# ps\_6

#### March 14, 2019

## 1 Problem Set 6: Welfare Instrumental Variables

```
In [1]: import numpy as np
        import pandas as pd
        from pathlib import Path
        import matplotlib.pyplot as plt
        import seaborn as sns
        import requests
        from IPython.display import display
        import statsmodels.api as sm
        import statsmodels.formula.api as smf
        from linearmodels.iv import IV2SLS
        %matplotlib inline
        sns.set_style('darkgrid')
In [2]: def fetch_and cache(data_url, file, data_dir="data", force = False):
            11 11 11
            (Credit: John DeNero)
            Download and cache a url and return the file object.
            Dependent: from pathlib import Path
            import requests
            data url: the web address to download
            file: the file in which to save the results.
            data dir: (default="data") the location to save the data
            force: if true the file is always re-downloaded
            return: The pathlib.Path to the file.
            data_dir = Path(data_dir)
            data_dir.mkdir(exist_ok=True)
            file_path = data_dir/Path(file)
            if force and file_path.exists():
                file_path.unlink()
            if force or not file_path.exists():
                print('Downloading...', end = ' ')
                resp = requests.get(data_url)
                with file_path.open('wb') as f:
                    f.write(resp.content)
```

```
print('Done!')
else:
    import time
    created = time.ctime(file_path.stat().st_ctime)
    print("Using cached version downloaded at", created)
    return file_path

data_urls = r"https://bcourses.berkeley.edu/files/74717033/download?download_frd=1"
file_names = r"welfare.csv"

file = fetch_and_cache(data_urls, file_names)

welfare_df = pd.read_csv(file)
display(welfare_df.head())
```

Using cached version downloaded at Fri Mar 8 14:20:01 2019

	imm	hsgrad	agelt25	age35p	treatment	working_at_baseline	anykidsu6	\
0	0	0	0	0	1	0	1	
1	0	1	0	1	1	0	0	
2	0	0	0	0	1	0	0	
3	0	0	0	0	0	1	0	
4	0	1	0	0	0	0	1	

	nevermarried	ft15	ft20	ft24	ft48	welfare15	welfare20	welfare24	\
0	1	0	0.0	0.0	0.0	1	1	1	
1	1	1	1.0	1.0	NaN	0	0	0	
2	1	0	0.0	0.0	0.0	1	1	1	
3	0	0	0.0	0.0	0.0	1	0	0	
4	1	0	0.0	0.0	0.0	1	1	1	

In [3]: welfare\_df.dropna(inplace = True)

#### 1.1 1)

We are interested in casual model of working full time affects welfare participation. Our casual model is

$$(1) y_i = \beta_0 + \beta_1 F T_i + u_i$$

where  $y_i$  is an indicator equal to 1 if parent i is on welfare in period t, and  $FT_i$  is indicator for full time status in the month. We are going to use "assigned to the treatment group" as our instrument, so  $z_i = T_i := Treatment_i$ . We will allow for different coefficients for different time horizon effects.

```
In [4]: months = [15, 20, 24, 48]

fts = ["ft{}".format(month) for month in months]
  welfares = ["welfare{}".format(month) for month in months]
```

#### 1.1.1 a)

Estimate first stage models for the probability of working FT in months 15, 20, 24, 48, using treatment as the instrument and no other controls.

$$FT_i = \pi_0 + \pi_1 T_i + \eta_i$$

There will be separate estimates of  $\pi_0$ ,  $\pi_1$  for each of months 15, 20, 24, 48.

```
In [5]: models = ["{} ~ 1 + treatment".format(ft) for ft in fts]

results = []
for model in models:
    results.append(smf.ols(formula = model, data = welfare_df, missing = 'drop').fit()
    #Must drop missing values since linearmodels (which is being used for IV estimatio)

pis = pd.DataFrame(
    {ft:result.params for ft, result in zip(fts, results)}
)
    display(pis)

ft15    ft20    ft24    ft48

Intercept 0.151399 0.162850 0.161154 0.233673
treatment 0.142694 0.114427 0.107509 0.050577
```

### 1.1.2 b)

Estimate reduced form models for the probability of being on welfare in months 15, 20, 24, 48, using treament as the instrumental variable and no other control variables.

$$y_i = \gamma_0 + \gamma_1 T_i + \nu_i$$

There will be separate estimates of  $\gamma_0$ ,  $\gamma_1$  for each of months 15, 20, 24, 48.

```
gammas = pd.DataFrame(
            {welfare:result.params for welfare, result in zip(welfares, results)}
        display(gammas)
           welfare15 welfare20 welfare24 welfare48
Intercept
            0.809584
                      0.769720
                                  0.738762
                                               0.591603
treatment -0.147977 -0.122058 -0.107507 -0.041972
1.1.3 c)
Esimate the casual model (1) by OLS for each of months 15,20,24,48.
In [7]: models = ["{} ~ 1 + {}".format(welfare, ft)
                   for welfare, ft in zip(welfares, fts)]
        results = []
        for model in models:
            results.append(smf.ols(formula = model, data = welfare_df, missing = "drop").fit()
        ols_betas = pd.DataFrame(
            {welfare:result.params for welfare, result in zip(welfares, results)}
        display(ols_betas)
           welfare15 welfare20 welfare24 welfare48
            0.861634
                      0.832976
                                   0.798990
                                               0.708896
Intercept
           -0.568337
ft15
                             {\tt NaN}
                                         \mathtt{NaN}
                                                     NaN
ft20
                      -0.566939
                 {\tt NaN}
                                         NaN
                                                     NaN
ft24
                 {\tt NaN}
                             {\tt NaN}
                                  -0.532323
                                                     NaN
ft48
                 NaN
                             {\tt NaN}
                                         NaN -0.534459
1.1.4 d)
Estimate the causal model by IV in each of months 15, 20, 24, 48.
In [8]: models = ["{0} ~ 1 + [{1} ~ treatment]".format(welfare, ft)
                   for welfare, ft in zip(welfares, fts)]
        results = []
        for model in models:
```

results.append(IV2SLS.from\_formula(

).fit())

betas = pd.DataFrame(

formula = model, data = welfare\_df

```
{welfare:result.params for welfare, result in zip(welfares, results)}
        )
        display(betas)
            welfare15 welfare20
                                   welfare24
                                               welfare48
Intercept
             0.966589
                         0.943431
                                     0.899911
                                                 0.785521
            -1.037020
ft15
                              {\tt NaN}
                                          NaN
                                                      NaN
ft20
                       -1.066693
                                          NaN
                                                      NaN
                  NaN
                                   -0.999974
ft24
                  NaN
                              {\tt NaN}
                                                      NaN
                              NaN
                                          NaN -0.829871
ft48
                  NaN
1.1.5 e)
Verify that in each month, \hat{\beta_1}^{IV} = \hat{\gamma_1}/\hat{\pi_1}.
In [9]: for welfare, ft, month in zip(welfares, fts, months):
             g_over_p = gammas[welfare].loc["treatment"] / pis[ft].loc["treatment"]
             print("for month {2}:\n beta_hat: {0} \n gamma_pi_ratio: {1}" .format(
                 betas[welfare].loc[ft], g_over_p, month))
for month 15:
 beta_hat: -1.037019699629429
 gamma_pi_ratio: -1.0370196996294272
for month 20:
 beta_hat: -1.0666934218687558
 gamma_pi_ratio: -1.0666934218687738
for month 24:
 beta_hat: -0.9999741121268855
 gamma_pi_ratio: -0.9999741121268908
for month 48:
 beta hat: -0.8298710946635879
 gamma_pi_ratio: -0.8298710946635985
```

We clearly see that  $\hat{\beta}_1^{IV} = \hat{\gamma}_1 / \hat{\pi}_1$  holds in every month observed.

#### 1.2 2)

Now repeat steps (a) - (e) from question (1) for month 15 only, but including as controls the variables {imm, hsgrad, agelt25, age35p, working\_at\_baseline, anykidsu6, nevermarried} in your first stage model, your reduced form model, and your OLS and IV versions of the causal model. Because SSP was a randomized experiment,  $T_i$  is (approximately) uncorrelated with all these control variables. Does their addition affect your different estimates?

```
In [10]: additional_variables = "imm + hsgrad + agelt25 + age35p + working_at_baseline + anyking_at_baseline + anyking_at_basel
```

```
1.2.1 a)
In [11]: models = ["{} ~ 1 + treatment + {}".format(ft, additional_variables) for ft in fts]
        results = []
        for model in models:
            results.append(smf.ols(formula = model, data = welfare_df, missing = 'drop').fit(
            #Must drop missing values since linearmodels (which is being used for IV estimati
        pis = pd.DataFrame(
            {ft:result.params for ft, result in zip(fts, results)}
        )
        display(pis)
                        ft15
                                  ft20
                                           ft24
                                                     ft48
Intercept
                    0.089979 0.080885 0.092306 0.157485
treatment
                    0.141824 0.113821 0.106826 0.048997
imm
                   -0.052285 -0.025376 -0.028026 -0.014446
                   0.092977 0.100354 0.101047 0.128781
hsgrad
agelt25
                    0.014932 0.021334 0.037112 0.047044
                   -0.042554 -0.022191 -0.036641 -0.032199
age35p
working_at_baseline 0.271514 0.244647 0.231532 0.190155
anykidsu6
                   -0.021173 -0.007451 -0.011784 -0.035446
                  -0.009805 -0.002040 -0.015590 0.006294
nevermarried
1.2.2 b)
In [12]: models = ["{} ~ 1 + treatment + {}".format(welfare, additional_variables)
                 for welfare in welfares]
        results = []
        for model in models:
            results.append(smf.ols(formula = model, data = welfare_df, missing = 'drop').fit(
        gammas = pd.DataFrame(
            {welfare:result.params for welfare, result in zip(welfares, results)}
        display(gammas)
                    welfare15 welfare20 welfare24 welfare48
Intercept
                     treatment
                    -0.146921 -0.120974 -0.106730 -0.039979
imm
                     0.035602 0.046574 0.057187 0.028725
hsgrad
                    -0.106124 -0.114205 -0.122399 -0.156687
                    -0.029367 \quad -0.033101 \quad -0.042715 \quad -0.090572
agelt25
age35p
                     0.062799 0.053035 0.045522 0.050122
working_at_baseline -0.222330 -0.223736 -0.218009 -0.193014
anykidsu6
                     0.017565 0.012456 -0.009699 0.046499
```

```
1.2.3 c)
In [13]: models = ["{} ~ 1 + {} + {}".format(welfare, ft, additional_variables)
                  for welfare, ft in zip(welfares, fts)]
        results = []
        for model in models:
            results.append(smf.ols(formula = model, data = welfare_df, missing = "drop").fit(
        ols_betas = pd.DataFrame(
            {welfare:result.params for welfare, result in zip(welfares, results)}
        )
        display(ols_betas)
                    welfare15 welfare20 welfare24 welfare48
Intercept
                     0.864487
                               0.828490 0.813167 0.719825
                     age35p
agelt25
                    -0.020830 -0.021300 -0.024015 -0.067026
anykidsu6
                    0.008149 0.010162 -0.014012 0.029275
ft15
                    -0.537471
                                    {\tt NaN}
                                               NaN
                                                          NaN
ft20
                          NaN -0.532697
                                               {\tt NaN}
                                                          NaN
                                    NaN -0.493343
ft24
                          NaN
                                                          NaN
ft48
                          {\tt NaN}
                                    NaN
                                               NaN -0.498130
                    -0.057406 -0.061818 -0.073507 -0.092814
hsgrad
imm
                     0.008339
                              0.033772 0.044002 0.021714
nevermarried
                     0.035033
                              0.049985
                                          0.058946 0.050059
working_at_baseline -0.075483 -0.092631 -0.103084 -0.098090
1.2.4 d)
In [14]: models = ["{0} ~ 1 + [{1} ~ treatment] + {2}".format(welfare, ft, additional_variable
                  for welfare, ft in zip(welfares, fts)]
        results = []
        for model in models:
            results.append(IV2SLS.from_formula(
                formula = model, data = welfare_df
            ).fit())
        betas = pd.DataFrame(
            {welfare:result.params for welfare, result in zip(welfares, results)}
        )
        display(betas)
                    welfare15 welfare20 welfare24 welfare48
```

```
Intercept
                       0.946299
                                  0.902918
                                             0.888098
                                                         0.778018
age35p
                      0.018716
                                  0.029449
                                             0.008914
                                                        0.023850
agelt25
                     -0.013898 \quad -0.010426 \quad -0.005636 \quad -0.052187
anykidsu6
                     -0.004368
                                  0.004536
                                            -0.021472
                                                         0.017577
ft15
                     -1.035941
                                       NaN
                                                  NaN
                                                              NaN
ft20
                            NaN -1.062845
                                                  NaN
                                                              NaN
ft24
                            {\tt NaN}
                                       {\tt NaN}
                                            -0.999099
                                                              NaN
ft48
                            {\tt NaN}
                                       NaN
                                                  NaN -0.815952
hsgrad
                     -0.009806 -0.007545
                                            -0.021443 -0.051608
imm
                     -0.018563
                                             0.029186
                                  0.019603
                                                       0.016938
                      0.030502
                                  0.049208
                                                        0.052138
nevermarried
                                             0.051333
                      0.058942
                                  0.036285
                                             0.013314 -0.037857
working_at_baseline
1.2.5 e)
In [15]: for welfare, ft, month in zip(welfares, fts, months):
             g_over_p = gammas[welfare].loc["treatment"] / pis[ft].loc["treatment"]
             print("for month {2}:\n beta_hat: {0} \n gamma_pi_ratio: {1}" .format(
                 betas[welfare].loc[ft], g_over_p, month))
for month 15:
beta_hat: -1.0359407430749634
gamma_pi_ratio: -1.0359407430749892
for month 20:
beta hat: -1.0628446924873316
 gamma_pi_ratio: -1.0628446924873447
for month 24:
 beta_hat: -0.9990992195414421
 gamma_pi_ratio: -0.9990992195414519
for month 48:
 beta_hat: -0.8159517190649126
 gamma_pi_ratio: -0.8159517190650901
```

The inclusion of the control variables seems to have negligible impact on our estimates.