

ePL: An Overture

CS4215: Programming Language Implementation

Răzvan Voicu

Week 2, 16-20 January 2017

- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs The meaning of the code
- 3 Static Semantics for ePL type inference
- 4 A Virtual Machine for **ePL**
- 5 Big-Step Semantics for **ePL**

- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs
- 3 Static Semantics for ePL
- 4 A Virtual Machine for **ePL**
- 5 Big-Step Semantics for **ePL**

Syntax of ePL

$$\frac{}{n}$$

$$\frac{}{\text{true}}$$

$$\frac{}{\text{false}}$$

$$\frac{E}{p_1[E]}$$

$$\frac{E_1 \quad E_2}{p_2[E_1, E_2]}$$

$$P_1 = \{\backslash, \sim\},$$

$$P_2 = \{ |, \&, +, -, *, /, =, >, < \}.$$

Syntactic Conventions

- We can use parentheses in order to group expressions together.
- We use the usual infix and prefix notation for operators. The binary operators are left-associative and the usual precedence rules apply such that $1 + 2 * 3 > 10 - 4$ stands for $>[+[1, *[2, 3]], -[10, 4]]$

Examples

42

$\sim 15 * (7 + 2)$

$\backslash \text{false} \ \& \ \text{true} \mid \text{false}$

$17 < 20 - 4 \ \& \ 10 = 4 + 11$

Implementation of Syntax

syntax 句法 semantic 语义

Lexer/Scanner

Language syntax is typically implemented in a two-step process:
(1) lexical analysis, (2) parsing

Lexical analysis 词法分析

Split program string into sequence of tokens

Parsing 句法分析

Construct a tree-like data structure that corresponds to the structure of the program

Syntax of ePL Programs (in OCaml)

```
type op_id = string
```

```
type ePL_expr =  
  | BoolConst of bool  
  | IntConst of int  
  | UnaryPrimApp of op_id * ePL_expr  
  | BinaryPrimApp of op_id * ePL_expr * ePL_expr
```


- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs
- 3 Static Semantics for ePL
- 4 A Virtual Machine for **ePL**
- 5 Big-Step Semantics for **ePL**

Values

Goal of evaluating an expression is to reach a *value*, an expression that cannot be further evaluated.

In ePL, a value is either an integer constant, or a boolean constant.

In the following rules, we denote values by v .

Contraction

$$\frac{}{p_1[v_1] >_{\text{ePL}} v} [\text{OpVals}_1]$$

$$\frac{}{p_2[v_1, v_2] >_{\text{ePL}} v} [\text{OpVals}_2]$$

One instance of the second rule is:

$$\frac{}{+[1, 1] >_{\text{ePL}} 2}$$

One-Step Evaluation

$$\frac{E >_{\text{ePL}} E'}{E \mapsto_{\text{ePL}} E'} [\text{Contraction}] \qquad \frac{E \mapsto_{\text{ePL}} E'}{p_1[E] \mapsto_{\text{ePL}} p_1[E']} [\text{OpArg}_1]$$

$$\frac{E_1 \mapsto_{\text{ePL}} E'_1}{p_2[E_1, E_2] \mapsto_{\text{ePL}} p_2[E'_1, E_2]} [\text{OpArg}_2]$$

$$\frac{E_2 \mapsto_{\text{ePL}} E'_2}{p_2[E_1, E_2] \mapsto_{\text{ePL}} p_2[E_1, E'_2]} [\text{OpArg}_3]$$

Evaluation Order

One-step evaluation does not prescribe the order in which a given ePL expression is evaluated. Both of the following statements hold:

$$3 * 2 + 4 * 5 \mapsto_{\text{ePL}} 3 * 2 + 20$$

$$3 * 2 + 4 * 5 \mapsto_{\text{ePL}} 6 + 4 * 5$$

Evaluation

Evaluation is the reflexive transitive closure of one-step evaluation.

$$\frac{E_1 \mapsto_{\text{ePL}} E_2}{E_1 \mapsto_{\text{ePL}}^* E_2} [\mapsto_{\text{ePL}}^*_B]$$

$$\frac{}{E \mapsto_{\text{ePL}}^* E} [\mapsto_{\text{ePL}}^*_R]$$

$$\frac{E_1 \mapsto_{\text{ePL}}^* E_2 \quad E_2 \mapsto_{\text{ePL}}^* E_3}{E_1 \mapsto_{\text{ePL}}^* E_3} [\mapsto_{\text{ePL}}^*_T]$$

Implementation (in OCaml)

Idea

Keep reducing expression until it is irreducible. Similar to small-step semantics.

Code snippet

```
let rec evaluate (e:ePL_expr): ePL_expr =  
  if (reducible e)  
  then evaluate (oneStep e)  
  else e  
}
```

- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs
- 3 Static Semantics for ePL**
- 4 A Virtual Machine for **ePL**
- 5 Big-Step Semantics for **ePL**

A Type System for ePL

Not all expressions in ePL make sense. For example,

`true + 1`

does not make sense, because `true` is a boolean expression, whereas the operator `+` to which `true` is passed as first argument, expects integers as arguments.

Typing Relation

The set of well-typed expressions is defined by the binary *typing relation*

$$“ : ” : \text{ePL} \rightarrow \{\text{int}, \text{bool}\}$$

We use infix notation for “:”, writing $E : t$, which is read as “the expression E has type t ”.

Examples

- $1+2 : \text{int}$
- $\text{false} \ \& \ \text{true} : \text{bool}$
- $10 < 17-8 : \text{bool}$

but:

- $\text{true} + 1 : t$ does not hold for any t
- $3 + 1 * 5 : \text{bool}$ does not hold

Typing Relation

$$\frac{}{\text{true} : \text{bool}} [\text{TrueT}]$$

$$\frac{}{\text{false} : \text{bool}} [\text{FalseT}]$$

$$\frac{}{n : \text{int}} [\text{NumT}]$$

$$\frac{E : \text{int}}{\sim[E] : \text{int}} [\text{PrimT}_1]$$

$$\frac{E : \text{bool}}{\backslash[E] : \text{bool}} [\text{PrimT}_1]$$

$$\frac{E_1 : t_1 \quad E_2 : t_2}{p[E_1, E_2] : t} [\text{PrimT}_2]$$

Types of Primitive Operations

p	t_1	t_2	t
+	int	int	int
-	int	int	int
*	int	int	int
/	int	int	int
&	bool	bool	bool
	bool	bool	bool
\	bool		bool
~	int		int
=	int	int	bool
<	int	int	bool
>	int	int	bool

Well-typed Expressions

An expression E is well-typed, if there is a type t such that $E : t$.

A Proof

$$\begin{array}{c}
 \frac{}{2 : \text{int}} [\text{NumT}] \quad \frac{}{3 : \text{int}} [\text{NumT}] \\
 \hline
 \frac{}{2*3 : \text{int}} [\text{PrimT}] \quad \frac{}{7 : \text{int}} [\text{NumT}] \\
 \hline
 2*3 > 7 : \text{bool}
 \end{array}$$

Implementation

Idea

Compute the type of an expression *bottom-up*, starting from the constants at the leaves of the syntax tree

Checking

At each node, check that the components have the right type wrt the operator

Type Safety

Type safety is a property of a given language with a given static and dynamic semantics. In a type-safe language, certain problems are guaranteed not to occur at runtime for well-typed programs.

Problems:

- No progress,
- No preservation

- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs
- 3 Static Semantics for ePL
- 4 A Virtual Machine for ePL**
- 5 Big-Step Semantics for ePL

Motivation

- How do we remember intermediate results?
- How do we know what to do next?

Idea: Translate ePL to a machine language. Execute machine code using an emulator.

Definition of eVML

inductive def

termination

$\frac{}{\text{DONE}}$	$\frac{s}{\text{LDCI } i . s}$	$\frac{s}{\text{LDCB } b . s}$
------------------------	--------------------------------	--------------------------------

Definition of eVML (cont'd)

$$\frac{s}{\text{PLUS}.s}$$

$$\frac{s}{\text{MINUS}.s}$$

$$\frac{s}{\text{TIMES}.s}$$

$$\frac{s}{\text{DIV}.s}$$

$$\frac{s}{\text{AND}.s}$$

$$\frac{s}{\text{OR}.s}$$

$$\frac{s}{\text{NOT}.s}$$

$$\frac{s}{\text{LT}.s}$$

$$\frac{s}{\text{GT}.s}$$

$$\frac{s}{\text{EQ}.s}$$

Example

The instruction sequence

[LDCI 1, LDCI 2, PLUS, DONE]

represents a valid eVML program.

Compiling ePL to eVML

$$\Rightarrow : \mathbf{ePL} \rightarrow \mathbf{eVML}$$

$$\frac{E \hookrightarrow s}{E \Rightarrow s.\text{DONE}}$$

Compiling ePL to eVML (cont'd)

$$n \hookrightarrow \text{LDCI } n$$

$$\text{true} \hookrightarrow \text{LDCB true}$$

$$\text{false} \hookrightarrow \text{LDCB false}$$

Compiling ePL to eVML (cont'd)

$$\frac{E_1 \hookrightarrow s_1 \quad E_2 \hookrightarrow s_2}{E_1 + E_2 \hookrightarrow s_1.s_2.PLUS}$$

$$\frac{E_1 \hookrightarrow s_1 \quad E_2 \hookrightarrow s_2}{E_1 * E_2 \hookrightarrow s_1.s_2.TIMES}$$

$$\frac{E_1 \hookrightarrow s_1 \quad E_2 \hookrightarrow s_2}{E_1 / E_2 \hookrightarrow s_1.s_2.DIV}$$

...

Examples

post traverse

$(1 + 2) * 3$

[LDCI 1, LDCI 2, PLUS, LDCI 3, TIMES, DONE]

$1 + (2 * 3)$

[LDCI 1, LDCI 2, LDCI 3, TIMES, PLUS, DONE].

Executing eVML Code

Registers:

- *pc*: program counter,
- *os*: operand stack

Example

$$pc = 2$$

$$s = [\text{LDCI } 1, \text{LDCI } 2, \text{PLUS}, \text{LDCI } 3, \text{TIMES}, \text{DONE}]$$

$$s(pc) = \text{PLUS}$$

Transition Function

Load Constant

$$s(pc) = \text{LDCI } i$$

$$(os, pc) \Rightarrow_s (i.os, pc + 1)$$

$$s(pc) = \text{LDCB } b$$

$$(os, pc) \Rightarrow_s (b.os, pc + 1)$$

Transition Function (cont'd)

$$s(pc) = \text{PLUS}$$

$$(i_2.i_1.os, pc) \Rightarrow_s (i_1 + i_2.os, pc + 1)$$

End Configuration

$$s(pc) = \text{DONE}$$

The result of the computation can be found on top of the operand stack of the end configuration.

$$R(M_s) = v, \text{ where } (\langle \rangle, 0) \Rightarrow_s^* (\langle v.os \rangle, pc), \text{ and } s(pc) = \text{DONE}$$

Example

[LDCI 10, LDCI 20, PLUS, LDCI 6, TIMES, DONE]

$(\langle \rangle, 0) \Rightarrow (\langle 10 \rangle, 1) \Rightarrow (\langle 20, 10 \rangle, 2) \Rightarrow$

$(\langle 30 \rangle, 3) \Rightarrow (\langle 6, 30 \rangle, 4) \Rightarrow (\langle 180 \rangle, 5)$

Implementation

Registers

Keep registers in local variables (or objects)

Execution

Use a switch statement (or match construct) to interpret each instruction

Implementation in OCaml

Instructions

Capture simple bytecode instructions.

```
type eVML_inst =
  | LDCI of int
  | LDCB of int (* 0 – false; 1 – true *)
  | PLUS | MINUS | TIMES | DIV | AND | NEG
  | NOT | OR | LT | GT | EQ | DONE

type eVML_prog = eVML_inst list
```

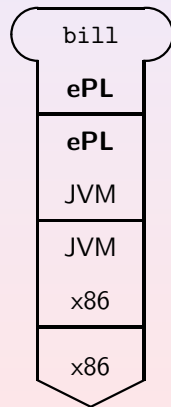
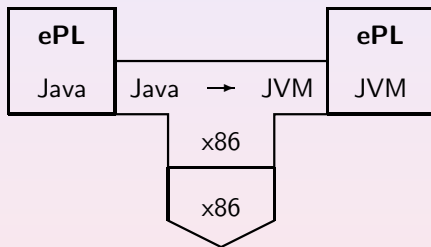
Virtual Machine in OCaml

Execution

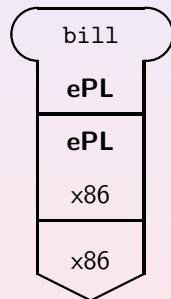
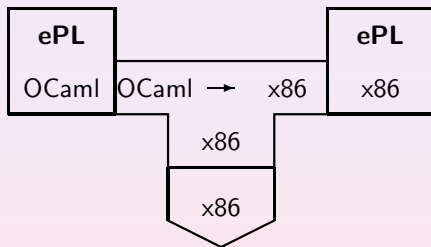
Use an array to store the instructions.

```
let eVML_mc (instArr:eVML_inst array) =  
  let stk = Stack.create () in  
  let rec execute pc =  
    let c = Array.get instArr pc in  
    match c with  
      | DONE -> Stack.pop stk  
      | - -> (proc_inst stk c; execute (pc+1))  
  in execute 0
```

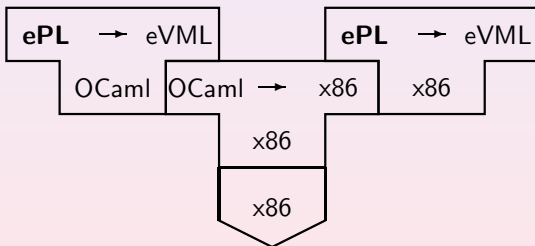
Interpreter for ePL in Java



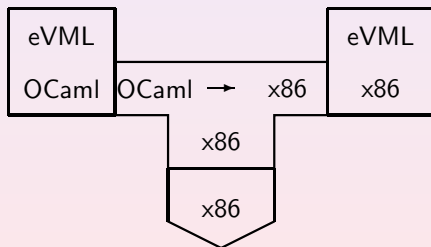
Interpreter for ePL in OCaml



Compiling the ePL Compiler in OCaml



Compiling the eVML Emulator



Simple Exercise

- Draw T-diagram for ePL programs compiled using an ePL compiler produced by the following steps.

```
> ocamlOPT eplc.ml -o eplc
```

```
> ocamlOPT eplm.ml -o eplm
```

```
> ./eplc bill.epl
```

```
bill.epl bill.evml
```

```
> ./eplm bill.evml
```

```
249
```


- 1 The Syntax of ePL
- 2 Dynamic Semantics of ePL Programs
- 3 Static Semantics for ePL
- 4 A Virtual Machine for **ePL**
- 5 Big-Step Semantics for ePL**

Values

Goal of evaluating an expression is to reach a *value*, an expression that cannot be further evaluated.

In ePL, a value is either an integer constant, or a boolean constant.

In the following rules, we denote values by v .

Contraction

$$\frac{}{p_1[v_1] >_{\text{ePL}} v} [\text{OpVals}_1]$$

$$\frac{}{p_2[v_1, v_2] >_{\text{ePL}} v} [\text{OpVals}_2]$$

One instance of the second rule is:

$$\frac{}{+[1, 1] >_{\text{ePL}} 2}$$

One-Step Evaluation

$$\frac{E >_{\text{ePL}} E'}{E \mapsto_{\text{ePL}} E'} [\text{Contraction}] \qquad \frac{E \mapsto_{\text{ePL}} E'}{p_1[E] \mapsto_{\text{ePL}} p_1[E']} [\text{OpArg}_1]$$

$$\frac{E_1 \mapsto_{\text{ePL}} E'_1}{p_2[E_1, E_2] \mapsto_{\text{ePL}} p_2[E'_1, E_2]} [\text{OpArg}_2]$$

$$\frac{E_2 \mapsto_{\text{ePL}} E'_2}{p_2[E_1, E_2] \mapsto_{\text{ePL}} p_2[E_1, E'_2]} [\text{OpArg}_3]$$

Big-Step Semantics

- One-step reduction approach to dynamic semantics is often referred to as *small-step* semantics.
- If you are interested only in the final outcome, rather than the intermediate steps, you can use *big-step* semantics.
- *Big-step* semantics will reduce each expression directly into its final value (not an intermediate value).
- For ePL, we denote it using $E \mapsto_{\text{ePL}}^* v_1$.

Big-Step Evaluation

$$\frac{E \mapsto_{\text{ePL}}^* v_1 \quad p_1[v_1] >_{\text{ePL}} v_2}{p_1[E] \mapsto_{\text{ePL}}^* v_2} [\text{OpArg}_1]$$

$$\frac{E_1 \mapsto_{\text{ePL}}^* v_1 \quad E_2 \mapsto_{\text{ePL}}^* v_2 \quad p_2[v_1, v_2] >_{\text{ePL}} v}{p_2[E_1, E_2] \mapsto_{\text{ePL}}^* v} [\text{OpArg}_2]$$

Next Week

- Introduction of simPL