REPORT

Course: Digital Signals Processing
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Signal Synthesis Using Inverse Discrete Fourier Transform (IDFT)

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1 Problem Statement

The task involves synthesizing discrete-time signals from their DFT coefficients using the Inverse Discrete Fourier Transform (IDFT) in matrix notation. The goal is to reconstruct time-domain signals from frequency-domain sequences $\mathbf{X}_\mu$ and visualize the results, including real and imaginary parts.

2 Input Data

The input data for this task is a sequence of DFT coefficients $\mathbf{X}_\mu$, defined as follows:

$$\mathbf{X}_\mu = [6, 2, 4, 4, 4, 5, 0, 0, 0, 0]$$

The corresponding time-domain signal is computed using the IDFT. The task also involves plotting the synthesized signal for analysis.

3 Python Code

The following Python code was used to synthesize signals from the input DFT coefficients using the IDFT:

```python
import numpy as np
import matplotlib.pyplot as plt

def idft_matrix(N):
    W_N = np.exp(-2j * np.pi * np.outer(np.arange(N), np.arange(N)
        ) / N)
    return W_N

def synthesize_signal(X_mu):
    N = len(X_mu)
    W_N = idft_matrix(N)
```

```python
    x_mu = np.dot(W_N.conj().T, X_mu) / N
    return x_mu

X_mu = np.array([6, 2, 4, 4, 4, 5, 0, 0, 0, 0], dtype=complex)

x_mu_synthesized = synthesize_signal(X_mu)

plt.figure(figsize=(10, 6))
plt.stem(np.real(x_mu_synthesized), linefmt='b-', markerfmt='bo',
    basefmt='r-')
plt.title('Synthesized Signal (Real Part)')
plt.xlabel('Sample Index')
plt.ylabel('Amplitude')
plt.grid(True)
plt.show()

plt.figure(figsize=(10, 6))
plt.stem(np.imag(x_mu_synthesized), linefmt='g-', markerfmt='go',
    basefmt='r-')
plt.title('Synthesized Signal (Imaginary Part)')
plt.xlabel('Sample Index')
plt.ylabel('Amplitude')
plt.grid(True)
plt.show()

plt.figure(figsize=(12, 6))
plt.plot(np.real(x_mu_synthesized), label='Real Part', marker='o',
    linestyle='-', color='b')
plt.plot(np.imag(x_mu_synthesized), label='Imaginary Part', marker
    ='x', linestyle='--', color='g')
plt.title('Signal Synthesis: Real and Imaginary Parts Combined')
plt.xlabel('Sample Index')
plt.ylabel('Amplitude')
plt.axhline(0, color='red', linewidth=0.8, linestyle='--', label='
    Zero Line')
plt.legend()
plt.grid(True)
plt.show()
```

4   Outcomes

The synthesized signals were analyzed and visualized. The results include the real part, the imaginary part, and the combined representation of both.
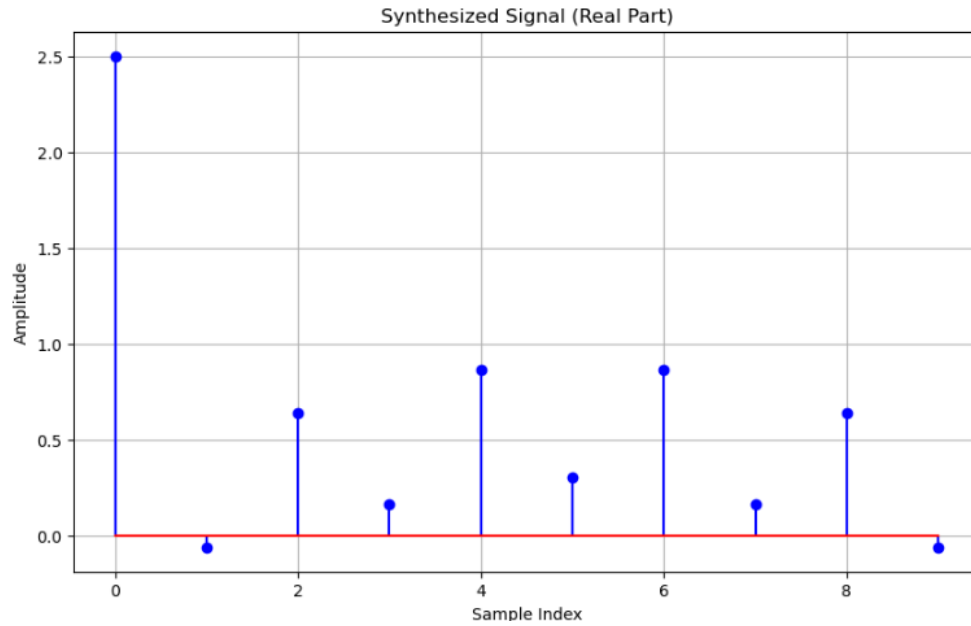
4.1   Real Part of the Signal

Figure 1: Synthesized Signal (Real Part)
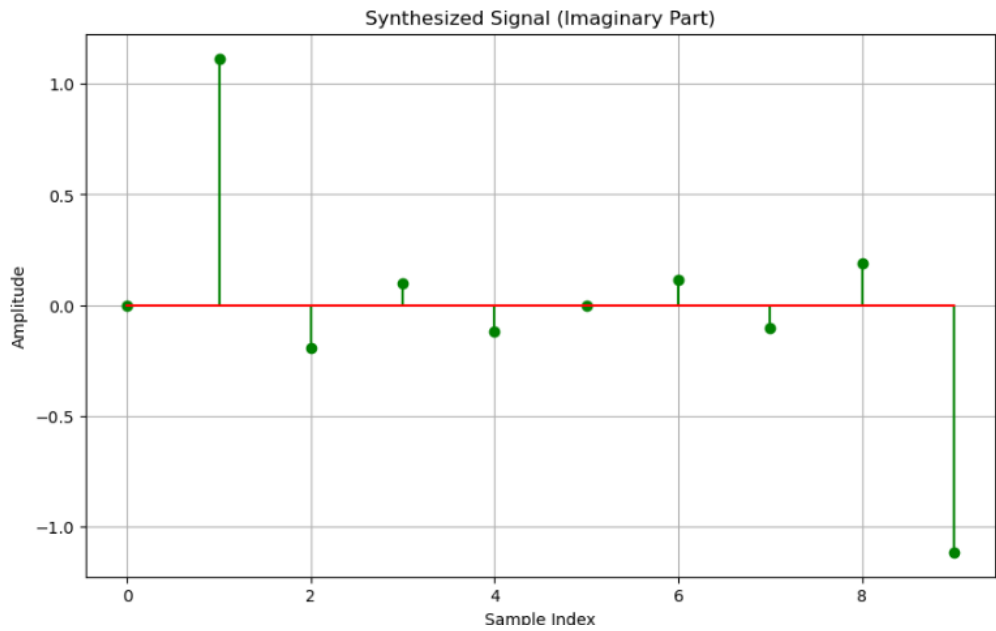
4.2 Imaginary Part of the Signal

Figure 2: Synthesized Signal (Imaginary Part)
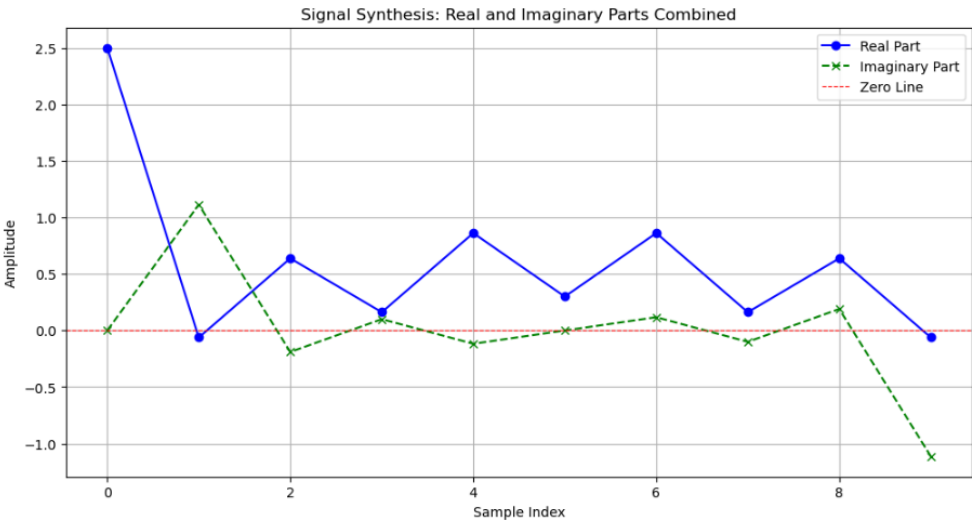
4.3 Combined Signal (Real and Imaginary)

Figure 3: Signal Synthesis: Real and Imaginary Parts Combined

5   Conclusions

- The comparison between the real and imaginary parts of the signal shows how these two components are interconnected in the signal synthesis process.

- The real part of the signal is more intuitive and easier to understand, as it reflects the signal's amplitude, while the imaginary part provides information about its phase.

- Both parts are essential to obtain a complete and accurate time-domain reconstruction of the signal.

- The zero line plays a crucial role in visualizing the signal's behavior, providing a reference point for identifying the positive and negative oscillations.

- The real and imaginary components fluctuate around this line, and it helps to better interpret the amplitude and phase changes, ensuring a more accurate understanding of the signal's characteristics.