

Step-1

(i) If the points $(x, y, z), (2, 1, 0), (1, 1, 1), (0, 0, 0)$ are coplanar we get that

$$\begin{vmatrix} x & y & z & 1 \\ 2 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{vmatrix} = 0$$

and hence expanding by 4th row we get

$$\begin{vmatrix} x & y & z \\ 2 & 1 & 0 \\ 1 & 1 & 1 \end{vmatrix} = 0$$

Step-2

(ii) Now we need to find whether the vectors $(1, 0, -1), (2, 1, 0), (1, 1, 1)$ are independent or not.

So, consider

$$\begin{vmatrix} 1 & 0 & -1 \\ 2 & 1 & 0 \\ 1 & 1 & 1 \end{vmatrix} = \begin{vmatrix} 1 & 0 \\ 1 & 7 \end{vmatrix} - \begin{vmatrix} 2 & 1 \\ 1 & 1 \end{vmatrix}$$

$$= 1 - (2 - 1)$$

$$= 0$$

Step-3

So,

$(1, 0, -1), (2, 1, 0), (1, 1, 1)$ are not independent. Or equivalently the points

$(1, 0, -1), (2, 1, 0), (1, 1, 1), (0, 0, 0)$ are coplanar.