

Step-1

Suppose T is a reflection across the 45° line and S is a reflection across the y -axis.

And the domain \mathbf{V} is the x - y plane.

Let $v = (1, 2)$

Then $T(v) = (1, 2)$

Now we have to find $S(T(v))$ and $T(S(v))$.

Step-2

Now

$$S(T(v)) = S(1, 2)$$

$$= (-1, 2) \quad (\text{because } S \text{ is reflection across } y\text{-axis})$$

$$T(S(v)) = T(S(2, 1))$$

$$= T(-2, 1) \quad (\text{because } S \text{ is reflection across } y\text{-axis})$$

$$= (1, -2) \quad (\text{since } T \text{ is reflection across } 45^\circ \text{ line})$$

Therefore $\boxed{ST \neq TS}$