```
(* f(x) возрастает, f(x+0)=f(x) *)
          m{(a,b)}=f(b-0)-f(a+0),
m{[a,b]} = f(b+0) = f(a-0)
                                      !! счетно-аддитивная мера *)
(* X_0=0 < X_1 < X_2 < X_3=1 *)
(* f(x_j)=v_j, j=0,1,2,3, f(x_j-0)=v_(j-0)
                                                                                j=1,2*)
(* x_j, v_j --- заданы в условии *)
(* f(x) = k_1 x^2, x_0 \le x < x_!; f(x) = k_2,
x_2 \le x < x_3; f(x) = k_4 - r_3(x_3 - x)^2, x_5 \le x < x_4;*)
(* k_j надо вычилсить *)
(* g(x) --- непрерывныя,
линейная на интервалах [u_0,u_1],[u_1,u_2],[u_2,u_3],[u_3,u_4] *)
(* u_0=0 ; u_1=x_1/2 ;
u_2 = (x_1 + x_2)/2;
u_3 = (x_2 + x_3)/2; u_4 = x_3 *
(* g(u_j)=y_j,y_j--- заданы в условии *)
_ _ _ _ _ _ _ _ _ _ _ _
{var., 1}
f(0) = 0, f(\frac{5}{13} - 0) = \frac{5}{8}, f(\frac{5}{13}) = 1, f(\frac{9}{13} - 0) = 1, f(\frac{9}{13}) = \frac{11}{8}, f(1) = 2
g(0) = 0, g(\frac{5}{26}) = 3, g(\frac{7}{13}) = 3, g(\frac{11}{13}) = 5, g(1) = 5
f(0) = 0, f(\frac{4}{9} - 0) = \frac{7}{11}, f(\frac{4}{9}) = \frac{12}{11}, f(\frac{2}{3} - 0) = \frac{12}{11}, f(\frac{2}{3}) = \frac{16}{11}, f(1) = 2
g(\theta) = 2, g(\frac{2}{9}) = 1, g(\frac{5}{9}) = 2, g(\frac{5}{6}) = 4, g(1) = 2
= = = = = = = = =
f(0) = 0, f(\frac{8}{15} - 0) = \frac{16}{21}, f(\frac{8}{15}) = \frac{26}{21}, f(\frac{11}{15} - 0) = \frac{26}{21}, f(\frac{11}{15}) = \frac{12}{7}, f(1) = 2
g(\theta) = 2, g(\frac{4}{15}) = 5, g(\frac{19}{30}) = 2, g(\frac{13}{15}) = 2, g(1) = 0
f(0) = 0, f(\frac{5}{14} - 0) = \frac{1}{2}, f(\frac{5}{14}) = \frac{6}{5}, f(\frac{5}{7} - 0) = \frac{6}{5}, f(\frac{5}{7}) = \frac{9}{5}, f(1) = 2
g(0) = 6, g(\frac{5}{28}) = 2, g(\frac{15}{28}) = 6, g(\frac{6}{7}) = 3, g(1) = 3
_ _ _ _ _ _ _ _ _ _ _
f(0) = 0, f(\frac{9}{20} - 0) = \frac{3}{4}, f(\frac{9}{20}) = \frac{9}{8}, f(\frac{7}{10} - 0) = \frac{9}{8}, f(\frac{7}{10}) = \frac{7}{4}, f(1) = 2
g(0) = 2, g(\frac{9}{40}) = 6, g(\frac{23}{40}) = 2, g(\frac{17}{20}) = 2, g(1) = 1
```

= = = = = = = = =

{var., 6}

$$f(\theta) = \theta$$
,  $f(\frac{1}{2} - \theta) = \frac{2}{5}$ ,  $f(\frac{1}{2}) = \frac{4}{5}$ ,  $f(\frac{3}{4} - \theta) = \frac{4}{5}$ ,  $f(\frac{3}{4}) = \frac{4}{3}$ ,  $f(1) = 2$ 

$$g(0) = 4$$
,  $g(\frac{1}{4}) = 6$ ,  $g(\frac{5}{8}) = 2$ ,  $g(\frac{7}{8}) = 4$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 7}

$$f(0) = 0$$
,  $f(\frac{7}{13} - 0) = 1$ ,  $f(\frac{7}{13}) = \frac{10}{7}$ ,  $f(\frac{9}{13} - 0) = \frac{10}{7}$ ,  $f(\frac{9}{13}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{7}{26}) = 1$ ,  $g(\frac{8}{13}) = 6$ ,  $g(\frac{11}{13}) = 6$ ,  $g(1) = 1$ 

= = = = = = = = =

{var., 8}

$$f(0) = 0$$
,  $f(\frac{9}{16} - 0) = \frac{4}{7}$ ,  $f(\frac{9}{16}) = \frac{8}{7}$ ,  $f(\frac{13}{16} - 0) = \frac{8}{7}$ ,  $f(\frac{13}{16}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(0) = 1$$
,  $g(\frac{9}{32}) = 4$ ,  $g(\frac{11}{16}) = 4$ ,  $g(\frac{29}{32}) = 3$ ,  $g(1) = 0$ 

= = = = = = = = =

 $\{\texttt{var., 9}\}$ 

$$f(0) = 0$$
,  $f(\frac{6}{11} - 0) = \frac{8}{21}$ ,  $f(\frac{6}{11}) = \frac{8}{7}$ ,  $f(\frac{8}{11} - 0) = \frac{8}{7}$ ,  $f(\frac{8}{11}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{3}{11}) = 3$ ,  $g(\frac{7}{11}) = 5$ ,  $g(\frac{19}{22}) = 1$ ,  $g(1) = 4$ 

= = = = = = = = =

{var., 10}

$$f(0) = 0$$
,  $f(\frac{7}{12} - 0) = \frac{12}{23}$ ,  $f(\frac{7}{12}) = \frac{22}{23}$ ,  $f(\frac{5}{6} - 0) = \frac{22}{23}$ ,  $f(\frac{5}{6}) = \frac{34}{23}$ ,  $f(1) = 2$ 

$$g(0) = 3$$
,  $g(\frac{7}{24}) = 1$ ,  $g(\frac{17}{24}) = 0$ ,  $g(\frac{11}{12}) = 5$ ,  $g(1) = 5$ 

= = = = = = = = =

 $\{var., 11\}$ 

$$f(0) = 0$$
,  $f(\frac{5}{13} - 0) = \frac{5}{8}$ ,  $f(\frac{5}{13}) = 1$ ,  $f(\frac{9}{13} - 0) = 1$ ,  $f(\frac{9}{13}) = \frac{11}{8}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{5}{26}) = 3$ ,  $g(\frac{7}{13}) = 3$ ,  $g(\frac{11}{13}) = 5$ ,  $g(1) = 5$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 12}

$$f(0) = 0, \quad f(\frac{4}{9} - 0) = \frac{7}{11}, \quad f(\frac{4}{9}) = \frac{12}{11}, \quad f(\frac{2}{3} - 0) = \frac{12}{11}, \quad f(\frac{2}{3}) = \frac{16}{11}, \quad f(1) = 2$$

$$g(0) = 2$$
,  $g(\frac{2}{9}) = 1$ ,  $g(\frac{5}{9}) = 2$ ,  $g(\frac{5}{6}) = 4$ ,  $g(1) = 2$ 

= = = = = = = = =

{var., 13}

$$f(0) = 0$$
,  $f(\frac{8}{15} - 0) = \frac{16}{21}$ ,  $f(\frac{8}{15}) = \frac{26}{21}$ ,  $f(\frac{11}{15} - 0) = \frac{26}{21}$ ,  $f(\frac{11}{15}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{4}{15}) = 5$ ,  $g(\frac{19}{30}) = 2$ ,  $g(\frac{13}{15}) = 2$ ,  $g(1) = 0$ 

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{var., 14}

$$f(0) = 0$$
,  $f(\frac{5}{14} - 0) = \frac{1}{2}$ ,  $f(\frac{5}{14}) = \frac{6}{5}$ ,  $f(\frac{5}{7} - 0) = \frac{6}{5}$ ,  $f(\frac{5}{7}) = \frac{9}{5}$ ,  $f(1) = 2$ 

$$g(0) = 6$$
,  $g(\frac{5}{28}) = 2$ ,  $g(\frac{15}{28}) = 6$ ,  $g(\frac{6}{7}) = 3$ ,  $g(1) = 3$ 

= = = = = = = = =

{var., 15

$$f(0) = 0$$
,  $f(\frac{9}{20} - 0) = \frac{3}{4}$ ,  $f(\frac{9}{20}) = \frac{9}{8}$ ,  $f(\frac{7}{10} - 0) = \frac{9}{8}$ ,  $f(\frac{7}{10}) = \frac{7}{4}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{9}{40}) = 6$ ,  $g(\frac{23}{40}) = 2$ ,  $g(\frac{17}{20}) = 2$ ,  $g(1) = 1$ 

= = = = = = = = =

{var., 16}

$$f(0) = 0$$
,  $f(\frac{1}{2} - 0) = \frac{2}{5}$ ,  $f(\frac{1}{2}) = \frac{4}{5}$ ,  $f(\frac{3}{4} - 0) = \frac{4}{5}$ ,  $f(\frac{3}{4}) = \frac{4}{3}$ ,  $f(1) = 2$ 

$$g(0) = 4$$
,  $g(\frac{1}{4}) = 6$ ,  $g(\frac{5}{8}) = 2$ ,  $g(\frac{7}{8}) = 4$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 17}

$$f(0) = 0$$
,  $f(\frac{7}{13} - 0) = 1$ ,  $f(\frac{7}{13}) = \frac{10}{7}$ ,  $f(\frac{9}{13} - 0) = \frac{10}{7}$ ,  $f(\frac{9}{13}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{7}{26}) = 1$ ,  $g(\frac{8}{13}) = 6$ ,  $g(\frac{11}{13}) = 6$ ,  $g(1) = 1$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 18}

$$f(0) = 0, \quad f(\frac{9}{16} - 0) = \frac{4}{7}, \quad f(\frac{9}{16}) = \frac{8}{7}, \quad f(\frac{13}{16} - 0) = \frac{8}{7}, \quad f(\frac{13}{16}) = \frac{32}{21}, \quad f(1) = 2$$

$$g(0) = 1$$
,  $g(\frac{9}{32}) = 4$ ,  $g(\frac{11}{16}) = 4$ ,  $g(\frac{29}{32}) = 3$ ,  $g(1) = 0$ 

= = = = = = = = =

 $\{var., 19\}$ 

$$f(0) = 0$$
,  $f(\frac{6}{11} - 0) = \frac{8}{21}$ ,  $f(\frac{6}{11}) = \frac{8}{7}$ ,  $f(\frac{8}{11} - 0) = \frac{8}{7}$ ,  $f(\frac{8}{11}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(\theta) = \theta$$
,  $g(\frac{3}{11}) = 3$ ,  $g(\frac{7}{11}) = 5$ ,  $g(\frac{19}{22}) = 1$ ,  $g(1) = 4$ 

= = = = = = = = =

{var., 20}

$$f(0) = 0$$
,  $f(\frac{7}{12} - 0) = \frac{12}{23}$ ,  $f(\frac{7}{12}) = \frac{22}{23}$ ,  $f(\frac{5}{6} - 0) = \frac{22}{23}$ ,  $f(\frac{5}{6}) = \frac{34}{23}$ ,  $f(1) = 2$ 

$$g(\theta) = 3$$
,  $g(\frac{7}{24}) = 1$ ,  $g(\frac{17}{24}) = 0$ ,  $g(\frac{11}{12}) = 5$ ,  $g(1) = 5$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 21}

$$f(0) = 0$$
,  $f(\frac{5}{13} - 0) = \frac{5}{8}$ ,  $f(\frac{5}{13}) = 1$ ,  $f(\frac{9}{13} - 0) = 1$ ,  $f(\frac{9}{13}) = \frac{11}{8}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{5}{26}) = 3$ ,  $g(\frac{7}{13}) = 3$ ,  $g(\frac{11}{13}) = 5$ ,  $g(1) = 5$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 22}

$$f(0) = 0$$
,  $f(\frac{4}{9} - 0) = \frac{7}{11}$ ,  $f(\frac{4}{9}) = \frac{12}{11}$ ,  $f(\frac{2}{3} - 0) = \frac{12}{11}$ ,  $f(\frac{2}{3}) = \frac{16}{11}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{2}{9}) = 1$ ,  $g(\frac{5}{9}) = 2$ ,  $g(\frac{5}{6}) = 4$ ,  $g(1) = 2$ 

= = = = = = = = =

{var., 23}

$$f(0) = 0$$
,  $f(\frac{8}{15} - 0) = \frac{16}{21}$ ,  $f(\frac{8}{15}) = \frac{26}{21}$ ,  $f(\frac{11}{15} - 0) = \frac{26}{21}$ ,  $f(\frac{11}{15}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{4}{15}) = 5$ ,  $g(\frac{19}{30}) = 2$ ,  $g(\frac{13}{15}) = 2$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 24}

$$f(0) = 0$$
,  $f(\frac{5}{14} - 0) = \frac{1}{2}$ ,  $f(\frac{5}{14}) = \frac{6}{5}$ ,  $f(\frac{5}{7} - 0) = \frac{6}{5}$ ,  $f(\frac{5}{7}) = \frac{9}{5}$ ,  $f(1) = 2$ 

$$g(0) = 6$$
,  $g(\frac{5}{28}) = 2$ ,  $g(\frac{15}{28}) = 6$ ,  $g(\frac{6}{7}) = 3$ ,  $g(1) = 3$ 

= = = = = = = = =

{var., 25}

$$f(0) = 0$$
,  $f(\frac{9}{20} - 0) = \frac{3}{4}$ ,  $f(\frac{9}{20}) = \frac{9}{8}$ ,  $f(\frac{7}{10} - 0) = \frac{9}{8}$ ,  $f(\frac{7}{10}) = \frac{7}{4}$ ,  $f(1) = 2$ 

$$g(\theta) = 2$$
,  $g(\frac{9}{4\theta}) = 6$ ,  $g(\frac{23}{4\theta}) = 2$ ,  $g(\frac{17}{2\theta}) = 2$ ,  $g(1) = 1$ 

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{var., 26}

$$f(0) = 0$$
,  $f(\frac{1}{2} - 0) = \frac{2}{5}$ ,  $f(\frac{1}{2}) = \frac{4}{5}$ ,  $f(\frac{3}{4} - 0) = \frac{4}{5}$ ,  $f(\frac{3}{4}) = \frac{4}{3}$ ,  $f(1) = 2$ 

$$g(0) = 4$$
,  $g(\frac{1}{4}) = 6$ ,  $g(\frac{5}{8}) = 2$ ,  $g(\frac{7}{8}) = 4$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 27}

$$f(0) = 0$$
,  $f(\frac{7}{13} - 0) = 1$ ,  $f(\frac{7}{13}) = \frac{10}{7}$ ,  $f(\frac{9}{13} - 0) = \frac{10}{7}$ ,  $f(\frac{9}{13}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{7}{26}) = 1$ ,  $g(\frac{8}{13}) = 6$ ,  $g(\frac{11}{13}) = 6$ ,  $g(1) = 1$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 28}

$$f(0) = 0$$
,  $f(\frac{9}{16} - 0) = \frac{4}{7}$ ,  $f(\frac{9}{16}) = \frac{8}{7}$ ,  $f(\frac{13}{16} - 0) = \frac{8}{7}$ ,  $f(\frac{13}{16}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(0) = 1$$
,  $g(\frac{9}{32}) = 4$ ,  $g(\frac{11}{16}) = 4$ ,  $g(\frac{29}{32}) = 3$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 29}

$$f(0) = 0$$
,  $f(\frac{6}{11} - 0) = \frac{8}{21}$ ,  $f(\frac{6}{11}) = \frac{8}{7}$ ,  $f(\frac{8}{11} - 0) = \frac{8}{7}$ ,  $f(\frac{8}{11}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(\theta) = \theta$$
,  $g(\frac{3}{11}) = 3$ ,  $g(\frac{7}{11}) = 5$ ,  $g(\frac{19}{22}) = 1$ ,  $g(1) = 4$ 

= = = = = = = = =

{var., 30

$$f(\theta) = \theta$$
,  $f(\frac{7}{12} - \theta) = \frac{12}{23}$ ,  $f(\frac{7}{12}) = \frac{22}{23}$ ,  $f(\frac{5}{6} - \theta) = \frac{22}{23}$ ,  $f(\frac{5}{6}) = \frac{34}{23}$ ,  $f(1) = 2$ 

$$g(0) = 3$$
,  $g(\frac{7}{24}) = 1$ ,  $g(\frac{17}{24}) = 0$ ,  $g(\frac{11}{12}) = 5$ ,  $g(1) = 5$ 

= = = = = = = = =

{var., 31}

$$f(0) = 0$$
,  $f(\frac{5}{13} - 0) = \frac{5}{8}$ ,  $f(\frac{5}{13}) = 1$ ,  $f(\frac{9}{13} - 0) = 1$ ,  $f(\frac{9}{13}) = \frac{11}{8}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{5}{26}) = 3$ ,  $g(\frac{7}{13}) = 3$ ,  $g(\frac{11}{13}) = 5$ ,  $g(1) = 5$ 

= = = = = = = = =

 $\{\texttt{var., 32}\}$ 

$$f(0) = 0$$
,  $f(\frac{4}{9} - 0) = \frac{7}{11}$ ,  $f(\frac{4}{9}) = \frac{12}{11}$ ,  $f(\frac{2}{3} - 0) = \frac{12}{11}$ ,  $f(\frac{2}{3}) = \frac{16}{11}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{2}{9}) = 1$ ,  $g(\frac{5}{9}) = 2$ ,  $g(\frac{5}{6}) = 4$ ,  $g(1) = 2$ 

= = = = = = = = =

{var., 33}

$$f(\emptyset) = \emptyset, \quad f(\frac{8}{15} - \emptyset) = \frac{16}{21}, \quad f(\frac{8}{15}) = \frac{26}{21}, \quad f(\frac{11}{15} - \emptyset) = \frac{26}{21}, \quad f(\frac{11}{15}) = \frac{12}{7}, \quad f(1) = 2$$

$$g(0) = 2$$
,  $g(\frac{4}{15}) = 5$ ,  $g(\frac{19}{30}) = 2$ ,  $g(\frac{13}{15}) = 2$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

 $\{var., 34\}$ 

$$f(\theta) = \theta$$
,  $f(\frac{5}{14} - \theta) = \frac{1}{2}$ ,  $f(\frac{5}{14}) = \frac{6}{5}$ ,  $f(\frac{5}{7} - \theta) = \frac{6}{5}$ ,  $f(\frac{5}{7}) = \frac{9}{5}$ ,  $f(1) = 2$ 

$$g(0) = 6$$
,  $g(\frac{5}{28}) = 2$ ,  $g(\frac{15}{28}) = 6$ ,  $g(\frac{6}{7}) = 3$ ,  $g(1) = 3$ 

= = = = = = = = =

{var., 35}

$$f(0) = 0$$
,  $f(\frac{9}{20} - 0) = \frac{3}{4}$ ,  $f(\frac{9}{20}) = \frac{9}{8}$ ,  $f(\frac{7}{10} - 0) = \frac{9}{8}$ ,  $f(\frac{7}{10}) = \frac{7}{4}$ ,  $f(1) = 2$ 

$$g(\theta) = 2$$
,  $g(\frac{9}{4\theta}) = 6$ ,  $g(\frac{23}{4\theta}) = 2$ ,  $g(\frac{17}{2\theta}) = 2$ ,  $g(1) = 1$ 

= = = = = = = = =

{var., 36}

$$f(0) = 0$$
,  $f(\frac{1}{2} - 0) = \frac{2}{5}$ ,  $f(\frac{1}{2}) = \frac{4}{5}$ ,  $f(\frac{3}{4} - 0) = \frac{4}{5}$ ,  $f(\frac{3}{4}) = \frac{4}{3}$ ,  $f(1) = 2$ 

$$g(\theta) = 4$$
,  $g(\frac{1}{4}) = 6$ ,  $g(\frac{5}{8}) = 2$ ,  $g(\frac{7}{8}) = 4$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 37}

$$f(\theta) = \theta$$
,  $f(\frac{7}{13} - \theta) = 1$ ,  $f(\frac{7}{13}) = \frac{10}{7}$ ,  $f(\frac{9}{13} - \theta) = \frac{10}{7}$ ,  $f(\frac{9}{13}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{7}{26}) = 1$ ,  $g(\frac{8}{13}) = 6$ ,  $g(\frac{11}{13}) = 6$ ,  $g(1) = 1$ 

= = = = = = = = =

{var., 38}

$$f(0) = 0$$
,  $f(\frac{9}{16} - 0) = \frac{4}{7}$ ,  $f(\frac{9}{16}) = \frac{8}{7}$ ,  $f(\frac{13}{16} - 0) = \frac{8}{7}$ ,  $f(\frac{13}{16}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(0) = 1$$
,  $g(\frac{9}{32}) = 4$ ,  $g(\frac{11}{16}) = 4$ ,  $g(\frac{29}{32}) = 3$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 39}

$$f(0) = 0, \quad f(\frac{6}{11} - 0) = \frac{8}{21}, \quad f(\frac{6}{11}) = \frac{8}{7}, \quad f(\frac{8}{11} - 0) = \frac{8}{7}, \quad f(\frac{8}{11}) = \frac{32}{21}, \quad f(1) = 2$$

$$g(0) = 0$$
,  $g(\frac{3}{11}) = 3$ ,  $g(\frac{7}{11}) = 5$ ,  $g(\frac{19}{22}) = 1$ ,  $g(1) = 4$ 

= = = = = = = = =

{var., 40}

$$f(0) = 0$$
,  $f(\frac{7}{12} - 0) = \frac{12}{23}$ ,  $f(\frac{7}{12}) = \frac{22}{23}$ ,  $f(\frac{5}{6} - 0) = \frac{22}{23}$ ,  $f(\frac{5}{6}) = \frac{34}{23}$ ,  $f(1) = 2$ 

$$g(0) = 3$$
,  $g(\frac{7}{24}) = 1$ ,  $g(\frac{17}{24}) = 0$ ,  $g(\frac{11}{12}) = 5$ ,  $g(1) = 5$ 

= = = = = = = = =

{var., 41}

$$f(0) = 0$$
,  $f(\frac{5}{13} - 0) = \frac{5}{8}$ ,  $f(\frac{5}{13}) = 1$ ,  $f(\frac{9}{13} - 0) = 1$ ,  $f(\frac{9}{13}) = \frac{11}{8}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{5}{26}) = 3$ ,  $g(\frac{7}{13}) = 3$ ,  $g(\frac{11}{13}) = 5$ ,  $g(1) = 5$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 42}

$$f(0) = 0$$
,  $f(\frac{4}{9} - 0) = \frac{7}{11}$ ,  $f(\frac{4}{9}) = \frac{12}{11}$ ,  $f(\frac{2}{3} - 0) = \frac{12}{11}$ ,  $f(\frac{2}{3}) = \frac{16}{11}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{2}{9}) = 1$ ,  $g(\frac{5}{9}) = 2$ ,  $g(\frac{5}{6}) = 4$ ,  $g(1) = 2$ 

= = = = = = = = =

{var., 43}

$$f(0) = 0$$
,  $f(\frac{8}{15} - 0) = \frac{16}{21}$ ,  $f(\frac{8}{15}) = \frac{26}{21}$ ,  $f(\frac{11}{15} - 0) = \frac{26}{21}$ ,  $f(\frac{11}{15}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{4}{15}) = 5$ ,  $g(\frac{19}{30}) = 2$ ,  $g(\frac{13}{15}) = 2$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 44}

$$f(0) = 0$$
,  $f(\frac{5}{14} - 0) = \frac{1}{2}$ ,  $f(\frac{5}{14}) = \frac{6}{5}$ ,  $f(\frac{5}{7} - 0) = \frac{6}{5}$ ,  $f(\frac{5}{7}) = \frac{9}{5}$ ,  $f(1) = 2$ 

$$g(0) = 6$$
,  $g(\frac{5}{28}) = 2$ ,  $g(\frac{15}{28}) = 6$ ,  $g(\frac{6}{7}) = 3$ ,  $g(1) = 3$ 

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{var., 45

$$f(0) = 0$$
,  $f(\frac{9}{20} - 0) = \frac{3}{4}$ ,  $f(\frac{9}{20}) = \frac{9}{8}$ ,  $f(\frac{7}{10} - 0) = \frac{9}{8}$ ,  $f(\frac{7}{10}) = \frac{7}{4}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{9}{40}) = 6$ ,  $g(\frac{23}{40}) = 2$ ,  $g(\frac{17}{20}) = 2$ ,  $g(1) = 1$ 

= = = = = = = = =

{var., 46}

$$f(\theta) = \theta$$
,  $f(\frac{1}{2} - \theta) = \frac{2}{5}$ ,  $f(\frac{1}{2}) = \frac{4}{5}$ ,  $f(\frac{3}{4} - \theta) = \frac{4}{5}$ ,  $f(\frac{3}{4}) = \frac{4}{3}$ ,  $f(1) = 2$ 

$$g(0) = 4$$
,  $g(\frac{1}{4}) = 6$ ,  $g(\frac{5}{8}) = 2$ ,  $g(\frac{7}{8}) = 4$ ,  $g(1) = 0$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 47}

$$f(0) = 0$$
,  $f(\frac{7}{13} - 0) = 1$ ,  $f(\frac{7}{13}) = \frac{10}{7}$ ,  $f(\frac{9}{13} - 0) = \frac{10}{7}$ ,  $f(\frac{9}{13}) = \frac{12}{7}$ ,  $f(1) = 2$ 

$$g(0) = 2$$
,  $g(\frac{7}{26}) = 1$ ,  $g(\frac{8}{13}) = 6$ ,  $g(\frac{11}{13}) = 6$ ,  $g(1) = 1$ 

\_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_ \_

{var., 48}

$$f(0) = 0, \quad f(\frac{9}{16} - 0) = \frac{4}{7}, \quad f(\frac{9}{16}) = \frac{8}{7}, \quad f(\frac{13}{16} - 0) = \frac{8}{7}, \quad f(\frac{13}{16}) = \frac{32}{21}, \quad f(1) = 2$$

$$g(0) = 1$$
,  $g(\frac{9}{32}) = 4$ ,  $g(\frac{11}{16}) = 4$ ,  $g(\frac{29}{32}) = 3$ ,  $g(1) = 0$ 

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 $\{var., 49\}$ 

$$f(0) = 0$$
,  $f(\frac{6}{11} - 0) = \frac{8}{21}$ ,  $f(\frac{6}{11}) = \frac{8}{7}$ ,  $f(\frac{8}{11} - 0) = \frac{8}{7}$ ,  $f(\frac{8}{11}) = \frac{32}{21}$ ,  $f(1) = 2$ 

$$g(0) = 0$$
,  $g(\frac{3}{11}) = 3$ ,  $g(\frac{7}{11}) = 5$ ,  $g(\frac{19}{22}) = 1$ ,  $g(1) = 4$ 

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{var., 50}

$$f(0) = 0$$
,  $f(\frac{7}{12} - 0) = \frac{12}{23}$ ,  $f(\frac{7}{12}) = \frac{22}{23}$ ,  $f(\frac{5}{6} - 0) = \frac{22}{23}$ ,  $f(\frac{5}{6}) = \frac{34}{23}$ ,  $f(1) = 2$ 

$$g(\theta) = 3$$
,  $g(\frac{7}{24}) = 1$ ,  $g(\frac{17}{24}) = 0$ ,  $g(\frac{11}{12}) = 5$ ,  $g(1) = 5$