

## Step-1

Let  $A$  be a Hermitian matrix and  $c$  be any real scalar.

The objective is to show that  $cA$  is also Hermitian.

## Step-2

A matrix  $A$  is said to be Hermitian if it is equal to the conjugate transpose, that is  $A^H = A$ .

Now consider the expression,

$$\begin{aligned}(cA)^H &= \bar{c}A^H \\ &= cA^H \quad \text{As } c \text{ is real, so } \bar{c} = c. \\ &= cA \quad \text{As } A \text{ is Hermitian, so } A^H = A.\end{aligned}$$

As  $(cA)^H = cA$ , for any real scalar  $c$ , so  $cA$  is **Hermitian**.

## Step-3

Suppose  $c = i$ .

Now show that  $(iA)$  is skew-Hermitian.

A matrix  $A$  is said to be skew-Hermitian if  $A = -A^H$ .

Consider the expression,

$$\begin{aligned}(iA)^H &= \bar{i}A^H \\ &= (-i)A^H \quad \text{Use } \bar{i} = -i. \\ &= -iA \quad \text{As } A \text{ is Hermitian, so } A^H = A.\end{aligned}$$

As  $(iA)^H = -iA$ , so  $iA$  is a **skew-Hermitian**.