Giving physical meaning to $\mathcal{W}^k(\mathfrak{g}, x, f)$

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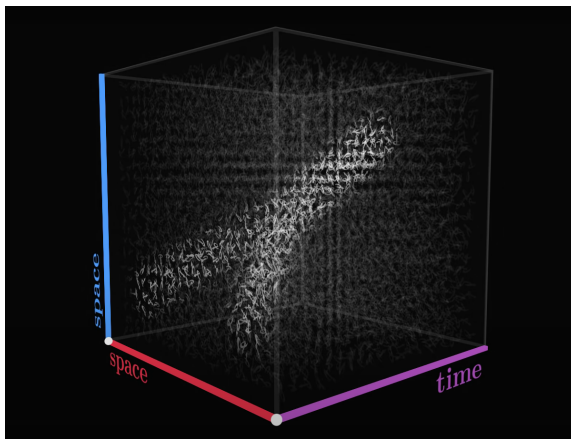
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