Fiche d'entraînement : trigonométrie (équations)

Résoudre les équations suivantes :

1)
$$\cos(x) = \frac{\sqrt{2}}{2}$$

a) dans $]-\pi$; π]

b) dans $[0; 2\pi[$

2)
$$\sin(x) = -\frac{1}{2}$$

a) dans $] - \pi ; \pi]$

b) dans $[0; 2\pi[$

3)
$$\cos(x) = \frac{1}{2}$$

a) dans $]-\pi$; π]

b) dans $[0; 2\pi[$

4)
$$\sin(x) = \frac{1}{2}$$

a) dans $] - \pi$; π]

b) dans $[0; 2\pi[$

5)
$$\cos(x) = -\frac{1}{2}$$

a) dans $]-\pi$; π]

b) dans $[0; 2\pi[$

6)
$$\sin(x) = -\frac{\sqrt{2}}{2}$$

a) dans $]-\pi$; π]

b) dans $[0; 2\pi[$

Solutions

1) **a)**
$$S = \left\{ -\frac{\pi}{4} ; \frac{\pi}{4} \right\}$$

b)
$$S = \left\{ \frac{\pi}{4} ; \frac{7\pi}{4} \right\}$$

2) a)
$$S = \left\{ -\frac{5\pi}{6}; -\frac{\pi}{6} \right\}$$

b)
$$S = \left\{ \frac{7\pi}{6} ; \frac{11\pi}{6} \right\}$$

3) a)
$$S = \left\{ -\frac{\pi}{3} ; \frac{\pi}{3} \right\}$$

b)
$$S = \left\{ \frac{\pi}{3} ; \frac{5\pi}{3} \right\}$$

4) a)
$$S = \left\{ -\frac{\pi}{6}; -\frac{5\pi}{6} \right\}$$

b)
$$S = \left\{ \frac{\pi}{6} \; ; \; \frac{5\pi}{6} \right\}$$

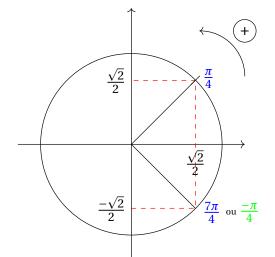
5) a)
$$S = \left\{ -\frac{2\pi}{3}; -\frac{2\pi}{3} \right\}$$

b)
$$S = \left\{ \frac{2\pi}{3} ; \frac{4\pi}{3} \right\}$$

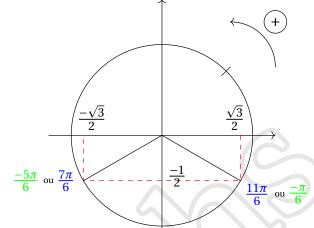
6) a)
$$S = \left\{ -\frac{3\pi}{4}; -\frac{\pi}{4} \right\}$$

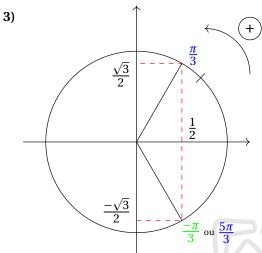
b)
$$S = \left\{ \frac{5\pi}{4} \; ; \; \frac{7\pi}{4} \right\}$$

1)

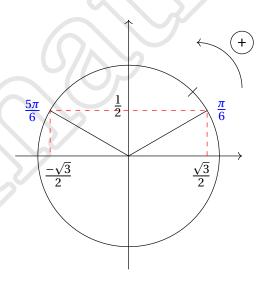


2)

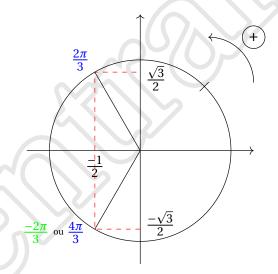




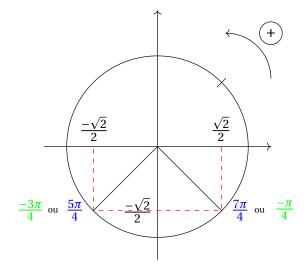
4)



5)



6)



Résoudre les inéquations suivantes :

1)
$$\sin(x) \ge \frac{\sqrt{3}}{2}$$

- a) dans $]-\pi$; π]
- **b)** dans $[0; 2\pi[$
- **2)** $\cos(x) \le \frac{1}{2}$
 - a) dans $]-\pi$; π]
 - **b)** dans $[0; 2\pi]$
- **3)** $\sin(x) \le \frac{1}{2}$
 - **a)** dans $]-\pi$; π]
 - **b)** dans $[0; 2\pi[$
- **4)** $\cos(x) \ge -\frac{\sqrt{3}}{2}$
 - a) dans $]-\pi$; π]
 - **b)** dans $[0; 2\pi[$

5)
$$-\frac{1}{2} \le \sin(x) \le \frac{\sqrt{3}}{2}$$

- a) dans $]-\pi$; π]
- **b)** dans $[0; 2\pi[$

6)
$$-\frac{\sqrt{2}}{2} \le \cos(x) \le \frac{1}{2}$$

- **a)** dans $] \pi ; \pi]$
- **b)** dans $[0; 2\pi[$

Solutions

1) **a)**
$$S = \left[\frac{\pi}{3}; \frac{2\pi}{3} \right]$$

b)
$$S = \left[\frac{\pi}{3} ; \frac{2\pi}{3} \right]$$

2) a)
$$S = \left[-\pi ; \frac{-\pi}{3} \right] \cup \left[\frac{\pi}{3} ; \pi \right]$$

b)
$$S = \left[\frac{\pi}{3}; \frac{5\pi}{3} \right]$$

3) a)
$$S = \left] -\pi \; ; \; \frac{\pi}{6} \right] \cup \left[\frac{5\pi}{6} \; ; \; \pi \right]$$

b)
$$S = \left[0; \frac{\pi}{6}\right] \cup \left[\frac{5\pi}{6}; 2\pi\right]$$

4) a)
$$S = \left[\frac{-5\pi}{6} ; \frac{5\pi}{6} \right]$$

b)
$$S = \left[0; \frac{5\pi}{6}\right] \cup \left[\frac{7\pi}{6}; 2\pi\right]$$

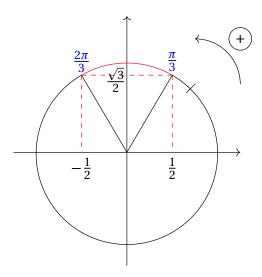
5) a)
$$S = \left[-\pi; -\frac{5\pi}{6} \right] \cup \left[-\frac{\pi}{6}; \frac{\pi}{3} \right] \cup \left[\frac{2\pi}{3}; \pi \right]$$

b)
$$S = \left[0; \frac{\pi}{3}\right] \cup \left[\frac{2\pi}{3}; \frac{7\pi}{6}\right] \cup \left[\frac{11\pi}{6}; 2\pi\right]$$

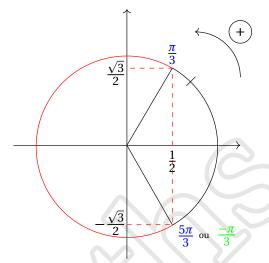
6) a)
$$S = \left[-\frac{3\pi}{4}; -\frac{\pi}{3} \right] \cup \left[\frac{\pi}{3}; \frac{3\pi}{4} \right]$$

b)
$$S = \left[\frac{\pi}{3} \; ; \; \frac{3\pi}{4} \right] \cup \left[\frac{5\pi}{4} \; ; \; \frac{5\pi}{3} \right]$$

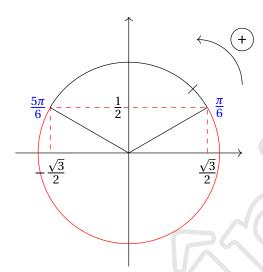
1)



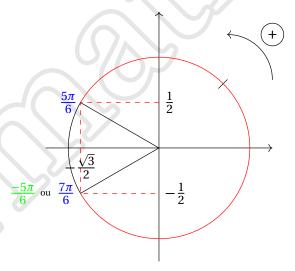
2)

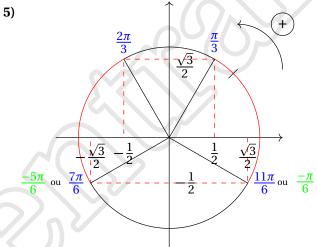


3)



4)





6)

