

# Package ‘mFLICA’

January 20, 2020

**Title** Leadership-Inference Framework for Multivariate Time Series: mFLICA

**Version** 0.1.0

**Description** A leadership-inference framework for multivariate time series. The framework uses a notion of a leader as an individual who initiates collective patterns that everyone in a group follows. Given a set of time series of individual activities, our goal is to identify periods of coordinated activity, find factions of coordination if more than one exist, as well as identify leaders of each faction. For each time step, the framework infers following relations between individual time series, then identifying a leader of each faction whom many individuals follow but it follows noone. A faction is defined as a group of individuals that everyone follows the same leader. mFLICA reports following relations, leaders of factions, and members of each faction for each time step. Please see Chainarong Amornbunchornvej and Tanya Berger-Wolf (2018) <doi:10.1137/1.9781611975321.62> when referring to this package in publications.

**License** GPL-3

**URL** <https://github.com/DarkEyes/mFLICA>

**BugReports** <https://github.com/DarkEyes/mFLICA/issues>

**Language** en-US

**Encoding** UTF-8

**LazyData** true

**Depends** R (>= 3.5.0),  
dtw

**Imports** ggplot2 (>= 3.0)

**Suggests** knitr, rmarkdown

**VignetteBuilder** knitr

**RoxygenNote** 7.0.2

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followingNetwork	<i>followingNetwork function</i>
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## Description

followingNetwork is a support function for calculating a following network of a set of time series

## Usage

```
followingNetwork(TS, timeLagWindow, lagWindow = 0.1, sigma = 0.1)
```

## Arguments

TS	is a set of time series where $TS[i, t, d]$ is a numeric value of $i$ th time series at time $t$ and dimension $d$ .
timeLagWindow	is a maximum possible time delay in the term of time steps.
lagWindow	is a maximum possible time delay in the term of percentage of time length of TS.
sigma	is a threshold of following relation. It is used to discretize an adjacency matrix adjWeightedMat to be a binary matrix adjBinMat.

## Value

This function returns adjacency matrices of a following network of TS.

adjWeightedMat	An adjacency matrix of a following network s.t. if $adjWeightedMat[i, j] > 0$ , then $TS[i, , ]$ follows $TS[j, , ]$ with a degree $adjWeightedMat[i, j]$ .
adjBinMat	A binary version of adjWeightedMat s.t. $adjBinMat[i, j] <- (adjWeightedMat[i, j] \geq sigma)$ for any $i, j$ .

## Examples

```
# Run the function

out<-followingNetwork(TS=mFLICA::TS[,60:90,],sigma=0.5)
```

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followingRelation	<i>followingRelation</i>
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## Description

followingRelation is a function that infers whether Y follows X.

## Usage

```
followingRelation(Y, X, timeLagWindow, lagWindow = 0.1)
```

## Arguments

Y	is a T-by-D matrix of numerical time series of a follower
X	is a T-by-D matrix numerical time series of a leader
timeLagWindow	is a maximum possible time delay in the term of time steps.
lagWindow	is a maximum possible time delay in the term of percentage of length(X). If timeLagWindow is missing, then timeLagWindow=ceiling(lagWindow*length(X)). The default is 0.2.

## Value

This function returns a list of following relation variables below.

fol1Val	is a following-relation value s.t. if fol1Val is positive, then Y follows X. If fol1Val is negative, then X follows Y. Otherwise, if fol1Val is zero, there is no following relation between X, Y.
dtwIndexVec	is a numeric vector of index-warping difference: dtwIndexVec[k] = dtwOut\$index1[k] - dtwOut\$index2[k] where dtwOut is the output from dtw::dtw(x=Y,y=X) function.

## Examples

```
# Load example data

leader<- mFLICA::TS[1,1:200,]
follower<- mFLICA::TS[2,1:200,]

# Run the function

out<-followingRelation(Y=follower,X=leader)
```

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getADJNetDen	<i>getADJNetDen function</i>
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### Description

getADJNetDen is a support function for calculating a network density of a network.

### Usage

```
getADJNetDen(adjMat)
```

### Arguments

adjMat is an adjacency matrix of a dominant-distribution network.

### Value

This function returns a value of network density of of a network for a given adjMat.

### Examples

```
# Given an example of adjacency matrix
A<-matrix(FALSE,5,5)
A[2,1]<-TRUE
A[c(3,4),2]<-TRUE

# Get a network density of an adjacency matrix

getADJNetDen(adjMat=A)
```

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getDynamicFollNet	<i>getDynamicFollNet function</i>
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### Description

getDynamicFollNet is a support function for calculating a dynamic following network of a set of time series

### Usage

```
getDynamicFollNet(TS, timeWindow, timeShift, sigma = 0.5, silentFlag = FALSE)
```

**Arguments**

TS	is a set of time series where $TS[i, t, d]$ is a numeric value of $i$ th time series at time $t$ and dimension $d$ .
timeWindow	is a time window parameter that limits a length of each sliding window. The default is 10 percent of time series length.
timeShift	is a number of time steps a sliding window shifts from a previous window to the next one. The default is 10 percent of timeWindow.
sigma	is a threshold of following relation. The default is 0.5.
silentFlag	is a flag that prohibit the function to print the current status of process.

**Value**

This function returns adjacency matrices of a dynamic following network of TS as well as the corresponding time series of network densities.

dyNetWeightedMat	An adjacency matrix of a dynamic following network s.t. if $dyNetWeightedMat[i, j, t] > 0$ , then $TS[i, , ]$ follows $TS[j, , ]$ at time $t$ with a degree $dyNetWeightedMat[i, j, t]$ .
dyNetBinMat	A binary version of dyNetWeightedMat s.t. $dyNetWeightedMat[i, j, t] < (dyNetWeightedMat[i, j, t] \geq \sigma)$ for any $i, j, t$ .
dyNetWeightedDensityVec	A time series of dynamic network densities of dyNetWeightedMat
dyNetBinDensityVec	A time series of dynamic network densities of dyNetBinDensityVec

**Examples**

```
# Run the function
out<-getDynamicFollNet(TS=mFLICA::TS[,1:10,],timeWindow=5,timeShift = 5,sigma=0.5)
```

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getFactions	<i>getFactions function</i>
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**Description**

getFactions is a support function for inferring faction leaders and their members as well as a faction size ratio of each faction. Leaders are nodes that have zero outgoing degree. Members of leader A's faction are nodes that have some directed path to A in a following network.

**Usage**

```
getFactions(adjMat)
```

**Arguments**

adjMat	is an adjacency matrix of a following network.
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**Value**

This function returns a list of leader IDs, a list of faction members, and network densities of factions.

`leaders` is a list of faction leader IDs

`factionMembers` is a list of members of factions where `factionMembers[[i]]` is a list of faction members of a leader `leaders[i]`'s faction.

`factionSizeRatio` is a vector of faction size ratio of each faction. `factionSizeRatio[i]` is a number of edges within a leader `leaders[i]`'s faction divided by  $N \choose 2$  where  $N$  is a number of all nodes.

**Examples**

```
# Given an example of adjacency matrix
A<-matrix(FALSE,5,5)
A[2,1]<-TRUE
A[c(3,4),2]<-TRUE
A[5,3]<-TRUE
# Get faction leaders and their members as well as a network density of each faction.

out<-getFactions(adjMat=A)
```

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`getFactionSizeRatio`     *getFactionSizeRatio function*

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**Description**

`getFactionSizeRatio` is a support function for calculating a faction size ratio of a given faction. A faction size ratio is a number of edges that connect between faction-member nodes divided by a number of total nodes within a following network.

**Usage**

```
getFactionSizeRatio(adjMat, members)
```

**Arguments**

`adjMat` is an adjacency matrix of a dominant-distribution network.

`members` is a list of member IDs of a given faction.

**Value**

This function returns a faction size ratio of a given faction.

## Examples

```
# Given an example of adjacency matrix
A<-matrix(FALSE,5,5)
A[2,1]<-TRUE
A[c(3,4),2]<-TRUE

# Get a faction size ratio of a given faction

getFactionSizeRatio(adjMat=A,members=c(1,2,3,4))
```

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getReachibleNodes	<i>getReachibleNodes function</i>
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## Description

getReachibleNodes is a support function for inferring reachable nodes that have some directed path to a node targetNode.

## Usage

```
getReachibleNodes(adjMat, targetNode)
```

## Arguments

adjMat	is an adjacency matrix of a following network of which its elements are binary: zero for no edge, and one for having an edge.
targetNode	is a node in a graph that we want to find a set of nodes that can reach this target node via some paths.

## Value

This function returns a set of node IDs followers that have some directed path to a node targetNode.

## Examples

```
# Given an example of adjacency matrix
A<-matrix(FALSE,5,5)
A[2,1]<-TRUE
A[c(3,4),2]<-TRUE
A[5,3]<-TRUE
# Get a set of reachable nodes of targetNode.

followers<-getReachibleNodes(adjMat=A,targetNode=1)$followers
```

## Description

A leadership-inference framework for multivariate time series. The framework uses a notion of a leader as an individual who initiates collective patterns that everyone in a group follows. Given a set of time series of individual activities, our goal is to identify periods of coordinated activity, find factions of coordination if more than one exist, as well as identify leaders of each faction. For each time step, the framework infers following relations between individual time series, then identifying a leader of each faction whom many individuals follow but it follows noone. A faction is defined as a group of individuals that everyone follows the same leader. mFLICA reports following relations, leaders of factions, and members of each faction for each time step. Please see Chainarong Amornbunchornvej and Tanya Berger-Wolf (2018) <doi:10.1137/1.9781611975321.62> when referring to this package in publications.

## Usage

```
mFLICA(TS, timeWindow, timeShift, sigma = 0.5, silentFlag = FALSE)
```

## Arguments

TS	is a set of time series where $TS[i, t, d]$ is a numeric value of $i$ th time series at time $t$ and dimension $d$ .
timeWindow	is a time window parameter that limits a length of each sliding window. The default is 10 percent of time series length.
timeShift	is a number of time steps a sliding window shifts from a previous window to the next one. The default is 10 percent of timeWindow.
sigma	is a threshold of following relation. The default is 0.5. Note that if sigma is not one, an individual might be a member of mutiple factions.
silentFlag	is a flag that prohibit the function to print the current status of process.

## Value

This function returns dynamic following networks, as well as leaders of factions, and members of each faction for each time step.

dyNetOut\$dyNetWeightedMat

An adjacency matrix of a dynamic following network s.t. if  $dyNetWeightedMat[i, j, t] > 0$ , then  $TS[i, , ]$  follows  $TS[j, , ]$  at time  $t$  with a degree  $dyNetWeightedMat[i, j, t]$ .

dyNetOut\$dyNetBinMat

A binary version of  $dyNetWeightedMat$  s.t.  $dyNetWeightedMat[i, j, t] <-(dyNetWeightedMat[i, j, t] >= sigma)$  for any  $i, j, t$ .

dyNetOut\$dyNetWeightedDensityVec

A time series of dynamic network densities of  $dyNetWeightedMat$

dyNetOut\$dyNetBinDensityVec

A time series of dynamic network densities of  $dyNetBinDensityVec$

leadersTimeSeries

A time series of leaders of each faction where  $leadersTimeSeries[[t]]$  is a set of leaders at time  $t$ . A number of factions is the same as a number of leaders.



**factionMembersTimeSeries**

A time series of sets of faction members where `factionMembersTimeSeries[[t]][[k]]` is a set of faction-members at time `t` leading by a leader `leadersTimeSeries[[t]][k]`.

**factionSizeRatioTimeSeries**

A time series of faction-size ratios of all individuals. A faction size ratio is a number of edges that connect between faction-member nodes divided by a number of total nodes within a following network. If a leader has a higher faction-size ratio, then it has more followers than a leader with a lower faction-size ratio. A faction-size ratio has a value between 0 and 1.

**Author(s)**

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**Examples**

```
# Run the function

obj1<-mFLICA(TS=mFLICA::TS[,60:90,],timeWindow=10,timeShift=10,sigma=0.5)

# Plot time series of faction size ratios of all leaders

plotMultipleTimeSeries(TS=obj1$factionSizeRatioTimeSeries, strTitle="Faction Size Ratios")
```

---

plotMultipleTimeSeries

*plotMultipleTimeSeries*

---

**Description**

plotMultipleTimeSeries is a function for visualizing time series

**Usage**

```
plotMultipleTimeSeries(TS, strTitle = "Time Series Plot", TSnames)
```

**Arguments**

TS	is a set of time series where <code>TS[i, t, d]</code> is a numeric value of <code>i</code> th time series at time <code>t</code> and dimension <code>d</code> .
strTitle	is a string of the plot title
TSnames	is a list of legend of X, Y where <code>TSnames[1]</code> is a legend of X and <code>TSnames[2]</code> is a legend of Y.

**Value**

This function returns an object of ggplot class.

Examples

```
# Run the function
plotMultipleTimeSeries(TS=mFLICA::TS[1:5,1:60,1])
```

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TS	<i>A simulation time series of movement coordination of 30 individuals</i>
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Description

A dataset containing simulated trajectories of 30 individuals moving to form coordination in x-y coordinates. In the interval [1,200], ID1 leads the group and everyone follows. ID2 leads the group during the interval [201,400]. Lastly, ID3 leads the group during the interval [401,600]. The interval [601,800] is the time when everyone trying to stop moving.

Usage

TS

Format

An array with 30 rows of individuals, 800 columns of time steps, and 2 dimensions of coordinate (x,y):

**TS** It is a set of time series where  $TS[i, t, d]$  is a numeric value of  $i$ th time series at time  $t$  and dimension  $d$ . ...

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