

Algorithms and Programming

Lecture 7 – Testing, GRASP patterns

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Course content

- Introduction in the software development process
- Procedural programming
- Modular programming
- Abstract data types
- Software development principles
- Testing and debugging
- Recursion
- Complexity of algorithms
- Search and sorting algorithms
- Backtracking
- Recap

Last time

- Classes
 - Data abstraction
 - Instance attributes vs Class attributes

• UML

Today

- Testing
 - Concept
 - Testing data
 - Examples

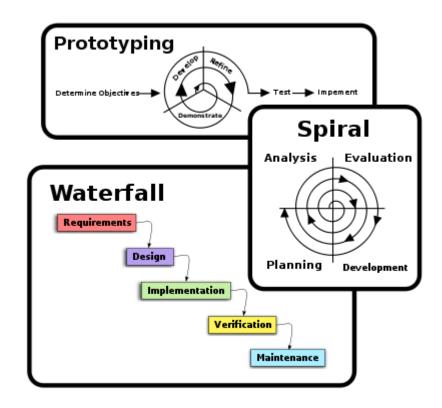
• GRASP - General Responsibility Assignment Software Patterns

Recap: Testing and debugging

- Separate the code in modules test and debug them separately
- Document modules and functions
- Debugging the code
 - Identify why a program is not working as expected
 - Study the events that generate an error
 - Use print!
- Testing the code
 - No syntax errors
 - No semantic errors
 - Use assertions
 - Unit testing: validate each unit, test each function separately

Stages in the life of a program (software)

- Requirements definition
- Analysis (decompose the problem in subproblems)
- Design (specification of ADT, structure / layers of the application)
- Implementation
- Testing



Testing

- Testing
 - Observing the behavior of an application for different test data
 - Program verification
 - Continuous activity
- Determine the data for testing (how to choose test data)
 - Exhaustive testing incomplete testing
 - Black box testing
 - White box testing (or glass box testing)

Why testing

- "UNTESTED == BROKEN", Schlomo Shapiro, EuroPython 2014
- "... we have as many testers as we have developers. And testers spend all their time testing, and developers spend half their time testing. We're more of a testing, a quality software organization than we're a software organization.", Bill Gates (Information Week, May 2002)
- "Everyone knows that debugging is twice as hard as writing a program in the first place. So if you're as clever as you can be when you write it, how will you ever debug it?", Brian Kernighan, "The Elements of Programming Style", 2nd edition, chapter 2
- "Pay attention to zeros. If there is a zero, someone will divide by it.", Cem Kaner

https://github.com/krother/python_testing_tutorial

Testing methods: Exhaustive testing

- Exhaustive testing
 - Verify a program for all possible testing data
 - Impossible to apply it in the real world need to choose a finite number of testing cases
- Incomplete testing
 - Verify a program for some testing data
 - Can be applied in the real world
 - Can use some intuition about natural boundaries of the problem

```
def bigger(a, b):
    """ Given two integer numbers a and b
    Returns True if a > b, False otherwise """
    if a > b:
        return True
    return False
```

- Random testing
 - more tests increase probability that code is correct

Testing methods: Black box testing

- Choose the testing data based on the specification of algorithms (data, results) without analyzing the code
- Test if the application does what is supposed to do
 - Normal values
 - Boundary conditions on the values e.g empty list, large numbers, etc.
 - Error conditions
- Verifies if the application respects the specification
- Designed without looking at the code can avoid implementation biases

Testing methods: White box testing

- Choose testing cases based on the code of the algorithms
 - Cover all possible execution flows based on the implementation
 - Path-complete: if every potential path through code is tested at least once
- Recommendations
 - If
 - Test all parts of conditionals
 - While, for
 - Test all cases to exit the loop
 - Loop not entered
 - Loop executed only once or several times

Examples Black box testing

```
def isPrime(x):
    checks if a number is prime or not
   Data: x - a positive integer number
   Results: True, if x is prime,
   False if x is composed
    raise ValueError if x < 0
   if (x < 0):
        raise ValueError("give a positive
         number to be tested...")
   else:
        if (x < 2):
            return False
        else:
            d = 2
            while (d * d <= x):
                if (x % d == 0):
                    return False
                d = d + 1
            return True
```

```
def testIsPrime():
    #black box testing
    #test a prime number
    assert isPrime(5) == True
    #test a composed number
    assert isPrime(15) == False
    #test 0
    assert isPrime(0) == False
    #test a negative number
   try:
        isPrime(-3)
        assert False
    except ValueError as ex:
        print("some errors: " + str(ex))
        assert True
def testIsPrime():
   for i in range(-100, 1):
        try:
            isPrime(i)
            assert False
        except ValueError:
            pass
    primes = [2, 3, 5, 7, 11, 13, 17, 19]
   for i in range(2, 20):
        assert isPrime(i) == (i in primes), "this is the
value where it fails: " + str(i)
```

Examples White box testing

```
def isPrime(x):
   checks if a number is prime or not
   Data: x - a potivie integer number
   Results: True, if x is prime,
   False if x is composed
   raise ValueError if x < 0
S1 if (x < 0):
S2
       raise ValueError("give a positive
        number to be tested...")
S3 else:
       if (x < 2):
S4
           return False
S5
     else:
S6
           d = 2
S7
S8
           while (d * d <= x):
               if (x % d == 0):
S9
S10
                   return False
       d = d + 1
S11
S12
      return True
```

```
def testIsPrime():
    #white box testing (cover all paths)
    # x < 0 \Rightarrow S1, S2
    try:
         isPrime(-5)
         assert False
    except ValueError as ex:
         print("some errors: " + str(ex))
         assert True
    \#0 <= x < 2 \Rightarrow S3, S4, S5
    assert isPrime(0) == False
    assert isPrime(1) == False
    \#x = 2 \text{ or } x = 3 \Rightarrow S3, S6, S7, S12
    assert isPrime(2) == True
    assert isPrime(3) == True
    \#x = 11 \Rightarrow S3, S6, S7, S8, S11, S8, S11, S12
    assert isPrime(11) == True
    \#x = 15 \Rightarrow S3,S6,S7,S8,S11,S8,S9,S10
    assert isPrime(15) == False
testIsPrime()
```

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Examples

```
def sumOfEvenValues(1):
    computes the sum of even values from a list
    Data: L - a list of integers
    Results: sum of even values of L
    '''
    s = 0
    for i in range(0, len(1)):
        if (1[i] % 2 == 0):
            s = s + 1[i]
    return s
```

```
def testSumOfEvenValues():
   #empty list
   assert sumOfEvenValues([]) == 0
   #no even value
    assert sumOfEvenValues([5,1,7,3]) == 0
   #one even value
   assert sumOfEvenValues([5,2,7,3]) == 2
   #more even values
   assert sumOfEvenValues([5,2,7,4,6,3])==12
   #all values are even
   assert sumOfEvenValues([4,8,2,6]) == 20
testSumOfEvenValues()
```

Examples

```
def changeElement(1, pos, e1):
    change the pos-th element of list to el
   Data: a list l, a position, a new element
   Results: list l' with l[pos] == el
   raise IndexError if pos < 0 or
    pos >= len(l)
    if (pos < 0):
        raise IndexError("pos must be positive")
    else:
        if (pos >= len(1)):
            raise IndexError("position must be
                  smaller to the length of list")
        else: #a valid position
            l[pos] = el
           return 1
```

```
def testChangeElement():
   #black box testing and white box testing
   #negative position
   try:
        changeElement([1,3,9,2], -2, 5)
        assert False
   except IndexError as ex:
        print("some errors: " + str(ex))
   #position > len(1)
   try:
        changeElement([1,3,9,2], 6, 5)
        assert False
   except IndexError as ex:
        print("some errors: " + str(ex))
   #valid data
   assert changeElement([1,3,9,2],2,5)==[1,3,5,2]
testChangeElement()
```

Black box testing	White box testing	
Advantages		
+ Acces to source code is not required	+ Knowing about the code: makes testing it easier	
+ Testing can be reused if implementation changes	+ Can help find hidden defects	
+ Efficient for large code sources	+ Can help optimize code	
+ Separates implementer - tester	+ Easier to obtain high test coverage	
Drawbacks Drawbacks		
- Test coverage might be low	- Problems with code that is completely missing	
- Testing might be inefficient	- Requires access to the code and good knowledge of the code	

Testing Levels

- Tests are frequently grouped
 - By where they are added in the software development process
 - By the level of specificity of the test
- Testing
 - Manual testing
 - Automated testing
 - Writing software to do testing that would otherwise need to be done manually
 - PyUnit Python unit testing framework

Testing Levels

Unit Test

- Verify the functionality of a specific section of code e.g. a function
- Test small parts of the program independently

Integration Test

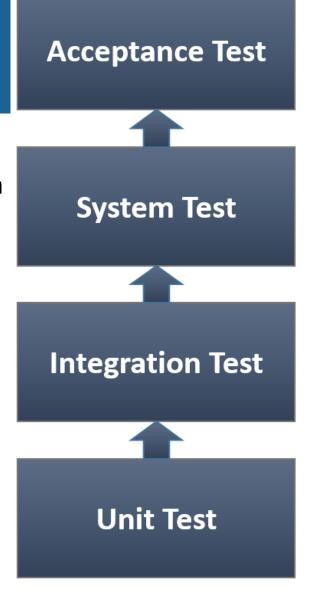
- Test different parts of the system in combination
- Bottom-up approach: based on the results of unit testing

System Test

 Tests how the program works as a whole after all modules have been tested

Acceptance Test

 Check that the system complies with user requirements and is ready for use



Testing in Python

- Automated Testing
 - The process of writing programs to do testing that would otherwise need to be done manually
 - Use of software to control the execution of tests, the comparison of actual outcomes to predicted outcomes, the setting up of test preconditions

unittest

- Python framework for writing Unit Tests, Integration Tests and Acceptance Test
- provides a class TestCase and a main() method
 from unittest import TestCase, main OR import unittest

Testing in Python: unittest

- Test classes in Python
 - Test classes should extend TestCase and contain at least one method starting with test_
 - Test methods contain assertions (assertEqual, assertTrue, etc)

```
from unittest import TestCase, main

class AdditionTests(TestCase):
    def test_add(self):
        self.assertEqual(add(3, 4), 7)
```

- Running the tests
 - unittest.main method looks for all classes derived from TestCase
 - Runs all the tests and reports

```
if __name__ == "__main__":
    main()
```

Methods setUp() and tearDown() can be used to prepare testing and clean up afterwards

Example

```
def isPrime(n):
   Verify if a number is prime
   Return True if n is prime, False otherwise
   Raise ValueError if n <= 0
   if n <= 0:
       raise ValueError("The number needs to be
   if n == 1:
       return False
   if n <= 3:
        return True
   for i in range(2, n):
        if n % i == 0:
           return False
   return True
```

```
import unittest
from utils import isPrime
class IsPrimeBlackBoxTest(unittest.TestCase):
    def setUp(self):
        unittest.TestCase.setUp(self)
    def tearDown(self):
        unittest.TestCase.tearDown(self)
    def test IsPrimeBlackBox(self):
        for i in range(-100, 1):
            try:
                isPrime(i)
                assert False
            except ValueError:
                assert True
        primes = [2, 3, 5, 7, 11, 13, 17, 19]
        for i in range(2, 20):
            self.assertTrue(isPrime(i) == (i in primes),
"The value where it fails: " + str(i))
if __name__ == "__main__":
    unittest.main()
```

Example

```
def isPrime(n):
    """"
    Verify if a number is prime
    Return True if n is prime, False otherwise
    Raise ValueError if n <= 0
    """
    if n <= 0:
        raise ValueError("The number needs to be positived:</pre>
```

```
Console 
Pu PyUnit

<terminated> test_cami.py [unittest] [C:\Program Files (x86)\Python36-32\python.exe]

Finding files... done.

Importing test modules ... done.

Ran 2 tests in 0.002s

OK
```

```
import unittest
from utils import isPrime
class IsPrimeWhiteBoxTest(unittest.TestCase):
    def setUp(self):
        unittest.TestCase.setUp(self)
    def tearDown(self):
        unittest.TestCase.tearDown(self)
    def test IsPrimeWhiteBox(self):
        try:
            isPrime(-5)
            assert False
        except ValueError:
            assert True
        self.assertFalse(isPrime(1))
        self.assertTrue(isPrime(2))
        self.assertTrue(isPrime(3), 3)
        self.assertFalse(isPrime(6), 6)
        self.assertTrue(isPrime(7), 7)
        self.assertFalse(isPrime(8), 8)
<u> т name == " main ":</u>
    unittest.main()
```

Assert methods in unittest.TestCase

Method	Checks that
assertEqual(a, b)	a == b
assertNotEqual(a, b)	a != b
assertTrue(x)	bool(x) is True
assertFalse(x)	bool(x) is False
assertIs(a, b)	a is b
assertIsNot(a, b)	a is not b
assertIsNone(x)	x is None
assertIsNotNone(x)	x is not None
assertIn(a, b)	a in b
assertNotIn(a, b)	a not in b

Method	Checks that
assertAlmostEqual(a, b)	round(a-b, 7) == 0
assertNotAlmostEqual(a, b)	round(a-b, 7) != 0
assertGreater(a, b)	a > b
assertGreaterEqual(a, b)	a >= b
assertLess(a, b)	a < b
assertLessEqual(a, b)	a <= b

https://docs.python.org/3/library/unittest.html

Example

domain.Person

```
class Person(object):
   def __init__(self, name, age):
       self.__name = name
       self. age = age
   def str (self):
       return self.__name + " , " + str(sel
   def getName(self):
       return self. name
   def setName(self, name):
       self. name = name
   def getAge(self):
       return self. age
   def setAge(self, age):
       self. age = age
   def incrementAge(self):
       self. age += 1
```

test.PersonTest

```
import unittest
from domain.Person import Person

class PersonTest(unittest.TestCase):

    def setUp(self):
        self.person = Person("Simpson", 8)

    def test_IncrementAge(self):
        self.person.setAge(9)
        self.person.incrementAge()
        self.assertEqual(self.person.getAge(), 10)

if __name__ == "__main__":
    unittest.main()
```

Debugging

When testing indicates the presence of errors -> debugging

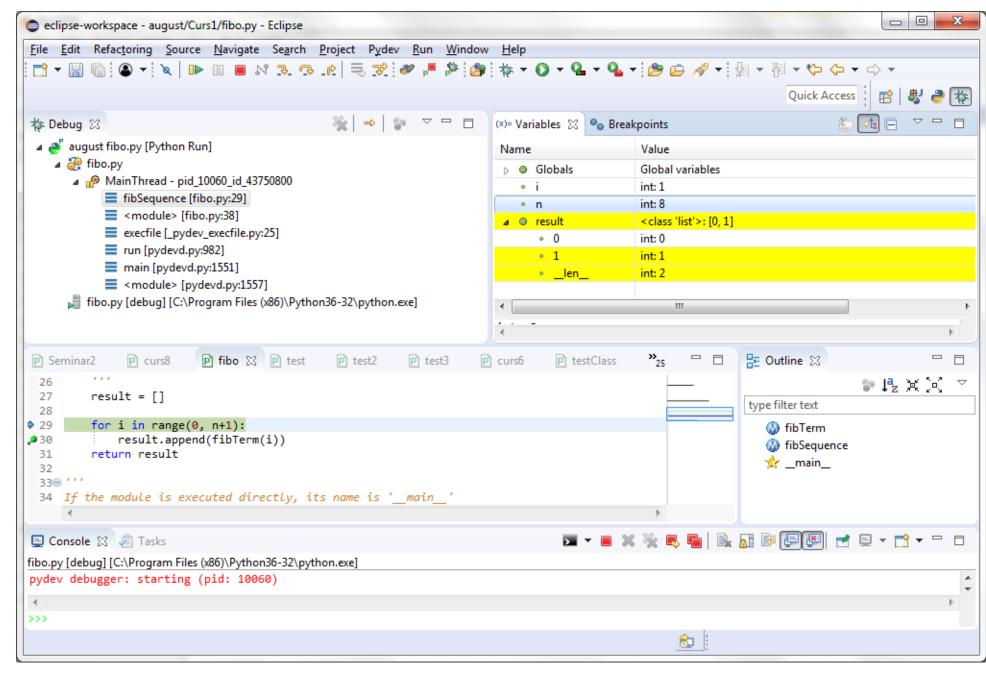
- Debugging the code
 - Identify why a program is not working as expected
 - Study the events that generate an error
 - Use print!

Rewrite the program with the purpose of eliminating the errors

Debugging in Eclipse

- Debug view
 - View the current execution trace (stack trace)
 - Execute step by step, resume/pause execution

- Variables view
 - View variable values



Coding style

- Readability
 - The main attribute of style
 - A good programmer writes code that humans can understand
- Coding style
 - Comments
 - Text formatting (indentation, white spaces)
 - Specification
 - Good names for entities (classes, functions, variables) of the program
 - Meaningful names
 - Use naming conventions

Recap: Design principles (see Lecture 4)

- Managing dependency:
 - Single Responsability
 - Separation of Concerns
 - Low Coupling
 - High Cohesion
- Create software:
 - Easy to understand, modify, maintain, test
 - Classes data abstraction, encapsulate, hide implementation
 - Easy to test, easy to reuse
- Example: create an application to manage students
 - CRUD operations Create Read Update Delete
 - Features Create student, List students, Find a student, Delete a student

Recap: Layered Architecture (see Lecture 4)

- Layered architecture
 - Low coupling between modules
 - Modules do not need to know details about other modules
 - High cohesion of each module
 - The elements of a module should be highly related
- Layers:
 - User Interface Layer (presentation layer)
 - Application Layer (service layer or controller layer)
 - Infrastructure Layer (data access, other persistence)
 - Domain Layer (business logic layer)
- Coordinator

GRASP

- General Responsibility Assignment Software Patterns (or Principles)
 - Guidelines for assigning responsibility to classes and objects
 - High Cohesion
 - Low Coupling
 - Information Expert
 - Creator
 - Pure Fabrication
 - Controller

GRASP: High cohesion, Low coupling

High cohesion

- The responsibilities of a given element are strongly related and highly focused
- To increase cohesion: break programs into classes and subsystems
- Low cohesion means that an element has too many unrelated responsibilities => problems: hard to understand, hard to reuse, hard to maintain

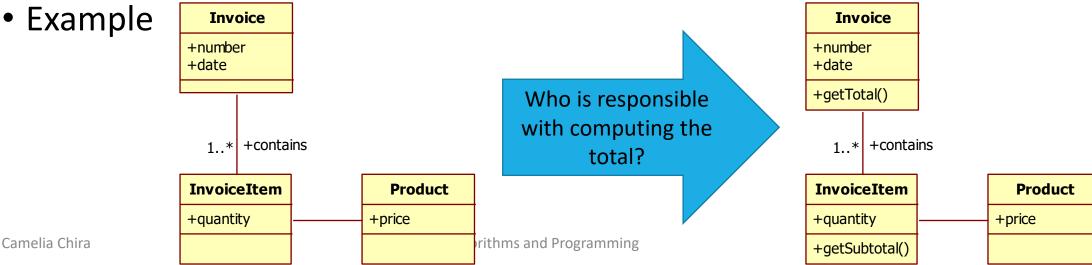
Low coupling

- Low dependency between classes
- Low impact in a class of changes in other classes
- High reuse potential
- Examples
 - Class A has an attribute that is an instance of class B
 - Class A has a method that references an instance of class B in any form

GRASP: Information Expert

- Assign a responsibility to the class that has the information necessary to fulfill the responsibility
- The principle of Information Expert:
 - Look at a given responsibility (e.g. method), determine the information needed to fulfill it, and then determine where that information is stored
 - Place the responsibility on the class with the most information required





GRASP: Creator

- Which class is responsible for creating objects?
- Creator pattern: responsible for creating an object of the class
 - Class B should be responsible for creating instances of class A if:
 - Instances of B contain instances of A
 - Instances of B closely use instances of A
 - Instances of B have the initializing information for instances of A and can use it for creation

Example

- Task 1: Create student
- Task 2: Store student (Repository)
- Task 3: Add student (Controller)
- Task 4: Create UI

Task 1: Create student

```
import unittest
from domain.Student import Student
class StudentTest(unittest.TestCase):
    def test_create(self):
        Testing Student creation
        st = Student("Zara", 21, 10)
        self.assertEqual(st.getName(), "Zara")
        self.assertEqual(st.getAge(), 21)
        self.assertEqual(st.getGrade(), 10)
if __name__ == "__main__":
    unittest.main()
```

```
class Student(object):
   def __init__(self, name, age, grade):
       self. name = name
       self.__age = age
       self. grade = grade
    def __str__(self):
        return self.__name + " " + str(self.__grade)
    def getName(self):
        return self. name
    def setName(self, name):
       self. name = name
    def getAge(self):
       return self.__age
    def setAge(self, age):
       self. age = age
    def getGrade(self):
       return self. grade
   def setGrade(self, grade):
       self. grade = grade
```

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GRASP: Pure Fabrication

- Pure Fabrication a class added to an application in order to achieve low coupling, high cohesion and reuse
- When an expert violates high cohesion and low coupling => assign a highly cohesive set of responsibilities to an artificial class that does not represent a concept in the problem domain
- Example
 - Task 2: Store student (in memory, file or database)
 - Expert pattern Student is the "expert" to perform this operation => low cohesion, poor reuse
 - Solution: Pure Fabrication

Task 2: Store student (Create Repository)

- Solution Pure Fabrication
 - Create a class with the responsibility to store students (StudentRepository)
 - Student class easy to reuse, high cohesion, low coupling
 - Repository will manage a list of students (persistent storage)

StudentRepository

+store(s: Student) +update(s: Student) +find(id: int): Student +delete(s: Student)

Repository

- Represents all objects of a certain type as a conceptual set
- Objects can be added, updated, removed and retrieved from the repository (persistent storage)

Task 2: Store student (Create Repository)

```
def test storeStudent():
   repo = StudentRepository()
   assert repo.size() == 0
   s1 = Student(1, "Zara", 10)
   repo.store(s1)
   assert repo.size() == 1
   s2 = Student(2, "Erin", 10)
   repo.store(s2)
   assert repo.size() == 2
   s3 = Student(2, "Carla", 10)
   try:
        repo.store(s3)
        assert False
   except:
        assert True
```

```
class StudentRepository(object):
   def __init__(self):
       Manage a list of Student objects
       self. students = {}
   def store(self, student):
       Stores a student.
       Input: student is of type Student
       Raises an exception if the repository already
       contains a student with the same id.
        if student.getId() in self. students:
           raise ValueError("A student with id " +
str(student.getId()) + " already exists.")
       self. students[student.getId()] = student
   def size(self):
        return len(self. students)
```

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GRASP: Controller

- Controller: the first object beyond the UI layer that receives and coordinates ("controls") a system operation
 - Delegates to other objects the work that needs to be done
 - Coordinates or controls the activity
 - It does not do much work itself
- Controller encapsulate knowledge about the current state of a use case presentation layer decoupled from problem domain
- Example
 - Task 3: Add student
 - Create controller

Task 3: Add student (create controller)

```
def testCreateStudent():
    repo = StudentRepository()

    ctrl = StudentController(repo)

    s = ctrl.createStudent(1, "Zara", 10)
    assert s.getId() == 1
    assert s.getName() == "Zara"

    try:
        s = ctrl.createStudent(1, "Erin", 10)
        assert False
    except:
        assert True
```

```
class StudentController():
   Controller for CRUD operations on Student list.
   def init (self, repo):
       self. repo = repo
   def createStudent(self, i, name, grade):
       Creates a student and stores it in the repository.
       Input: the id of student as int, name of student as
       string, age and grade of student as ints
       Returns a student.
       Raises ValueError if id of student already exists.
        s = Student(i, name, grade)
        self. repo.store(s)
   def addStudent(self, s):
       self. repo.store(s)
```

Task 4: Create UI

```
class StudentUI(object):
   def __init__(self, controller):
         self.__controller = controller
   @staticmethod
   def printMenu():
   def mainMenu(self):
        while True:
            try:
                StudentUI.printMenu()
                command = input("Enter command: ").strip()
                if command == "\theta":
                    print("exit...")
                    return
                elif command == "1":
                    s = StudentUI.readStudent()
                    self.__controller.addStudent(s)
                else:
                    print("Invalid command!")
            except Exception as e:
                print("Error encountered : " + str(e))
```

Coordinator: App start

```
from infrastructure.studentRepo import StudentRepository
from application.studentController import StudentController
from ui.console import StudentUI
from domain.Student import Student
def start():
    #create repository
    repo = StudentRepository()
    repo.store(Student(1, "Erin", 10))
    repo.store(Student(2, "Zara", 10))
    #create controller, provide repository
    controller = StudentController(repo)
    # create UI, provide controller
    ui = StudentUI(controller)
    ui.mainMenu()
```

Acronym for "Numerical Python"

Useful to perform mathematical and logical operations on arrays

- Library
 - Multidimensional arrays and matrices
 - Collection of routines for processing arrays

SciPy (Scientific Python) extends NumPy

Has to be installed

http://www.numpy.org

- Free Python distributions with SciPy for Windows
 - Anaconda, Canopy, Python(x,y)
- Installing via pip (Python's standard package manager)
 - Need to have Python and pip already installed

python install numpy

```
Microsoft Windows [Version 6.1.7601]
Copyright (c) 2009 Microsoft Corporation. All rights reserved.

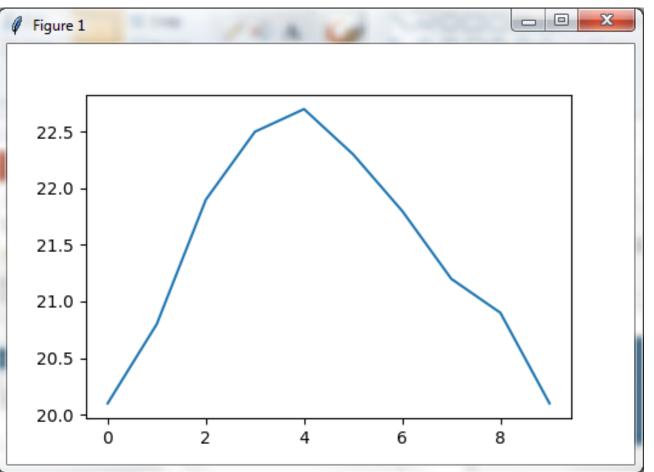
C:\Users\cami>python -m pip install --user matplotlib ipython jupyter pandas sympy nose
Collecting matplotlib
Downloading matplotlib-2.1.0-cp36-cp36m-win32.whl (8.5MB)
99% | 8.5MB 1.3MB/s eta 0:00:01
```

import numpy import numpy as np

```
Python 3.6.2 Shell
File Edit Shell Debug Options Window Help
>>> import numpy as np
>>> cvalues = [20.1, 20.8, 21.9, 22.5, 22.7]
>>> C = np.array(cvalues)
>>> C
array([ 20.1, 20.8, 21.9, 22.5, 22.7])
>>> print(C)
[ 20.1 20.8 21.9 22.5 22.7]
>>> print(C * 9 / 5 + 32)
[ 68.18 69.44 71.42 72.5 72.86]
>>> print(C)
[ 20.1 20.8 21.9 22.5 22.7]
>>> type(C)
<class 'numpy.ndarray'>
>>>
                                                                   Ln: 16 Col: 4
```

```
>>> import numpy as np
>>> a = np.arange(20).reshape(4,5)
>>> print(a)
 [10 11 12 13 14]
 [15 16 17 18 19]]
>>> a.shape
(4, 5)
>>> a.shape[1]
>>> a.ndim
>>> a.size
20
```

```
>>> import numpy as np
>>> cvalues = [20.1, 20.8, 21.9, 22
>>> C = np.array(cvalues)
>>> import matplotlib.pyplot as plt
>>> plt.plot(C)
[<matplotlib.lines.Line2D object at
>>> plt.show()
```



NumPy: Array creation

```
>>> a = np.array([1,2,3])
>>> print(a)
[1 2 3]
```

```
a = np.array(1,2,3,4) # WRONG
a = np.array([1,2,3,4]) # RIGHT
```

```
>>> b=np.array([[1,2,3],[4,5,6]])
>>> print(b)
[[1 2 3]
[4 5 6]]
```

```
>>> np.random.random(5)
array([ 0.13501571,  0.84082373,  0.9451692 ,  0.0359
4509,  0.96148578])
```

```
0 0
Python 3.6.2 Shell
 File Edit Shell Debug Options Window Help
>>> np.zeros(3)
array([ 0., 0., 0.])
>>> np.zeros((3,4))
array([[ 0., 0., 0., 0.],
       [ 0., 0., 0., 0.],
       [ 0., 0., 0., 0.]])
>>> np.ones(10)
array([ 1., 1., 1., 1., 1., 1., 1., 1., 1.])
>>> np.ones((2,2), dtype=np.int16)
array([[1, 1],
       [1, 1]], dtype=int16)
>>> c=np.ones((2,2), dtype=np.int16)
>>> print(c)
[[1 1]
 [1 1]]
>>> np.arange(10, 50, 5)
array([10, 15, 20, 25, 30, 35, 40, 45])
>>> np.arange(10)
array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
>>> x=np.arange(5)
>>> print(x)
 [0 1 2 3 4]
>>> y=np.arange(12).reshape(3,4)
>>> print(v)
 [[0 1 2 3]
 [4 5 6 7]
 [8 9 10 11]]
                                                   Ln: 164 Col: 4
```

NumPy: Basic operations

```
>>> a=np.arange(10)**2
>>> print(a)
[ 0 1 4 9 16 25 36 49 64 81]
>>> a[1]
>>> a[9]
81
>>> a[10]
Traceback (most recent call last):
 File "<pyshell#103>", line 1, in <module>
   a[10]
IndexError: index 10 is out of bounds for axis 0 with
size 10
>>> a[2:5]
array([ 4, 9, 16], dtype=int32)
>>> a[:2]
array([0, 1], dtype=int32)
>>> for el in a:
        print(el)
```

NumPy: Basic operations

```
>>> a = np.array([10,20,30])
>>> b = np.arange(3)
>>> b
array([0, 1, 2])
>>> c=a+b
>>> C
array([10, 21, 32])
>>> a-b
array([10, 19, 28])
>>> b**2
array([0, 1, 4], dtype=int32)
>>> np.sin(a)
array([-0.54402111, 0.91294525, -0.98803162])
>>> a<20
array([ True, False, False], dtype=bool)
>>>
```

Elementwise product

```
>>> a*b
array([ 0, 20, 60])
```

Array product

```
>>> a.dot(b)
80
>>> np.dot(a,b)
80
```

NumPy: Basic operations

```
>>> b += 1
>>> b
array([1, 2, 3])
>>> b *= 2
>>> b
array([2, 4, 6])
>>> a
array([10, 20, 30])
>>> a.sum()
60
>>> a.min()
10
>>> a.max()
30
```

```
>>> b = np.arange(12).reshape(3,4)
>>> print(b)
 [8 9 10 11]]
>>> b.sum()
66
>>> b.sum(axis=0)
array([12, 15, 18, 21])
>>> b.sum(axis=1)
array([ 6, 22, 38])
>>> b.min()
>>> b.min(axis=0)
array([0, 1, 2, 3])
>>> b.min(axis=1)
array([0, 4, 8])
```

Recap today

- Testing
 - Concept
 - Testing data
 - Examples
 - Testing in Python: unittest
- Organize a software application
 - Layers
 - GRASP patterns
 - Examples

Next time

Recursivity