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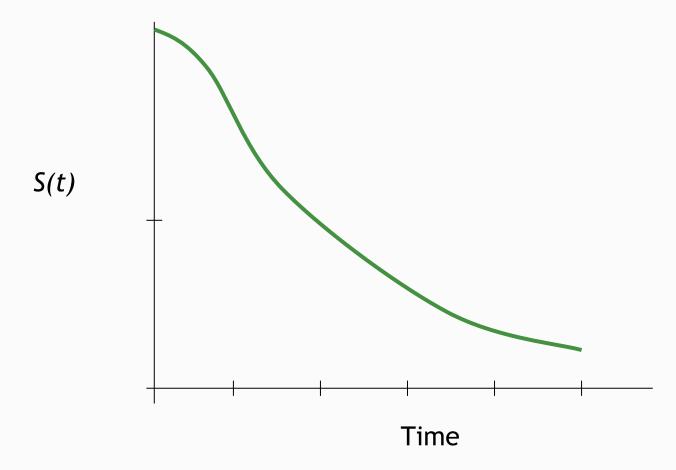
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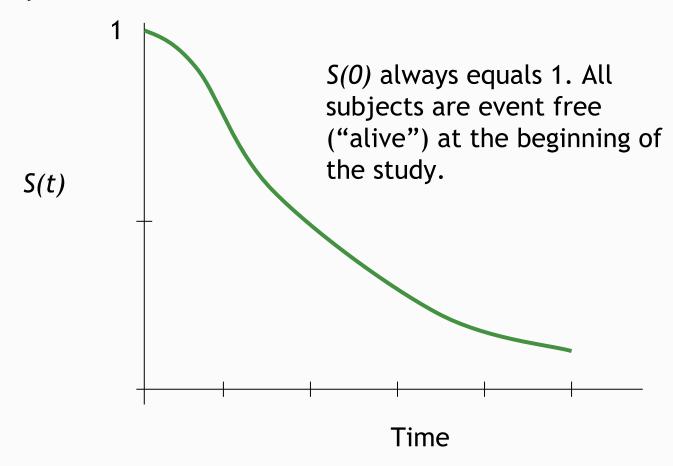
Section B

Estimating the Survival Curve: The Kaplan Meier Approach

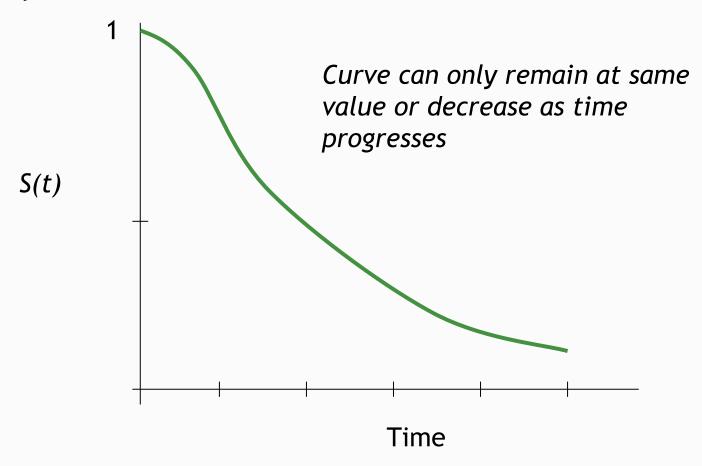
- Estimation of the "survival curve"
- S(t) = proportion remaining event free (surviving) at least to time t or beyond



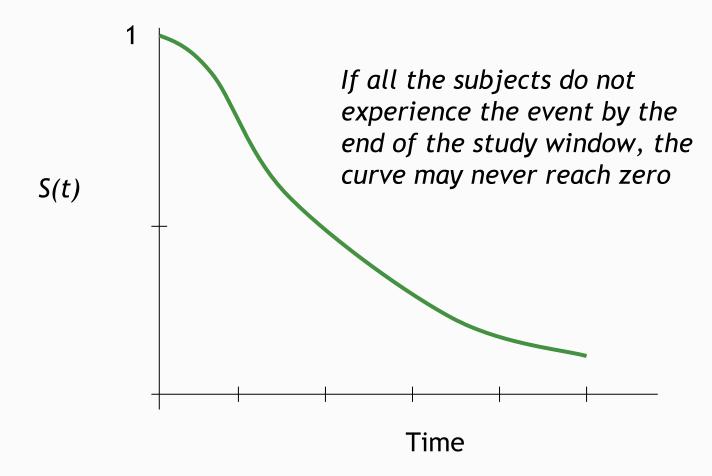
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- Estimation of the "survival curve"
 - S(t) = proportion remaining event free (surviving) at least to time t or beyond
 - We can estimate S(t) from a sample of data: out statistic is $\hat{S}(t)$



Approaches

- Life table method
 - Grouped in intervals
- Kaplan-Meier (1958)
 - Ungrouped data
 - Small samples

- Example: time (months) from primary AIDS diagnosis for a sample of 12 hemophiliac patients under 40 years old at time of HIV seroconversion*
 - Event times (n = 12):
 - 2 3+ 5 6 7+ 10 15+ 16 16 27 30 32

Notes: * Example based on data taken from Rosner, B. (1990). Fundamentals of biostatistics, 6th ed. (2005). Duxbury Press. (based on research by Ragni, et al. (1990). Cumulative risk for AIDS in *Journal of Acquired Immune Deficiency Syndromes*, Vol. 3.

- $\hat{S}(t) = 1$, to start
- After starting at time 0, curve can be estimated at each event time t, but not at censoring times

$$\hat{S}(t) = \left(\frac{N(t) - E(t)}{N(t)}\right) \times \hat{S}(Previous Event Time)$$

- E(t) = # events at time t
- N(t) = # subjects at risk for event at time t

Curve can be estimated at each event, but not at censoring times

$$\hat{S}(t) = \left(\frac{N(t) - E(t)}{N(t)}\right) \times \hat{S}(Previous Event Time)$$

Proportion of original sample making it to time *t*

Curve can be estimated at each event, but not at censoring times

$$\hat{S}(t) = \left(\frac{N(t) - E(t)}{N(t)}\right) \times \hat{S}(Previous Event Time)$$

Proportion surviving to time *t* who survive beyond time *t*

Start estimate at first (ordered) event time

$$\hat{S}(2) = \left(\frac{N(2) - E(2)}{N(2)}\right) = \frac{12 - 1}{12} = \frac{11}{12} = .92$$

- \blacksquare Can estimate S(t) at each subsequent event time
 - (Censoring times inform estimate about number at risk of having the event at a time t until censoring occurs)
 - 2 3+ 6 6 7+ 10 15+ 15 16 27 30 32

$$\hat{S}(6) = \left(\frac{N(6) - E(6)}{N(6)}\right) \times \hat{S}(2) = \left(\frac{10 - 2}{10}\right) \times .92 = .80 \times .92 = .74$$

- \blacksquare Can estimate S(t) at each subsequent event time
 - (Censoring times inform estimate about the number at risk of having the event at a time t)
 - 2 3+ 6 6 7+ **10** 15+ 15 16 27 30 32

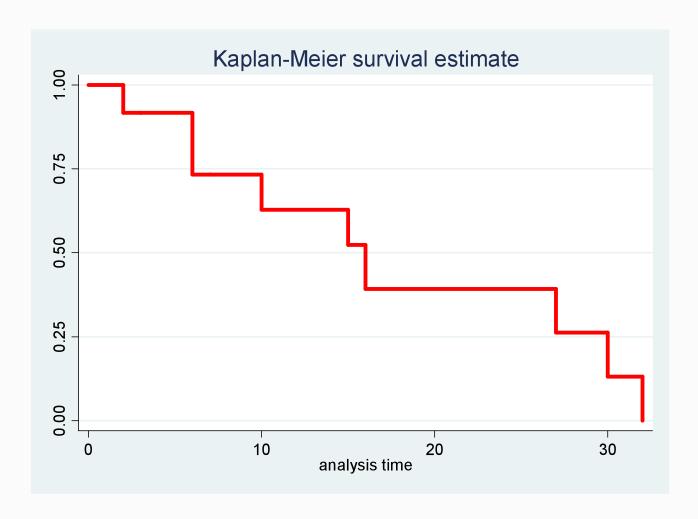
$$\hat{S}(10) = \left(\frac{N(10) - E(10)}{N(10)}\right) \times \hat{S}(6) = \left(\frac{7 - 1}{6}\right) \times .74 = .86 \times .74 = .64$$

Continue through final event time

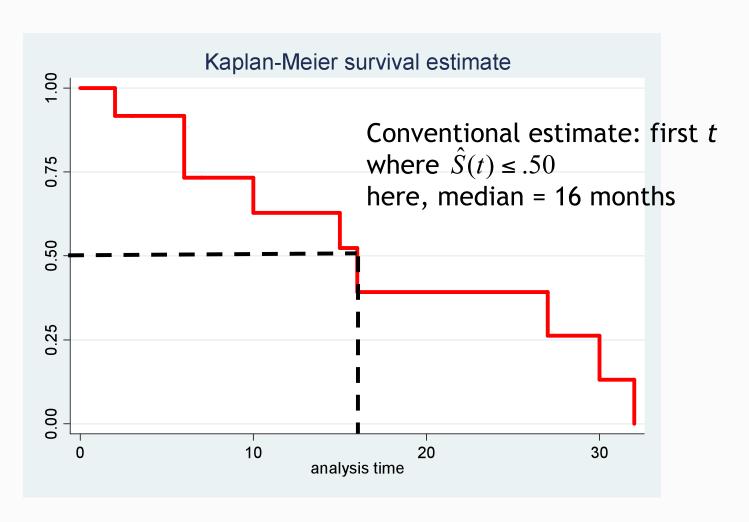
t	$\hat{S}(t)$
2	.92
6	.74
10	.64
15	.52
16	.39
27	.26
30	.13
32	0

- Graph is a step function
- "Jumps" at each observed event time
- Nothing is assumed about curved shape between each observed event time

Kaplan-Meier estimate graphically presented



 You can use these to estimate single number summary statistics, like the median survival time (median time remaining event free)



- Time days to resuming smoking in first month following completion of five one-hour group coaching sessions on smoking cessation (10 subjects)
- - 15 3+ 30+ 5 10+ 30+ 7 1 24+ 27

- Time days to resuming smoking in first thirty day period following completion of five one-hour group coaching sessions on smoking cessation (10 subjects): ordered times
- **-** 1 3+ 5 7 10+ 15 24+ 27 30+ 30+

- Time days to resuming smoking in first thirty day period following completion of five one-hour group coaching sessions on smoking cessation (10 subjects): ordered times
- **-** 1 3+ 5 7 10+ 15 24+ 27 30+ 30+

$$- \hat{S}(1) = \left(\frac{N(1) - E(1)}{N(1)}\right) = \frac{10 - 1}{10} = \frac{9}{10} = .90$$

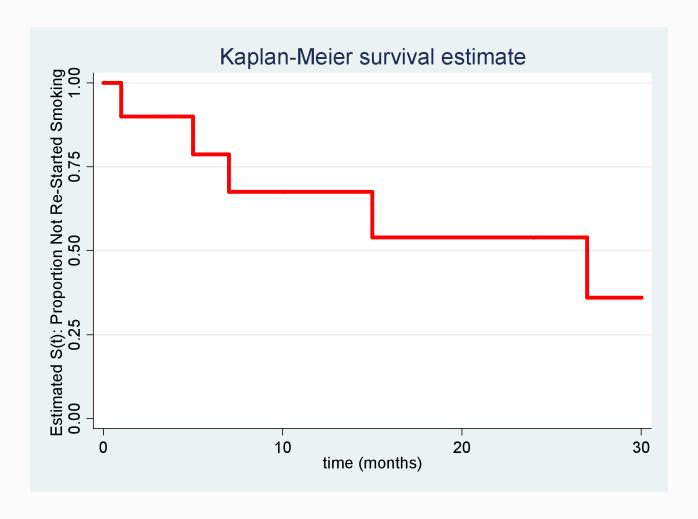
- Time days to resuming smoking in first thirty day period following completion of five one-hour group coaching sessions on smoking cessation (10 subjects): ordered times
- **1** 3+ 5 7 10+ 15 24+ 27 30+ 30+

$$- \hat{S}(5) = \left(\frac{N(5) - E(5)}{N(5)}\right) \times \hat{S}(1) = \left(\frac{8 - 1}{8}\right) \times .90 = .88 \times .90 = .79$$

 Continue through final event time: notice this estimated curve never reaches 0 because largest time values are censoring times

t	$\hat{S}(t)$
1	.90
5	.79
7	.68
15	.54
27	.36

Graphical presentation



Big Assumption

- Independence of censoring and survival
- Those censored at time t have the same prognosis as those not censored at t
- Examples of possible violations
 - Time to tumor—animal
 - Occupational health—loss to follow up