

Estrutura de Dados I

**Estrutura de dados: lista
duplamente encadeada**

Prof. Rodrigo Minetto

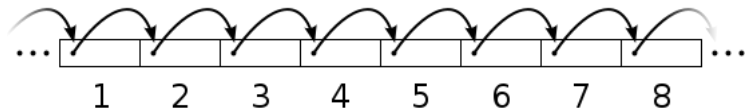
Universidade Tecnológica Federal do Paraná

Sumário

- 1 Introdução
- 2 Função: **inserir**
- 3 Função: **inserir (funcionamento)**
- 4 Função: **remover**

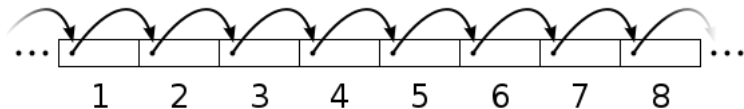
Introdução

O tipo abstrato de dados **lista** visto aula passada caracteriza-se por formar um **encadeamento simples** entre os elementos — cada nó armazena um ponteiro para o próximo elemento da lista.



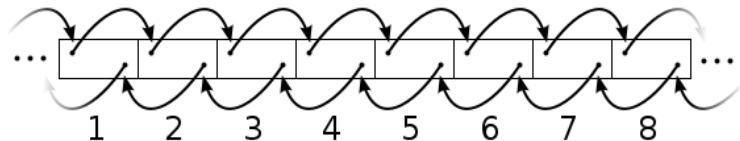
Introdução

Problemas: **1)** não é possível percorrer eficientemente os elementos em **ordem inversa** (do fim para o início); **2)** dificuldade para remoção, pois dado um determinado nó não temos como acessar diretamente seu antecessor.



Introdução

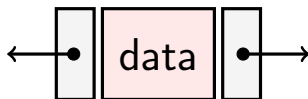
Solução: implementar o que chamamos de **lista duplamente encadeada**. Nela, cada elemento tem um ponteiro para o **próximo** elemento e um ponteiro para o elemento **anterior**.



Estrutura

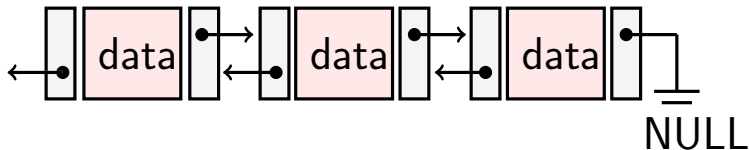
Observe a similaridade entre a estrutura de uma lista simples e uma lista dupla. A única diferença é a adição de mais um ponteiro para o elemento anterior.

```
typedef struct node {  
    int data;  
    struct node* next;  
    struct node* prev;  
} List;
```



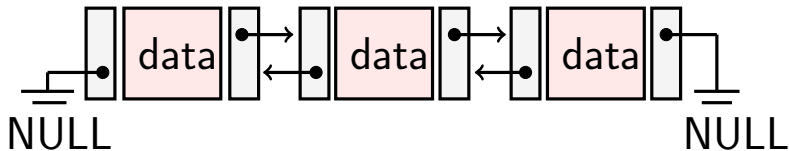
Listas duplamente encadeadas

O encadeamento em duas vias permite acessar ambos os elementos adjacentes: o próximo e o anterior, e desta forma, percorrer a lista em ordem inversa.



Listas duplamente encadeadas

Da mesma forma que o último elemento da lista tem como **next** o valor NULL, o primeiro elemento da lista não tem elemento anterior, e portanto o ponteiro **prev** é NULL.



Tipo abstrato de dados

Lista duplamente encadeada (interface)

create: inicializa uma estrutura de dados lista

insert-front: adiciona um nó na cabeça da lista

remove: remove um nó da lista

size: retorna o número de nós na lista

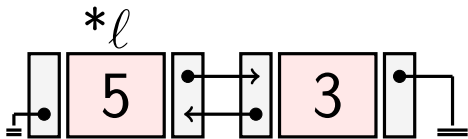
print: imprime todos os nós da lista

destroy: remove todos os nós da lista

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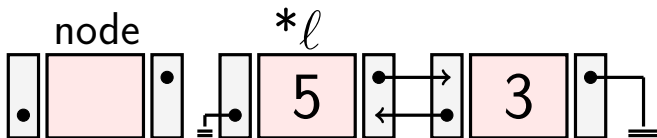
Inserir (início)



- 1: **List*** insert-front (List $*l$, int elem)
- 2: List* node = (List*)malloc(sizeof(List));
- 3: node→data = elem;
- 4: node→next = l ;
- 5: node→prev = NULL;
- 6: **if** ($l \neq \text{NULL}$) { $l \rightarrow \text{prev} = \text{node}$; }
- 7: **return** node;

Inserir: 7

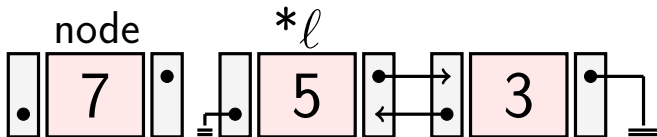
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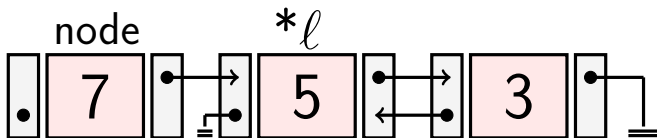
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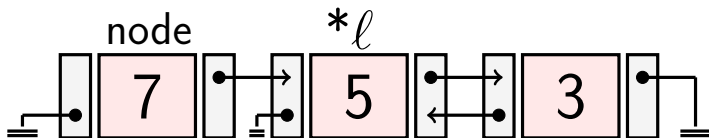
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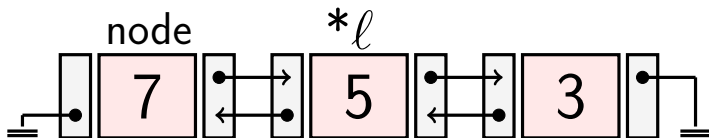
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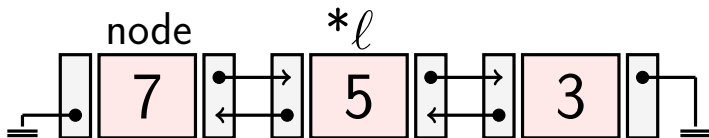
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Importante: a função **main** sempre (e somente) guarda a **cabeça** da lista.

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1: int main (void)


---


2:     List * $\ell$  = create ();
3:      $\ell$  = insert-front ( $\ell$ , 3);
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6: return 0
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Inserir (início)

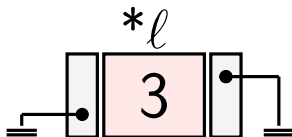
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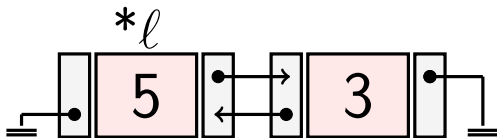
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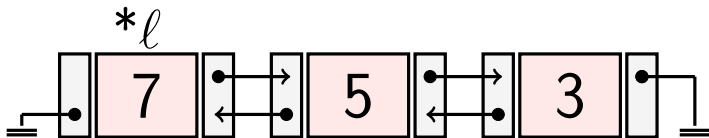
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Remover

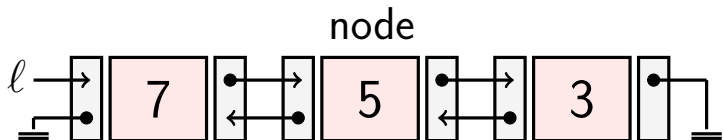


1: **List* remove** (List * ℓ , int elem)

```
2:   List *node = search ( $\ell$ , elem); /*busca pelo nó!*/
3:   if (node = NULL) { return  $\ell$ ; }
4:   List *a = node→prev;   /*antecessor!*/
5:   List *s = node→next;   /*sucessor!*/
6:   if ( $\ell$  = node) {  $\ell$  = s; }
7:   if (s  $\neq$  NULL) { s→prev = a; }
8:   if (a  $\neq$  NULL) { a→next = s; }
9:   free (node);
10:  return  $\ell$ ;
```

Remover: 5

Remover



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3: if (node = NULL) { return ℓ ; }

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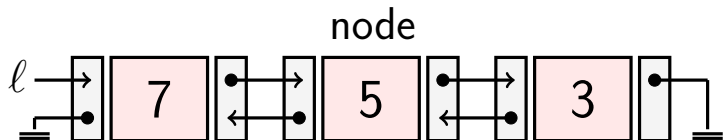
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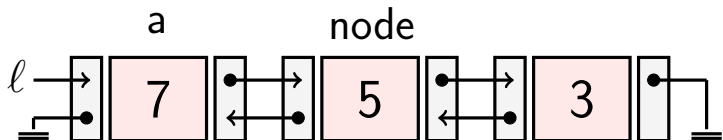
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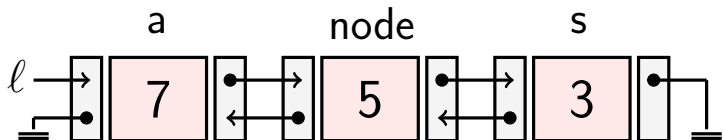
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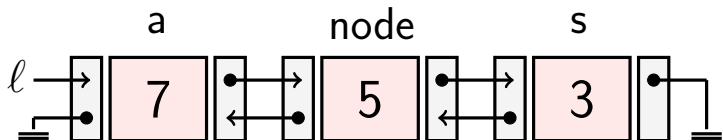
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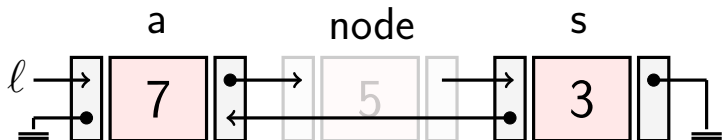
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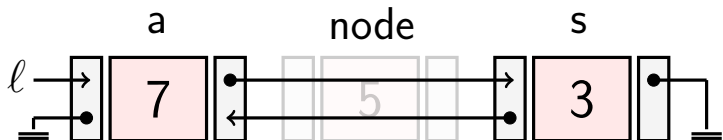
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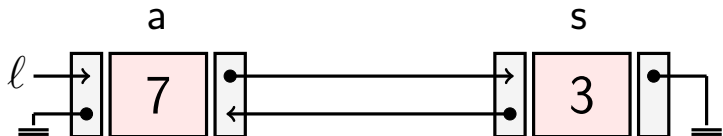
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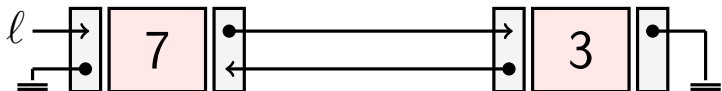
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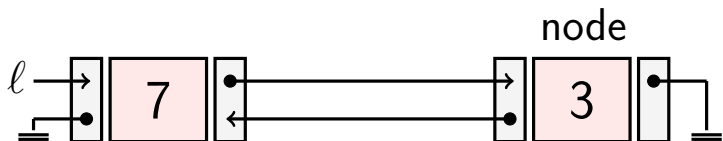


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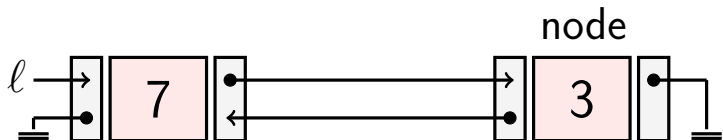
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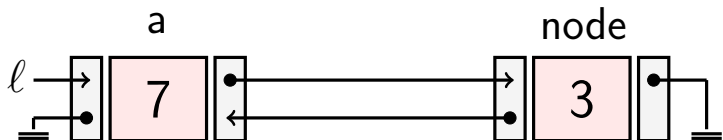
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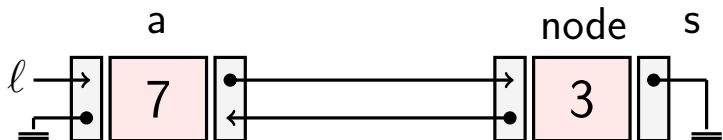


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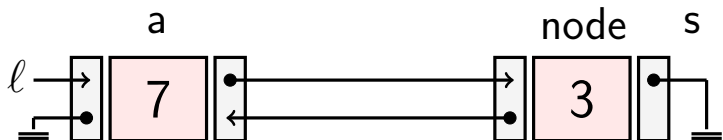
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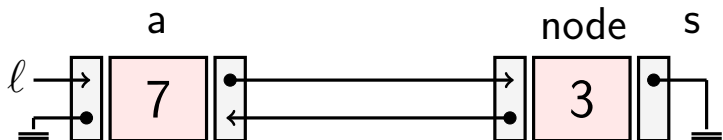
```
8:   if (a ≠ NULL) { a→next = s; }
```

```
9:   free (node);
```

```
10: return l;
```

Remover: 3

Remover



```
1: List* remove (List *l, int elem)
```

```
2:   List *node = search (l, elem); /*busca pelo nó!*/
```

```
3:   if (node = NULL) { return l; }
```

```
4:   List *a = node→prev; /*antecessor!*/
```

```
5:   List *s = node→next; /*sucessor!*/
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```
6:   if (l = node) { l = s; }
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7:   if (s ≠ NULL) { s→prev = a; }
```

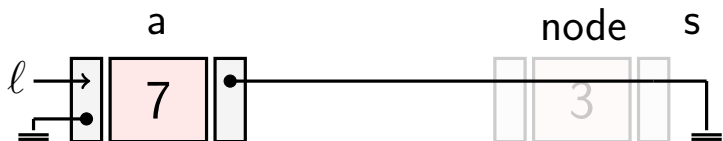
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Remover: 3

Remover



1: **List*** remove (List * ℓ , int elem)

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3: **if** (node = NULL) { return ℓ ; }

4: List *a = node→prev; */*antecessor!*/*

5: List *s = node→next; */*sucessor!*/*

6: **if** (ℓ = node) { ℓ = s; }

7: **if** (s \neq NULL) { s→prev = a; }

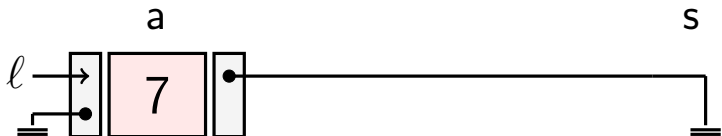
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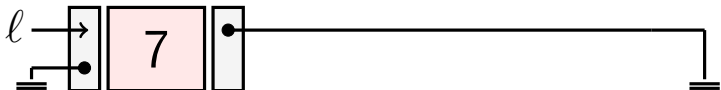
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Remover: 3

Remover



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3: **if** (node = NULL) { return l ; }

4: List $*a$ = node \rightarrow prev; */*antecessor!*/*

5: List $*s$ = node \rightarrow next; */*sucessor!*/*

6: **if** (l = node) { l = s ; }

7: **if** ($s \neq$ NULL) { $s\rightarrow$ prev = a ; }

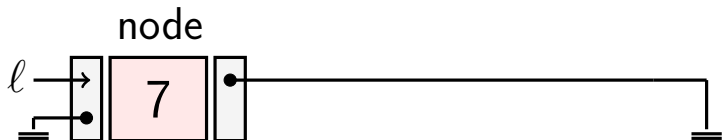
8: **if** ($a \neq$ NULL) { $a\rightarrow$ next = s ; }

9: **free** (node);

10: **return** l ;

Remover: 7

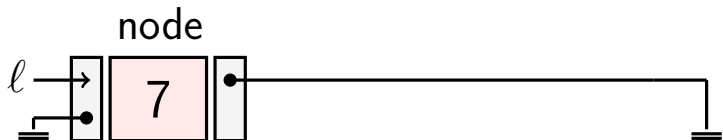
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```

Remover: 7

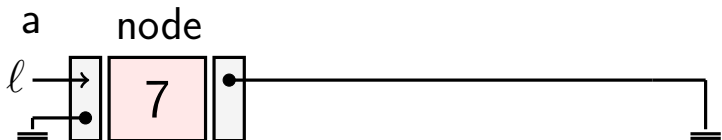
Remover



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7:   if (s != NULL) { s->prev = a; }
8:   if (a != NULL) { a->next = s; }
9:   free (node);
10: return l;
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Remover: 7

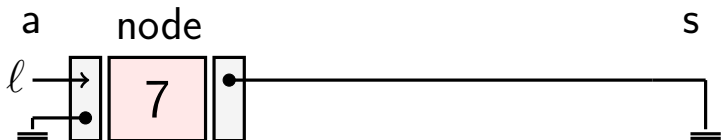
Remover



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7:   if (s ≠ NULL) { s→prev = a; }
8:   if (a ≠ NULL) { a→next = s; }
9:   free (node);
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Remover: 7

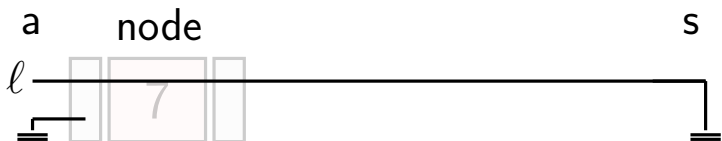
Remover



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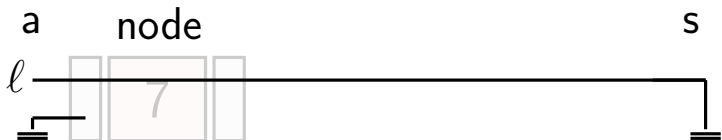
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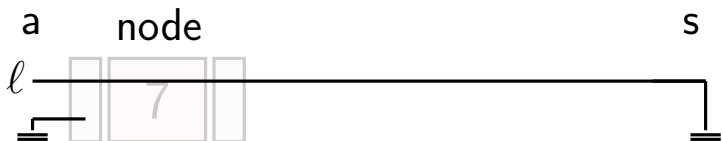
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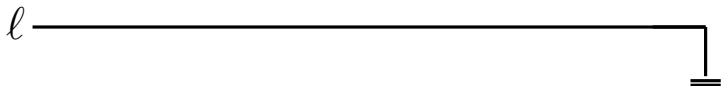
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Remover: 7