

Step-1

(a)

The area of a triangle with coordinates of its three points (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is computed by the below formula:

$$\text{Area}(\Delta) = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} \quad (1)$$

Step-2

From the question, the three coordinates of the triangle are $(2, 1)$, $(3, 4)$ and $(0, 5)$. Substitute the coordinates in equation (1) to compute the area of the triangle:

$$\begin{aligned} \text{Area}(\Delta) &= \frac{1}{2} \begin{vmatrix} 2 & 1 & 1 \\ 3 & 4 & 1 \\ 0 & 5 & 1 \end{vmatrix} \\ &= \frac{1}{2} (2 \cdot (4 - 5) + 3 \cdot (5 - 1) + 0 \cdot (1 - 4)) \\ &= \frac{1}{2} (10) \\ &= 5 \end{aligned}$$

The area of the triangle is 5 square unit.

Step-3

(b)

Due to a new corner $(-1, 0)$, the area of the lopsided figure is the sum of the area of triangle calculated in part (a) and the area of the triangle formed by the three coordinates $(2, 1)$, $(0, 5)$ and $(-1, 0)$.

Step-4

Substitute the coordinates $(2, 1)$, $(0, 5)$ and $(-1, 0)$ in the expression (1) of part (a) to calculate the area of the triangle:

$$\begin{aligned}
 \text{Area}(\Delta) &= \frac{1}{2} \begin{vmatrix} 2 & 1 & 1 \\ 0 & 5 & 1 \\ -1 & 0 & 1 \end{vmatrix} \\
 &= \frac{1}{2} (2 \cdot (5 - 0) + 0 \cdot (0 - 1) - 1 \cdot (1 - 5)) \\
 &= \frac{1}{2} (10 + 4) \\
 &= 7
 \end{aligned}$$

Hence, the area of the lopsided figure is the sum areas of two triangles calculated in part **(a)** and part **(b)**:

$$\begin{aligned}
 \text{Area} &= 5 + 7 \\
 &= 12
 \end{aligned}$$

Therefore, the area of the lopsided figures comes out to be 12 square unit.