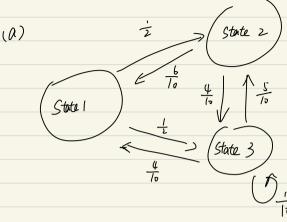
EECS 551 YUZHAN JIANG

Pol.



This is Markov chain with P + I, To is an equilibrium distribution

(b)
$$TLP = T$$

$$TL_1 = \frac{6}{70} TL_2 + \frac{4}{10} TL_3$$

$$TL_2 = \frac{1}{2} TL_1 + \frac{4}{10} TL_3 + \frac{4}{10} TL_3$$

$$TL_3 = \frac{1}{2} TL_1 + \frac{4}{10} TL_1 + \frac{4}{10} TL_3$$

$$TL_4 + \frac{4}{10} TL_2 + \frac{4}{10} TL_3 + \frac{4}{10} TL_3$$

=)
$$\pi_1 = \frac{1}{3}, \pi_2 = \frac{1}{3}$$

TV is the unique equilibrium distribution.

(C) This P matrix is irreducible and aperiodic \Rightarrow P is primitive \Rightarrow Therefore, the power iteration converges. \Rightarrow Therefore \Rightarrow P TUK is guaranteed to converge \Rightarrow TU.

P2.

Let
$$N=4$$
.

$$P = \begin{bmatrix} 0 & 0 & 0 & 1 \\ -p & 0 & 0 & 0 \\ -p & 0 & 0 & 0 \end{bmatrix}$$

$$PN = N$$

$$P = \begin{cases} 70_1 & 70_4 & 70_4 \\ 70_1 & 70_4 & 70_4 \\ 70_1 & 70_4 & 70_4 \end{cases}$$

$$PN = N$$

$$P = \begin{cases} 70_1 & 70_4 \\ 70_1 & 7$$

P3,

Convex Set:

if
$$\int \partial x_1 + (1-\theta) X_2 \in C$$
, then C is convex set

Let
$$P_1 = (x_1, x_1) \in B_r$$
 where $||x_1|| \in N$
 $P_2 = (x_2, x_2) \in B_r$ where $||x_1|| \in R$

$$\therefore \quad \chi = \quad \theta \times_1 + (1-\theta) \times_2 \quad \text{and} \quad \gamma = \quad \theta r_1 + (1-\theta) r_1$$

$$||X|| = ||\theta X_1 + (1-\theta) X_2|| \le ||\theta X_1|| + ||(-\theta) X_2||$$

P4:

(A) We rewrite
$$V(t) \triangleq (\max(1-t_10))^2 \implies V(t) = \begin{cases} (1-t)^2, & t \leq 1 \\ 0, & t \leq 1 \end{cases}$$

$$V(t) = \begin{cases} -2(t-t), & t \leq 1 \\ 0, & t \geq 1 \end{cases}$$

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$$= \frac{1}{2} \left(\frac{2}{AH} AM, : \mathcal{C}(AM) : \mathcal{K} \right) + \mathcal{F} \times$$

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$$= \frac{1}{2} \left(\frac{2}{A} (AX) + \mathcal{F} \times - A^{2} (AY) - \mathcal{F} Y \right) \left| \frac{1}{2} (AX) - \mathcal{C}(AY) \right| + \frac{2}{2} \left| \frac{2}{A} (AX) - \mathcal{C}(AX) \right$$

P6:

(A)

The eigenvalue of
$$I - \lambda NA$$

eig($I - \lambda NA$) = $I - \lambda$ eig (AA)
 $= I - \lambda \sigma_1^2(A) \leq I - \lambda \sigma_2^2(A) \cdots \leq I - \lambda \sigma_n^2$

$$P(1-\partial_{\frac{1}{2}}A/A) = 1-\partial_{\frac{1}{2}}\sigma_{N}^{2}A$$

$$= 1-\frac{2}{\sigma_{1}^{2}(A)+\sigma_{N}^{2}A}$$

$$= \sigma_{1}^{2}(A)-\sigma_{N}^{2}(A)$$

$$= \frac{\sigma_i^2(A) - \sigma_{N}^2(A)}{\sigma_i^2(A) + \sigma_{N}^2(A)}$$

(a)
$$x_{k+1} = x_k - \lambda Po A'(Ax - y)$$
, this is governed by the eigenvalue of $I - \lambda P^{\frac{1}{2}} A'A P^{\frac{1}{2}}$

$$\partial_{\psi} = \frac{2}{5i'(A\beta^{\frac{1}{2}}) + 5i'(A\beta^{\frac{1}{2}})}$$

$$= \frac{2}{0i(\beta^{\frac{1}{2}}A'A\beta^{\frac{1}{2}}) + 5i'(\beta^{\frac{1}{2}}A'A\beta^{\frac{1}{2}})}$$

b)
$$p_0 = (A'A)^{-1}$$

 $Thus, \qquad p_0^{\frac{1}{2}} A'A p_0^{\frac{1}{2}}$
 $= p_0^{\frac{1}{2}} p_0^{-1} p_0^{\frac{1}{2}}$
 $= I$
 $\therefore \quad b_* = \frac{2}{\sigma_1 + \sigma_N}$

P8, I wrote self-reflection on google form

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	. ,							
		I	have	None	Course	evaluation		
		<u> </u>	1.0.7		•			