Giving physical meaning to $\mathcal{W}^k(\mathfrak{g},x,f)$

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September 2024

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- 1 Introduction: CFTs and RCFTs
- 2 The WZW model
- 3 Reductions of the model
- 4 Classifying through pyramids

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- Introduction: CFTs and RCFTs
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Quantum field theories

Quantum field theories

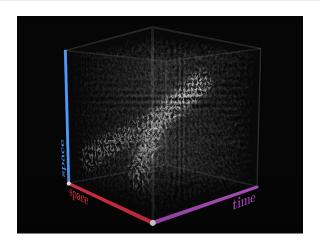


Figure 1: Illustration of a field

Quantum field theories

Correlation functions

-Introduction: CF Is and RCF

Quantum field theories

OPE and algebra

Conformal field theories

conformal symmetry made up of generators

2D CFTs and chirality

in 2D, on a string, massless => left or right

RCFTs

classification

W algebras

general definition

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The objective

Objective

└ The Sigma Model

The Sigma model

└─The WZW model

The Sigma Model

Sigma model on Lie algebras

The Sigma Model

Conformality at two levels

Geometrical obstruction

In CFTs
$$[T, T] = 0$$

In our model
$$[J, J] = [T, T]$$

Adding the topological term

The topological term

└─The WZW model

Adding the topological term

The WZW model

Hypothesis

Hypothesis: curved AKM algebras

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Reducing the model

Toda field theory

Reducing the model

Generalizing conditions

Conditions

First-classness of the conditions

Conditions

Conformality of the reduction

Conditions

Other conditions

 \sqsubseteq The algebra $\mathcal{W}(\mathfrak{g}, x, f)$

Good gradings

Necessary for BRST, studied by Kac and ..

Lagran The algebra $\mathcal{W}(\mathfrak{g}, x, f)$

$$\mathcal{W}(\mathfrak{g},x,f)$$

Hypothesis

Hypothesis: relaxing the conditions

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Good gradings

Good gradings

Necessary for BRST, studied by Kac and ..

From shifting constant to blocks

From Hamiltonian term to pyramids

Reading a pyramid

└ Hypothesis

Hypothesis: explaining infinite W algebras

Hypothesis about infinite W algebra, linked to infinite pyramid, nice meaning