m}{\sqrt{2}} e^{j\varphi} = U e^{j\varphi} =$$

$$= 2 e^{j120^\circ}$$

$$\underline{U_2} = 5 e^{j30^\circ}$$

$$U_1 - U_2 = \left( 2 e^{j120^\circ} - 5 e^{j30^\circ} \right)$$

$$\underline{U} = \underline{U}_1 + \underline{U}_2 = \left( \nearrow e^{j30^\circ} \right)$$

$$u(t) = u_1(t) + u_2(t) = 7\sqrt{2} \sin(\omega t + 30^\circ)$$

$$-j \Rightarrow e^{-j90^\circ}$$

$$j \Rightarrow e^{j90^\circ}$$

$$\begin{aligned} \underline{U}_1 &= 2 e^{j120^\circ} = \\ &= 2 (\cos 120^\circ + j \sin 120^\circ) = \\ &= \text{Re} + j \text{Im} \end{aligned}$$

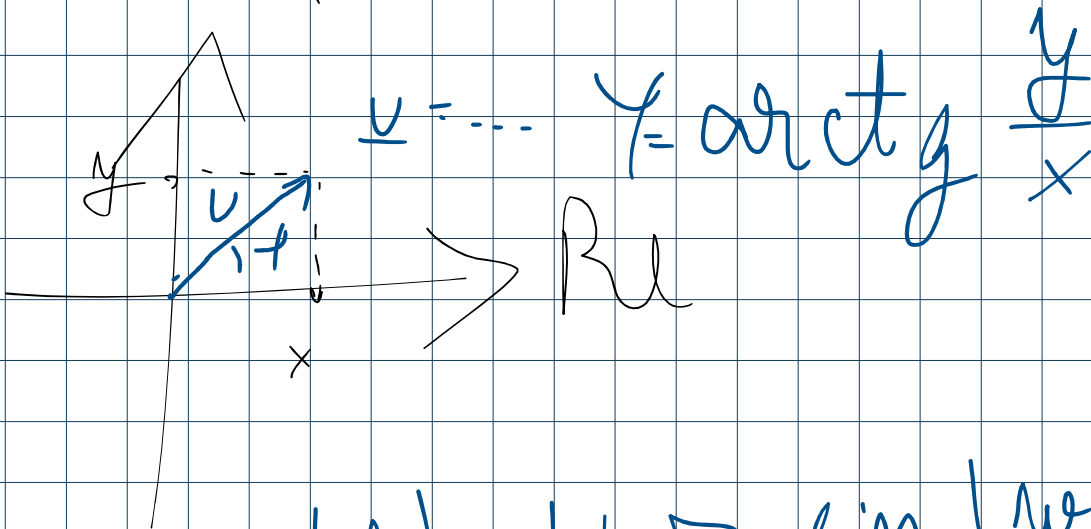
$$\boxed{\varphi = \arctan \frac{\text{Im}}{\text{Re}}}$$

$$\begin{aligned} \underline{U}_2 &= 5 e^{j30^\circ} = \\ &= 5 (\cos 30^\circ + j \sin 30^\circ) = \end{aligned}$$

$$Re_1 + j Im_1$$

$$\underline{U} = \underline{U}_1 + \underline{U}_2 = (Re + jIm) + (Re_1 + jIm_1)$$

$$Im = \dots e^{j\phi} \dots$$



$$\Rightarrow u(t) = U\sqrt{2} \sin(\omega t + \varphi)$$

3.6. a)  $\underline{U} = -10 e^{j30^\circ}$

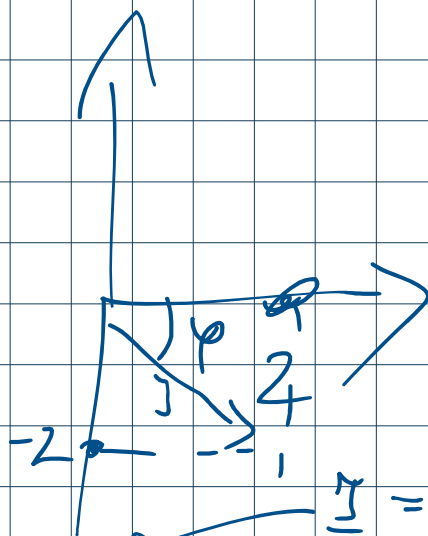
$u(t) = ?$

$$u(t) = -10\sqrt{2} \sin(\omega t + 30^\circ)$$

$$- \sin(\omega t + \varphi) = \sin(\omega t + \varphi - 180^\circ)$$

$$\underline{I} = \frac{I_m}{\sqrt{2}}$$

$$\begin{aligned} b) \underline{I} &= 2\sqrt{2} (\cos 45^\circ - j \sin 45^\circ) = \\ &= 2\sqrt{2} \cdot \frac{\sqrt{2}}{2} - j 2\sqrt{2} \frac{\sqrt{2}}{2} = \\ &= 2 - j \cdot 2 \end{aligned}$$



$$\begin{aligned} \varphi &= \arctg \frac{-2}{2} = \\ &= \arctg(-1) = \\ &= -45^\circ \end{aligned}$$

$$\begin{aligned} \Rightarrow i(t) &= 4 \sin(\omega t - 45^\circ) \\ \underline{I} &= 2\sqrt{2} e^{j(-45^\circ)} \end{aligned}$$

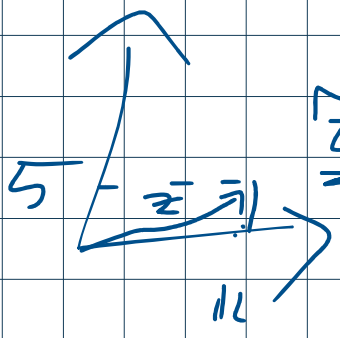


$$c) \underline{U} = j(5 - j12) \text{ V}$$

$$\sqrt{-1} = j$$

$$\underline{U} = 5j - \cancel{j^2} 12 =$$

$$= 12 + 5j$$



$$\underline{Z} = 12 + 5j$$

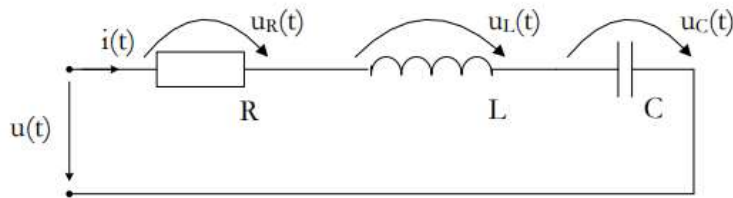
$$\varphi = \operatorname{arctg} \frac{5}{12}$$

$$\sqrt{5^2 + 12^2} = 13$$

$$\underline{U} = 13 e^{j23^\circ}$$

$$\Rightarrow i(t) = 13\sqrt{2} \sin(\omega t + 23^\circ)$$

**3-14** The circuit parameters for the RLC series circuit below are  $R=20\Omega$ ,  $L=40\text{mH}$ ,  $C=50\mu\text{F}$ , and the supplying voltage:  $u(t) = 200 \sin(1000t - 30^\circ)\text{V}$ . Calculate: a) the inductive and capacitive reactances and the circuit impedance,  $X_L$ ,  $X_C$ ,  $Z$ ; b) the rms and the instantaneous value of the current,  $I$ ,  $i(t)$ ; c) the rms and the instantaneous value of resistance-voltage,  $U_R$ ,  $u_R(t)$ ; d) the rms and the instantaneous value of inductance-voltage,  $U_L$ ,  $u_L(t)$ ; e) the rms and the instantaneous value of capacitance-voltage,  $U_C$ ,  $u_C(t)$ . Draw the circuit diagram.



Problem 3-14

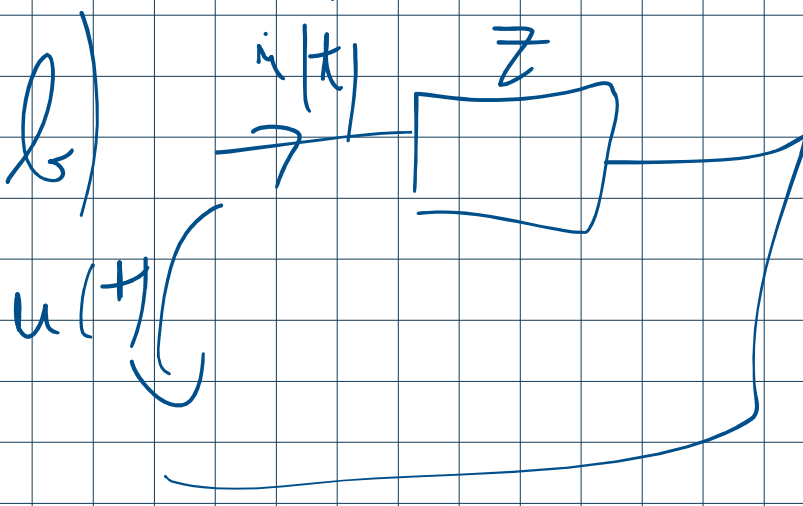
$$a) \omega = 1000 \frac{\text{rad}}{\text{s}}$$

$$X_L = \omega L = 1000 \cdot 40 \cdot 10^{-3} = 40 \Omega$$

$$X_C = \frac{1}{\omega C} = \frac{1}{1000 \cdot 50 \cdot 10^{-6}} = \frac{100}{5} = 20 \Omega$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2} =$$

$$= \sqrt{400 + 400} = 20\sqrt{2} \Omega$$



$$I = \frac{U}{Z} = \frac{200}{\sqrt{2}} \cdot \frac{1}{20\sqrt{2}} =$$

$$= 5 \text{ A}$$

$$\varphi = \arctg\left(\frac{X_L - X_C}{R}\right) = 45^\circ$$

$X_L > X_C \rightarrow$  c. ind.

currentul e în urmă cu  $45^\circ$

$$i(t) = 5\sqrt{2} \sin(1000t - 30^\circ - 45^\circ) =$$

$$= 5\sqrt{2} \sin(1000t - 75^\circ) \text{ A}$$

$$c) U_R = IR = 100 \text{ V}$$

$$u_R(t) = 100\sqrt{2} \sin(\omega t - 75^\circ) \text{ V}$$

$$a) U_L = IX_L = 200 \text{ V}$$

$$a) V_L = I X_L = 200 \text{ V}$$

$$u_L(t) = 200\sqrt{2} \sin(1000t - 75^\circ + 90^\circ) \text{ V}$$

$$b) V_C = I X_C = 100 \text{ V}$$

$$u_C(t) = 100\sqrt{2} \sin(1000t - 75^\circ - 90^\circ)$$