

# Side Channel Attacks

## -- More Attacks and Countermeasures

Cybersecurity Specialization  
-- Hardware Security

## RSA Algorithm

### # Key generation:

- Generate large (say, 2048-bit) primes  $p, q$
- Compute  $n=pq$
- Choose small  $e$ , relatively prime to  $(p-1)(q-1)$
- Compute the unique  $d$  such that  $ed = 1 \bmod (p-1)(q-1)$
- Public key =  $(e, n)$ ; private key =  $d$ 
  - Security relies on the assumption that it is difficult to factor  $n$  into  $p$  and  $q$

### # Encryption of $m$ : $c = m^e \bmod n$

### # Decryption of $c$ : $c^d \bmod n = (m^e)^d \bmod n = m$

### # Square and multiply for " $y^x \bmod n$ ".

## Kocher's Timing Attack on RSA

- # Guess some bits of the exponent and predict how long decryption will take.
- # Run decryption and compare the run time with the prediction.
  - if the guess is correct, correlation in execution time can be observed
  - otherwise, the prediction will look random
- # Start by guessing a few top bits, look at correlations for each guess, pick the most promising candidate and continue.

## Montgomery Reduction

- # Let  $R > N$  be two integers and  $\gcd(N, R) = 1$ . For  $0 \leq T < NR$ , the Montgomery reduction of  $T$  modulo  $N$  w.r.t.  $R$  is defined as  $TR^{-1} \pmod{N}$ .
- # Montgomery reduction algorithm
  - $m = T \times (-N^{-1}) \pmod{R}$
  - $t = (T + mN)/R$
  - if  $(N \leq t)$
  - $t = t - N$
- # Claim:  $t = TR^{-1} \pmod{N}$ 
  - $tR = T \pmod{N}$
  - $0 \leq t < N$

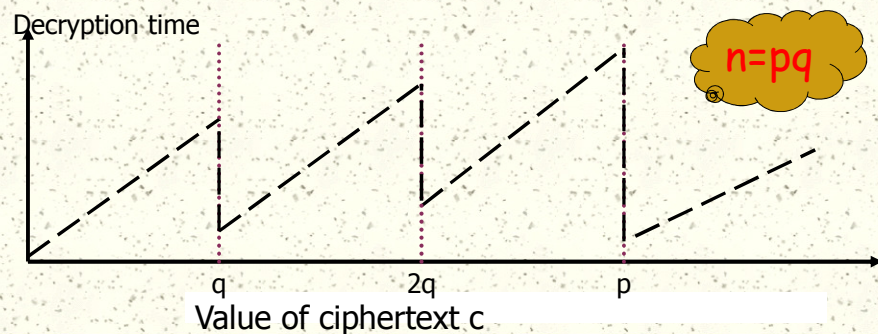
Montgomery reduction can be used to compute modular multiplication efficiently

for larger  $T$ , multiple subtractions will be needed to have  $t < N$



## Schindler's Observation

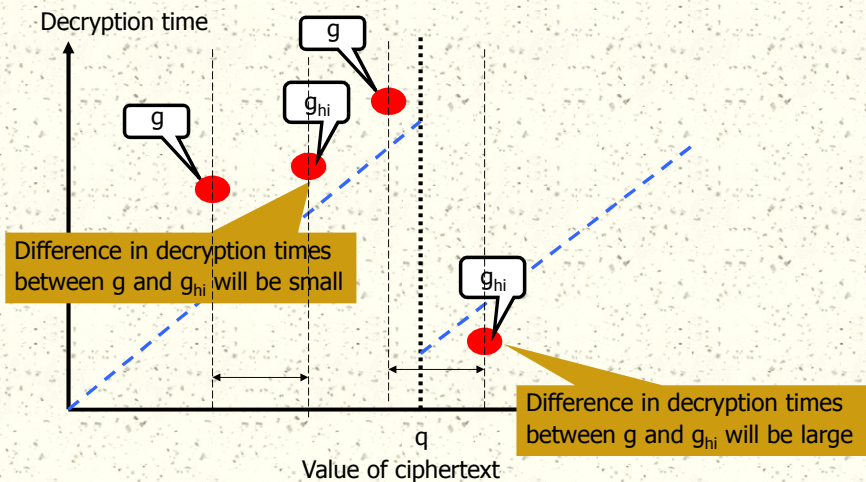
- # Probability of the subtraction step  $\propto c \bmod q$ 
  - If  $c$  is close to  $q$ , a lot of subtractions will be needed
  - If  $c \bmod q = 0$ , very few subtractions
- # An attacker can guess  $q$  by observing the decryption time with different values of  $c$ .



## Attack Overview

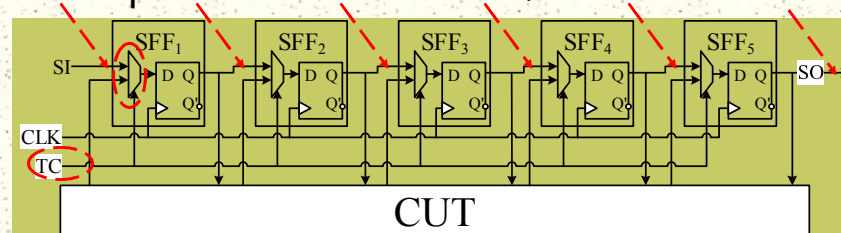
- # Initial guess  $g$  for  $q$  between  $2^{511}$  and  $2^{512}$  (for 1024-bit RSA)
- # Try all possible guesses for the top few bits
- # Suppose we know that top  $i-1$  bits of  $q$  are **101001**, to guess the  $i^{\text{th}}$  bit
  - Set  $g = \text{101001000...000}$
  - Set  $g_{hi} = \text{101001100...000}$
  - If  $g < q < g_{hi}$  then the  $i^{\text{th}}$  bit of  $q$  is 0
  - If  $g < g_{hi} < q$  then the  $i^{\text{th}}$  bit of  $q$  is 1

## Determine the Next Bit for q



# Scan Chain Attacks

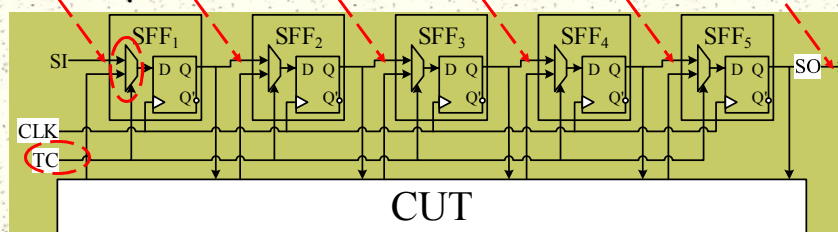
- # Attacks based on observability
  - TC=0, provide primary input to the system
  - TC=0, run for one or more clock cycles
  - TC=1, test mode to capture internal state from scan out
  - Repeat to collect more information





## Scan Chain Attacks

- # Attacks based on **controllability**
  - **TC=1, test mode to set the system state**
  - TC=0, run for one or more clock cycles
  - TC=1, test mode to capture internal state from scan out
  - Repeat to collect more information



## Countermeasures to SCA

- # Hiding
  - Make it more challenging for the attackers to extract information from side channels
  - Noise generator
    - Use extra circuits to draw current randomly or add random delay to certain paths or logic units
    - Keep the total power consumption constant
    - Add EM noise
  - Balanced logic styles
    - Make logic unit's power/delay independent of input data (and the key)

## Countermeasures to SCA

### # Hiding

- Asynchronous logic
  - No clock and global synchronization, so many side channel attacks will fail
- Low power design
  - Reduce total power weakens the signals from most of the side channels.
- Shielding
  - Physically shield or filter the side channel leakage
  - Use the upper level metal layer (EM emission)
  - Use sound dampening materials (acoustic)

## Countermeasures to SCA

### # Hiding

### # Masking/blinding

- Remove the correlation between input data and side channel emissions.
- Gate level: XOR the output of a logic unit with pre-selected data values to mask the real values
  - Word level: randomize input data, might be hard because the operation needs to be modified as well to generate the correct output



## Countermeasures to SCA

- # Hiding
- # Masking/blinding
- # Design partitioning/separation
  - Memory: RED (plain text) vs. BLACK (cipher text)
  - On-chip infrastructure: power supply, clock network, testing
  - Fabrication: 3D stacking, split fabrication
- # Physical security
  - Denial of proximity, access, and possession
  - Acoustic shielding of the target devices
  - Secure zone (against EM emission attacks)