

# Rojas Neural Networks Chapter 3

## Linear separability:

Two sets of points  $A$  and  $B$  are linearly separable if  $n+1$  real numbers exist  $w_1, \dots, w_{n+1}$  such that every point  $x_1, \dots, x_n \in A$

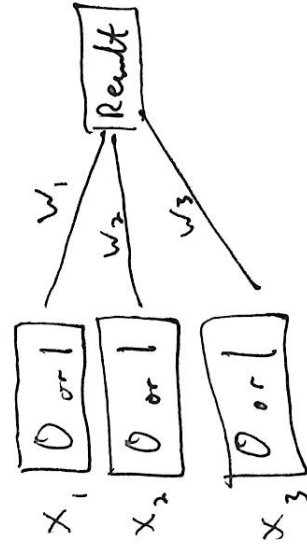
satisfies  $\sum_{i=1}^n w_i x_i \geq w_{n+1}$  and every point  $x_1, x_2, \dots, x_n \in B$

satisfies  $\sum_{i=1}^n w_i x_i < w_{n+1}$

$\Rightarrow$  No rule has been established/found to give the number of linearly separable functions of  $n$  binary arguments

Possible solution: Randomized perception

for  $n=3$ :



$\neq$  weights in  $w$  are randomized

$x_1$	$x_2$	$x_3$	$f_n$
0	0	0	$r_1$
0	0	1	$r_2$
0	1	0	$\vdots$
1	1	1	$r_N$

$W = \begin{bmatrix} r_1 \\ r_2 \\ \vdots \\ r_N \end{bmatrix}$

Each function  $f_n$  describes an output pattern for each input possibility

To test for computability of an output pattern, generate random weights and see if each vector

$r_i$  is output where 0, where  $r_i$  is greater than each  $0$  or  $1$  where