## Assignment 1

## Vibhavasu Pasumarti - EP20BTECH11015

Download all python codes from

https://github.com/VIB2020/AI1103/blob/main/ Assignment%201/code/Assignment 1.py

and latex-tikz codes from

https://github.com/VIB2020/AI1103/blob/main/ Assignment%201/Assignment%201.tex

## 1 Problem

A bag contains 2 white and 1 red balls. One ball is drawn at random and then put back in the box after noting it's color. The process is repeated again. If X denotes the number of red balls recorded in the two draws, describe X

## 2 SOLUTION

Possible events:

E1: 2 Red balls are drawn

E2: 1 Red and 1 White ball is drawn

E3: 0 Red / 2 White balls are drawn

Let X denote the number of red balls recorded in the two draws

$$P(X=2) = \frac{1}{3} * \frac{1}{3} = \frac{1}{9}$$
 (1)

$$P(X = 1) = \left(\frac{1}{3} * \frac{2}{3}\right) * 2 = \frac{4}{9}$$
 (2)

$$P(X=0) = \frac{2}{3} * \frac{2}{3} = \frac{4}{9}$$
 (3)

X	0	1	2
P(X)	$\frac{4}{9}$	$\frac{4}{9}$	<u>1</u>

TABLE 0: Probability distribution table of X

Expectation value of X

$$\mu = E(X) = \sum x_i P(X = x_i) \tag{4}$$

$$= 0\left(\frac{4}{9}\right) + 1\left(\frac{4}{9}\right) + 2\left(\frac{1}{9}\right) \tag{5}$$

(6)

$$\mu = E(X) = \frac{2}{3}$$

Variance of X:

$$\sigma(X) = \sum (x_i - \mu)^2 P(X = x_i) \quad (7)$$

$$= \left(0 - \frac{2}{3}\right)^2 \left(\frac{1}{9}\right) + \left(1 - \frac{2}{3}\right)^2 \left(\frac{4}{9}\right) + \left(2 - \frac{2}{3}\right)^2 \left(\frac{4}{9}\right) \tag{8}$$

$$\sigma(X) = \frac{8}{9}$$