numpy and scipy (1/2)

Computing Methods for Experimental Physics and Data Analysis

L. Baldini luca.baldini@pi.infn.it

Università and INFN-Pisa





- Python is notorious for coming with batteries included...
- ...but as a data scientist numpy and and scipy will be your best friends!
- → Among (many) other things, numpy offers:
 - □ a powerful n-dimensional array object
- ▷ And scipy provides:

 - > optimization (a.k.a. fitting)
 - ▷ interpolation



numpy arrays

— https://bitbucket.org/lbaldini/programming/src/tip/snippets/numpy_arrays.py

```
1
    import numpy as np
2
3
    # Initialization from a list
4
    a1 = np.array([1., 2., 3])
5
    print (a1)
6
7
    # Zeros, ones, and fixed values
    a2 = np.zeros(10)
    a3 = np.ones((2, 2))
9
    a4 = np.full(7, 3.)
10
11
    print (a2)
    print (a3)
12
    print (a4)
13
14
15
    # Grids
    a5 = np.linspace(0., 10., 11)
16
17
    a6 = np.logspace(0., 1., 11)
    print (a5)
18
    print (a6)
19
20
21
22
    [1. 2. 3.]
    [0. 0. 0. 0. 0. 0. 0. 0. 0. 0.]
23
24
    [[1. 1.]
    [1. 1.1]
25
    [3. 3. 3. 3. 3. 3. 3.]
26
    [0. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10.]
2.7
28
    [1. 1.25892541 1.58489319 1.99526231 2.51188643 3.16227766
29
    3.98107171 5.01187234 6.30957344 7.94328235 10.
```

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numpy arrays vs. Python lists

import numpy as np 1 2 # arravs and lists seem similar ... 4 1 = [1., 2., 3.]a = np.array(1)print(1) print (a) 8 9 # ...but they support basic arithmetic in a different fashion 10 print(1 + 1) print(a + a) 12 13 14 [1.0, 2.0, 3.0] [1. 2. 3.] 15 [1.0, 2.0, 3.0, 1.0, 2.0, 3.0] 16 17 [2. 4. 6.]

- > arrays and lists are fundamentally different objects

 - > arrays are homogeneous, lists don't need to
 - > arrays offer a much more powerful indexing/slicing
 - > arrays interoperate with numpy mathematical functions

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Broadcasting

https://bitbucket.org/lbaldini/programming/src/tip/snippets/numpy_arrays_broadcasting.p

```
import numpy as np
2
3
    a1 = np.arrav([1., 2.1)
4
    a2 = np.array([[1., 2.], [3., 4.]])
5
    c = np.pi
6
7
    print (a1)
    print (a2)
8
9
    print(c)
    print(a1 * a1)
10
11
    print(a1 * c)
12
    print (a1 * a2)
13
14
15
    [1. 2.]
    [[1. 2.]
16
17
    [3. 4.11
    3.141592653589793
18
    [1. 4.]
19
2.0
    [3.14159265 6.28318531]
    [[1. 4.]
21
    [3. 8.11
22
```

- Under certain conditions, numpy can make operations on arrays of different shape
- > This is extremely useful when vectorizing problems



Mathematical functions in numpy

```
import numpy as np
 1
2
    import math
3
4
    a = np.array([0.1, 1., 10.])
5
    print (np.log10(a))
6
    print (np.exp(a))
7
    print (np.sin(a))
9
10
    print (np.log10(0.1))
11
12
    print (math.log10(a))
13
14
    [-1. 0. 1.]
15
    [1.10517092e+00 2.71828183e+00 2.20264658e+04]
16
17
    18
    Traceback (most recent call last):
19
      File "snippets/numpy_functions.py", line 12, in <module>
20
2.1
        print (math.log10(a))
22
    TypeError: only size-1 arrays can be converted to Python scalars
```

- numpy mathematical functions interoperate natively with arrays
 (and work on plain old numbers, too)
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Arrays and masks

```
import numpy as np
1
2
   a = np.linspace(0., 10., 11)
3
   mask1 = a >= 2.5
   mask2 = a < 8.5
6
7
   print (a)
   print (mask1)
   print (mask2)
   print(a[mask1])
10
   print (a[mask2])
11
12
   print (a[np.logical_and(mask1, mask2)])
13
14
   [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10,]
15
16
   17
   [3, 4, 5, 6, 7, 8, 9, 10,]
18
   [0. 1. 2. 3. 4. 5. 6. 7. 8.]
19
   [3. 4. 5. 6. 7. 8.]
20
```

- Masks are a powerful tool in numpy
- They can replace conditional expressions in a for loop in vectorization context (more on this later)



Digression: pseudo-random number generators

1 2

```
import random
x = random.random()
```

- Every programming language comes with a Pseudo Random Number Generator (PRNG)
 - Python is no exception: https://docs.python.org/3/library/random.html
 - \triangleright Mersenne-Twister, 53-bit precision, period of $2^{19937}-1$.
- > PRNGs are an interesting (and fun) subject by themselves:
 - ▷ Donald E. Knuth, The Art of Computer Programming, Volume 2: Seminumerical Algorithms, 3rd Edition
 - M. Matsumoto and T. Nishimura, Mersenne Twister: A 623-dimensionally equidistributed uniform pseudorandom number generator, ACM Transactions on Modeling and Computer Simulation Vol. 8, No. 1, January pp.3–30 1998.
- → A PRNG produces random floats uniformly in [0.0, 1.0).



Vectorization

a.k.a. avoid explicit for loops in Python whenever you can

https://bitbucket.org/lbaldini/programming/src/tip/snippets/vectorization.py

```
import random
2
    import time
    import numpy as np
3
4
    # How many random numbers (uniformly distributed between 0 and 1) do you
5
6
    # want to throw?
7
    n = 1000000
8
9
    # The slow way: explicit for loop in Python.
10
    t0 = time.time()
    x = []
11
12
    for i in range(n):
        x.append(random.random())
13
    dt = time.time() - t0
14
15
    print('Elapsed time: %.3f s' % dt)
16
    # The quick way: vectorizing in numpy
17
    t0 = time.time()
18
    x = np.random.random(size=n)
19
20
    dt = time.time() - t0
    print('Elapsed time: %.3f s' % dt)
21
22
2.3
    Elapsed time: 0.131 s
24
    Elapsed time: 0.015 s
25
```

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How does vectorizaion work?

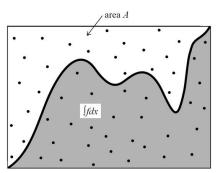
- ▷ Python is know to be slooow
 - → This is the price you pay for being so beautiful and flexible
- ▷ Does it matter? If depends...
 - ▷ If you are parsing a text file or fetching a web page probably not
 - If you are performing a CPU-intensive processing on a TB of data probably yes
- > numpy is written in C as a Python extension

 - When you perform an array operation in Python you are actually executing optimized C code
- Basic message: avoid for loops in pure Python when crunching numbers



How do I throw PRN with arbitrary pdf?

Hit or miss



- → Hit or miss, aka acceptance/rejection method:
 - ▷ Enclose your pdf in a rectangle
 - \triangleright Throw a x and a y
 - \triangleright Accept x if $y \le f(x)$
- → This is horrible—please don't use it!

How do I throw PRN with arbitrary pdf?

Inverse transform

Probability density function (pdf)

$$p(x) (\geq 0)$$

$$F(x) = \int_{-\infty}^{x} p(x') dx'$$

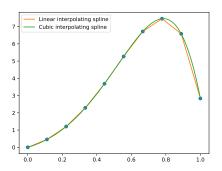
▷ Percent-point function (ppf)

$$x = F^{-1}(q)$$

Awesome fact: if q is uniformly distributed in [0, 1], then $x = F^{-1}(q)$ is distributed according to p(x)!



An interesting object: splines



- ightarrow Defined piecewsise by polinomials of degree k (k=3 fairly popular)
 - ▷ Interpolating: passing through a set of pre-defined points
 - \triangleright First k-1 derivatives continuos at the control points
- ▷ Superior to polynomial interpolation or curve fitting in many cases



Splines: construction and properties

__https://bitbucket.org/lbaldini/programming/src/tip/snippets/spline.pv

```
1
    import numpy as np
    from scipy.interpolate import InterpolatedUnivariateSpline
3
4
    x = np.linspace(0., 1., 10)
    y = np.exp(3. * x) * np.sin(3. * x)
5
6
    s1 = InterpolatedUnivariateSpline(x, v, k=1)
    s3 = InterpolatedUnivariateSpline(x, y, k=3)
8
9
10
    print(s1(0.234))
    print(s1.integral(0.2, 0.8))
11
12
13
14
    1.3192110648078448
15
```

- - If the input x-array is sorted can do a binary search in O(log(N)) complexity
- ▷ Derivatives and integrals are easy
 - Can be calculated exactly by means of elementary arithmetic operations

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References

- b https://numpy.org/
- https://www.scipy.org/
- > https://docs.scipy.org/doc/numpy/reference/arrays.indexing.html
- https://docs.scipy.org/doc/numpy/user/basics.broadcasting.html
- https://docs.scipy.org/doc/scipy/reference/interpolate.html