Syllabus

| Date | Course |
|------|---|
| 2/17 | Syllabus + Overview |
| 2/24 | Introduction + Find your partner for final presentation (5 members for each team) |
| 3/03 | ◢■■■ 崩 └(〒皿〒)┘ 潰 ■■■■ ► |
| 3/10 | Syntax and Semantics + Lexical and Syntax Analysis + Quiz 1 |
| 3/17 | Perl Regular Expressions, Matching and Substitutions + HW1 (1 week) |
| 3/24 | Functional Programming Languages (LISP) + HW2 (2 weeks) |
| 3/31 | Spring Vacation |
| 4/07 | Logic Programming Languages (Prolog) + HW3 (2 weeks) |
| 4/14 | Names, binding and scopes + Quiz 2 |
| 4/21 | Data types + HW4 (2 weeks) |

Syllabus (Cont.)

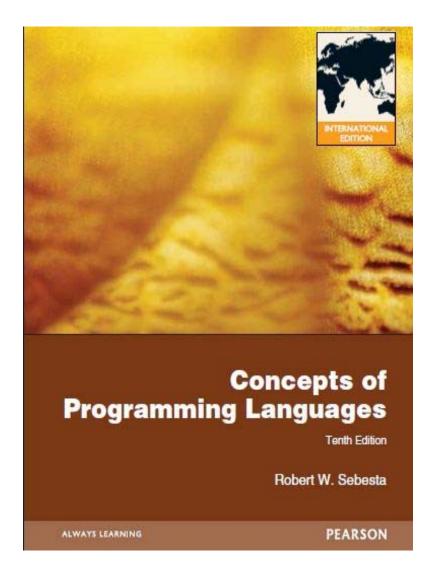
| Date | Course | |
|------|---|--|
| 4/28 | Abstract Data Types and Encapsulation Constructs | |
| 5/05 | Expressions and Assignment Statements Statement-Level Control Structures + Quiz 3 | |
| 5/12 | Subprograms Concurrency+ HW5 (2 weeks) | |
| 5/19 | Exception Handling and Event Handling | |
| 5/26 | Final Presentation (6 teams) | |
| 6/02 | Dragon Boat Festival | |
| 6/09 | Final Presentation (6 teams) | |
| 6/16 | Final Presentation (6 teams) | |
| 6/23 | Final Presentation (6 teams) | |

Final Exam:

Programming Language

Instructor:

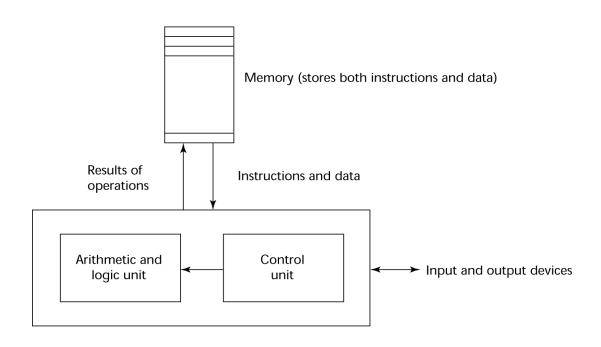
Min-Chun Hu anita_hu@mail.ncku.edu.tw



Lecture 2 Syntax and Semantics

- Introduction
- ☐ The General Problem of Describing Syntax
- Formal Methods of Describing Syntax
- Attribute Grammars
- Describing the Meanings of Programs: Dynamic Semantics

The von Neumann Architecture



Central processing unit

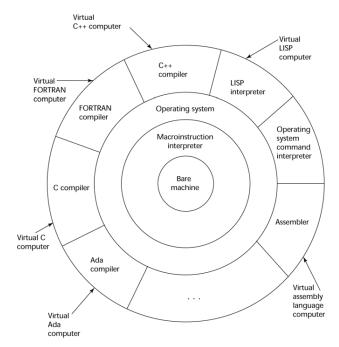
The von Neumann Architecture

 Fetch-execute-cycle: the execution of a machine code program (on a von Neumann architecture computer)

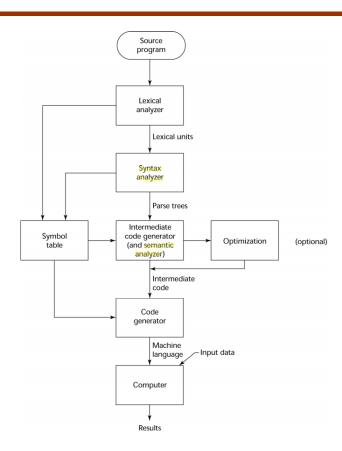
```
initialize the program counter
repeat forever
  fetch the instruction pointed by the counter
  increment the counter
  decode the instruction
  execute the instruction
end repeat
```

Layered View of Computer

 The operating system and language implementation are layered over machine interface of a computer



The Compilation Process



Additional Compilation Terminologies

- Load module (executable image): the user and system code together
- Linking and loading: the process of collecting system program units and linking them to a user program

Syntax vs Semantics 語意學

文法 語意

- Syntax + Semantics → language's definition
- Syntax: the form or structure of the expressions, statements, and program units
- Semantics: the meaning of the expressions, statements, and program units
- e.g. while (Boolean_expr) statement

The General Problem of Describing Syntax: Terminology

- A sentence is a string of characters over some alphabet
- A language is a set of sentences
- A lexeme is the lowest level syntactic unit of a language 基本語法單位
 - □ e.g., *, sum, begin
- A token is a category of lexemes
 - e.g., *identifier* (names of variables/methods/classes) 變數、方法

```
Ex : Arithmetic (+, -, *, /)
```

Lexemes vs Tokens

$$a = 2 * count + 17;$$

| Lexemes | Tokens |
|---------|-------------|
| Α | identifier |
| = | equal_sign |
| 2 | int_literal |
| * | mult_op |
| count | identifier |
| + | plus_op |
| 17 | int_literal |
| ; | semicolon |

Formal Definitions of Languages

Recognizers

- □ A recognition device reads input strings over the alphabet of the language and decides whether the input strings belong to the language 不產生句子,只判斷是否合乎語法
- Example: syntax analysis part of a compiler

Generators

- A device that generates sentences of a language
- One can determine if the syntax of a particular sentence is syntactically correct by comparing it to the structure of the generator

BNF and Context-Free Grammars

- Context-Free Grammars 前後文無關的文法
 - Developed by Noam Chomsky in the mid-1950s
 - Language generators, meant to describe the syntax of natural languages
 - Define a class of languages called context-free languages
- Backus-Naur Form (BNF, 1959)
 - Invented by John Backus to describe the syntax of ALGOL 58
 - Modified by Peter Naur for the description of ALGOL 60
 - BNF is nearly identical to context-free grammars

BNF Fundamentals

N: non-terminal symbols

G = (N,T,S,P) T: terminal symbols

S: Start

P: 所有rule的集合

- BNF is a metalanguage, which is a language used for describing another language 可用來描述其它語言
- BNF uses abstractions to represent classes of 可被替换,不能出在句子結果 syntactic structures □ abstractions act like syntactic variables (no terminal symbol)

 - also called *nonterminal symbols*, or simply *nonterminals*
- A rule consists of 不可被替换,可出現在句子結果(terminal symbol)
 - □ left-hand side (LHS), which is an nonterminal (abstraction) being defined
 - right-hand side (RHS), which is the definition of the LHS and is a string of terminals (lexemes or tokens) and/or nonterminals (abstractions)
 - \square e.g. <assign> \rightarrow <var> = <expression> LHS RHS

BNF Fundamentals (Cont.)

 Nonterminals are often enclosed in angle brackets and can have two or more distinct definitions

Variable-length lists can be described by recursion:

- Grammar: a finite non-empty set of rules that define languages
- A *start symbol*, often named program>, is a special element of the nonterminals of a grammar
- Derivation: a sequence of rule applications, starting with the start symbol and ending with a sentence (all terminal symbols)

將所有abstract以terminal symbol, rule取代,產生符合此grammar的句子16

An Example Grammar

An Example Derivation (Leftmost)

```
sentential form
         => begin <stmt>;<stmt list> end
         => begin <var>=<expression>;<stmt list> end
         => begin A=<expression>;<stmt list> end
         => begin A=<var>+<var>;<stmt list> end
         => begin A=B+<var>;<stmt list> end
         => begin A=B+C;<stmt list> end
         => begin A=B+C;<stmt> end
         => begin A=B+C; <var>=<expression> end
         => begin A=B+C;B=<expression> end
         => begin A=B+C;B=<var> end
         => begin A=B+C;B=C end
```

Exercise

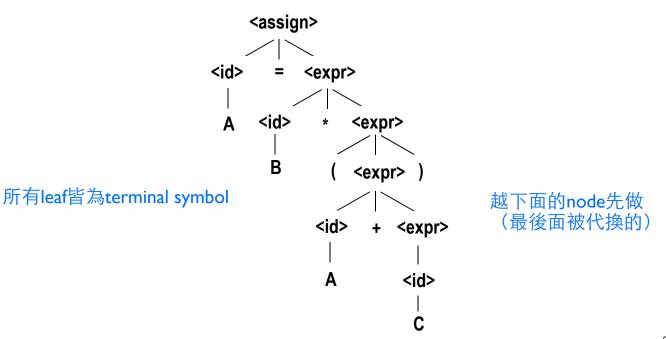
Write a grammar that generates the statement
 A=B*(A+C) and show how the statement is derived.

Derivations

- Every string of symbols (including program>) in a
 derivation is a sentential form
- A sentence is a sentential form that has only terminal symbols
- A leftmost derivation is one in which the leftmost nonterminal in each sentential form is the one that is expanded 每次挑最左邊代換掉non terminal form
- A derivation may be neither leftmost nor rightmost

Parse Tree

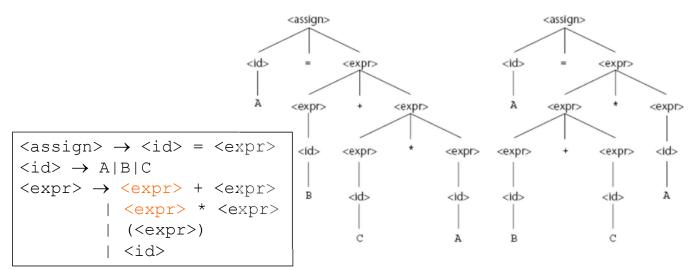
A hierarchical representation of a derivation



Ambiguity in Grammars

同一個sentence ,會產生兩個以上的parsing tree

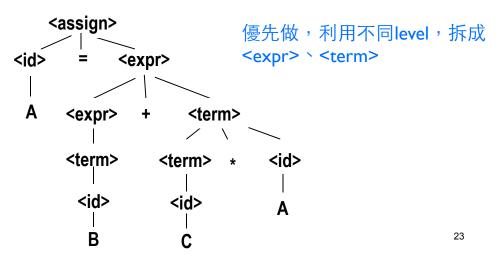
- A grammar is ambiguous if and only if it generates a sentential form that has two or more distinct parse trees
- e.g. the following grammar is ambiguous because the sentence A=B+C*A has two distinct parse trees:



An Unambiguous Expression Grammar

 If we use the parse tree to indicate precedence levels of the operators, we will not have ambiguity

```
<assign> \rightarrow <id> = <expr> <id> \rightarrow A|B|C <expr> \rightarrow <expr> + <term> | <term> <term> \rightarrow <term> * <id> | <id> |
```



Associativity of Operators

結合律

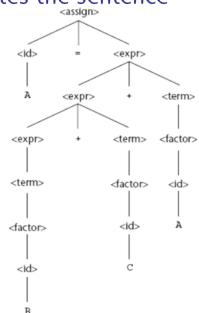
 Associativity: When two operators have the same precedence (* and /, + and +), a semantic rule is required to specify which should have precedence.

e.g. the following grammar generates the sentence

A=B+C+A with left associativity 先加和後加會影響結果(進位問題)

Left associativity: <expr> + <term>
Right associativity: <term> + <expr>

```
<assign> → <id> = <expr>
<id> → A|B|C
<expr> → <expr> + <term> | <term>
<term> → <term> * <factor> | <factor>
<factor> → (expr) | <id>
```



Extended BNF (EBNF)

- Optional parts are placed in brackets [] 可有可無
 - \blacksquare e.g. $\langle \text{if_stmt} \rangle \rightarrow \text{if} (\langle \text{expr} \rangle) \langle \text{stmt} \rangle [\text{else} \langle \text{stmt} \rangle]$
- Alternative parts of RHSs are placed inside parentheses and separated via vertical bars
 - \square e.g. <term> \rightarrow <term> (*|/|%) <factor>
- Repetitions (0 or more) are placed inside braces {}
 - e.g. <ident_list> → <ident> {, <ident>}

BNF and **EBNF**

BNF

EBNF

```
\langle expr \rangle \rightarrow \langle term \rangle \{ (+ | -) \langle term \rangle \}
\langle term \rangle \rightarrow \langle factor \rangle \{ (* | /) \langle factor \rangle \}
```

Recent Variations in EBNF

- Alternative RHSs are put on separate lines instead of use |
- Use of a colon instead of → and RHS is placed on the next line
- Use of opt for optional parts
- Use of one of for choices

Static Semantics

- Nothing to do with meaning
- Context-free grammars (CFGs) cannot describe all of the syntax of programming languages
- Categories of constructs that are trouble:
 - □ Context-free, but cumbersome (e.g., types of operands in expressions)
 - Non-context-free (e.g., variables must be declared before they are used)

Attribute Grammars

- Attribute grammars (AGs) have additions to CFGs to carry some semantic info on parse tree nodes
- Primary value of AGs:
 - Static semantics specification
 - □ Compiler design (static semantics checking)

Attribute Grammars: Definition

- Def: An attribute grammar is a contextfree grammar G = (S, N, T, P) with the following additions:
 - \blacksquare For each grammar symbol x there is a set A(x) of attribute values
 - Each rule has a set of functions that define certain attributes of the nonterminals in the rule
 - Each rule has a (possibly empty) set of predicates to check for attribute consistency

Attribute Grammars: Definition

- Let $X_0 \rightarrow X_1 \dots X_n$ be a rule
- Functions of the form $S(X_0) = f(A(X_1), ..., A(X_n))$ define *synthesized attributes* (passing semantic information up a parse tree)
- Functions of the form $I(X_j) = f(A(X_0), ..., A(X_n))$, for i <= j <= n, define inherited attributes (passing semantic information down and cross a parse tree)
- Initially, there are *intrinsic attributes* (synthesized attributes on the leaves) whose values are stored in a symbol table.

Attribute Grammars: An Example

Syntax

```
<assign> -> <var> = <expr> <expr> -> <var> + <var> | <var> <ur> A | B | C
```

- actual_type: synthesized for <var> and <expr>
- expected_type: inherited for <expr>

Attribute Grammar (Cont.)

```
1. Syntax rule: \langle assign \rangle \rightarrow \langle var \rangle = \langle expr \rangle
   Semantic rules: <expr>.expected type ← <var>.actual_type
     檢查data type
2. Syntax rule: \langle expr \rangle \rightarrow \langle var \rangle[2] + \langle var \rangle[3]
   Semantic rules: <expr>.actual type ←if(<var>[2].actual type==int)
                                              and (<var>[3].actual type==int)
                                              then int
                                            else real
                                            end if
   Predicate: <expr>.actual type == <expr>.actual type
3. Syntax rule: \langle expr \rangle \rightarrow \langle var \rangle
   Semantic rule: <expr>.actual type ← <var>.actual type
   Predicate: <expr>.actual type == <expr>.actual type
4. Syntax rule: \langle var \rangle \rightarrow A|B|C
   Semantic rule: <var>.actual type ← lookup (<var>.string)
```

Attribute Grammars (Cont.)

- How are attribute values computed?
 - □ If all attributes were inherited, the tree could be decorated in top-down order.
 - □ If all attributes were synthesized, the tree could be decorated in bottom-up order.
 - In many cases, both kinds of attributes are used, and it is some combination of top-down and bottom-up that must be used.

Attribute Grammars (Cont.)

Sentence : A=A+B1. <var>.actual type ← lookup (A) (Rule4) 2. <expr>.expected type ← <var>.actual type (Rule1) 3. $\langle var \rangle$ [2].actual type \leftarrow lookup (A) (Rule4) $\langle var \rangle$ [3].actual type \leftarrow lookup (B) (Rule4) 4. <expr>.actual type ← either int or real (Rule2) 5. <expr>.expected type == <expr>.actual type is either TRUE or FALSE (Rule2) <assign> • type checking, 宣告: static semantic (compile期間) expected_type <expr> <expr> <a hr • variables變化: dynamic semantic (執行期間)

actual type

actual type

Semantics (Dynamic Semantics)

- There is no single widely acceptable notation or formalism for describing semantics
- Several needs for a methodology and notation for semantics:
 - □ Programmers need to know what statements mean
 - Compiler writers must know exactly what language constructs do
 - □ Correctness proofs of programs would be possible
 - Compiler generators would be possible
 - Designers could detect ambiguities and inconsistencies

Operational Semantics

- Operational Semantics
 - Describe the meaning of a program by executing its statements on a machine, either simulated or actual.
 - The change in the state of the machine (memory, registers, etc.) defines the meaning of the statement
- To use operational semantics for a high-level language, a virtual machine is needed
 - Natural operational semantics
 - □ Structural operational semantics

Operational Semantics (Cont.)

- A hardware pure interpreter would be too expensive
- A software pure interpreter also has problems
 - The detailed characteristics of the particular computer would make actions difficult to understand
 - Such a semantic definition would be machinedependent

Operational Semantics (Cont.)

- A better alternative: A complete computer simulation
- The process:
 - Build a translator (translates source code to the machine code of an idealized computer)
 - Build a simulator for the idealized computer
- Evaluation of operational semantics:
 - Good if used informally (language manuals and textbooks, teaching programming languages)
 - Extremely complex if used formally (e.g., VDL), it was used for describing semantics of PL/I.

Denotational Semantics 以數學方式表示

- The most rigorous and most widely known formal method for describing the meaning of the program
- Based on recursive function theory
- Originally developed by Scott and Strachey (1970)
- The process of building a denotational specification for a language:
 - □ Define a mathematical object for each language entity
 - Define a function that maps instances of language entities onto instances of the corresponding mathematical objects
- The meaning of language constructs are defined by only the values of the program's variables

Example: Decimal Numbers

Syntax rule:

Denotational mapping:

```
M_dec ('0') = 0, M_dec ('1') = 1, ..., M_dec ('9') = 9
M_dec (<dec_num> '0') = 10 * M_dec (<dec_num>)
M_dec (<dec_num> '1') = 10 * M_dec (<dec_num>) + 1
...
M_dec (<dec_num> '9') = 10 * M_dec (<dec_num>) + 9
```

Denotational Semantics: program state

 The state of a program is the values of all its current variables

$$s = \{\langle i_1, v_1 \rangle, \langle i_2, v_2 \rangle, ..., \langle i_n, v_n \rangle\}$$

 Let VARMAP be a function that, when given a variable name and a state, returns the current value of the variable

$$VARMAP(i_j, s) = v_j$$

Expressions

- Map expressions onto Z ∪ {error}
- We assume expressions are decimal numbers, variables, or binary expressions having one arithmetic operator and two operands, each of which can be an expression

Mapping Function for a given Expression E and State s

```
<binary expr> → <left expr> <operator> <right expr>
           <left expr> \rightarrow <dec num> | <var>
           <right expr> \rightarrow <dec num> | <var>
           \langle operator \rangle \rightarrow + | *
M_{o} (<expr>, s) \Delta= case <expr> of
       <dec num> => M_{dec} (<dec num>, s)
        \langle var \rangle = \rangle
              if VARMAP(<var>, s) == undef
                     then error
                     else VARMAP(<var>, s)
      <br/><br/>dinary expr> =>
             if (M<sub>a</sub>(<binary expr>.<left expr>, s) == undef
              OR M<sub>a</sub>(<binary expr>.<right expr>, s) == undef)
                   then error
              else
              if (<binary expr>.<operator> == '+' then
                  M<sub>a</sub>(<binary expr>.<left expr>, s) +
                           M<sub>o</sub>(<binary expr>.<right expr>, s)
              else M<sub>a</sub>(<binary expr>.<left expr>, s) *
```

M_a (<binary expr>.<right expr>, s)

 $\langle expr \rangle \rightarrow \langle dec num \rangle \mid \langle var \rangle \mid \langle binary expr \rangle$

Assignment Statements

- Assignment: an expression evaluation plus the setting of the target variable to the expression's value.
- → Maps state sets to state sets U {error}

```
M_a (x := E, s) \Delta = if M_e (E, s) == error
then error
else s' = \{\langle i_1, v_1' \rangle, \langle i_2, v_2' \rangle, \ldots, \langle i_n, v_n' \rangle\},
where for j = 1, 2, \ldots, n,
if i_j == x
then v_j' = M_e (E, s)
else v_j' = VARMAP(i_j, s)
```

Logical Pretest Loops

Maps state sets to state sets U {error}

```
M_1 (while B do L, s) \Delta =

if M_b (B, s) == undef

then error

else if M_b (B, s) == false

then s

else if M_{s1} (L, s) == error

then error

else M_1 (while B do L, M_{s1} (L, s))
```

Loop Meaning

- The meaning of the loop is the value of the program variables after the statements in the loop have been executed the prescribed number of times, assuming there have been no errors
- In essence, the loop has been converted from iteration to recursion, where the recursive control is mathematically defined by other recursive state mapping functions
 - Recursion, when compared to iteration, is easier to describe with mathematical rigor

Evaluation of Denotational Semantics

- Can be used to prove the correctness of programs
- Provides a rigorous way to think about programs
- Can be an aid to language design
- Has been used in compiler generation systems
- Because of its complexity, it are of little use to language users

Axiomatic Semantics

- Based on formal logic (predicate calculus)
- Applications:
 - program verification (prove the correctness of programs)
 - program semantics specification
- Rather than directly specifying the meaning of a program, axiomatic semantics specifies what can be proven about the program based on the relationship among program variables
- Axioms or inference rules are defined for each statement type in the language (to allow transformations of logic expressions into more formal logic expressions)

Axiomatic Semantics (Cont.)

適用於驗證程式 (P、Q)

- Each statement of the program is preceded and followed by a logical expression (assertions/predicates) specifying relationships and constraints on program variables before/after execution
- Pre-, post form: {P} statement {Q}
 - \square *Precondition* (P): ex. {x>10} sum=2*x+1
 - \square *Postcondition* (Q): ex. sum=2*x+1 {sum>1}
- A weakest precondition is the least restrictive precondition that will guarantee the associated postcondition 限制條件最寬鬆
 - \blacksquare Ex. $\{x>10\}$, $\{x>50\}$ and $\{x>1000\}$ are all valid preconditions.
 - \rightarrow The weakest of all preconditions in this case is $\{x>0\}$

Program Proof Process

- The postcondition for the entire program is the desired result
 - Work back through the program to the first statement. If the precondition on the first statement is the same as the program input specification, the program is correct.
- Inference rule: inferring the truth of one assertion on the basis of the values of other assertions.
 - □ General form: $\frac{S_1, S_2, ..., S_n}{S}$
 - □ If $S_1, S_2 ..., S_n$ (antecedent) are true, then the truth of S (consequent) can be inferred.
- Axiom: a logical statement assumed to be true
 - → an axiom is an inference rule without an antecedent

Axiomatic Semantics: Assignment

• The precondition (axiom) P for assignment statements given the postcondition Q is defined by $P = Q_{v->F}$

{P} S {Q}

$$(x = E): \{Q_{x->E}\}\ x=E \ \{Q\}$$

Ex1: $a = b/2 - 1 \{a < 10\}$
 $\Rightarrow b/2 - 1 < 10$
 $\Rightarrow b < 22$ (weakest precondition)
Ex2: $a = a + b - 3 \{a > 10\}$
 $\Rightarrow a + b - 3 > 10$
 $\Rightarrow b > 13 - a$ (weakest precondition)

Axiomatic Semantics: Assignment

The Rule of Consequence:

- P' 較嚴格
- $\frac{\{P\}S\{Q\}, P'=>P, Q=>Q'}{\{P'\}S\{Q'\}}$ P 較寛鬆
- A postcondition can always be weakened and a precondition can always be strengthened.
- Ex. $\frac{\{x>3\}x=x-3\{x>0\}, \{x>5\}\Rightarrow \{x>3\}, \{x>0\}\Rightarrow \{x>0\}}{\{x>5\}x=x-3\{x>0\}}$

Axiomatic Semantics: Sequences

• An inference rule for a sequence of statements:

If S1 and S2 are assignment statements (x1=E1 and x2 =E2), then we have:

$${P3_{x2 \to E2}} x2 = E2 {P3}$$

 ${(P3_{x2 \to E2})_{x1 \to E1}} x1 = E1 {P3_{x2 \to E2}}$

Ex:
$$y = 3 * x + 1$$
;
 $x = y + 3$;
 $\{x < 10\}$

Precondition of S2: $y < 7$
Precondition of S1: $x < 2$

Axiomatic Semantics: Selection

An inference rules for selection

```
Ex: if x > 0 then Precondition for then: y > 1
y = y - 1 Precondition for else: y > -1
else Since \{y > 1\} implies \{y > -1\}, y = y + 1 we can use \{y > 1\} as the \{y > 0\}
```

Axiomatic Semantics: Loops

• An inference rule for logical pretest loops:

```
□ {P} while B do S end {Q}
```

{I and B} S {I}

{I} while B do S end {I and (not B)}

where I is the loop invariant (the inductive hypothesis)

I: invariant condition 不管有沒有loop需滿足的條件

Axiomatic Semantics: Axioms

- The loop invariant must meet the following conditions:
 - \square P => I : the loop invariant must be true initially
 - □ {I} B {I} : evaluation of the Boolean must not change the validity of I
 - {I and B} S {I} : I is not changed by executing the body of the loop
 - □ (I and (not B)) => Q : if I is true and B is false, Q is implied
 - ☐ The loop terminates (can be difficult to prove)

Loop Invariant

- The loop invariant I is a weakened version of the loop postcondition, and it is also a precondition.
- I must be weak enough to be satisfied prior to the beginning of the loop, but when combined with the loop exit condition, it must be strong enough to force the truth of the postcondition

Evaluation of Axiomatic Semantics

- Developing axioms or inference rules for all of the statements in a language is difficult
- It is a good tool for correctness proofs, and an excellent framework for reasoning about programs, but it is not as useful for language users and compiler writers

Denotation Semantics vs Operational Semantics

- In operational semantics, the state changes are defined by coded algorithms
- In denotational semantics, the state changes are defined by rigorous mathematical functions

Summary

- BNF and context-free grammars are equivalent meta-languages
 - Well-suited for describing the syntax of programming languages
- An attribute grammar is a descriptive formalism that can describe both the syntax and the semantics of a language
- Three primary methods of semantics description
 - □ Operational, denotational, axiomatic