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Unit 3: Syntax Directed Definitions

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Lecture Overview



In this lecture, you will learn about -

- Dependency graphs
- Topological Sort
- Evaluating SDDs Example Simple Desk Calculator
- S-Attributed SDD Examples :
 - Counting Binary bits
 - Binary to Decimal conversion
 - Counting parentheses
 - Identifying the type of an expression int or float
 - Identifying the sign of the evaluated expression positive or negative

Recap - Evaluating SDDs - Parse tree method



Evaluating an SDD over a given input consists of the following steps -

- 1. Construct Parse Tree for given input.
- 2. Construct Dependency graph.
- 3. Topologically sort the nodes of Dependency graph.
- 4. Produce as output Annotated Parse Tree.

Dependency Graphs



- Dependency Graphs are the syntax directed definitions attributes.
 Dependency Graphs are the most general technique used to evaluate with both synthesized and inherited
- A Dependency Graph shows the interdependencies among the attributes of the various nodes of a parse tree.
 - There is a node for each attribute.
 - If attribute b depends on an attribute c there is a link from the node for c to the node for b ($b \leftarrow c$).
- Dependency Rule If an attribute b depends from an attribute c, then we need to fire the semantic rule for c first and then the semantic rule for b.

Dependency Graphs - Example



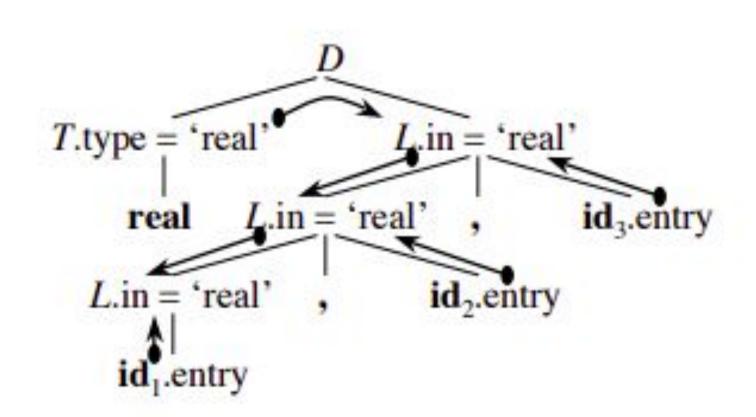
- Consider the earlier example of Syntax
 Directed Definition for Type
 Declarations.
- This SDD has both inherited and synthesised attributes.
- Construct the Annotated parse tree with dependency graph for the input real id1, id2, id3

Production	Semantic Rule
$D \rightarrow TL$	{ L.in = T.type;}
$T \rightarrow int$	{ T.type = integer; }
T → real	{ T.type = float; }
$L \rightarrow L_1$, id	{ L ₁ .in= L.in; addType(id.entry, L.in); }
L → id	{ addType(id.entry, L.in); }

Dependency Graphs - Example



• The figure illustrates the annotated parse tree with the dependencies between attributes.



Compiler Design Topological Sort

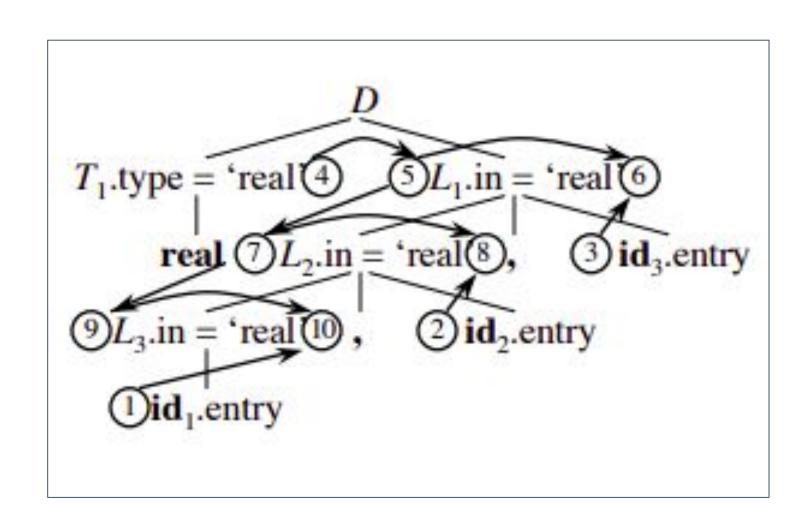


- The evaluation order of semantic rules depends from a Topological Sort derived from the dependency graph.
- Topological Sort Any ordering m_1, m_2, \ldots, m_k such that if $m_i \to m_j$ is a link in the dependency graph then $m_i < m_i$.
- Any topological sort of a dependency graph gives a valid order to evaluate the semantic rules.

Topological Sort - Example



- Consider the previous example of SDD for Type declarations
- The topological sort of the parse tree is as follows -
 - 1. Get id1.entry
 - 2. Get id2.entry
 - 3. Get id3.entry
 - 4. T₁.type='real'
 - 5. L_1 .in= T_1 .type
 - 6. addtype(id3.entry, L₁.in)
 - 7. L_2 .in= L_1 .in
 - 8. addtype(id2.entry, L₂.in)
 - 9. L_3 .in= L_2 .in
 - 10. addtype(id1.entry, L₃.in)



Evaluating SDDs - General Remarks



- Attributes can be evaluated by building a dependency graph at compile-time and then finding a topological sort.
- Disadvantages
 - 1. This method fails if the dependency graph has a cycle We need a test for non-circularity.
 - 2. This method is time consuming due to the construction of the dependency graph.
- Alternative Approach
 - Obesign the syntax directed definition in such a way that attributes can be evaluated with a fixed order avoiding the need to build the dependency graph for example, Sattributed definitions.
 - This method is followed by many compilers.

Evaluating S-Attributed Definitions



- Synthesized Attributes can be evaluated by a **bottom-up parser** as the input is being analyzed avoiding the construction of a dependency graph.
- The parser keeps the values of the synthesized attributes in its stack.
- Whenever a reduction $A \to \alpha$ is made, the attribute for A is computed from the attributes of α which appear on the stack.
- Thus, a translator for an S-Attributed Definition can be simply implemented by extending the stack of an LR-Parser.

Example - Evaluating SDD to implement a Simple Desk Calculator



Evaluate the following SDD for the input 3 + 4 * 5

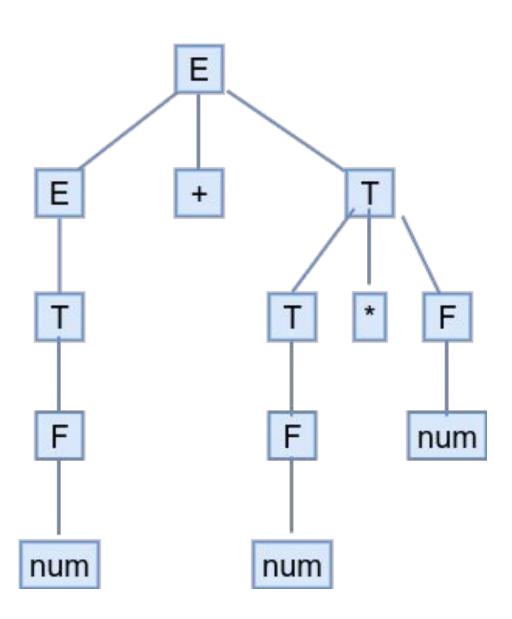
Production	Semantic Rule
$E \rightarrow E_1 + T$	$\{ E.val = E_1.val + T.val \}$
E → T	{ E.val = T.val }
$T \rightarrow T_1 * F$	{ T.val = T ₁ .val * F.val }
$T \rightarrow F$	{ T.val = F.val }
F → num	{ F.val = num.lexval }

Example - Evaluating SDD to implement a Simple Desk Calculator



Evaluate the following SDD for the input 3 + 4 * 5 Solution -

- 1. Construct Parse tree
 - Nodes are Terminals or Non-Terminals



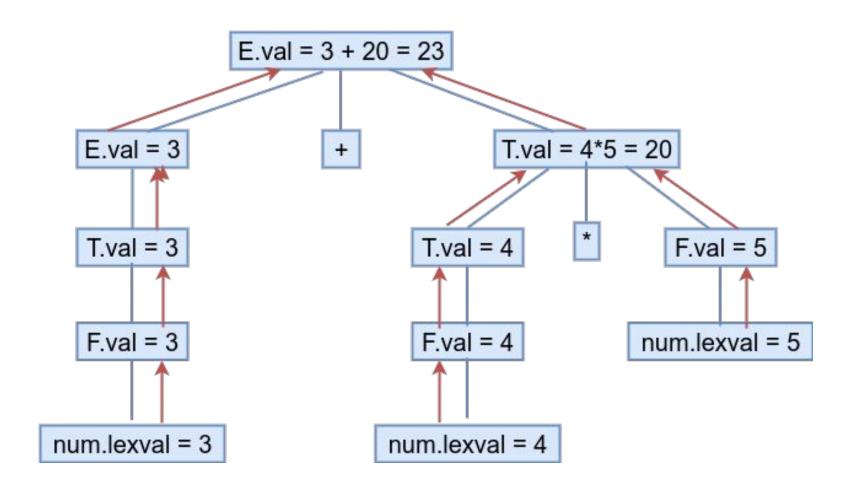
Example - Evaluating SDD to implement a Simple Desk Calculator



Evaluate the following SDD for the input 3 + 4 * 5

Solution -

- 2. Construct dependency graph
 - Nodes are attributes



Example - Evaluating SDD to implement a Simple Desk Calculator



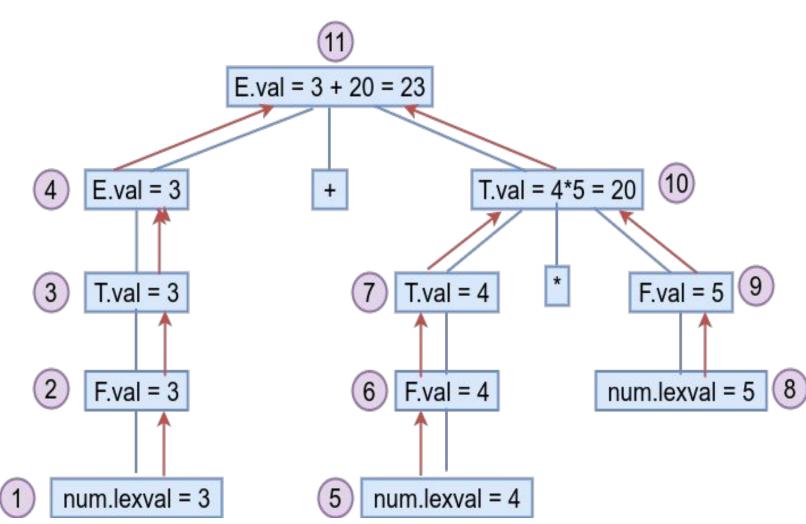
Evaluate the following SDD for the input 3 + 4 * 5

Solution -

3. Decide Evaluation order of the nodes in Dependency graph

1,5,8,2,3,6,7,8,9,4,10,11

Output -Annotated Parse tree carrying out the input.





S-attributed SDDs - Examples

Example 1 - SDD to count no. of 1s in a Binary Number



Production	Semantic Rule
$L \rightarrow L_1 B$	$\{L.count = L_1.count + B.count;\}$
$L \rightarrow B$	{ L.count = B.count; }
B → 0	{ B.count = 0; }
B → 1	{ B.count = 1; }

Example 2 - SDD to count no. of 0s in a Binary Number



Production	Semantic Rule
$L \rightarrow L_1 B$	{ L.count = L ₁ .count + B.count; }
$L \rightarrow B$	{ L.count = B.count; }
$B \rightarrow 0$	{ B.count = 1; }
B → 1	{ B.count = 0; }

Example 3 - SDD to count no. of bits in a Binary Number



Production	Semantic Rule
$L \rightarrow L_1 B$	$\{L.count = L_1.count + B.count;\}$
$L \rightarrow B$	{ L.count = B.count; }
$B \rightarrow 0$	{ B.count = 1; }
B → 1	{ B.count = 1; }

Example 4 - SDD to convert Binary to Decimal



Production	Semantic Rule
$L \rightarrow L_1 B$	$\{L.val = 2 * L1.val + B.val; \}$
$L \rightarrow B$	{ L.val = B.val; }
$B \rightarrow 0$	{ B.val = 0; }
B → 1	{ B.val = 1; }

Example 5 - SDD to convert Binary Fraction to Decimal

Production	Semantic Rule
$S \rightarrow L_1 L_2$	$\{S.val = L_1.val + L_2.val / 2^{L2.count};\}$
$L \rightarrow L_1 B$	$\{L.val = 2 * L_1.val + B.val;$ $L.count = L_1.count + B.count;\}$
L → B	{ L.val = B.val; L.count = B.count; }
B→ 0	{ B.val = 0; B.count = 1; }
B → 1	{ B.val = 1; B.count = 1;}



Example 6 - SDD to count no. of balanced Parentheses



Production	Semantic Rule
$S \rightarrow (S_1)$	$\{ S.count = S_1.count + 1; \}$
$S \rightarrow a$	{ S.count = 0; }

Example 7- SDD to convert infix to postfix



Production	Semantic Rule
$E \rightarrow E_1 + T$	{ printf("+"); }
E → T	
T→ T ₁ * F	{ printf("+"); }
$T \rightarrow F$	
F → num	{ printf("%d",num.lexval); }

Example 8 - SDD to determine type of each Term and Expression



The given grammar is for expressions involving operator + and integer or floating-point operands.

Floating-point numbers are distinguished by having a decimal point.

Write an SDD to determine the type of each term T and expression.

Example 8 - SDD to determine type of each Term and Expression



Production	Semantic Rule
$E \rightarrow E_1 + T$	<pre>{ if(E₁.type == float T.type == float) { E.type = float; } else { E.type = integer; } }</pre>
E o T	{ E.type = T.type }
T → num.num	{ T.type = float ; }
T → num	{ T.type = integer; }

Example 9 - SDD to Identify the sign of the evaluated expression



- Given an attribute grammar G for arithmetic expressions using multiplication, unary -, and unary +.
- Complete the SDD -
 - Add semantic actions to compute an attribute E.sign for non-terminal E to record whether the arithmetic value of E is positive or negative.
 - The attribute sign can have two values, either POS or NEG.
- Also, show the parse tree for input 2 * 3

Production	Semantic Rule
S → E	{ if(E.sign == POS) print("Result is positive"); else print("Result is negative"); }
E → num	
$E \rightarrow + E_1$	
$E o extbf{-} E_{1}$	
$E \rightarrow E_1^* E_2$	

Example 9 - SDD to Identify the sign of the evaluated expression

Production	Semantic Rule
S → E	{ if(E.sign == POS) print("Result is positive"); else print("Result is negative"); }
E → num	{ E.sign == POS; }
$E \rightarrow + E_1$	$\{E.sign = E_1.sign\}$
$E \rightarrow - E_1$	{ if (E.sign == POS) E.sign = NEG; else E.sign = POS; }
$E \rightarrow E_1^* E_2$	{ if (E ₁ .sign == E ₂ .sign

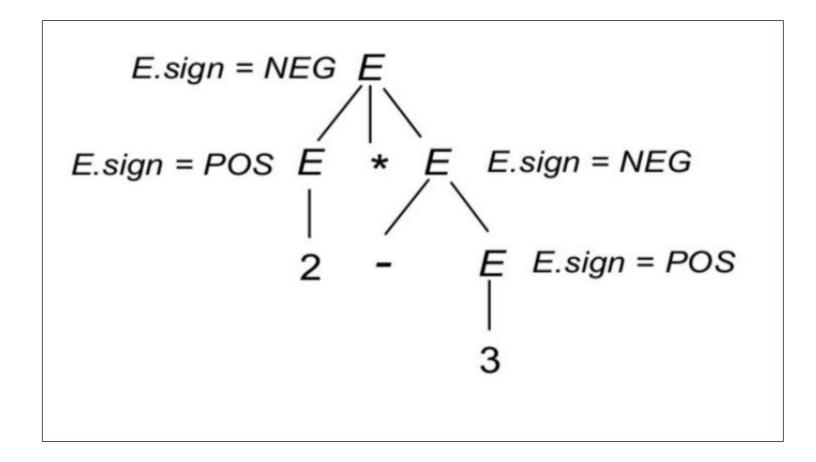


Example 9 - SDD to Identify the sign of the evaluated expression (cont.)



Show the parse tree for input 2 * - 3 (where 2 and 3 are "unsigned_ints"). Indicate at each node what the values of associated attributes are.

Solution -





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Unit 3: L-Attributed SDD

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Lecture Overview



In this lecture, you will learn about -

- What is an L-attributed SDD?
- L-Attributed SDD Examples
 - Simple Type declaration
 - Array type Variable Declaration
 - Variable declaration verification
 - Desk calculator

Recap



- Syntax Directed Definitions (SDD) are a generalization of context-free grammars in which -
 - Grammar symbols have an associated set of attributes
 - Productions are associated with Semantic Rules for computing the values of attributes.
- Two kinds of attributes
 - Synthesized Attributes computed from the values of the attributes of the children nodes.
 - Inherited Attributes computed from the values of the attributes of both the siblings and the parent nodes.
- An SDD with only synthesized attributes is called an S-attributed definition.

Compiler Design What is an L-attributed SDD?



A Syntax Directed Definition is L-attributed if all attributes are either -

- 1. Synthesized
- 2. Extended synthesized attributes, which can depend not only on attributes at the children, but on inherited attributes at the node itself
- 3. Inherited, but depending only on inherited attributes at the parent and any attributes at siblings to the left.

L-attributed SDD



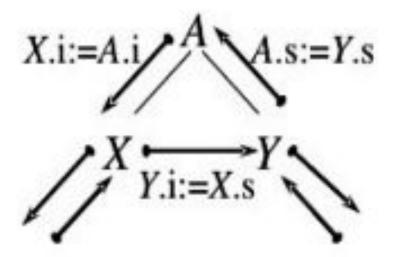
- The formal definition of an L-Attributed SDD is as follows -
 - A syntax directed definition is L-Attributed if each inherited attribute of X_j in a production $A \to X_1 \dots X_n$, depends only on -
 - 1. The attributes of the symbols to the left (this is what L in L-Attributed stands for) of X_j , i.e., $X_1 X_2 \dots X_{j-1}$
 - 2. The inherited attributes of A.
- Theorem Inherited attributes in L-Attributed Definitions can be computed by a PreOrder traversal of the parse-tree.

L-attributed SDD



- L-attributed definitions allow for the natural order of evaluating attributes, i.e, depth first, left to right.
- For example -

$$A \rightarrow XY$$



$$X.i := A.i$$

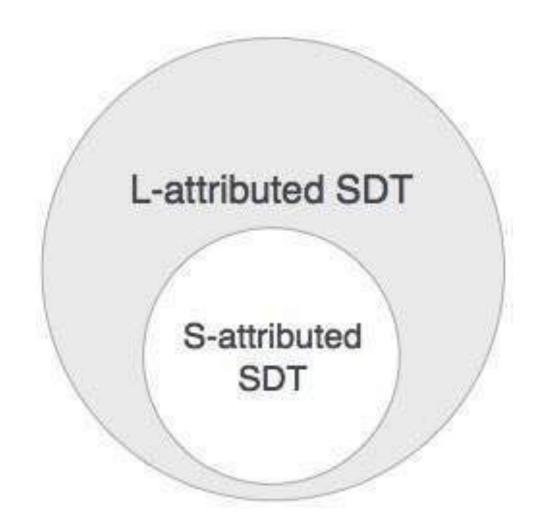
$$Y.i := X.s$$

$$A.s := Y.s$$

L-attributed SDD



Every S-attributed Syntax-Directed Definition is also L-attributed.



L-Attributed SDD to implement a Simple Desk Calculator



Complete the semantic rules for the following L-attributed SDD.

Evaluate the SDD for the input 3 + 5

Production	Semantic Rule
E → TE'	
$E' \rightarrow + T E'_{1}$	
$E \rightarrow \lambda$	
T → F T'	
$T \rightarrow *FT_1'$	
$T' \rightarrow \lambda$	
F → num	

L-Attributed SDD to implement a Simple Desk Calculator



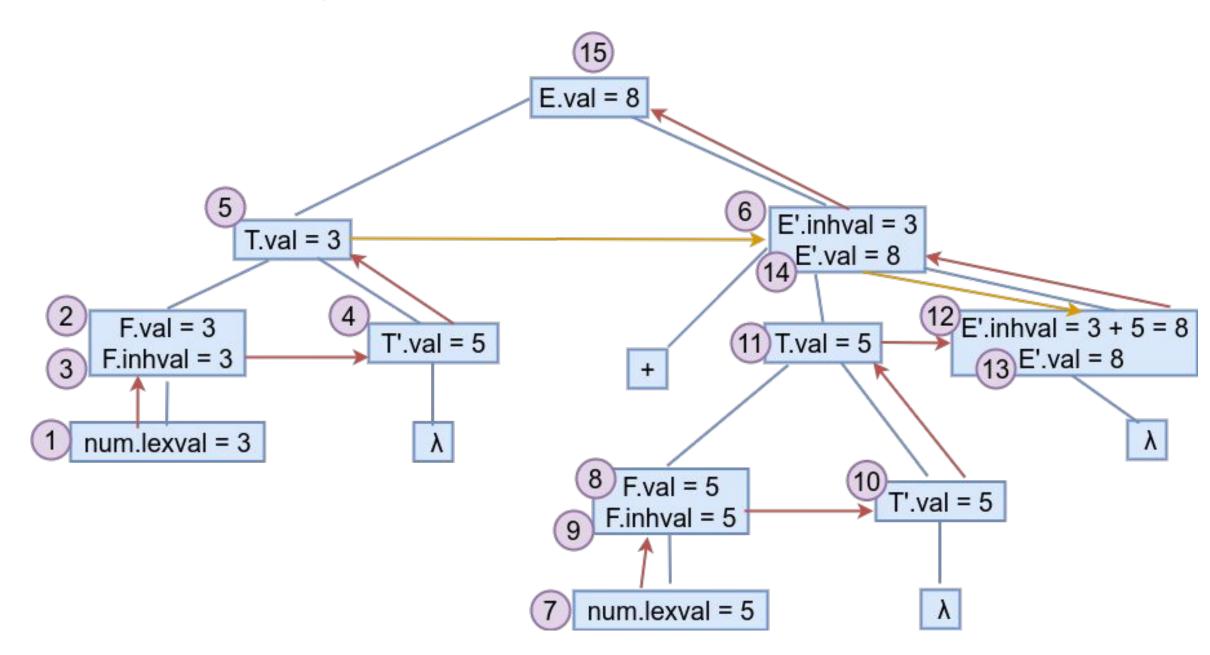
Production	Semantic Rule
E → TE'	{ E'.inhval = T.val; E.val = E'.val; }
$E' \rightarrow + T E'_{1}$	$\{E_{1}^{'}.inhval = E'.inhval + T.val;$ $E'.val = E_{1}^{'}.val;\}$
$E \rightarrow \lambda$	{ E'.val = E ₁ .inhval; }
T → F T'	{ T'.inhval = F.val; T.val = T'.val; }
$T \rightarrow *FT_1'$	$\{T_{1}^{'}.inhval = T'.inhval + F.val;$ $T'.val = T_{1}^{'}.val; \}$
$T' \rightarrow \lambda$	{ T'.val = T'.inhval }
F → num	{ F.val = num.lexval }

This is an LDD In E → TE',
the attribute for
E' is inherited
from T, which is
the left-sibling.

L-Attributed SDD to implement a Simple Desk Calculator



Evaluate the SDD for the input 3 + 5



L-attributed SDD for Simple Type declaration



Complete the semantic rules for the following L-attributed SDD. Evaluate the SDD for the input int a,b

Production	Semantic Rule
$D \rightarrow TL$	
T → int	
T → float	
$L \rightarrow L_1$, id	
$L \rightarrow id$	

L-attributed SDD for Simple Type declaration



Production	Semantic Rule
D → TL	{ L.inhType = T.type; L.inhWidth = T.width; }
T → int	{ T.type = integer; T.width = 4;}
T → float	{ T.type = float; T.width = 8; }
$L \rightarrow L_1$, id	{ L ₁ .inhType = L.inhType; L ₁ .inhWidth = L.inhWidth; update(id.entry, L.inhType,L.inhWidth); }
L → id	{update(id.entry, L.inhType,L.inhWidth); }

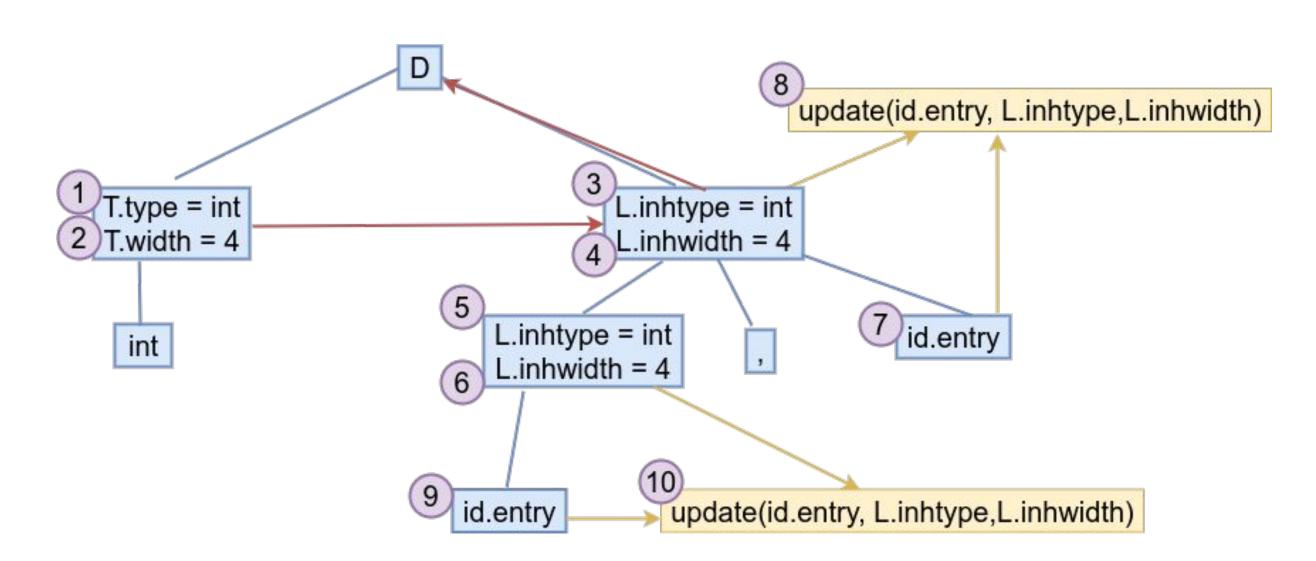
This is an LDD In D → T L, the attribute for L is inherited from T, which is the left-sibling.

update() is used to update type and storage in the symbol table.

L-attributed SDD for Simple Type declaration



Evaluate the SDD for the input int a,b;



L-attributed SDD to identify Array Type



Complete the semantic rules for the following L-attributed SDD. Evaluate the SDD for the input int [2][3]

Production	Semantic Rule
$T \rightarrow BC$	
$B \rightarrow int$	
B→ float	
$C \rightarrow [num] C_1$	
$C \rightarrow \lambda$	

L-attributed SDD to identify Array Type



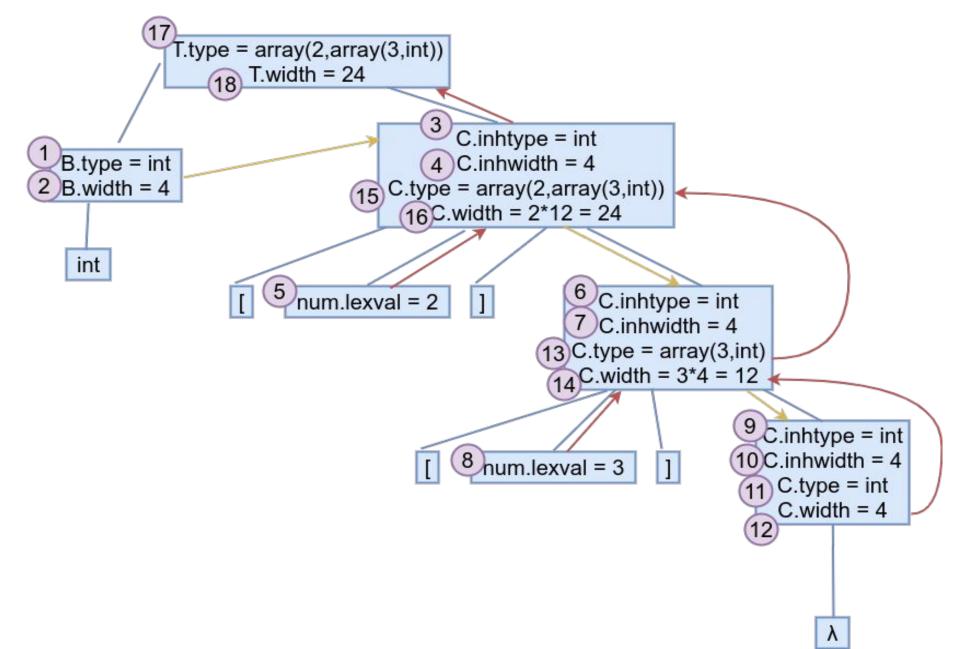
Product	ion	Semantic Rule
T → B C		ne = B.type; C.inhWidth = B.width; C.type; T.width = C.width; }
$B \rightarrow int$	{ B.type =	integer; B.width = 4;}
B→ float	{ B.type =	float; B.width = 8; }
C → [nui	C.type = c C.width = addType(pe = C.inhType; C ₁ .inhWidth = C.inhWidth; array(num.lexval , C ₁ .type); num.lexval * C ₁ .width ;); id.entry, L.inhType); n(id.entry, L.inhWidth; }
$C \rightarrow \lambda$	{ C.type =	C.inhType; C.width = C.inhWidth; }

L-attributed SDD for Simple Type declaration



Evaluate the SDD for the input int a[2][3]

int a[2][3] translates to array(2,array(3,int))



L-attributed SDD for Basic vs Array Type declaration in C Semantics



Construct an SDD to identify an array of the following format -

float[4] x, y

Follow C Semantics - i.e, x is an array type, y is a basic type

Production	Semantic Rule
D→ TL	
$T \rightarrow BC$	
$B \rightarrow int$	
B→ float	
$C \rightarrow [num] C_1$	
$C \rightarrow \lambda$	
$L \rightarrow L_1$, id	
$L \rightarrow id$	

L-attributed SDD for Basic vs Array Type declaration in C Semantics



Production	Semantic Rule
D→ TL	{ L.inhType = T.type; L.inhWidth = T.width; L.inhbasicType = T.basicType; L.inhbasicWidth = T.basicWidth; }
T → B C	{ C.inhType = B.type; C.inhWidth = B.width; T.type = C.type; T.width = C.width; T.basicType = B.type; T.basicWidth = B.width;}
$B \rightarrow int$	{ B.type = integer; B.width = 4;}
B→ float	{ B.type = float; B.width = 8; }
C → [num] C ₁	$\{C_1.inhType = C.inhType; C_1.inhWidth = C.inhWidth; Should be C C.type = array(num.lexval, C_1.type); C.width = num.lexval * C_1.width; \{C_1.inhWidth = C.inhWidth; Should be C \}$
$C \rightarrow \lambda$	$\{C_1.inhType = C.inhType; C_1.inhWidth = C.inhWidth;\}$

L-attributed SDD for Basic vs Array Type declaration in C Semantics



Production	Semantic Rule
$L \rightarrow L_1$, id	L_1 .inhType = L.inhType;
_	L_1 .inhWidth = L.inhWidth;
	L_1 .inhbasicType = L.inhbasicType;
	L_1 .inhbasicWidth = L.inhbasicWidth;
	addType(id.entry, L.inhbasicType);
	addWidth(id.entry, L.inhbasicWidth;
$L \rightarrow id$	{ addType(id.entry, L.inhType);
	addWidth(id.entry, L.inhWidth; }



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Unit 3: Syntax Directed Definitions

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Lecture Overview



In this lecture, you will learn about -

- S-Attributed SDD Examples :
 - To generate Syntax tree for Expressions
 - To generate Syntax tree for Statements

Example 1 - SDD to generate Syntax tree for Expressions

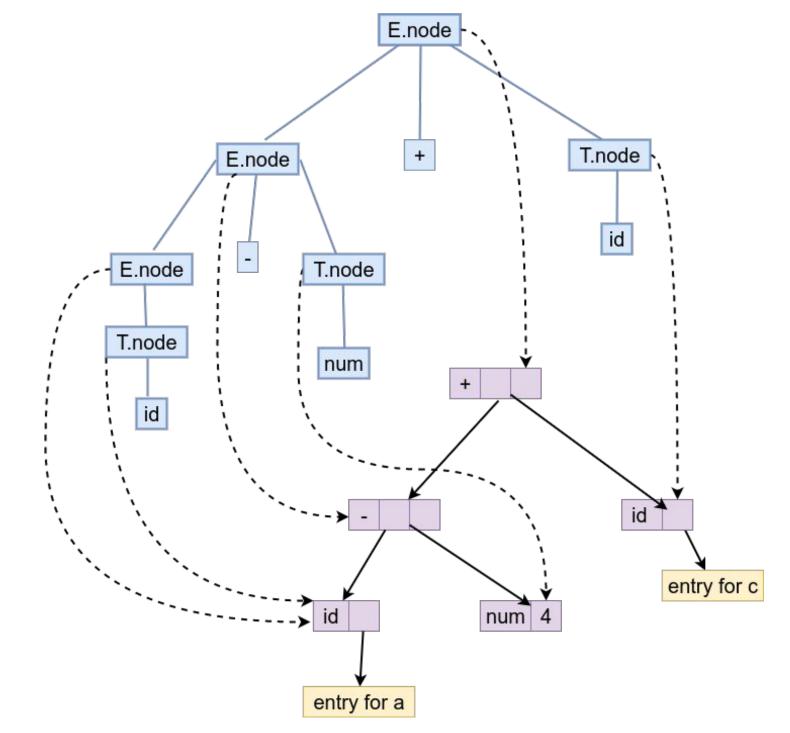


Production	Semantic Rule
E -> E ₁ + T	{ E.node = new Node('+', E ₁ .node, T.node); }
E -> E ₁ - T	{ E.node = new Node('-', E ₁ .node, T.node); }
E -> T	{ E.node = T.node ; }
T -> (E)	{ T.node = E.node ; }
T -> id	{ T.node = new Leaf(id , id.entry); }
T -> num	{ T.node = new Leaf(num , num.lexval); }

Example 1 - SDD to generate Syntax tree for Expressions



Use the previous grammar to construct the syntax tree for the input a - 4 + c



Example 2 - SDD to generate Syntax tree for Statements



Production	Semantic Rule
Stmt -> S Stmt	{ Stmt.node = new Node(Seq, S.node, Stmt.node); }
Stmt -> S	{ Stmt.node = S.node; }
S -> if (cond) { Stmt }	{ S.node = new Node(if, Cond.node, Stmt.node); }
S -> while (cond) { Stmt }	{ S.node = new Node(while, Cond.node, Stmt.node); }
S -> AssignExpr	{ S.node = AssignExpr.node ; }
Cond -> E ₁ > E ₂	{ Cond.node = new Node(>, E ₁ .node, E ₂ .node); }
Cond -> E ₁ < E ₂	{ Cond.node = new Node(<, E ₁ .node, E ₂ .node); }
Cond -> E ₁ E ₂	{ Cond.node = new Node(, E ₁ .node, E ₂ .node); }
Cond -> E ₁ && E ₂	{ Cond.node = new Node(&&, E ₁ .node, E ₂ .node); }
AssignExpr -> id = E;	{ AssignExpr.node = new Node(=, new Leaf(id,id.entry), E.node); }

Example 2 - SDD to generate Syntax tree for Statements



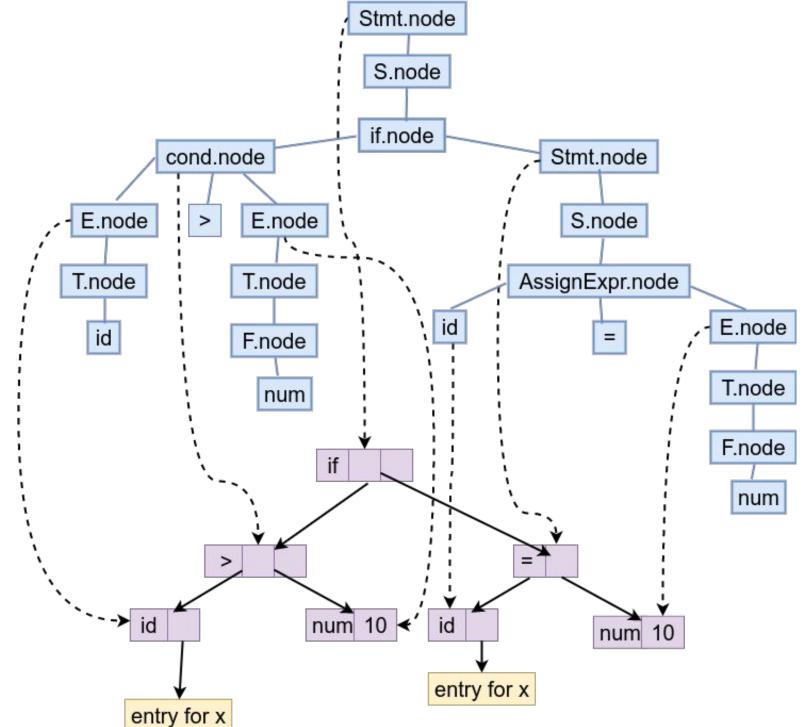
Production	Semantic Rule
$E \rightarrow E_1 + T$	{ E.node = new Node('+', E ₁ .node, T.node); }
E → T	{ E.node = T.node; }
$T \rightarrow T_1 * F$	{ T.node = new Node('*', T ₁ .node, F.node); }
$T \rightarrow F$	{ T.node = F.node; }
F o id	{ F.node = new Leaf(id , id.entry); }
F → num	{ F.node = new Leaf(num , num.lexval); }

Example 2 - SDD to generate Syntax tree for Statements



Use the previous grammar to construct the syntax tree for the input

```
if ( x > 10 )
{
    x = 10;
}
```





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Unit 3: L-Attributed SDD - Intermediate Code Generation

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Lecture Overview



In this lecture, you will learn about -

- L-Attributed SDD to generate intermediate code for -
 - Expressions
 - Condition statement
 - If statement
 - If-else statement
 - While statement
 - Do while statement
 - For statement
 - Boolean expressions

Recap



- There are 2 kinds of attributes Synthesized and Inherited.
- An SDD with only synthesized attributes is an S-attributed definition.
- An SDD is L-attributed if all its attributes are either -
 - Synthesized
 - Extended synthesized dependent on children as well as inherited attributes.
 - Inherited but dependent only on inherited attributes at parent and any siblings at left.
- Every S-attributed SDD is also L-attributed.

SDD to generate Intermediate Code - Arithmetic Expressions



Write the SDD to generate intermediate code.

The given example indicates the code and its corresponding intermediate code for an expression a = b + - c.

Input	Output
a = b + - c	t1 = minus c
	t2 = b + t1
	a = t2

SDD to generate Intermediate Code - Arithmetic Expressions



Assigning appropriate semantic rules to each production -

Production	Semantic Rule
S -> id = E;	S.code = E.code gen(id.lexval '=' E.addr)
E -> E1 + E2	E.addr = new Temp(); E.code = E1.code E2.code gen(E.addr '=' E1.addr '+' E2.addr)
E -> -E1	E.addr = new Temp(); E.code = E1.code gen(E.addr '=' 'minus' E1.addr)
E -> (E1)	E.addr = E1.addr E.code = E1.code
E -> id	E.addr = id.lexval E.code = ' '

SDD to generate Intermediate Code - Conditions



Production	Semantic Rule
B -> id1 rel id2	B.code = gen('if' id1.lexval rel.op id2.lexval 'goto' B.true) gen('goto' B.false)
rel -> >	rel.op = ">"
rel -> <	rel.op = "<"
rel -> >=	rel.op = ">="
rel -> <=	rel.op = "<="

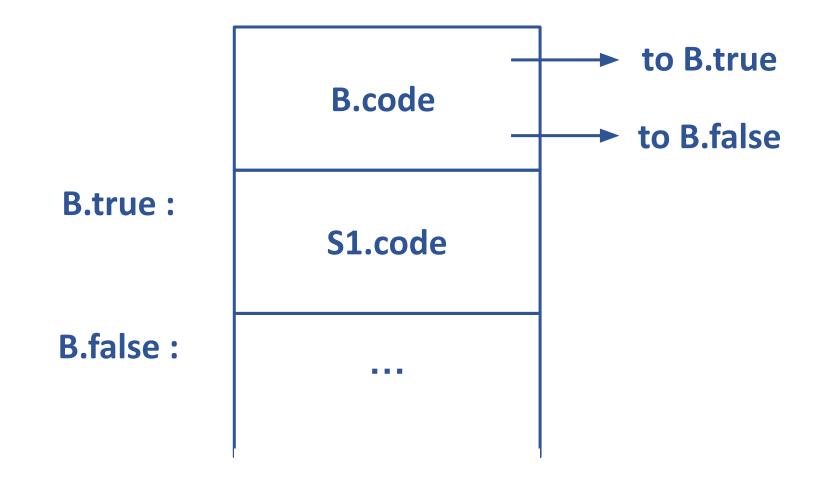
SDD to generate Intermediate Code - If Statement



Production	Semantic Rule
S -> if (B) S1	L1 = new Label();
	B.true = L1;
	B.false = S.next;
	S1.next = S.next;
	S.code = B.code label(L1) S1.code

SDD to generate Intermediate Code - If statement





SDD to generate Intermediate Code



• If Else

```
S -> if ( C ) S1 else S2

S2.next = S.next;

C.true = new label();

C.false = new label();

S1.next = S.next;

S.code = C.code || label(C.true) || S1.code || gen("goto" label(S.next)) || label(C.false) || S2.code
```

SDD to generate Intermediate Code



If Else

S -> if (C) S1 else S2

C.true:

C.false:

S.next:

C.code → to C.false

➤ to C.true

S1.code gen("goto label (S.next))

S2.code

SDD to generate Intermediate Code



While

```
S -> while ( C ) S1

begin = new label();

C.true = new label();

C.false = S.next;

S1.next = begin;

S.code = label(begin) || C.code || label(C.true) || S1.code || gen("goto" label(begin))
```

SDD to generate Intermediate Code



While

S-> while (C) S1

begin:

C.code

to C.true

➤ to C.false

C.true:

S1.code

gen("goto label

(begin))

C.false =

S.next:

. . .

SDD to generate Intermediate Code



Do - While

```
S -> do (S1) while (C)

C.true = new label();

C.false = S.next;

S.code = label(C.true) | | S1.code | | C.code
```

SDD to generate Intermediate Code



• Do - While

S -> do (S1) while (C)

C.true:

S1.code

C.code

to C.true

→ to C.false

C.false =

S.next:

...

SDD to generate Intermediate Code



For

```
S -> for (S1; C; S3) S4

C.true = new label();
C.false = S.next;
S3.next = new label();
S.code = S1.code || label(S3.next) || C.code || label(C.true) || S4.code || S3.code || gen("goto S3.next);
```

SDD to generate Intermediate Code



to C.true

→ to C.false

For

S -> for (S1; C; S3) S4

S3.next:

C.code

C.true:

ac.

C.false = S.next :

S4.code

S1.code

S3.code

goto S3.next

...

SDD to generate Intermediate Code



Boolean Expressions

```
B -> B1 || B2

B.true = B1.true

B1.false = newl label();

B.true = B2.true

B.false = B2.false

B.code = B1.code || label (B1.false) || B2.code
```

SDD to generate Intermediate Code



Boolean Expressions

```
B -> B1 && B2
```

```
B.false = B1.false
```

B1.true = newl label();

B.true = *B2.true*

B.false = B2.false

SDD to generate Intermediate Code



Boolean Expressions

SDD to generate Intermediate Code



• Generate Intermediate Code for the following example:

```
if ( x > 10)
{
    x = x
}
```

• Grammar -



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Unit 3: Syntax Directed Translation

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Lecture Overview



In this lecture, you will learn about -

- Syntax Directed Translation
- Design of Translation Schemes
- Types of Translation Schemes
- Problematic SDT
- Postfix schemes

Recap



- The Principle of Syntax Directed Translation states that the meaning of an input sentence is related to its syntactic structure, i.e., to its Parse-Tree.
- Translations for programming language constructs guided by context-free grammars.
- There are 2 kinds of attributes Synthesized and Inherited.
- An SDD with only synthesized attributes is an S-attributed definition.
- Every S-attributed SDD is also L-attributed.

Recap - Syntax Directed Translation



- We associate Attributes to the grammar symbols representing the language constructs.
- Values for attributes are computed by Semantic Rules associated with grammar productions.
- There are two notations for attaching semantic rules:
 - Syntax Directed Definitions: High-level specification hiding many implementation details.
 - Translation Schemes: More implementation oriented, indicate the order in which semantic rules are to be evaluated.

Compiler Design Syntax Directed Translation Schemes



- Translation Schemes are more implementation oriented than syntax directed definitions since they indicate the order in which semantic rules and attributes are to be evaluated.
- A Translation Scheme is a context-free grammar in which,
 - Attributes are associated with grammar symbols.
 - Semantic Actions are enclosed between braces {} and are inserted within the right-hand side of productions.
- Yacc uses Translation Schemes.

Design of Translation Schemes



- When designing a Translation Scheme we must be sure that an attribute value is available when a semantic action is executed.
- When the semantic action involves only synthesized attributes, the action can be put at the end of the production.
- If we have an L-Attributed SDD we must enforce the following restrictions:
 - An inherited attribute for a symbol in the right-hand side of a production must be computed in an action before the symbol
 - A synthesized attribute for the non terminal on the left-hand side can only be computed when all the attributes it references have been computed - The action is usually put at the end of the production.

Compiler Design Problematic SDT



Implementation

- Ignoring the actions, parse the input and produce a parse tree as a result.
- Then, examine each interior node N, say one for production A -> α . Add additional children to N for the actions in α , so the children of N from left to right have exactly the symbols and the actions of α .
- Perform a preorder traversal of the tree, and as soon as a node labelled by an action is visited, perform that action.

Problematic SDT



Infix to prefix example

```
L -> En

E -> {printf("+");} E + T

E -> T

T -> {printf("*");} T * F

T -> F

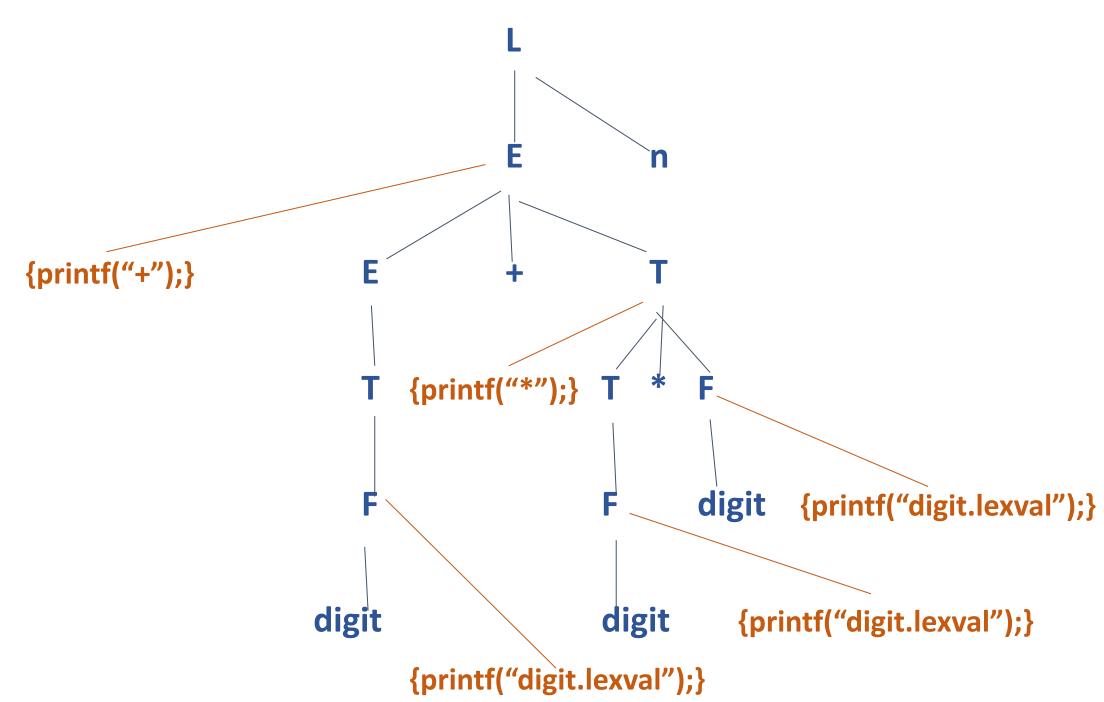
F -> (E)

F -> digit {printf("digit.lexval");}
```

Problematic SDT



Infix to prefix example (contd.)



Problematic SDT



What does the following SDT scheme print for 5 + 4 - 2

```
E -> TR

R \rightarrow +T \{print("+");\} R1

R \rightarrow -T \{print("-");\} R1

R \rightarrow \epsilon

T -> F

F -> digit \{print(digit.lexval);\}
```

Compiler Design Postfix SDT



S attributed to SDT.

Evaluation of S-attributed SDD

• S-attributed SDDs will have only synthesized attributes and can be evaluated by a bottom up parser.

• Since the attributes in the semantic actions are only synthesized, the actions can be placed at the end of the production.

Postfix SDT



Rules for evaluation

Consider the following production,

before reducing BCD to A, the attributes of B, C and D must be computed before attribute of A which appears on the stack.

• Corresponding semantic action associated with the production must be executed.

Compiler Design Postfix SDT



Rules for evaluation

• The parser stack is extended to have parallel value stack.

If the Action appears at the end of production in a SDT, such SDTs are

called Postfix SDTs.

A B	A.a B.b	Parser / Value Stack
•	•	Value Stack

Parser Stack



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Unit 3: SDD to SDT

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Lecture Overview



In this lecture, you will learn about -

- L-attributed SDD to SDT
- SDT Implementation
- S-attributed SDD to SDT (Postfix SDT)



Translation by traversing a parse tree

- Build parse tree and annotate.
- Build the parse tree, add actions and execute the actions in pre-order.



Translation by traversing a parse tree

- Build parse tree and annotate.
- Build the parse tree, add actions and execute the actions in pre-order.



Translation during parsing

- Use a RDP with a function for each non-terminal.
- Generate code on the fly, using a RDP.
- Implement an SDT in conjunction with an LL parser.
- Implement an SDT in conjunction with an LR parser.



- Place the computation of inherited attributes for a non-terminal before that non-terminal appears in the right hand side of the production.
- Place the computation of synthesized attributes at the end of production.

Compiler Design Evaluation of L-attributed SDD



• L-attributed SDDs can have both synthesized attributes and inherited attributes.

Rule to be followed for evaluation

 Place the semantic rule corresponding to the inherited attributes of the non-terminal before the non-terminal appears on the right hand side of the production.

 Place the semantic rule corresponding to the synthesized attributes of the non-terminal at the end of the production.

Conversion of L-attributed SDD



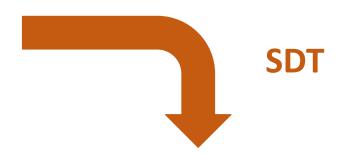
Example

Production	Semantic Rule
T -> FT'	T .in = F.syn; T.syn = T .syn
T ->*FT'	T'.inh = T'.inh * F.syn; T' .syn = T'1.syn
T'-> 🗆	T'.syn = T'.inh
F -> digit	F.syn = digit.lexval

Conversion of L-attributed SDD



Example (contd.)



```
T -> F { T'.in = F.syn;} T' {T.syn = T'.syn}

T' -> *F {T'1.inh = T'.inh * F.syn;} T'1 {T'.syn = T'1.syn}

T1 -> □ { T'.syn = T'.inh;}

F -> digit { F.syn = digit.lexval; }
```

L-attributed SDD to SDT - Type Declarations



Production	Semantic Rule	Translation Scheme
$D \rightarrow TL$	{ L.in = T.type;}	D → T { L.in := T.type } L
T → int	{ T.type = integer; }	T → int { T.type := 'integer' }
T → real	{ T.type = float; }	T → real { T.type := 'real' }
$L \rightarrow L_1$, id	{ L ₁ .in= L.in; addType(id.entry, L.in); }	L → { L1.in := L.in } L1, id { addtype(id.entry, L.in) }
L → id	{ addType(id.entry, L.in); }	L → id { addtype(id.entry, L.in) }

L-attributed SDD to SDT - Intermediate Code Generation



Convert the L-attributed SDD to generate intermediate code for If statement to SDT -

Production	Semantic Rule	
$S \rightarrow if(C) S1$	L1 = new label();	
	C.true = L1;	
	C.false = S.next;	
	S1.next = S.next;	
	S.code = C.code label(L1) S1.code	

L-attributed SDD to SDT



Translation Scheme -

L-attributed SDD to SDT



Convert the L-attributed SDD to generate intermediate code for while statement to SDT:

Production	Semantic Rule
S → while (C) S1	L1 = new label();
	L2 = new label();
	C.true = L2
	C.false = S.next
	S1.next = L1
	S.code = label(L1) C.code label(L2) S1.code gen('goto' begin)

L-attributed SDD to SDT



Translation Scheme -

```
S → while ( L1 = new label ();

L2 = new label ();

C.true = L2;

C.false = S.next;

S1.next = L1;
```

Compiler Design SDT Implementation



- Ignoring the actions, parse the input and produce a parse tree as a result.
- Examine each interior node N.
- Add additional children to N for the actions.
- Perform a preorder traversal of the tree, and as soon as a node labelled by an action is visited, perform that action.

SDT Implementation



Consider the following translation scheme.

```
S \rightarrow ER
R \rightarrow *E \{ print("*"); \} R \mid \epsilon
E \rightarrow F + E \{ print("+"); \} \mid F
F \rightarrow (S) \mid id \{ print(id.value); \}
```

Here id is a token that represents an integer and id.value represents the corresponding integer value.

For an input 2 * 3 + 4, this translation scheme prints ______.

SDT Implementation - Infix to Postfix



• Convert the SDD for infix expression to prefix to SDT.

Production	Semantic Rule
E → E1 + T	
$E \longrightarrow T$	
T → T1 * F	
$T \rightarrow F$	
F → num	
$F \rightarrow id$	

SDT Implementation - Infix to Postfix



• Convert the SDD for infix expression to prefix to SDT.

Production	Semantic Rule				
E → E1 + T	<i>E</i> → { <i>printf("+");</i> } <i>E</i> 1+ <i>T</i>				
$E \to T$	$E \rightarrow T$				
T → T1 * F	$T \rightarrow \{printf("*");\} T1*F$				
$T \to F$	$T \longrightarrow F$				
F → num	$F \rightarrow num \{printf("%d", num.lexval);\}$				
$F \rightarrow id$	$F \rightarrow id \{printf("%d", id.lexval);\}$				

Evaluation of S-Attributed Definitions



- Synthesized Attributes can be evaluated by a bottom-up parser as the input is being analyzed avoiding the construction of a dependency graph.
- The parser keeps the values of the synthesized attributes in its stack.
- Whenever a reduction $A \to \alpha$ is made, the attribute for A is computed from the attributes of α which appear on the stack.
- Thus, a translator for an S-Attributed Definition can be simply implemented by extending the stack of an LR-Parser.

Extending a Parser Stack



- Extra fields are added to the stack to hold the values of synthesized attributes.
- In the simple case of just one attribute per grammar symbol the stack has two fields state and val.
- The current top of the stack is indicated by the pointer top.

Parser Stack



- Synthesized attributes are computed just before each reduction :
 - Before the reduction A → XY Z is made, the attribute for A is computed :

state	val
Z	Z.x
Y	Y.x
X	X.x

Postfix SDT scheme for simple desk calculator



```
E \rightarrow E1 + T
                   {stack[top-2].val = stack[top-2].val + stack[top].val;
                       top = top - 2; }
E \rightarrow T
T → T1 * F
                 {stack[top-2].val = stack[top-2].val * stack[top].val;
                       top = top - 2; }
T \longrightarrow F
F \rightarrow (E)
                  {stack[top-2].val = stack[top-1].val;
                       top = top - 2; }
F \rightarrow digit
```

Implementing L-attributed SDD during LR Parsing



 Introduce a Marker Non-terminal in place of each embedded action.

 There is one production for each Marker M,

 $M \rightarrow epsilon$

Example:

A → alpha {a} beta

would convert to

A → alpha **M** beta

M → epsilon {a}

Implementing L-attributed SDD during LR Parsing



Example

Implementing L-attributed SDD during LR Parsing



```
S \rightarrow while (MC)NS1
```

```
S.code = L1 ||
C.code || L2 ||
S1.code
```

Implementing L-attributed SDD during LR Parsing



```
M → epsilon

L1 = new label();
L2 = new label();
C.true = L2;
C.false = S.next;

N → epsilon

S1.next = L1;
```

Implementing L-attributed SDD during LR Parsing



Parser Stack Structure

Stack record

A Synthesized attributes of A

Record of Inherited attributes of A

Marker A

Note: We perform general style of bottom-up parsing - shift-reduce parsing. A - non terminal

Implementing L-attributed SDD during LR Parsing



Stack	Input Buffer	Action
\$	while (cond)Stmt \$ (dummy string)	Shift while
\$ while while	(cond)Stmt $\$$ Shift (S \rightarrow while (MC)NS1	
\$ while (while \$	cond)Stmt \$ L1 = new label(); L2 = new label(); C.true = L2; C.false = S.next;	Reduce using M → epsilon and execute the action

Implementing L-attributed SDD during LR Parsing



Stack	Input Buffer	Action	
\$ while (M	cond)Stmt \$	Shift C	
M L1 L2 C.true C.f while			
\$ while (M C)Stmt \$	Shift)	
C C.code			
M L1 L2 C.true C.f			
(while			
\$			

Implementing L-attributed SDD during LR Parsing



Stack					Input Buffer	Action
\$ while (M C))	Stmt \$	Reduce using N → epsilon
)						S1.next = L1;
C C.code			C.co	ode		
М	L1	L2	C.true	C.false		
		(
		whil	е			
\$					S → while	e (MC)NS1

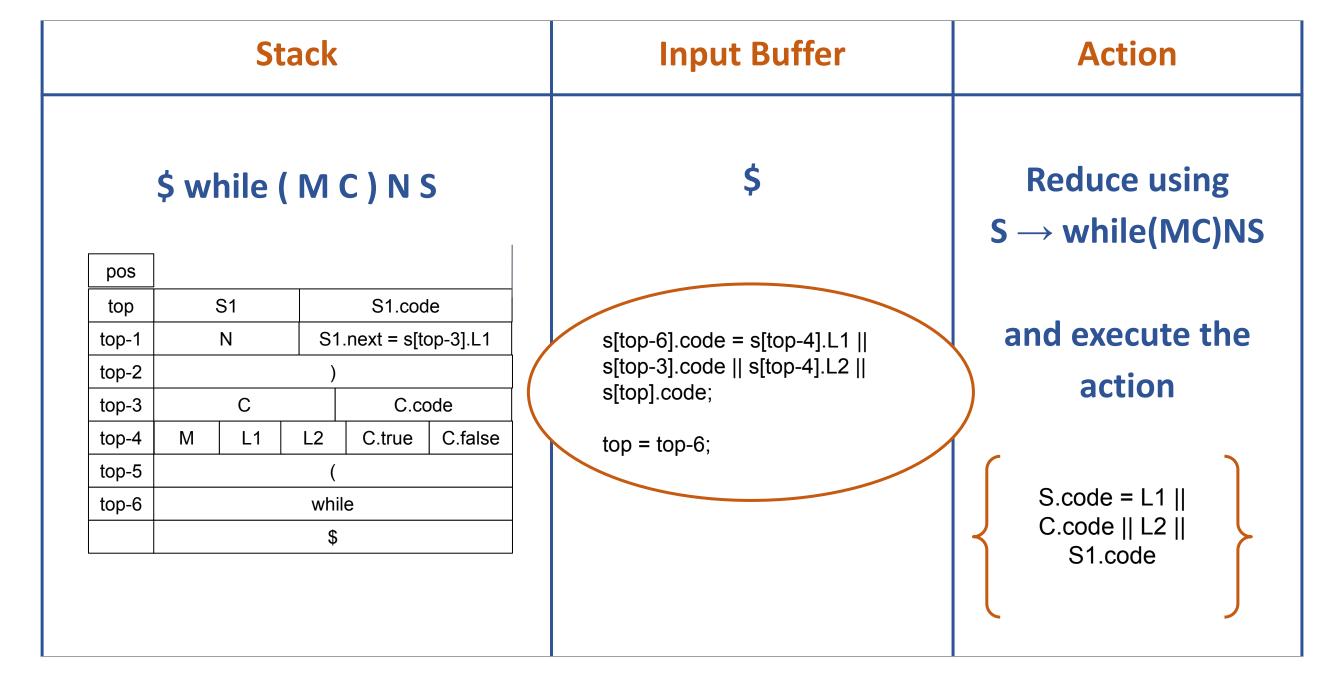
Implementing L-attributed SDD during LR Parsing



	Sta	ck			Input Buffer	Action
\$ while (M C) N					Stmt \$	Shift S1
N S1.next = s[top-3].L1						
C C.code			ode			
M L1	L2	C.true	C.false			
(
while						
\$						

Implementing L-attributed SDD during LR Parsing





Implementing L-attributed SDD during LR Parsing



Stack	Input Buffer	Action
\$ S	\$	Accept
S S.code \$		

Implementing L-attributed SDD during LR Parsing



Example

Implementing L-attributed SDD during LR Parsing



Example

$$S \rightarrow if (MC) NS1 \qquad S.code = C.code || L1 || S1.code$$

$$M \rightarrow epsilon \qquad L1 = new label();$$

$$C.true = L1;$$

$$C.false = S.next;$$

$$N \rightarrow epsilon \qquad S1.next = S.next;$$



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Unit 4: Intermediate Code Generation

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Lecture Overview



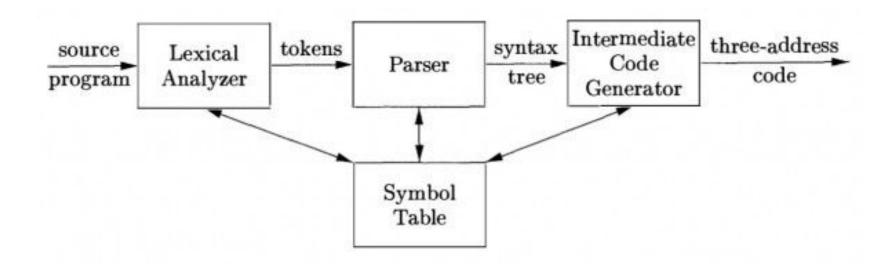
In this lecture, you will learn about -

- What is intermediate code?
- Why intermediate code generation?
- Advantages of ICG
- Types of Intermediate Representation
- Directed Acyclic Graph
 - Applications
 - SDD to construct a DAG
 - Examples of Syntax tree vs DAG

What is Intermediate code?



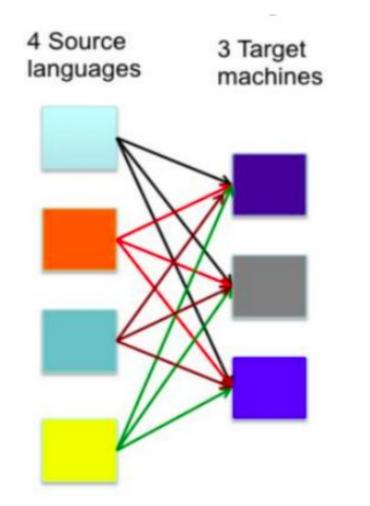
- Intermediate code is used to translate the source code into the machine code.
- It lies between the high-level language and the machine language.
- The Intermediate code generator receives input from the semantic analyzer. It takes input in the form of an annotated syntax tree.
- Using the intermediate code, the second phase of the compiler (synthesis phase) is changed according to the target machine.



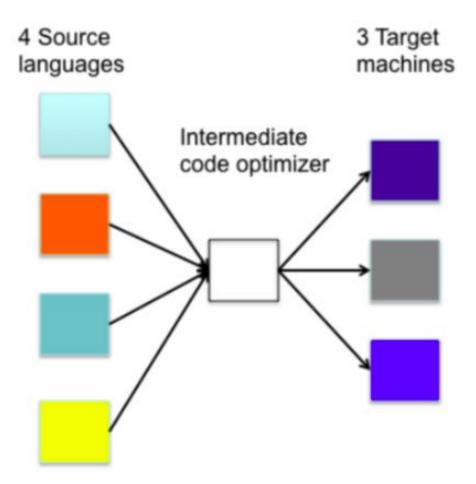
Why Intermediate code generation?



 Intermediate code eliminates the need of a new full compiler for every unique machine by keeping the analysis portion same for all the compilers.



4 front-ends + 4x3 optimisers + 4x3 code generators



4 front-ends + 1 optimiser + 3 code generators

Advantages of Intermediate Code Generation



- ICG makes it easier to construct compilers for different architectures.
- Target code can be generated for any machine just by attaching new machine as the back end - this is called retargeting.
- It is possible to apply machine independent code optimization helps in faster generation of code.

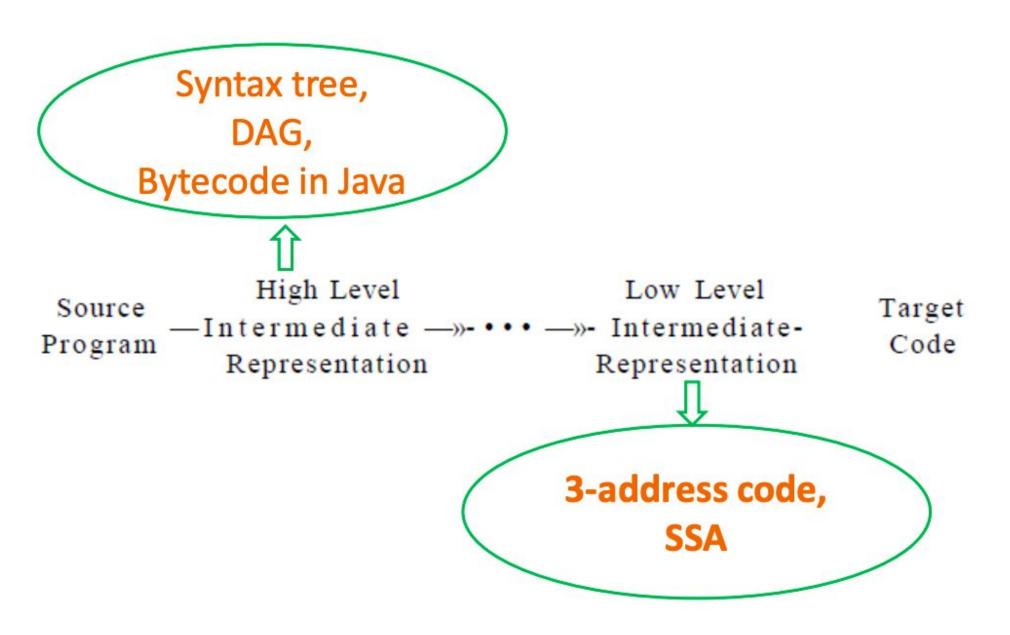
Types of Intermediate Representation



- An intermediate representation is a representation of a program between the source and target languages.
- A good IR is one that is fairly independent of the source and target languages - this maximizes its ability to be used in a retargetable compiler.
- There are three ways to classify Intermediate representation -
 - High-level or Low-level
 - Language-specific or Language independent
 - Graphical or Linear

Intermediate Representation - High level vs Low level representation





Intermediate Representation - High level representation



- High-level intermediate code representation is very close to the source language itself.
- They can be easily generated from the source code
- Code modifications can be easily applied to enhance performance.
- Examples- Syntax trees, DAG, Java Bytecode

Intermediate Representation - Low level representation



- Low level intermediate code representation is close to the target machine.
- This makes it suitable for register and memory allocation, instruction set selection, etc.
- It is good for machine-dependent optimizations.
- Examples Three Address Code, SSA

Compiler Design Intermediate Representation

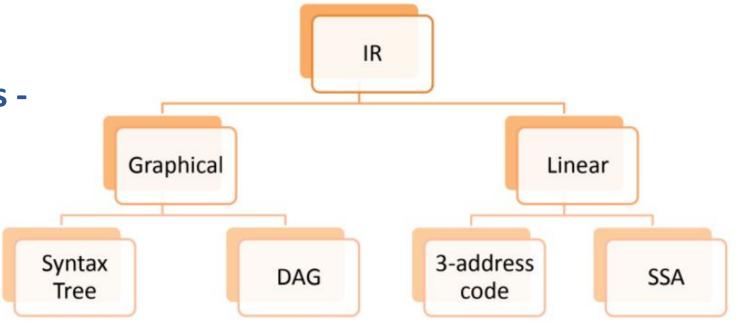


In terms of language, Intermediate code can be either -

- Language specific Byte Code for Java, P-code for Pascal
- Language independent three-address-code

Intermediate code can be also classified as -

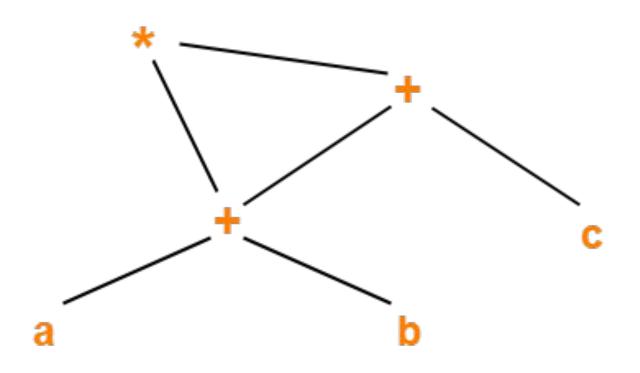
- Graphical
- Linear



DAG - Directed Acyclic Graph



- It is a variant of Syntax tree with a unique node for each value.
- It does not contain cycles.
- In a DAG,
 - Interior nodes always represent the operators.
 - Exterior nodes (leaf nodes) always represent the names, identifiers or constants.
- The given figure represents the DAG for the expression (a + b) x (a + b + c)



Directed Acyclic Graph

Applications of DAG



- It helps optimize code by identifying common subexpressions in a syntax tree.
- It reduces no. of calculations to be done calculate once, refer anywhere.
- It can be used to determine the names whose computation has been done outside the block but used inside the block.
- It can also be used to determine the statements of the block whose computed value can be made available outside the block.

Compiler Design SDD to construct a DAG



 SDD used to generate Syntax tree will be used to construct DAG too, with a simple check -

if an identical node exists

RETURN existing node

else

CREATE a new node

- The assignment instructions of the form x:=y are not performed unless they are necessary.
- The process of making this check is an overhead; hence constructing DAG is costly.

Exercise 1 - Construct DAG for the given expression



Consider the following unambiguous grammar -

Using this, construct Syntax tree and DAG for the following expression -

$$((x + y) - ((x + y) * (x - y))) + ((x + y) * (x - y))$$

Exercise 1 - Solution



Given -
$$((x + y) - ((x + y) * (x - y))) + ((x + y) * (x - y))$$

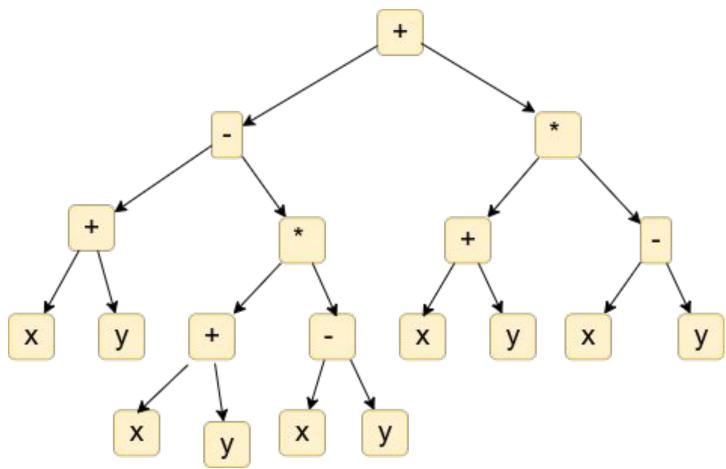
Step 1 - Rewrite the expression for clear understanding

Exercise 1 - Solution



Given -
$$((x + y) - ((x + y) * (x - y))) + ((x + y) * (x - y))$$

Step 2 - Draw the Syntax tree

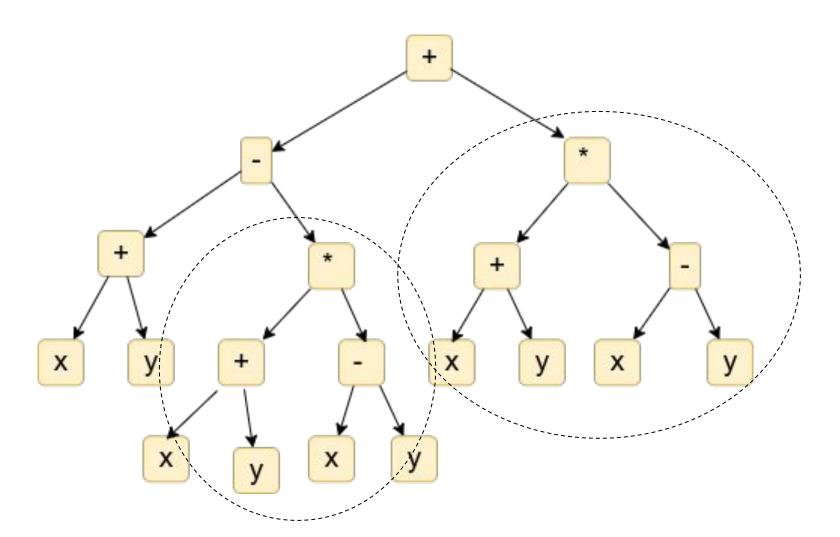


Exercise 1 - Solution



Given -
$$((x + y) - ((x + y) * (x - y))) + ((x + y) * (x - y))$$

Step 3 - Identify the common subexpressions and eliminate step wise



Exercise 2

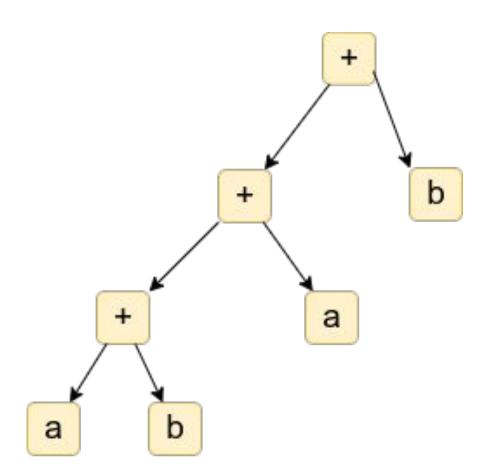


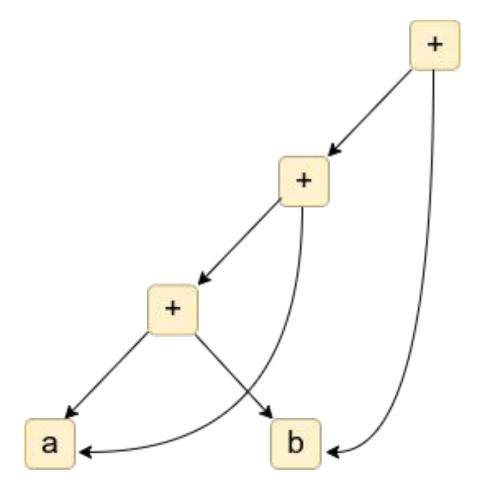
Consider the following unambiguous grammar -

Using this, construct Syntax tree and DAG for the following expressions -

- 1) a + b + a + b
- 2) a + b + (a + b)
- 3) a + a * (b c) + (b c) * d
- 4) (((a + a) + (a + a)) + ((a + a) + (a + a)))
- 5) [(a + b) * c + ((a + b) + e) * (e + f)] * [(a + b) * c]

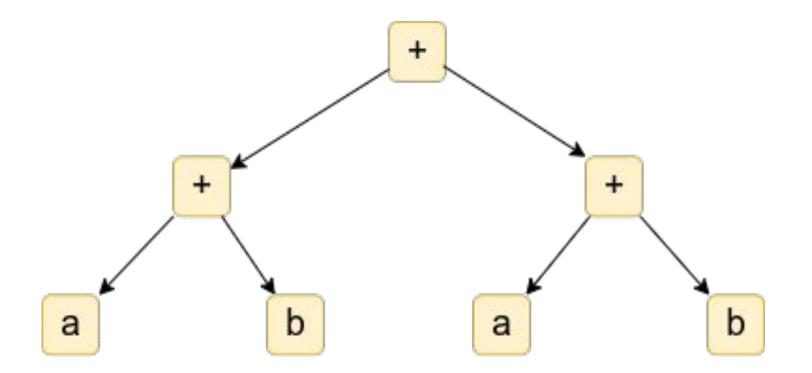


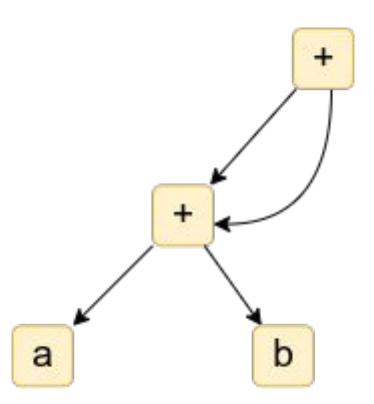






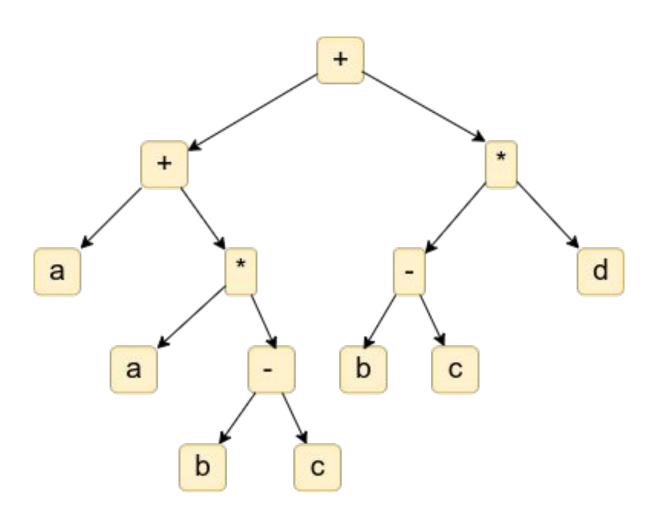
2)
$$a + b + (a + b)$$

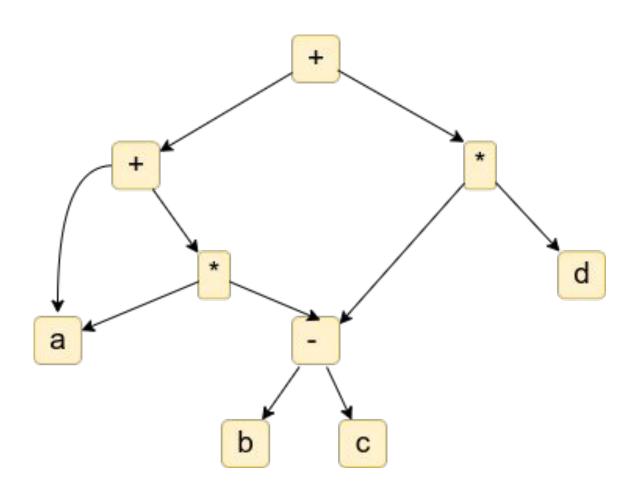






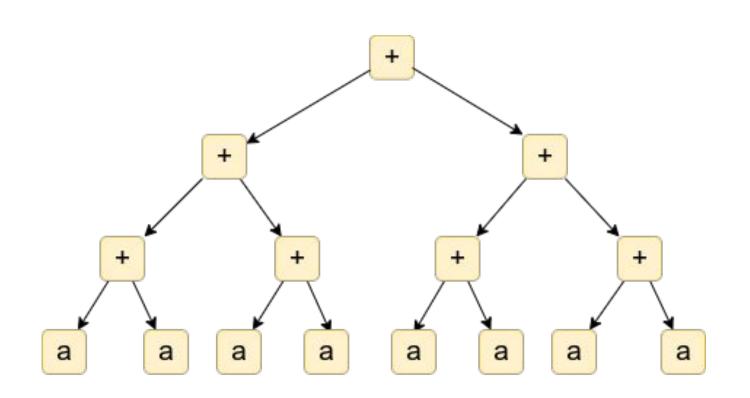
3)
$$a + a * (b - c) + (b - c) * d$$

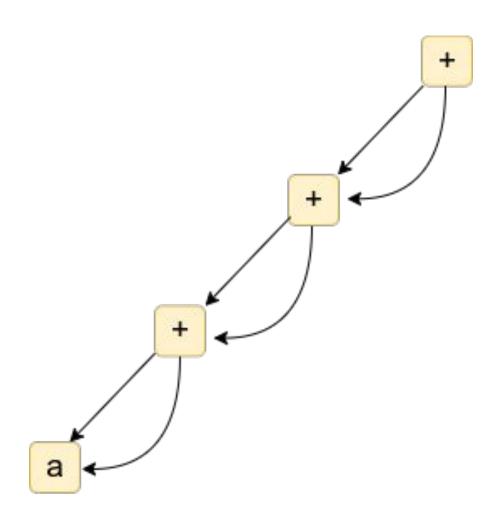






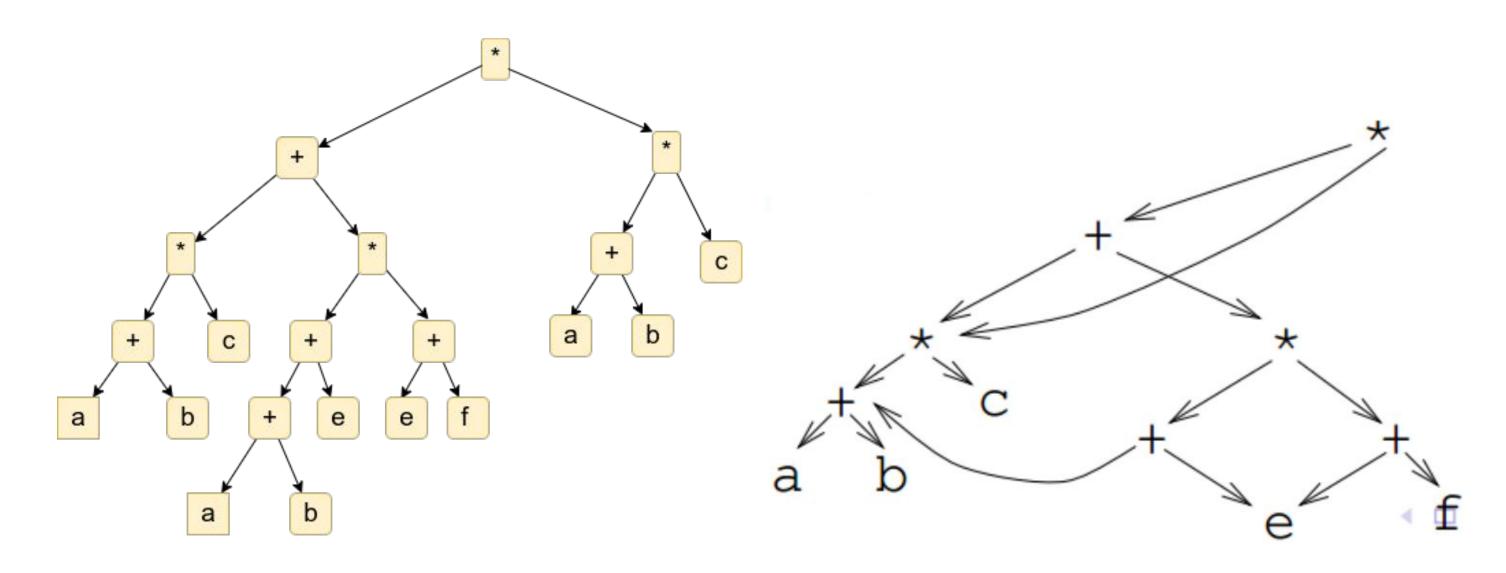
4)
$$(((a + a) + (a + a)) + ((a + a) + (a + a)))$$







$$5)[(a + b) * c + ((a + b) + e) * (e + f)] * [(a + b) * c]$$





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Unit 4: Intermediate Code Generation

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Lecture Overview



In this lecture, you will learn about -

- What is Three-Address Code?
- Format of TAC instructions
- Recap Address Calculation for 1-D and 2-D arrays
- Example Questions

Compiler Design What is Three Address Code?



- Three-Address Code(TAC) is a Linearized representation of syntax tree or DAG.
- It has at most one operator on RHS of an instruction.
- Each instruction can have up to three addresses.
- The Address can either be a
 - Name (identifier)
 - Constant (number)
 - Temporary (holds an intermediate result)

Compiler Design Format of TAC instructions



The following table represents statements and their corresponding TAC format -

Statement	TAC Format
Assignment Statement	x = y op z (op : Binary operator) x = op y (op : Unary operator)
Copy statement	x = y
Unconditional jumps	goto L
Conditional Jumps	if x goto L ifFalse goto L
Compare and jump	if x relop y goto L ifFalse x relop y goto L

Format of TAC instructions



Statement	TAC Format
Address or Pointers	x = &y z = * x *x = a
Indexed Copy	x[i] = y y = x[i]
Procedure call: foo(a, b,)	param a param b call (foo, n) where, n is the number of arguments in function foo().
return statement	return y

Exercise 1



Generate Three-Address Code for the following statements -

1)
$$a + b * c - d / b * c$$

2)
$$x = *p + &y$$

3)
$$x = f(y+1) + 2$$

4)
$$x = foo (2 * x + 3, y + 10, g(i), h(3, j))$$

5)
$$x = f(g(i), h(3, j))$$

Exercise 1.1 - Solution



Given Statements	Three Address Code
a + b * c - d / b * c	t1 = b * c
	t2 = a + t1
	t3 = d / b
	t4 = t3 * c
	t5 = t2 - t4



Given Statements	Three Address Code
x = *p + &y	t1 = *p
	t2 = &y
	t3 = t1 + t2
	x = t3

Exercise 1.3 - Solution



Given Statements	Three Address Code
x = f(y+1) + 2	t1 = y + 1
	param t1
	t2 = call f, 1
	t3 = t2 + 2
	x = t3

Exercise 1.4 - Solution



Given Statements	Three Add	lress Code
x = foo (2 * x + 3, y + 10,	t1 = 2 * x	t5 = call h, 2
g(i), h(3, j))	t2 = t1 + 3	param t5
	param t2	t6 = call foo, 4
	t3 = y + 10	x = t6
	param t3	
	param i	
	t4 = call g, 1	
	param t4	
	param 3	
	param j	

Exercise 1.5 - Solution



Given Statements	Three Address Code
x = f(g(i), h(3, j))	param i
	t1 = call g, 1
	param t1
	param 3
	param j
	t2 = call h,2
	param t2
	t3 = call f, 2
	x = t3

Exercise 1.6 - Solution



Given Statements	Three Address Code
alpha = (65 <= c && c<=90) (97 <= c && c<=122)	t1 = 65 <= c iffalse t1 goto L1 t2 = c <= 90 iffalse t2 goto L1 L0 : alpha = true goto next L1 : t3 = 97 <= c iffalse t3 goto L3 t4 = c <= 122 iffalse t4 goto L3 goto L0 L3 : alpha = false next :

Exercise 2



Generate Three-Address Code for the following function -

```
void main() {
    int x, y;
    int m2 = x * x + y * y;
    while (m2 > 5)
    {
        m2 = m2 - x;
    }
}
```



Given Statements	Three Address Code	
	void main()	L1:
void main() {	{	ifFalse m2 > 5 goto L2
int x, y;	int x;	t4 = m2 - x
int m2 = x * x +	int y;	m2 = t4
y * y;	int m2;	goto L1
while (m2 > 5)	t1 = x * x	L2:
{	t2 = y * y	
m2 = m2 - x;	t3 = t1 + t2	
}	m2 = t3	
}		

Exercise 3



Generate Three-Address Code for the following code snippet -

```
x = i + 10;
switch(x)
   case 1 : x = x * i;
   break;
   case 2 : x = 5;
   case 3: x = i;
   default: x = 0;
```



Given Statements	Three Address Code	
<pre>x = i + 10; switch(x) { case 1 : x = x * i; break; case 2 : x = 5; case 3 : x = i; default: x = 0; }</pre>	t1 = i + 10 x = t1 if x == 1 goto L1 goto L2 L1: t2 = x * i x = t2 goto next L2: if x == 2 goto L3 goto L4 L3: x = 5 goto L5	L4: if x ==3 goto L5

Recap - Address Calculation for 1-D Arrays



Array of an element of an array say A[i] is calculated using the following formula -

Address of A [i] = A + W * ($i - L_B$)

where,

A = Name of the array denotes the Base address

W = Storage Size of one element stored in the array (in bytes)

i = Subscript of element whose address is to be found

L_R = Lower limit of subscript, if not specified assume 0

Exercise 4



Generate Three-Address Code for the following code snippets -

```
    1) a = b[i]
    2) do

            i = i + 1;
            while(a[i] < v)</li>
```

```
3) Product = 0;
    i = 1;
    do
        Product = Product + A[i] * B[i];
        i = i + 1;
    while( i < 20)</pre>
```



Given Statements	Three Address Code
a = b[i]	t1 = 4 * i t2 = b + t1 or t2 = b[t1] a = t2
<pre>do i = i + 1; while(a[i] < v)</pre>	L1: t1 = i + 1 i = t1 t2 = 4 * i t3 = a[t2] if t3 < v goto L1



Given Statements	Three Address Code
Product = 0; i = 1; do	Product =0 i = 1 L1: t1 = 4 * i t2 = A[t1] t3 = 4 * i t4 = B[t3] t5 = t2 * t4 t6 = product + t5 product = t6 t7 = i + 1 i = t7 if i < 20 goto L1

Recap - Address Calculation for 2-D Arrays



- While storing the elements of 2-D array in memory, elements are allocated a contiguous memory locations.
- A 2-D array must be linearized so as to enable their storage.
- There are two ways to achieve linearization -
 - Row-major
 - Column-major

Recap - Address Calculation for 2-D Arrays - Row Major



The address of a location in Row Major System is calculated using the following formula:

Address of A [i][j] = A + W * [N * (i - L_r) + (j - L_c)] where,

N = Number of columns of the given matrix

L = Lower limit of row/start row index of matrix, if not given assume 0

L = Lower limit of column/start column index of matrix, if not given assume 0

Recap - Address Calculation for 2-D Arrays - Column Major



The address of a location in Row Major System is calculated using the following formula:

Address of A [i][j] = A + W * [(i - L_r) + M * (j - L_c)] where,

N = Number of columns of the given matrix

L = Lower limit of row/start row index of matrix, if not given assume 0

L = Lower limit of column/start column index of matrix, if not given assume 0

Compiler Design TAC for 2-D Arrays -Assumptions



- Assume all 2-D arrays follow row-major method.
- If the size of array is not mentioned assume it to be m x n array.
- Assume array type as integer and width of an array element as 4 bytes.

Exercise 5



Generate Three-Address Code for the following code snippets -

```
1) for(i = 0; i < n; i ++)
        for(j = 0; j < n; j++)
        c[i][j] = 0;
        where c is a 5x5 array</pre>
```

Exercise 5.1 - Solution



where c is a 5x5 array

Address calculation for c[i][j]

c[i][j] = B + W * [N * (i -
$$L_r$$
) + (j - L_c)]
= c + 4 * [n * (i - 0) + (j - 0)]
= c + 4 * (5 * i + j)

Exercise 5.1 - Solution



Given Statements	Three Address Code	
	i = 0	c[t5] = 0
for(i = 0; i < n; i ++)	L0: t1 = i < n	t6 = j + 1
for(j = 0; j <n ;="" j++)<="" td=""><td>if t1 goto L1</td><td>j = t6</td></n>	if t1 goto L1	j = t6
c[i][j] = 0;	goto next	goto L4
	L1: j=0	L3: t7 = i + 1
	L4:t2=j <n< td=""><td>i = t7</td></n<>	i = t7
	if t2 goto L2	goto L0
	goto L3	
	L2:t3 = 5 * i	
	t4 = t3 + j	
	t5 = 4 * t4	

Exercise 5.1 - Solution



Given Statements		Three Address Code	
<pre>for (i=1; i<=10; i++)</pre>	<pre>i = 1 L5: t1 = i <= 10 if t1 goto L1 goto next L1: j = 1 L4: t2 = j <= 10 if t2 goto L2 goto L3 //inc i L2: t1 = i - 1 t2 = 10 * t1 t3 = j - 1 t4 = t2 + t3 t5 = 8 * t4 t6 = A[t5]</pre>	t7 = i - 1 t8 = 10 * t7 t9 = j - 1 t10 = t8 + t9 t11 = 8 * t10 t12 = B[t11] t13 = t6 + t12 t14 = i - 1 t15 = 10 * t14 t16 = j - 1 t17 = t15 + t16 t18 = 8 * t17 c[t18] = t13	t19 = j + 1 j = t19 goto L4 L3: t20 = i + 1 i = t20 goto L5 next:



THANK YOU

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Unit 4: Three-Address Code

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Lecture Overview



In this lecture, you will learn about -

- Data Structures for Three-Address Code
 - Quadruples
 - Triples
 - Indirect Triples
 - Example Questions

Data Structures for TAC



- Three address code is represented as a record structure with fields for operator and operands.
- These records can be stored as an array or a linked list.
- There three types of record structures -
 - 1. Quadruples [4 fields]
 - 2. Triples [3 fields]
 - 3. Indirect Triples [Triples + List of pointers to Triples]

Compiler Design Quadruples



A Quadruple is an array type data structure with 4 fields -

ор	arg1	arg2	result
1.0			

where,

op - operator.

arg1, arg2 - the two operands used.

result - the result of the expression.

Compiler Design Quadruples





- arg1, arg2 and result are pointers to symbol table entries.
- This means even temporaries must be placed in symbol table as they are created.
- Any unused field is left blank/NULL
- Disadvantage Temporary names have to be entered into symbol table.

Quadruples Format - Unary Operators



The given table describes the quadruple format for unary operators -

Statement	ор	arg1	arg2	result
Unary operators - arg2 is empty	ор	arg1	null	arg2
Example: x=-y	-	y	null	X
Example: x=y	=	У	null	X

Quadruples Format - Functions



The given table describes the quadruple format for functions -

Statement	ор	arg1	arg2	result
param operator - arg2 and result are empty	param	arg1	null	null
Example: param x	param	X	null	null
Function Call - call func_name, func_param	call	func_name	value	X
Example: call foo,3	call	foo	3	null
Example: x = call foo,3	call	foo	3	X

Compiler Design Quadruples Format - Jumps



The given table describes the quadruple format for jumps -

Statement	ор	arg1	arg2	result
For unconditional jumps - result is label	goto	null	null	label
conditional jump Example - if x goto L	if	X	null	L
conditional jump Example - ifFalse x goto L	ifFalse	X	null	L

Quadruples Format - Labels and return



The given table describes the quadruple format for labels and return statements -

Statement	ор	arg1	arg2	result
Label generation Example - L1:	Label	null	null	L1
return	return	X	null	null
return x	return	X	null	null

Quadruples Format - Array indexing



The given table describes the quadruple format for array indexing -

Statement	ор	arg1	arg2	result
x[i] = y	[]=	X	i	У
	STAR	X	i	У
x = y[i]	[]=	y	i	X
	LDAR	y	i	X

Exercise 1



Write the Three-Address Code and corresponding Quadruple representation for the following code snippet -

Exercise 1 - Solution



```
Three-Address Code -
```

$$t1 = x == 0$$

$$u = 1$$

$$t2 = x - 1$$

param t2

$$t4 = t3 * x$$

$$u = t4$$

Exercise 1 - Solution



Quadruple -

$$t1 = x == 0$$

ifFalse t1 goto L1

u = 1

goto L2

L1:

t2 = x - 1

param t2

t3 = call fact, **1**

t4 = t3 * x

u = t4

L2:

ор	arg1	arg2	result
==	х	0	t1
ifFalse	t1		L1
=	1		u
goto			L2
Label			L1
1-	х	1	t2
param	t2		
call	fact	1	t3
*	t3	х	t4
=	t4		u
Label			L2

Triples



A Triple is an array type data structure with 3 fields -



where,

op - operator.

arg1, arg2 - the two operands used.

Triples



- Triples are alternative ways for representing syntax tree or Directed acyclic graph.
- Triples avoid entering temporary names into symbol table.
- For a temporary, use serial number of statement computing its value.
- Problem: Code Immovability
 - No temporary variables stored in symbol table
 - All references are only to the position of statement and not location.
 - This requires the compiler to change all references to arg1 and arg2.
 - Thus, triples are not very efficient in optimizing compilers.

Triples Format - Jumps and Label



The given table describes the triple format for jumps and label -

Statement	ор	arg1	arg2
Unconditional jumps	goto	(2)	
conditional jump Example - if x goto L	if	X	(2)
conditional jump Example - ifFalse x goto L	ifFalse	X	(2)
Label	Label		

Triples Format - Array indexing



The given table describes the triple format for array indexing -

Statement	Stmt no.	ор	arg1	arg2
x[i] = y	(0)	[]=	X	i
	(1)	=	(0)	у
x = y[i]	(0)	=[]	У	i
	(1)	=	X	(0)

Exercise 2



Write the Triple representation for the following Three-Address Code -

$$t2 = t1 * d$$

$$t3 = t1 + c$$

$$t4 = -b$$

$$t5 = t4 * d$$

$$t6 = t3 + t5$$

$$a = t6$$

Exercise 2 - Solution



t1 = -b
t2 = t1 * d
t3 = t1 + c
t4 = -b
t5 = t4 * d
t6 = t3 +t5
a = t6

Stmt no	Ор	Arg1	Arg2		
(0)	-	b			
(1)	*	d	(0)		
(2)	+	С	(1)		
(3)	-	b			
(4)	*	d	(3)		
(5)	+	(2)	(4)		
(6)	=	а	(5)		

The value of a temporary variable can be accessed by the position of the statement that computes it.

Compiler Design Indirect Triples



- A separate list of pointers to the triple structure (i.e, statement numbers) is maintained.
- The statements can be moved by reordering the statement list.
- The utility of indirect triples is almost the same as that of quadruples, but requires less space.

Exercise 2 (cont.)



Write the Indirect Triple representation for the following Three-Address Code -

$$t1 = -b$$

$$t2 = t1 * d$$

$$t3 = t1 + c$$

$$t4 = -b$$

$$t5 = t4 * d$$

$$t6 = t3 + t5$$

$$a = t6$$

Exercise 2 (cont.)



t1 = -b
t2 = t1 * d
t3 = t1 + c
t4 = -b
t5 = t4 * d
t6 = t3 +t5
a = t6

	Stmt no
(0)	(10)
(1)	(11)
(2)	(12)
(3)	(13)
(4)	(14)
(5)	(15)
(6)	(16)

Stmt no	Ор	Arg1	Arg2
(10)	-	b	
(11)	*	d	(0)
(12)	+	С	(1)
(13)	-	b	
(14)	*	d	(3)
(15)	+	(2)	(4)
(16)	=	a	(5)

No change in the Structure

Advantage of Indirect Triples



Suppose the code changes to -

a = t6

	Stmt no
(0)	(10)
(1)	(11)
(2)	(12)
(3)	(10)
(4)	(14)
(5)	(15)
(6)	(16)

Stmt no	Ор	Arg1	Arg2				
(10)	-	- b					
(11)	*	d	(0)				
(12)	+	С	(1)				
(13)	>	b					
(14)	*	d	(3)				
(15)	+	(2)	(4)				
(16)	=	a	(5)				

No change in the Structure

Exercise 3



Write the Quadruple and Triple representation for the following code snippets -

```
1) a = b[i] + c[j]

2) x = f(y + 1) + 2

3) X[i] = a * c + y[i] - n[j] / v

4) for(j=0; j<=10; j++)

{

a = a * (j* (b/c));

}
```

Exercise 3 - Solutions



Quadruples

ор	arg1	arg2	res		
*	4	i	t1		
=[]	b	t2			
*	4	j	t3		
=[]	С	t3	t4		
+	t2	t4	t5		
=	t5		а		

Triples

Stmt No.							
1	*	4	i				
2	2 =[] b						
3	*	4	j				
4	=[]	С	(3)				
5	+	(2)	(4)				
6	=	а	(5)				

Exercise 3 - Solutions



2)
$$x = f(y + 1) + 2$$

3-addr stmt	Qua	adrupl	e Forn	nat	Triple Format				Indirect Triple Format							
	ор	arg1	arg2	result	Stmt#	ор	arg1	arg2	Ptr	Stmt#		Stmt#	ор	arg1	arg2	
T1 = y + 1	+	У	1	T1	1	+	У	1	11	1		1	+	У	1	
Param T1	Param	T1			2	param	(1)		12	2		2	param	<11>		
T2 = call f, 1	call	f	1	T2	3	call	f	1	13	3		3	call	f	1	
T3 = T2 + 2	+	T2	2	Т3	4	+	(3)	2	14	4		4	+	<13>	2	
X = T3	=	ТЗ		X	5	=	X	(4)	15	5		5	=	X	<14>	

Exercise 3 - Solutions



3) X[i] = a * c + y[i] - n[j] / v

	Qu	adrupl	le Forr	mat		Triple Format Indirect Triple						iple Format			
3-addr stmt	ор	arg1	arg2	result	Stmt#	ор	arg1	arg2	Ptr	Stmt#		Stmt#	ор	arg1	arg2
T1 = a * c	*	а	С	T1	1	*	а	С	111	1		1	*	а	С
T2= 4 * I	*	4	I	T2	2	*	4	I	112	2		2	*	4	I
T3 = y[T2]	=[]	У	T2	T3	3	=[]	У	(2)	113	3		3	=[]	у	<112>
T4 = T1 + T3	+	T1	T3	T4	4	+	(1)	(3)	114	4		4	+	(1)	<113>
T5 = 4 * j	*	4	j	T5	5	*	4	j	115	5		5	*	4	j
T6 = n[T5]	=[]	n	T5	T6	6	=[]	n	(5)	116	6		6	=[]	n	<115>
T7 = T6/v	/	T6	V	T7	7	/	(6)	V	117	7		7	/	<116>	V
T8 = T4 - T7	-	T4	T7	T8	8	-	(4)	(7)	118	8		8	-	<114>	<117>
T9 = 4 * i	*	4	I	Т9	9	*	4	ı	119	9		9	*	4	I
X[T9] = T8	[]=	Х	Т9	T8	10	[]=	Х	(9)	120	10		10	[]=	X	<119>
					11	=	(10)	(8)	121	11		11	=	<120>	<118>

Exercise 3 - Solutions



4) for(j=0; j<=10; j++){ a = a * (j* (b/c));}

L1:

$$t1 = j <= 10$$

ifFalse t1 goto L2

$$t2 = b/c$$

$$t3 = j * t2$$

$$t4 = a * t3$$

$$a = t4$$

$$t5 = j + 1$$

$$j = t5$$

goto L1

L2:

Quadruples

ор	arg1	arg2	res
=	0		j
Label			L1
<=	j	10	t1
ifFalse	t1		L2
/	b	С	t2
*	j	t2	t3
*	а	t3	t4
=	t4		а
+	j	1	t5
=	t5		j
goto			L1
Label			L2

Triples

Iripies				
Stmt No.	ор	arg1	agr2	
1	=	j	0	
2	Label			
3	<=	j	10	
4	ifFalse	(3)	(12)	
5	/	b	С	
6	*	j	(5)	
7	*	a	(6)	
8	=	а	(7)	
9	+	j	1	
10	=	j	(9)	
11	goto	(2)		
12	Label			



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Unit 4: Static Single-Assignment(SSA)

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Lecture Overview



In this lecture, you will learn about -

- Static Single-Assignment (SSA) Form
- φ-function
- φ-function Examples

Static Single Assignment (SSA) Form



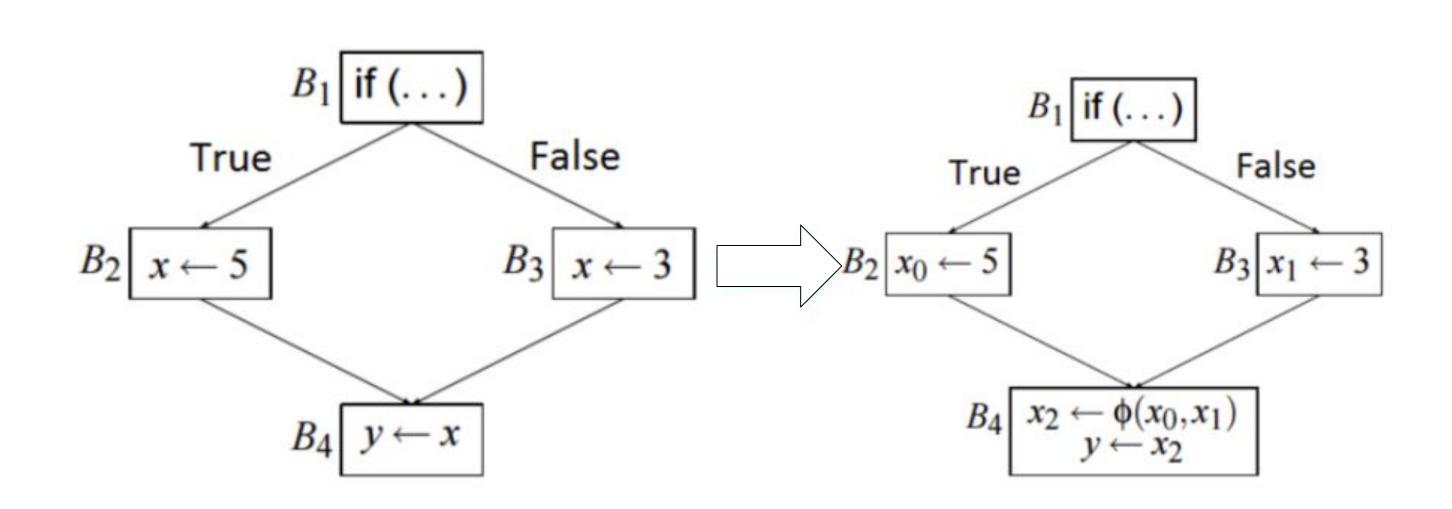
- Each variable is assigned exactly once but may be used multiple times.
- Existing variables in the original IR are split into versions:
- New version of variable is typically indicated by the original name with a subscript, so that every definition gets its own version.
- SSA is an intermediate form widely used by modern optimizing compilers.

Compiler Design ф-function



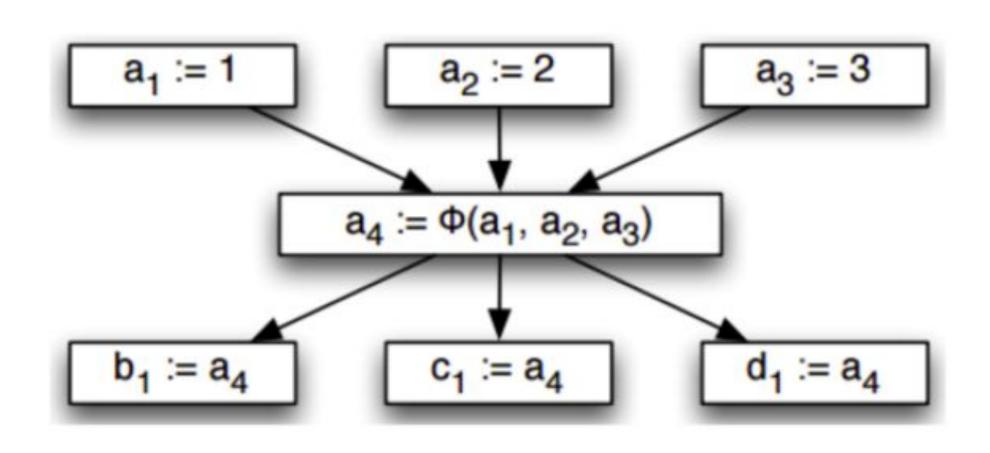
- Control flow can't be predicted in advance, so we can't always know which definition of a variable reached a particular use.
- Notation represents natural "meet points" where values are combined.
- No. of arguments to $\phi(a1, a2)$ is the number of incoming flow edges.
- Return value of the function corresponds to the control-flow path taken to get to the statement.



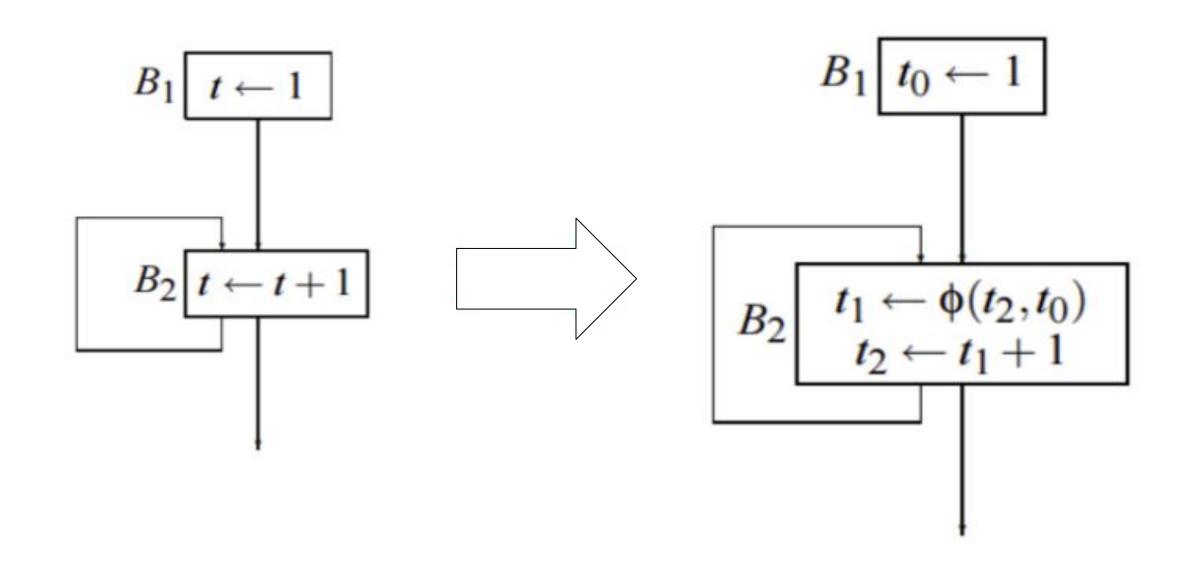




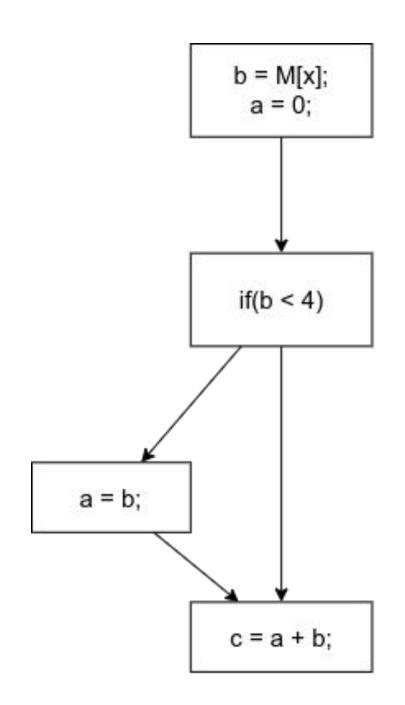
```
case (...) of
    0: a := 1;
    1: a := 2;
    2: a := 3;
end
case (...) of
    0: b := a;
    1: c := a;
    2: d := a;
end
```



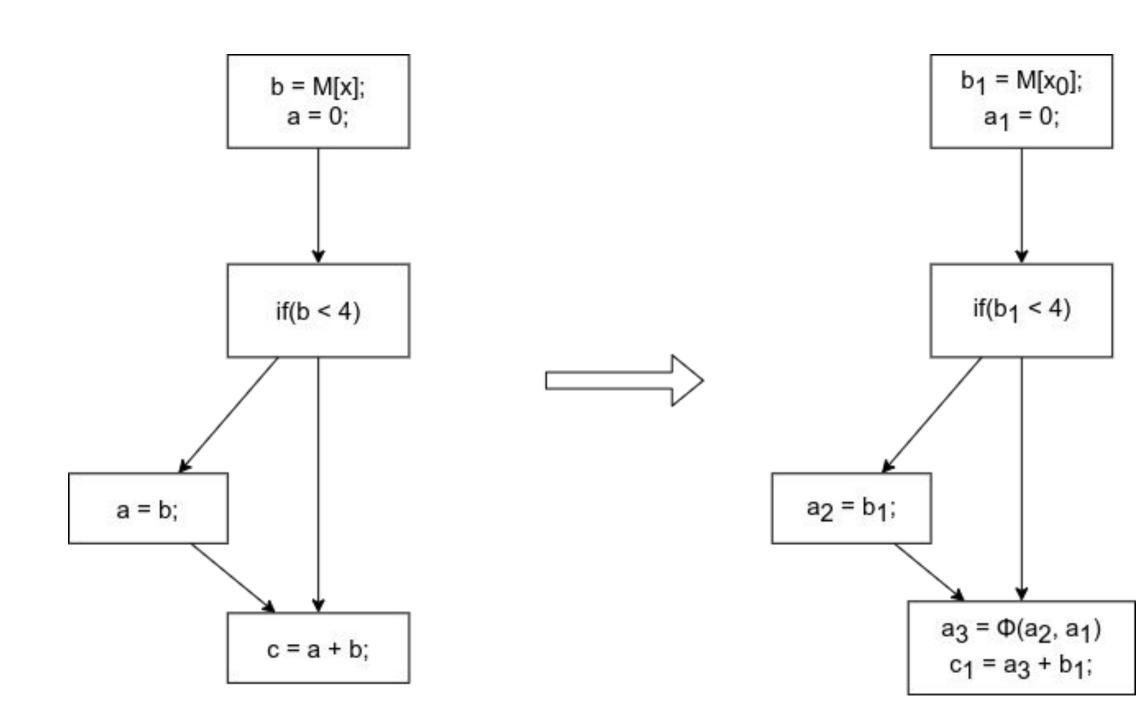




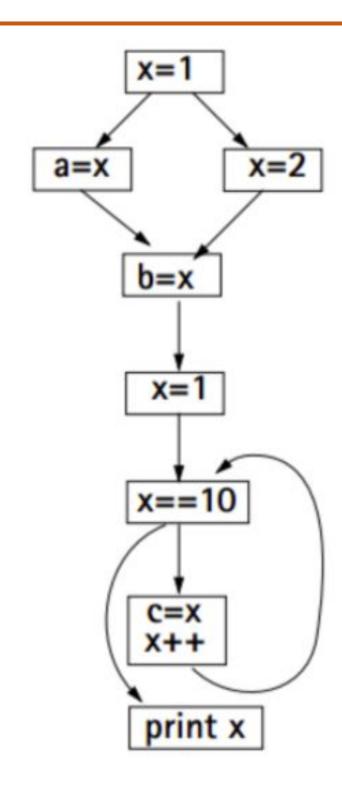




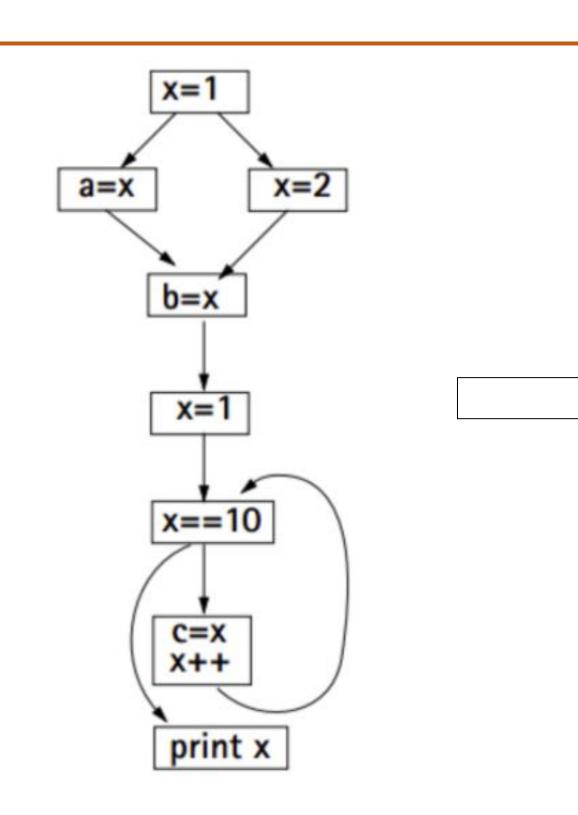


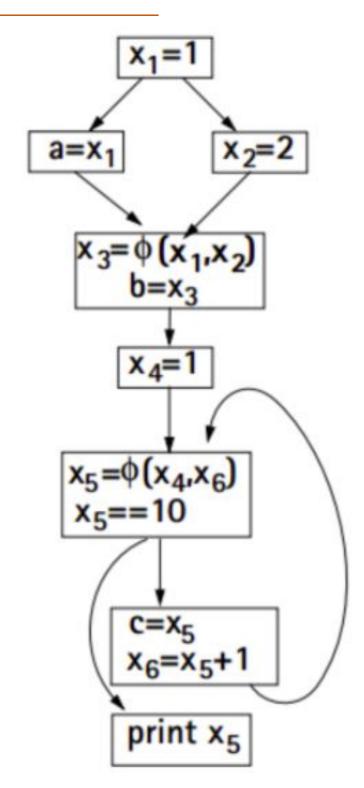




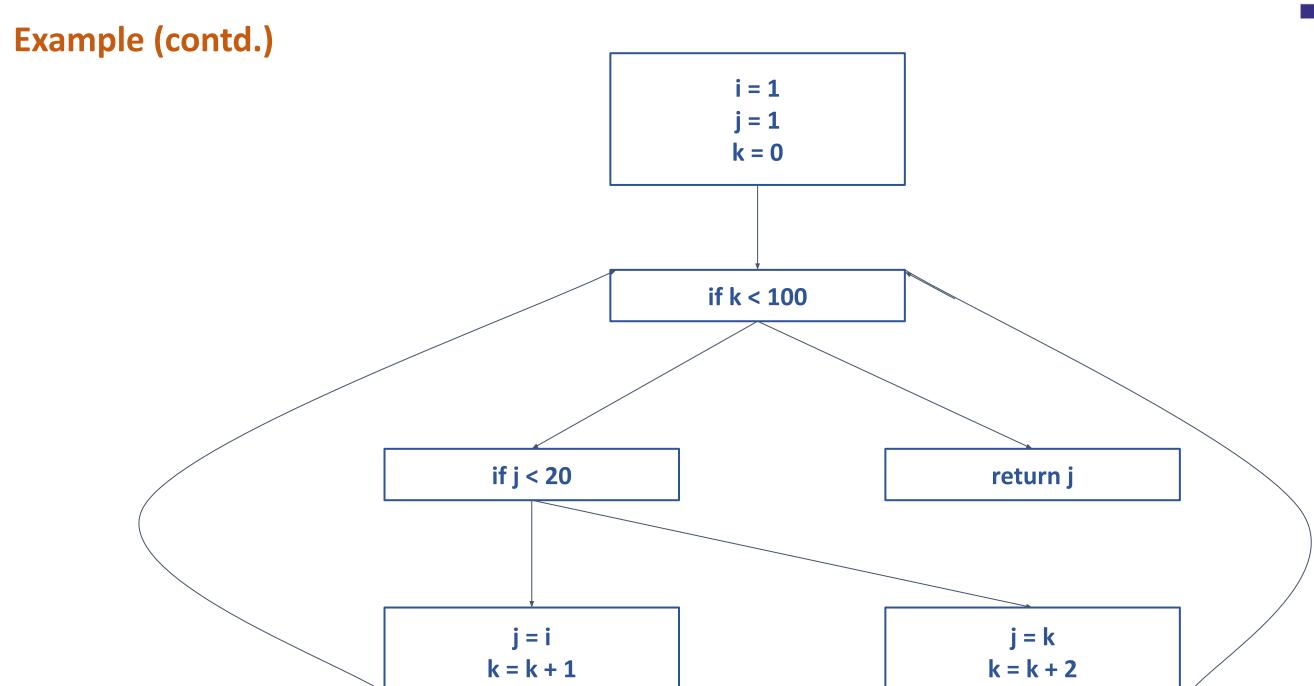




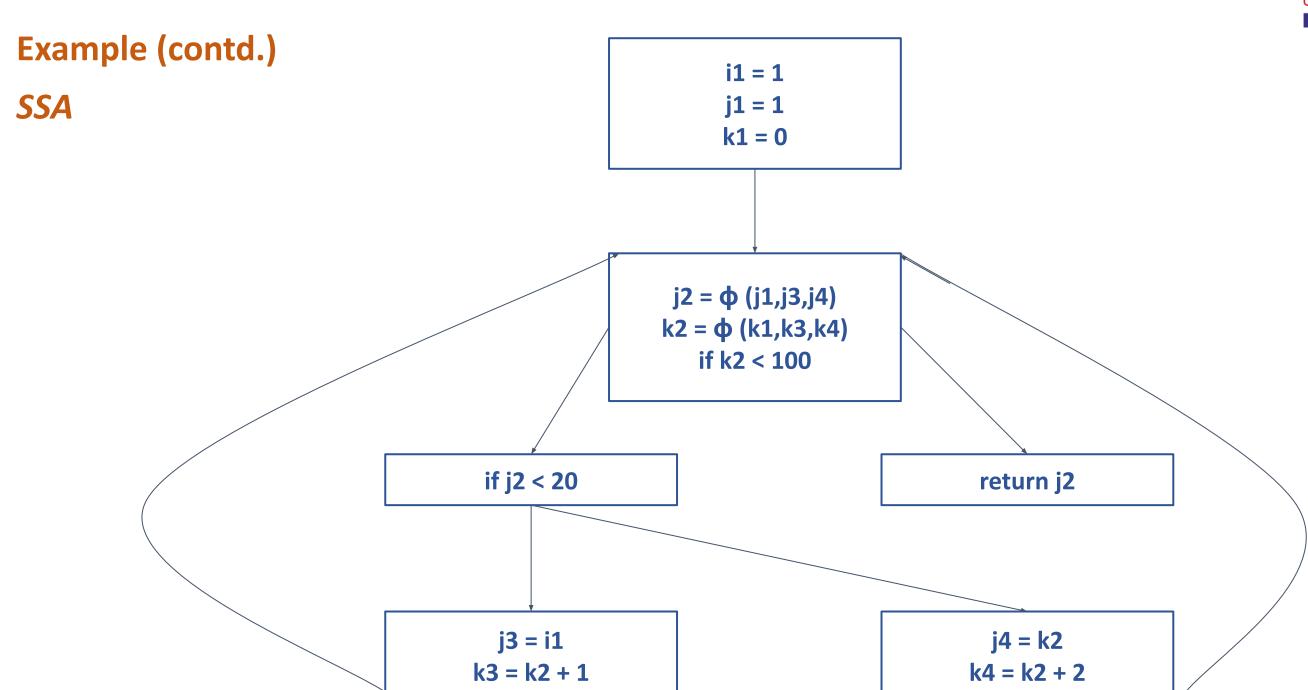












Compiler Design ф-function - Example 7

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Example

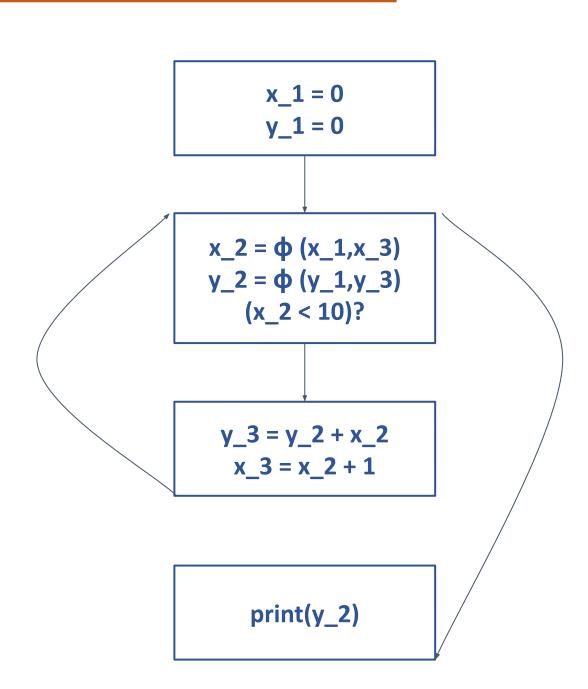
```
x = 0;
y = 0;
while (x<10){
y = y+x;
x = x+1;
}
print(y);</pre>
```

Compiler Design ф-function - Example 7

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Example

```
x = 0;
y = 0;
while (x<10){
y = y+x;
x = x+1;
}
print(y);</pre>
```



Note -



- Most modern production compilers use SSA form (eg. gcc, suif, llvm, hotspot etc.)
- Popular compiler optimizations (eg. constant propagation) become easier to write (and in some cases, algorithmically faster) when applied to programs in SSA form.
- Conversion to SSA form introduces a lot of assignments compilers that do this need to have good register allocators that can eliminate most of them again (not a concern these days).



THANK YOU

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Unit 4: Control Flow Graph Generation

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Lecture Overview



In this lecture, you will learn about -

- CFG Generation
- Converting program to SSA
- Basic blocks
- Generate TAC

Compiler Design CFG Representation of Intermediate Code



- A flow graph is graphical representation that exhibits flow of control information.
- Helps in performing machine independent optimization.
- Benefits of code generation:
 - Better register allocation.
 - Better instruction selection.
 - Helps reduce program cost.

Compiler Design CFG Representation of Intermediate Code



Rules for constructing flow graph

- The nodes of the flow graph are the basic blocks.
- Number the nodes(For example:B1,B2).
- The first basic block (i.e B1)is called initial block.
- Draw a directed edge from the initial block i.eB1to the next block following B1 i.e B2if B2 immediately follows B1.

Compiler Design CFG Representation of Intermediate Code



- Partition intermediate code into basic blocks.
- Nodes of FG : Basic blocks
- Add nodes :
 - Entry node (edge to first block)
 - Exit node (edge from last block)
- Edges of FG: indicate which blocks can follow other blocks. (determine predecessor and successor of a Block).

Compiler Design Basic Blocks



- A basic block consists of set of statements which are executed sequentially without branching.
- Maximal sequence of consecutive instructions such that,
 - Flow of control can only enter the basic block from the first instruction
 - Control leaves the block only at the last instruction
- Each instruction is assigned to exactly one basic block.

Compiler Design Basic Blocks



Rules for determining basic blocks

- Identify leaders
 - The first three address instruction in the intermediate code is a leader.
 - Any instruction that is the target of a conditional or unconditional jump is a leader.
 - Any instruction that immediately follows a conditional or unconditional jump is a leader.
- The first instruction in the basic block is a leader and the basic block ends just before another leader instruction.

Basic Blocks



Example

2.
$$j = 1$$

3.
$$t1 = 10 * i$$

4.
$$t2 = t1 + j$$

6.
$$t4 = t3 - 88$$

7.
$$a[t4] = 0.0$$

8.
$$j = j + 1$$

9. if
$$j \le 10$$
 goto (3)

10.
$$i = i + 1$$

11. if
$$i \le 10$$
 goto (2)

12.
$$i = 1$$

13.
$$t5 = i - 1$$

15.
$$a[t6] = 1.0$$

16.
$$i = i + 1$$

17. if
$$i \le 10$$
 goto (13)

Basic Blocks

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Example (contd.)

- 1. i = 1
- 2. j = 1
- 3. t1 = 10 * i
- 4. t2 = t1 + j
- 5. t3 = 8 * t2
- 6. t4 = t3 88
- 7. a[t4] = 0.0
- 8. j = j + 1

- 9. if $j \le 10$ goto (3)
- 10. i = i + 1
- 11. if $i \le 10$ goto (2)
- 12. i = 1
- 13. t5 = i 1
- 14. t6 = 88 * t5
- 15. a[t6] = 1.0
- 16. i = i + 1
- 17. if $i \le 10$ goto (13)

First instruction in IC is a leader

Any Instruction
that is the Target
of a conditional or
unconditional
jump is a Leader

Any Instruction that follows a conditional or unconditional jump is a Leader

CFG



Example (contd.)

1.
$$i = 1$$

2.
$$j = 1$$

3.
$$t1 = 10 * i$$

4.
$$t2 = t1 + j$$

5.
$$t3 = 8 * t2$$

6.
$$t4 = t3 - 88$$

7.
$$a[t4] = 0.0$$

8.
$$j = j + 1$$

9. if
$$j \le 10$$
 goto (3)

10.
$$i = i + 1$$

11. if
$$i \le 10$$
 goto (2)

12.
$$i = 1$$

13.
$$t5 = i - 1$$

15.
$$a[t6] = 1.0$$

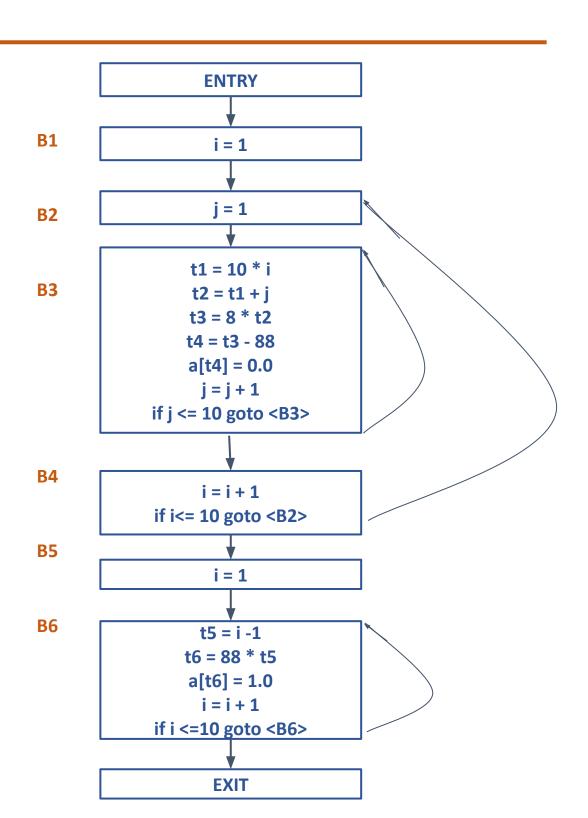
16.
$$i = i + 1$$

17. if
$$i \le 10 \text{ goto } (13)$$

For each leader, its basic block consists of itself and all instructions up to but not including the next leader

CFG

Example (contd.)





CFG



Example

```
int add(n, k){
s = 0;
a = 4;
i = 0;
if(k == 0)
b = 1;
else
b = 2;
```

```
while(i < n) {
    s = s + a * b;
    i = i + 1;
}
return s;
}</pre>
```

CFG



Example (contd.) ICG

CFG



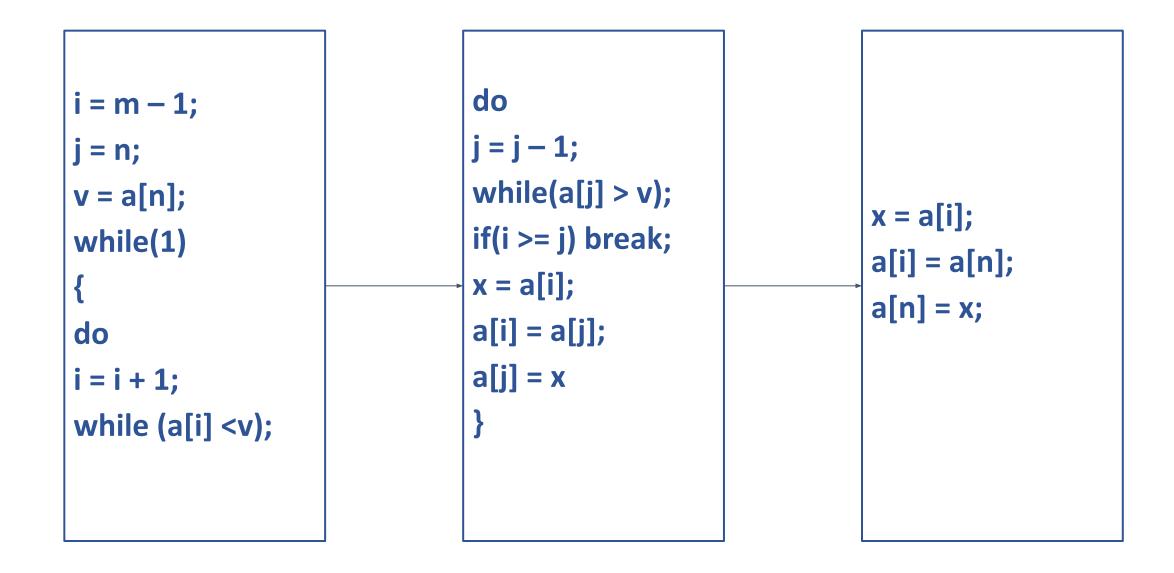
Example (contd.) CFG

L3: return s;

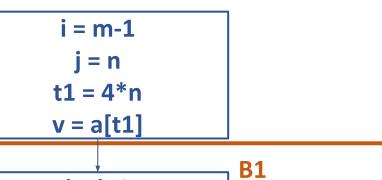
CFG



Example



CFG



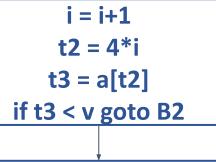
B2

B3

B4



Example (contd.)



t5 = a[t4] if t5 > v goto B3

if i >= j goto B6

B6

$$t13 = 4*n$$

$$t14 = a[t13]$$

$$t15 = 4*n$$

$$a[t15] = x$$

t6 = 4*i x = a[t6] t7 = 4*i t8 = 4*j t9 = a[t8] a[t7] = t9 t10] 4*j a[t10] = x goto B2

B5

CFG

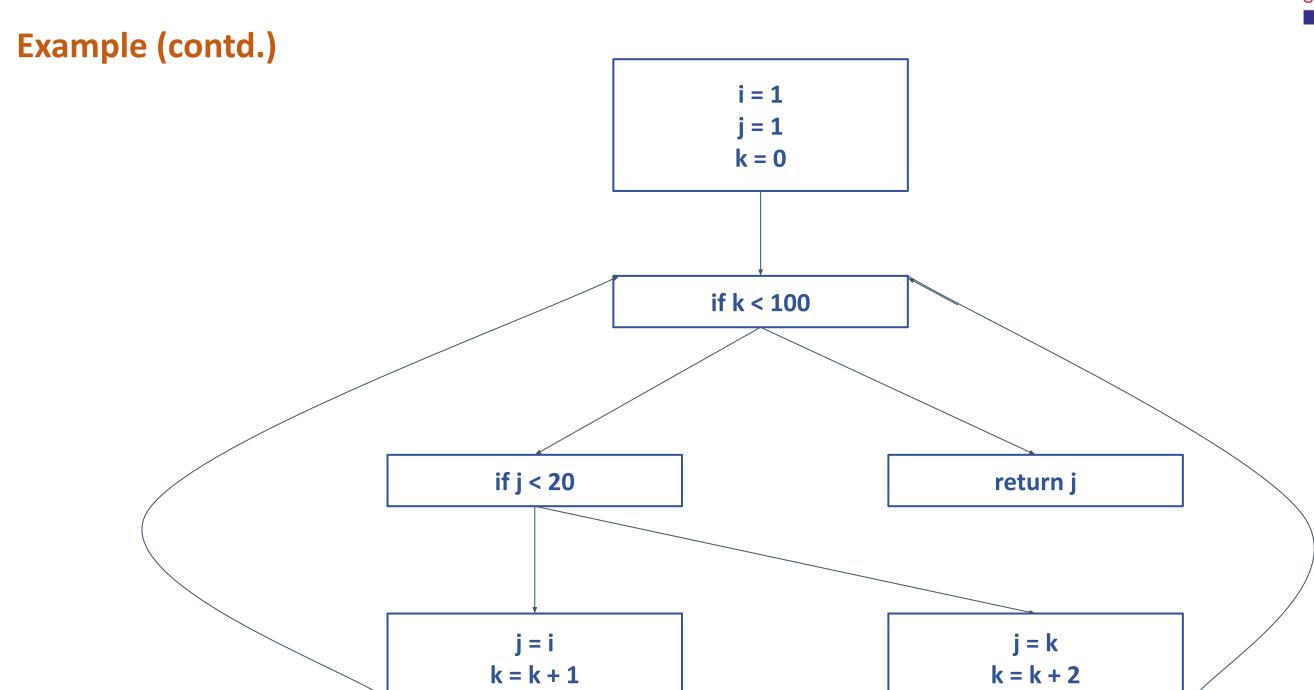


Example

```
i = 1
   j = 1
   k = 0
   while k < 100
      if j < 20
          j = i
          k = k + 1
      else
          j = k
          k = k + 1
      end
   end
return j
```

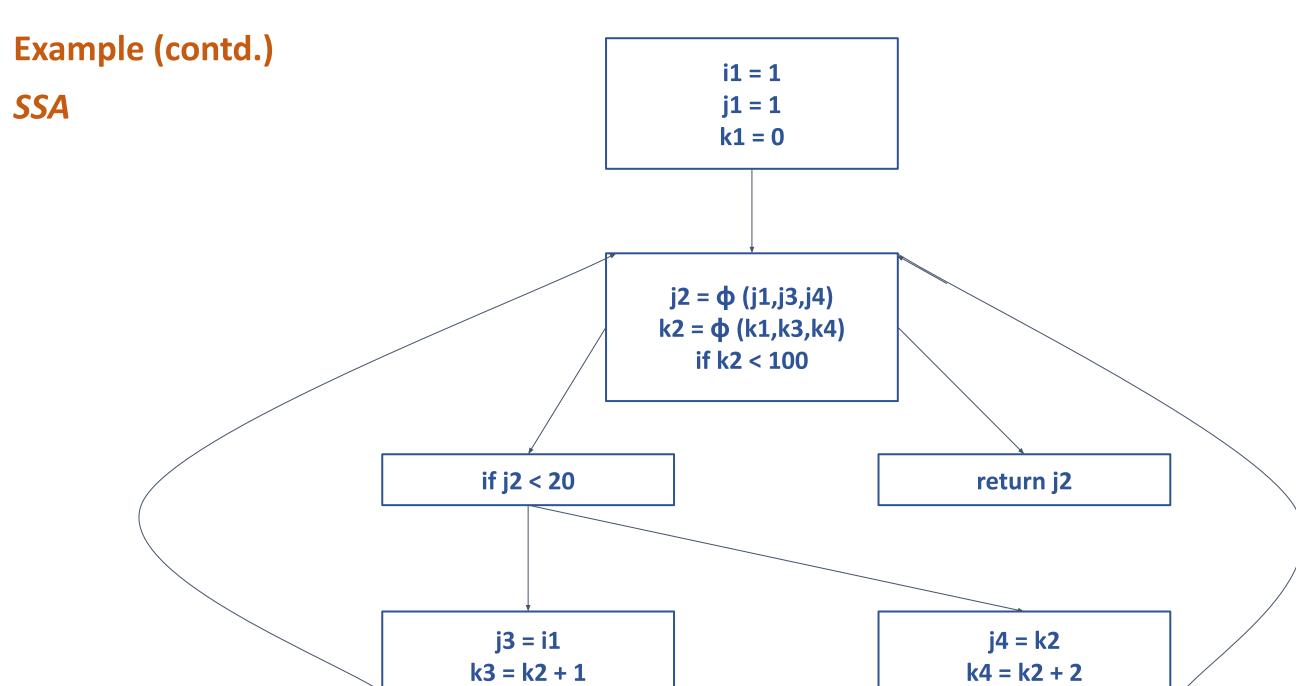
CFG





CFG

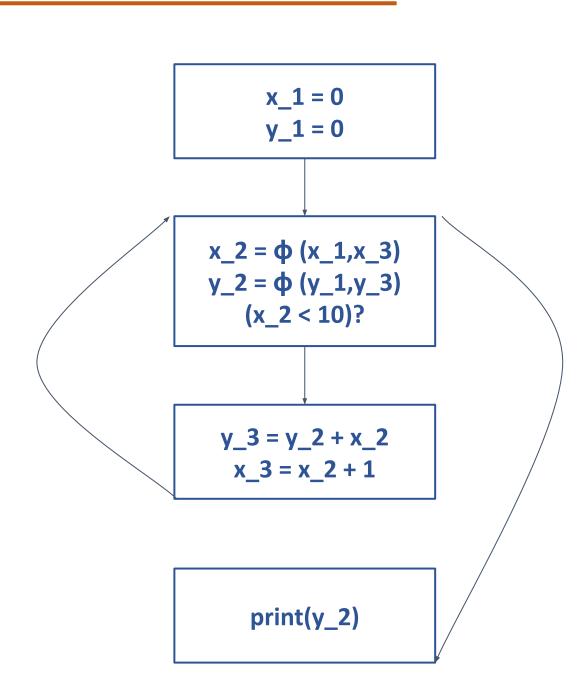




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Example

```
x = 0;
y = 0;
while (x<10){
y = y+x;
x = x+1;
}
print(y);</pre>
```



CFG



Example

```
prod = 0
i = 1
do
{

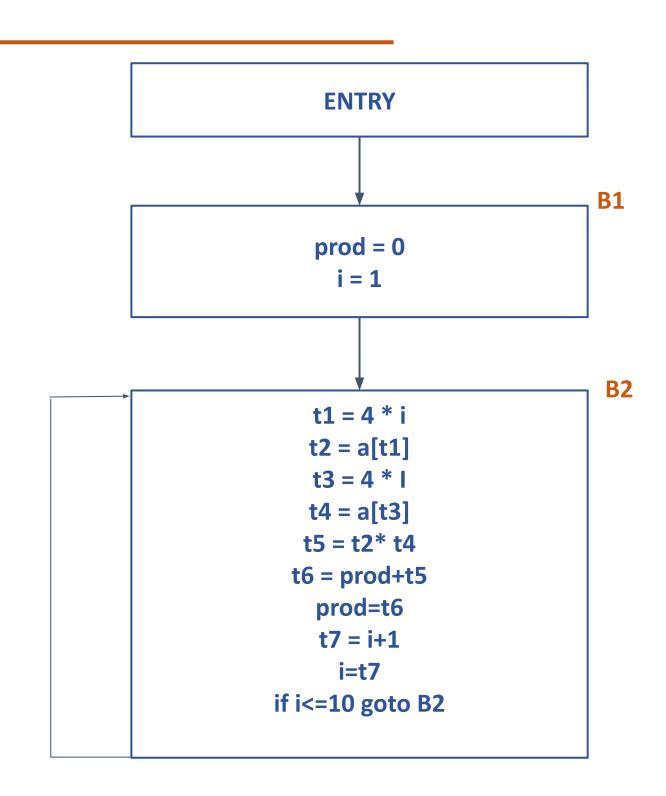
prod = prod + a[i] * b[i];
i = i + 1
}
while(i <= 10)</pre>
```

CFG



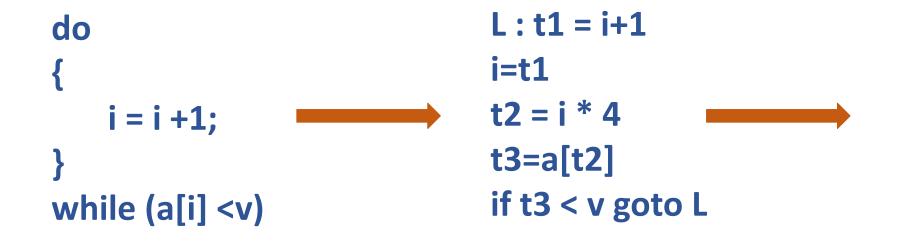
Example (contd.)

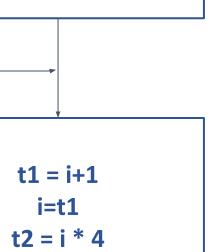
```
prod = 0
i = 1
L: t1 = 4 * i
t2 = a[t1]
t3 = 4 * i
t4 = a[t3]
t5 = t2* t4
t6 = prod+t5
prod=t6
t7 = i+1
i=t7
if i<=10 goto L
```



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Example





ENTRY

t3=a[t2]

if t3 < v goto L

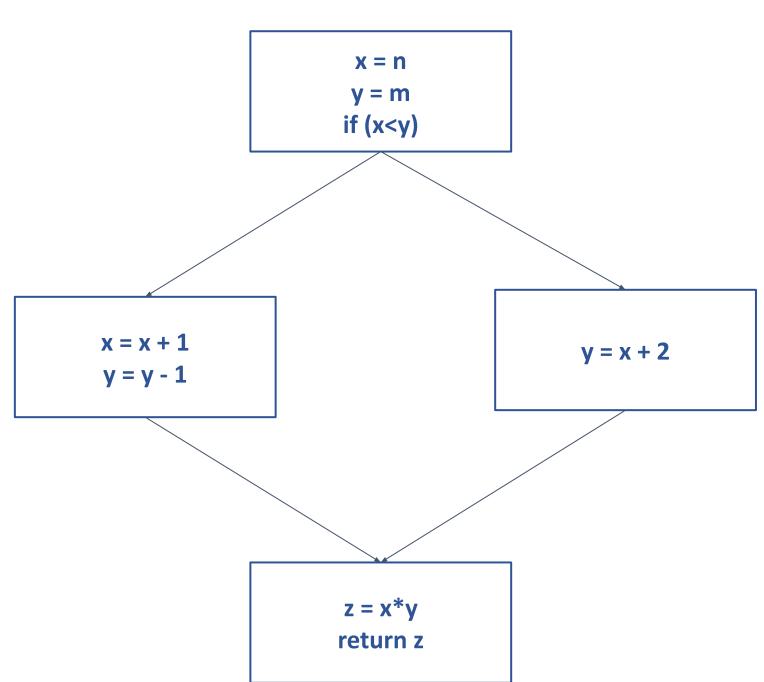
B1

CFG to SSA

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Example - Program to SSA

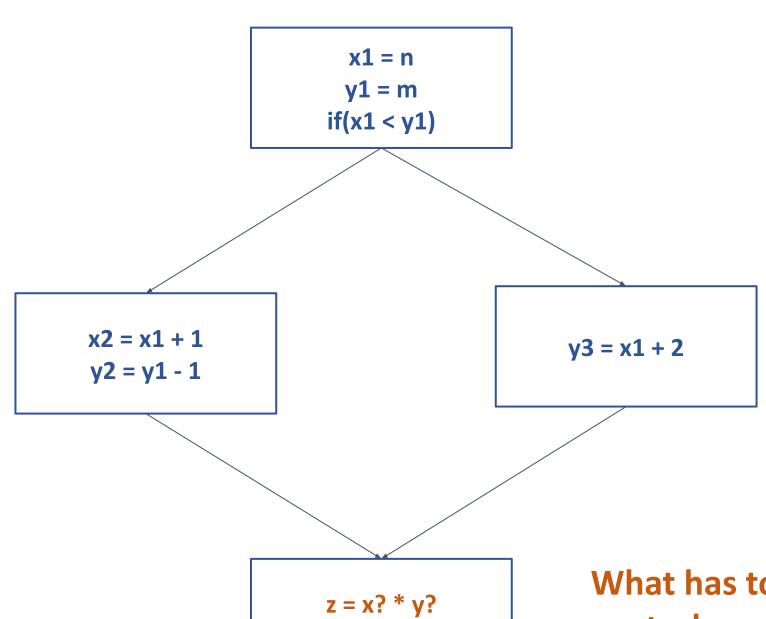
```
x = n
y = m
if(x < y)
   x = x + 1;
   y = y - 1;
else
   y = x + 2;
z = x * y;
return z;
```



Compiler Design CFG to SSA



Example(contd.)



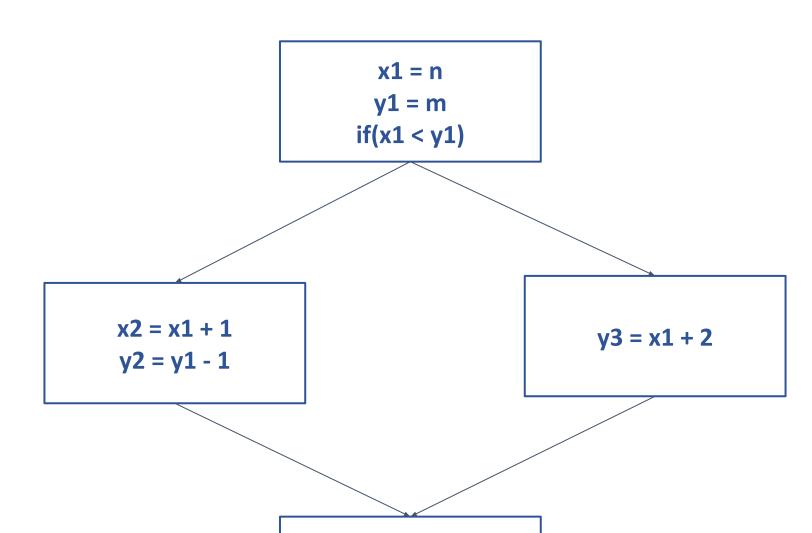
return z

What has to be done when control merges?

Compiler Design CFG to SSA

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Example(contd.)



set x3 to either x1 or x2 based on which control flow edge is used to get here

$$x3 = \phi(x1, x2)$$

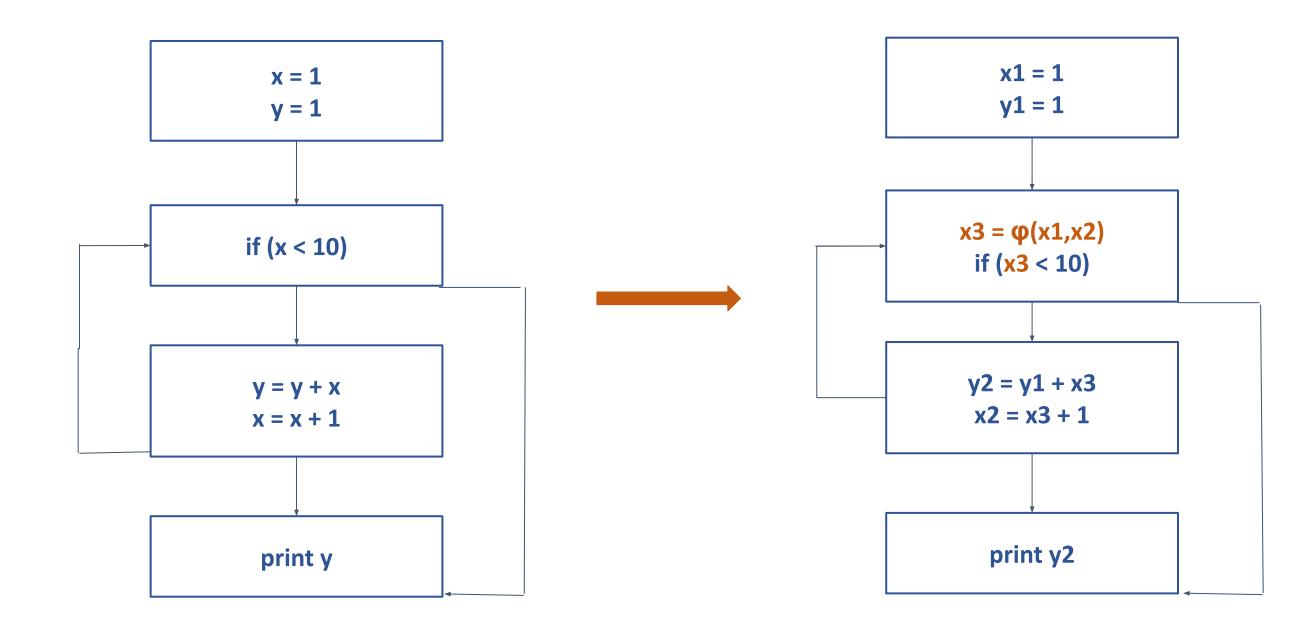
 $y4 = \phi(y2, y3)$
 $z1 = x3 * y4$
return z

set y4 to either y2 or y3 based on which control flow edge is used to get here

CFG



Example - CFG to SSA



Two Types of Questions



- 1) Convert a given program to Three address code and then construct the CFG.
- 2) Convert a given program to SSA
 - The question could specify the student to convert the program to CFG (change the working of every loop - while or for in terms of if loop) and then SSAify it.



THANK YOU

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Unit 4: Next-Use Algorithm

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Lecture Overview



In this lecture, you will learn about -

- Basic Block Generation Current Scenario
- Next-Use Information
- Next-Use Algorithm
- Examples

Basic Block Generation - Current Scenario



- Currently, in basic block generation -
 - We don't know through which path the flow-graph has taken us to reach the current basic block.
 - We can't assume that any variables are in registers.
 - We don't know where we will go from this block.
 - Thus, values kept in registers must be stored back into their memory locations before the block is exited.

Requirements



- We want to keep variables in registers for as long as possible, to avoid having to reload them whenever they are needed.
- When a variable isn't needed any more we need to free the register to reuse it for other variables.
- Thus, we must know if a particular value will be used later in the basic block, i.e, its next-use.

Next-Use Information



- Goal: To know when the value of a variable will be used next.
- Next-use information must be computed within a basic block.
- In the given example -
 - Statement S5 uses the value of X computed (defined) at L1.
 - That is, X is live at S1.
 - Also at S1, we say X's next use is at S5.
 - Thus, it is a good idea to keep X in a register between S1 and S5.
- Advantage knowing that a variable (assigned a register) is not used any further helps reassign the register to some other variable.

Compiler Design Assumptions



The following assumptions are made -

- All variables are live on exit. Thus, they will be stored back into their respective memory locations.
- Temporaries are dead on exit.

Next-use Algorithm



- It is a two-pass algorithm that computes next-use and liveness information of a basic block.
- Pass 1
 - In the first pass we scan forward over the basic block to find the end.
 - For each variable X used in the block we create fields X.live and X.next_use in the symbol table.
 - Set X.live:=FALSE; X.next use:=NONE;

Statement	X.live	Y.live	Z.live	X.next_use	Y.next_use	Z.next_use
i	False	False	False	-	-	-

Next-use Algorithm



• Pass 2

- Scan backwards over the basic block.
- \circ For every tuple (i) $x = y \circ p z$, do the following -
 - Copy the live/next use-info from x, y, z's symbol table entries into the tuple data for tuple (i).
 - Update x, y, z's symbol table entries as follows -

Statement	X.live	Y.live	Z.live	X.next_use	Y.next_use	Z.next_use
i	False	True	True	-	i	i

Example 1



• Go through the next-use algorithm for the following code

Statement		Sy	mbo	l Table	Info				Instruc	tion Inf	fo	
		live next-use						live		r	next-us	е
	X	Y	Z	X	Y	Z	X	Υ	Z	X	Y	Z
i												

Example 1 - Solution



First pass - Set live variables in each statement to False, next_use to None.

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	e
		X	Υ	Z	Х	Υ	Z	Х	Υ	Z	X	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	F	F	F				F	F	F			
(3)	y := z - 7	F	F	F				F	F	F			
(4)	x := z + y	F	F	F				F	F	F			

Example 1 - Solution



Second pass - Scan backwards over the basic block - start with (4)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		Х	Υ	Z	Х	Υ	Z	X	Υ	Z	X	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	F	F	F				F	F	F			
(3)	y := z - 7	F	F	F				F	F	F			
(4)	x := z + y	F	<i>T</i>	T	-	4	4	F	F	F			

Example 1 - Solution



Copy the live/next use-info from x, y, z's symbol table entries into the tuple data.

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		Х	Υ	Z	Х	Υ	Z	X	Υ	Z	X	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	F	F	F				F	F	F			
(3)	y := z - 7	F	F	F				F	T	<i>T</i>	-	4	4
(4)	x := z + y	F	<i>T</i>	<i>T</i>	-	4	4	F	F	F			

Example 1 - Solution



Statement (3)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		X	Υ	Z	Х	Υ	Z	Х	Υ	Z	Х	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	F	F	F				F	F	F			
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	Τ	-	4	4	F	F	F			

Example 1 - Solution



Statement (3)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		Х	Υ	Z	Х	Υ	Z	Х	Υ	Z	Х	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	F	F	F				F	F	T	-	-	3
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	T	-	4	4	F	F	F			

Example 1 - Solution



Statement (2)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		X	Υ	Z	Х	Υ	Z	Х	Υ	Z	X	Υ	Z
(1)	x := y + z	F	F	F				F	F	F			
(2)	z := x * 5	T	F	F	2	-	-	F	F	T	-	-	3
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	T	-	4	4	F	F	F			

Example 1 - Solution



Statement (2)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		Х	Υ	Z	Х	Υ	Z	X	Υ	Z	X	Υ	Z
(1)	x := y + z	F	F	F				T	F	F	2	-	-
(2)	z := x * 5	<i>T</i>	F	F	2	-	-	F	F	T	-	-	3
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	T	-	4	4	F	F	F			

Example 1 - Solution



Statement (1)

	Statement		Syn	nbol	Table	Info			In	struc	tion I	nfo	
			live		n	ext-u	se		live		n	ext-us	se
		Х	Υ	Z	Х	Υ	Z	X	Υ	Z	X	Y	Z
(1)	x := y + z	F	T	T	-	1	1	T	F	F	2	-	-
(2)	z := x * 5	T	F	F	2	-	-	F	F	T	-	-	3
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	T	-	4	4	F	F	F			

Example 1 - Solution



	Statement		Syn	nbol	Table	Info			lr	istruc	ction I	nfo	
			live		n	ext-u	se		live		r	ext-us	e
		X	Υ	Z	Х	Υ	Z	X	Υ	Z	Х	Υ	Z
(1)	x := y + z	F	T	T	-	1	1	T	F	F	2	-	-
(2)	z := x * 5	T	F	F	2	-	-	F	F	T	-	-	3
(3)	y := z - 7	F	F	T	-	-	3	F	T	T	-	4	4
(4)	x := z + y	F	T	T	-	4	4	F	F	F	-	-	-

The data in each row reflects the state in the symbol table and in the data section of each instruction i after i has been processed.

Example 2



Go through the next-use algorithm for the following code -

$$(1) a = a - b$$

(2)
$$u = a - c$$

$$(3) v = t + u$$

$$(4) d = v + u$$

Statement					Sy	mk	ool	Tak	ole	Inf	O								In	str	uct	ior	ı In	fo				
			I	ive						ne	ext-	·use						live	9					ne	ext-	use		
	A	В	С	D	Т	U	V	A	В	С	D	Т	U	V	A	В	С	D	Т	U	V	A	В	С	D	Т	U	V

Example 2 - Solution



First pass - Set live variables in each statement to False, next_use to None.

St	atement					Sy	mk	ool	Tal	ole	Inf	fo								In	str	uct	ior	ı In	fo				
					live	9					n	ext-	-use	9					live	9					ne	ext-	use)	
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	A	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
3	v = t+ u	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
4	d = v +u	F	F	F	F	F	F	F								F	F	F	F	F	F	F							

Example 2 - Solution



Second pass - Scan backwards over the basic block - start with (4)

St	atement		Symbol Table Info																	In	str	uct	ior	ı In	fo				
			live next-use																live	9					ne	ext-	use		
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
3	v = t+ u	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Copy the live/next use-info from symbol table entries into the tuple data.

St	atement					Sy	mk	ool	Tak	ole	Inf	O								In	str	uct	ior	ı In	fo				
					live	9					ne	ext-	use	9					live	9					ne	ext-	use		
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	A	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
3	v = t+ u	F	F F F F F F F													F	F	F	F	F	T	<i>T</i>	-	-	-	-	-	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Statement (3)

St	atement		Symbol Table Info																	In	str	uct	ior	ı In	fo				
			live next-use																live	9					ne	ext-	use	1	
		A	В	С	D	Т	U	V	A	В	С	D	Т	U	V	A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
3	v = t + u	F	F	F	F	<i>T</i>	T	F	-	-	-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	_	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Statement (3)

St	atement		Symbol Table Info																	In	str	uct	ior	ı In	fo				
			live next-use																live	2					ne	ext-	use		
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	F	F	F	F	F	F	F								F	F	F	F	T	T	F	_	_	-	-	3	3	-
3	v = t + u	F	F	F	F	<i>T</i>	T	F	-	-	-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	_	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Statement (2)

St	atement					Sy	mk	ool	Tal	ole	Inf	fo								lr	str	uct	ior	ı In	fo				
			live next-use A B C D T U V A B C D T U V																live	9					ne	ext-	use)	
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								F	F	F	F	F	F	F							
2	u = a - c	T	F	<i>T</i>	F	F	F	F	2	-	2	-	-	-	-	F	F	F	F	T	Τ	F	-	-	-	-	3	3	-
3	v = t+ u	F									-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	-	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Statement (2)

St	atement					Sy	mk	ool	Tal	ole	Inf	fo								In	str	uct	ior	n In	fo				
					live	9					n	ext-	·use						live	9					ne	ext-	use	i I	
		A	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	A	В	С	D	Т	U	V
1	a = a - b	F	F	F	F	F	F	F								<i>T</i>	F	T	F	F	F	F	2	-	2	-	-	-	-
2	u = a - c	<i>T</i>	F	<i>T</i>	F	F	F	F	2	-	2	-	-	-	-	F	F	F	F	T	T	F	-	-	-	-	3	3	-
3	v = t + u	F	F	F	F	T	T	F	-	-	-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	-	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Statement (1)

St	atement		Symbol Table Info																	lr	str	uct	ior	ı In	fo				
		live next-use																	live	9					ne	ext-	use		
		Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	Α	В	С	D	Т	U	V	A	В	С	D	Т	U	V
1	a = a - b	T	T	F	F	F	F	F	1	1	-	-	-	-	-	T	F	T	F	F	F	F	2	-	2	-	-	-	-
2	u = a - c	T	F	T	F	F	F	F	2	-	2	-	-	-	-	F	F	F	F	T	Τ	F	-	-	-	-	3	3	-
3	v = t + u	F	F	F	F	T	T	F	-	-	-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	-	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F							

Example 2 - Solution



Finally -

St	atement		Symbol Table Info																	lr	str	uct	ior	ı In	fo				
			live next-use A B C D T U V A B C D T U V																live	9					ne	ext-	use)	
		A	В	С	D	Т	U	V	A	В	С	D	Т	U	V	A	В	С	D	T	U	V	A	В	С	D	Т	U	V
1	a = a - b	T	T	F	F	F	F	F	1	1	-	-	-	-	-	T	F	T	F	F	F	F	2	-	2	-	-	-	-
2	u = a - c	T	F	T	F	F	F	F	2	-	2	-	-	-	-	F	F	F	F	T	T	F	-	-	-	-	3	3	-
3	v = t + u	F F F F T T F								-	-	-	3	3	-	F	F	F	F	F	T	T	-	-	-	-	-	4	4
4	d = v +u	F	F	F	F	F	T	T	-	-	-	-	-	4	4	F	F	F	F	F	F	F	-	-	-	-	-	-	-

Example 3 - Homework



Go through the next-use algorithm for the following code -

$$(2) v := c - a$$

$$(3) a := u + v$$

S	tatement			Syı	mb	ol ⁻	Гab	le	Info	0				Ir	ıstr	uct	ior	n In	fo		
			ı	ive				ne	ext-	use				live	9			ne	xt-	use	
		A	В	С	U	V	A	В	С	U	V	A	В	С	U	V	A	В	С	U	V
1	u = a - b																				
2	v = c - a																				
3	a = u + v																				



THANK YOU

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