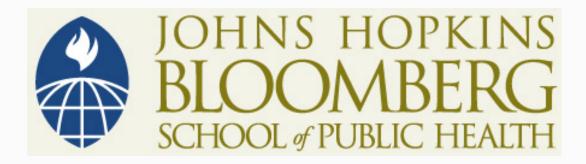
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#### Section B

Two Sample t-test: Getting a p-value

# Hypothesis Test to Compare Two Independent Groups

- Two sample (unpaired) t-test
- Is the (mean) weight change equal in the two diet groups?
  - $H_0$ :  $\mu_1 = \mu_2$
  - $H_A$ :  $\mu_1 \neq \mu_2$
- In other words, is the expected difference in weight change zero?
  - $H_0$ :  $\mu_1 \mu_2 = 0$
  - $H_{\Delta}$ :  $\mu_1 \mu_2 \neq 0$

## Hypothesis Test to Compare Two Independent Groups

- Recall, general "recipe" for hypothesis testing . . .
  - 1. Start by assuming H<sub>o</sub> true
  - 2. Measure distance of sample result from  $\mu_o$  (here again its 0)
  - 3. Compare test statistic (distance) to appropriate distribution to get p-value

$$t = \frac{(observed \ dif \ f) - (null \ dif \ f}{SE \ of \ observed \ dif \ f \ erence}$$

$$t = \frac{\vec{x}_1 - \vec{x}_2}{S\hat{E}(\vec{x}_1 - \vec{x}_2)} = \frac{\vec{x}_1 - \vec{x}_2}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

# Diet Type and Weight Loss Study

In the diet types and weight loss study, recall:

$$\overline{x}_1 - \overline{x}_2 = -3.9kg$$

$$S\hat{E}(\overline{x}_1 - \overline{x}_2) = 1.17kg$$

So in this study:

$$t = \frac{-3.9}{1.17} \approx -3.3$$

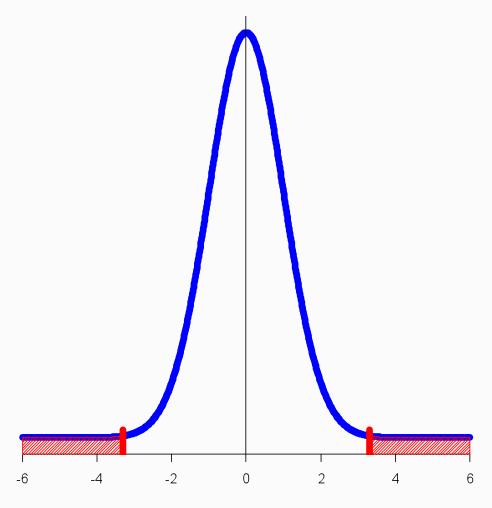
 So this study result was 3.3 standard errors below the null mean of 0 (i.e., 3.3 standard errors from the mean weight less expected if null was true)

## How Are p-values Calculated?

- Is a result 3.3 standard errors below 0 unusual?
  - It depends on what kind of distribution we are dealing with
- The p-value is the probability of getting a test statistic as extreme as (or more extreme than) what you observed (-3.3) by chance if was true
- The p-value comes from the sampling distribution of the difference in two sample means
- What is the sampling distribution of the difference in sample means?
  - If both groups are large (more than 60 subjects) then this distribution is approximately normal
  - This sampling distribution will be centered at true difference
  - Under null hypothesis, this true difference is 0

# Diet/Weight Loss Sample

 To compute a p-value, we would need to compute the probability of being 3.3 or more standard errors away from 0 on a standard normal curve



## How to Use Stata to Perform a 2-Sample T-Test

#### Command syntax:

- ttesti  $n_1$   $\overline{x}_1$   $s_1$   $n_2$   $\overline{x}_2$   $s_2$ , unequal

```
. ttesti 64 -5.7 8.6 68 -1.8 3.9, unequal
```

Two-sample t test with unequal variances

	l Obs		Std. Err.	Std. Dev.	-	Interval]
х У	l 64 l 68	-5.7 -1.8		8.6 3.9	-7.848216 -2.744001	8559989
combined	132	-3.690909	.5978226	6.868458	-4.873545	-2.508273
diff			1.174437		-6.234436	
	iff < 0 ) = 0.0007	Pr(	Ha: diff !=			diff > 0 c) = 0.9993

### How to Use Stata to Perform a 2-Sample T-Test

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```
. ttesti 64 -5.7 8.6 68 -1.8 3.9, unequal
```

Two-sample t test with unequal variances

	l Obs	Mean	Std. Err.		[95% Conf	-
× Y	64   68	-5.7 -1.8	1.075 .4729445	8.6 3.9	-7.848216 -2.744001	-3.551784
combined	I 132	-3.690909	.5978226	6.868458	-4.873545	
diff	•		1.174437		-6.234436	

```
diff = mean(x) - mean(y)
Ho: diff = 0
                                Satterthwaite's degrees of freedom = 86.6941
```

Ha: 
$$diff < 0$$
  
Pr(T < t) = 0.0007

Ha: 
$$diff > 0$$
  
 $Pr(T > t) = 0.9993$ 

### How to Use Stata to Perform a 2-Sample T-Test

#### Command syntax:

- ttesti  $n_1$   $\overline{x}_1$   $s_1$   $n_2$   $\overline{x}_2$   $s_2$ , unequal

. ttesti 64 -5.7 8.6 68 -1.8 3.9, unequal

Two-sample t test with unequal variances

	Obs	Mean	Std. Err.	Std. Dev.	[ 95% Conf	. Interval]
х У	I 64	-5.7 -1.8	1.075 .4729445	8.6	-7.848216 -2.744001	8559989
combined	l 132		.5978226	6.868458	-4.873545	-2.508273
diff	•		1.174437			-1.565564

diff = mean(x) - mean(y) t = -3.3207

Ho: diff = 0

Satterthwaite's degrees of freedom = 86.6941

Ha: diff < 0Pr(T < t) = 0.0007 Ha: diff != 0 Pr(|T| > |t|) = 0.0013

Ha: diff > 0Pr(T > t) = 0.9993

## Summary: Weight Loss Example

#### Statistical method

- "We randomly assigned 132 severely obese patients . . . to a carbohydrate restricted (low-carbohydrate) diet or a calorieand fat-restricted diet"
- "For comparison of continuous variables between the two groups, we calculated the change from baseline to six months in each subject, and compared the mean changes in the two diet groups using an unpaired t-test"

#### Result

"Subjects on the low-carbohydrate diet lost more weight than those on a low fat diet (95% confidence interval for the difference in weight loss between groups, -1.6 to -6.2 kg; p < .01)"</p>