

## Step-1

Consider the matrix:

$$A = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

Calculate eigenvalues of  $A$  by  $|A - \lambda I| = 0$ ,

This implies;

$$\begin{bmatrix} 1-\lambda & 1 \\ 1 & 1-\lambda \end{bmatrix} = 0$$

This implies;

$$(1-\lambda)^2 - 1 = 0$$

$$(1-\lambda)^2 = 1$$

$$(1-\lambda) = \pm 1$$

This implies;

$$\lambda_1 = 2$$

$$\lambda_2 = 0$$

Thus, the Jordan form of  $A$  is given by,

$$J = \begin{bmatrix} 2 & 0 \\ 0 & 0 \end{bmatrix}$$

## Step-2

Consider the matrix:

$$B = \begin{bmatrix} 0 & 1 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
$$= \begin{bmatrix} 0 & C \\ 0 & 0 \end{bmatrix}$$

Thus,

$$C = \begin{bmatrix} 1 & 2 \\ 0 & 0 \end{bmatrix}$$

Calculate eigenvalues of  $C$  by  $|C - \lambda I| = 0$ ,

This implies;

$$\begin{bmatrix} 1-\lambda & 2 \\ 0 & -\lambda \end{bmatrix} = 0$$

This implies;

$$-\lambda(1-\lambda) = 0$$

This implies;

$$\lambda_1 = 1$$

$$\lambda_2 = 0$$

Thus, the Jordan form of  $B$  is given by,

$$J = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

### Step-3

Thus,  $J = \begin{bmatrix} 2 & 0 \\ 0 & 0 \end{bmatrix}$  and  $J = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ .