Step-1

We have to find that under what conditions on the columns of A (which may be rectangular) is $A^T A$ invertible.

If the columns of A are orthonormal, then $A^T A$ is a unit matrix.

Since a unit matrix is invertible and hence $A^T A$ is invertible.

Hence the required condition is the columns of A are orthonormal