

# q13

**Due** Oct 12 at 9am **Points** 5 **Questions** 5

**Available** Oct 11 at 9am - Oct 12 at 9am 1 day **Time Limit** 20 Minutes

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	14 minutes	2 out of 5

⚠ Correct answers will be available on Oct 12 at 9:01am.

Score for this quiz: **2** out of 5

Submitted Oct 11 at 10:46pm

This attempt took 14 minutes.

Incorrect

### Question 1

0 / 1 pts

Let  $A$  have SVD  $A = U\Sigma V'$ . The solution to

$$\hat{x} = \arg \max_{x: \|x\|_2=1} \|AA'x\|_2$$

, where  $A$  is a  $M \times N$  matrix of rank  $r$  is

☐  $u_M$

☐  $\sigma_1^2$

☐  $\sigma_1$

☐  $v_r$

☐  $v_1$

☐  $u_1$

☐  $u_N$ 
☐  $v_N$ 
☒  $u_r$ 
☐  $v_M$ 
☐ none of these

$$AA' = U\Sigma\Sigma'U'$$

so its principal right singular vector is  $u_1$ .

## Question 2

1 / 1 pts

A Hermitian matrix having some elements that are negative can be positive definite.

☒ True

☐ False

Yes, consider  $[3 \ -1; -1 \ 2]$

Incorrect

## Question 3

0 / 1 pts

The pseudoinverse of

$$A = \begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$$

is

☐  $\begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$

☐  $\begin{bmatrix} 1/2 & 1/2 \\ 0 & 0 \end{bmatrix}$

☐  $\begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix}$

☐  $\begin{bmatrix} 0 & 0 \\ 1/2 & 1/2 \end{bmatrix}$

☐  $\begin{bmatrix} 0 & 1/2 \\ 0 & 1/2 \end{bmatrix}$

☒  $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$

☐ None of these.

Here we have an outer product:

$$A = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \end{bmatrix}$$

.

Incorrect

Question 4

0 / 1 pts

Let  $U$  be an  $N \times N$  unitary matrix and let  $y$  be an  $N$ -dimensional vector. Which is the most computationally efficient Julia code for solving  $\arg \min_x \|Ux - y\|_2^2$ ?

☐ `x = inv(U) * y`

☒ `x = U \ y`

☐ `x = U' * y`

☐ `x = U / y`

☐ `y = U * y`

☐ The question cannot be answered with the given information.

☐ `x = pinv(U) * y`

Because  $U$  is unitary  $U^+ = U'$ .

### Question 5

1 / 1 pts

If  $U_1, U_2, U_3$  are all  $N \times N$  unitary matrices and  $\Phi = [U_1 \ U_2 \ U_3] / \sqrt{3}$  then the frame bound of  $\Phi$  is

☐  $1/\sqrt{3}$

☐ 3

☐  $1/3$

☐  $1/9$

☐ 9☐ 2☐  $\sqrt{3}$ ☐ None of these.☒ 1

$$\Phi\Phi' = I$$

$$\text{so } \sigma_1 = \sigma_N = 1$$

.

Quiz Score: **2** out of 5