

test1

March 18, 2023

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[ ]: import numpy as np
import matplotlib.pyplot as plt
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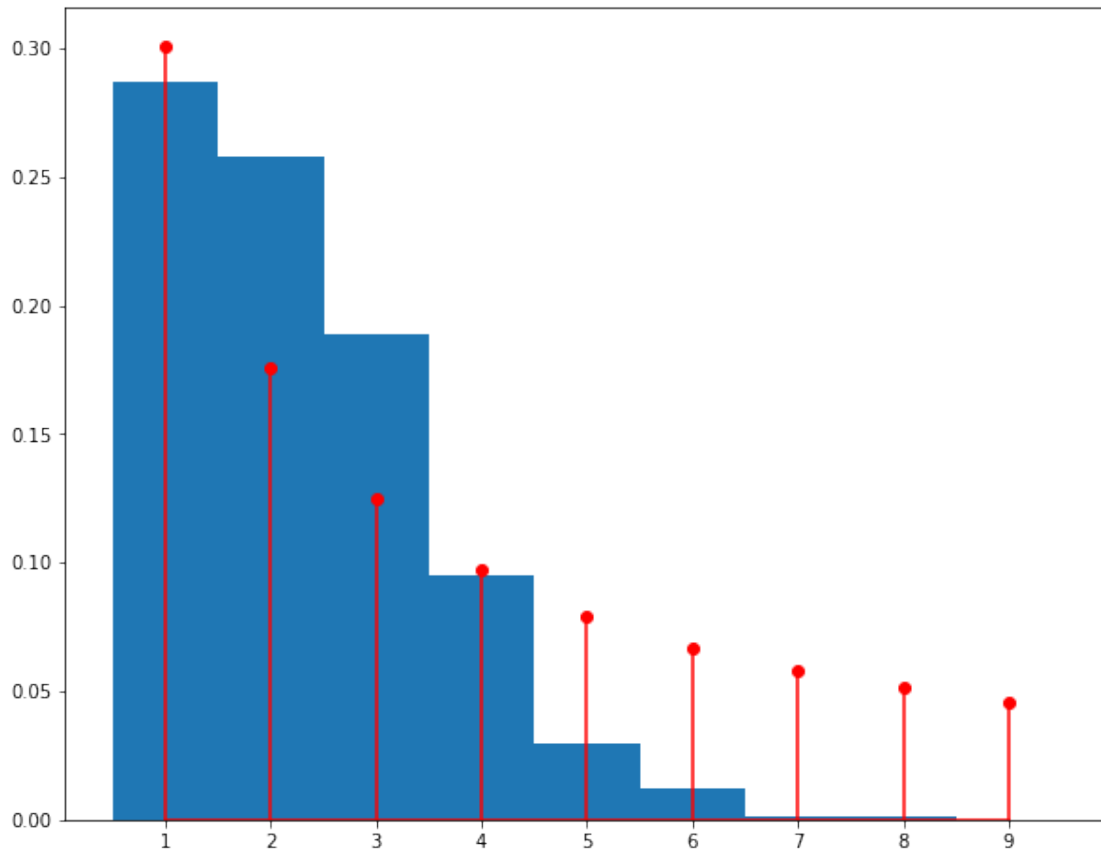
```
[ ]:
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[ ]: #arr = np.random.normal(2, 3, 1000) #DOES NOT FOLLOW BENFORD'S LAW
#arr = np.random.uniform(2, 3, 1000) #DOES NOT FOLLOW BENFORD'S LAW
#arr= np.random.randint(1, 1000, 1000) #DOES NOT FOLLOW BENFORD'S LAW
# arr = np.random.exponential(2, 1000) #FOLLOWS BENFORD'S LAW
# arr = np.random.lognormal(2, 3, 1000) #FOLLOWS BENFORD'S LAW
arr = np.random.poisson(2, 1000) #FOLLOWS BENFORD'S LAW
```

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[ ]: ndigits = 10
p_ndigits = np.log(1 + 1/np.arange(1, ndigits))/np.log(ndigits)
a = np.zeros(ndigits)
for i in arr:
    a[int(str(i).replace('0.', '').replace('-', ''))[0]] += 1
```

a = [a[(i+1)%ndigits]/ndigits for i in range(ndigits)]

```
[ ]: plt.figure(figsize=(10, 8))
plt.bar(range(1, ndigits), a[1:]/np.sum(a), width=1)
plt.stem(range(1, ndigits), p_ndigits, linefmt='r-', markerfmt='ro',
        ↪basefmt='r-')
plt.xticks(range(1, ndigits))
plt.show()
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[ ]: array([127., 287., 258., 189., 95., 30., 12., 1., 1., 0.])
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```
[ ]: def benford_law_test(arr, ndigits=10):
    a = np.zeros(ndigits)
    for i in arr:
        a[int(str(i).replace('0.', '').replace('-', ''))[0]] += 1

    return a[1:]/np.sum(a)

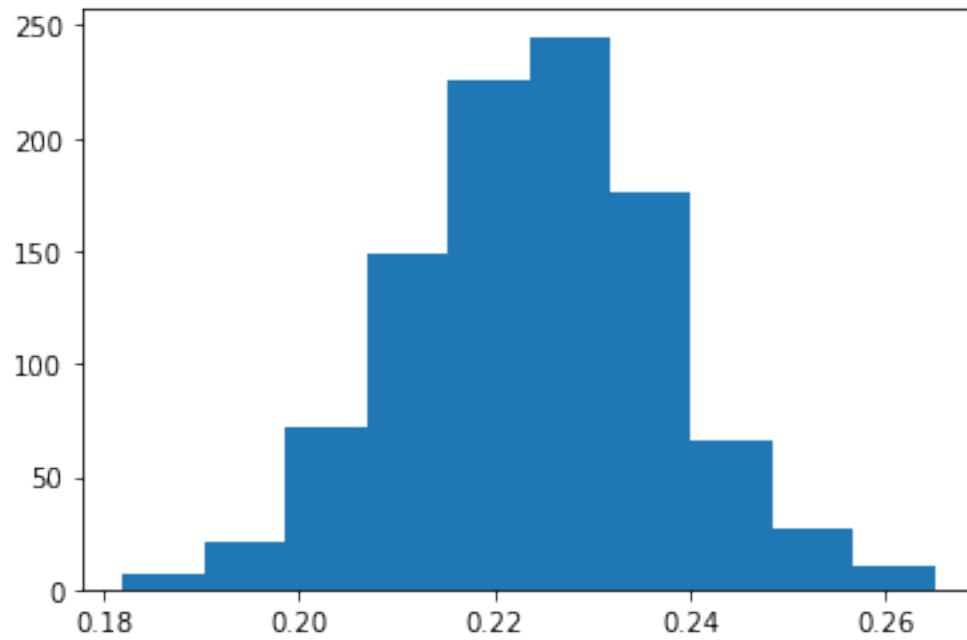
def ideal_benford_law(ndigits=10):
    return np.log(1 + 1/np.arange(1, ndigits))/np.log(ndigits)
```

```
[ ]: all_a = []
for i in range(1000):
    arr = np.random.normal(2, 3, 1000)
    all_a.append(benford_law_test(arr)[0])
    #assert np.allclose(a, b, atol=0.05)
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[ ]: all_a = np.asarray(all_a)
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[ ]: plt.hist(all_a, bins=10)
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[ ]: (array([ 7., 21., 72., 149., 226., 245., 176., 66., 27., 11.]),  
      array([0.182, 0.1903, 0.1986, 0.2069, 0.2152, 0.2235, 0.2318, 0.2401,  
            0.2484, 0.2567, 0.265 ]),  
      <BarContainer object of 10 artists>)
```



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