

## Step-1

(a)

Use the Cramer's rule to solve for  $y$ :

$$ax + by = 1$$

$$cx + dy = 0$$

Calculate the determinant:

$$\begin{aligned}\det A &= \begin{vmatrix} a & b \\ c & d \end{vmatrix} \\ &= ad - bc\end{aligned}$$

## Step-2

To calculate only  $y$  therefore, calculate determinant of only matrix  $B_2$ :

$$\begin{aligned}|B_2| &= \begin{vmatrix} a & 1 \\ c & 0 \end{vmatrix} \\ &= c\end{aligned}$$

Use Cramer's rule ratio to determine  $y$ :

$$\begin{aligned}y &= \frac{|B_2|}{\det A} \\ &= \frac{c}{ad - bc}\end{aligned}$$

Hence,  $\boxed{y = \frac{c}{ad - bc}}$

## Step-3

(b)

Use the Cramer's rule to solve for  $y$ :

$$ax + by + cz = 1$$

$$dx + ey - fz = 0$$

$$gx + hy + iz = 0$$

From the question 3 by 3 determinant is  $D$ , hence,

$$\det A = \begin{vmatrix} a & b & c \\ d & e & -f \\ g & h & i \end{vmatrix}$$

$$= D$$

## Step-4

As we have to calculate only  $y$  therefore, calculate determinant of only matrix  $B_2$ :

$$|B_2| = \begin{vmatrix} a & 1 & c \\ d & 0 & -f \\ g & 0 & i \end{vmatrix}$$

$$= a \cdot (0 - 0) + d \cdot (0 - i) + g \cdot (0 + f)$$

$$= fg - id$$

Use Cramer's rule ratio to determine  $y$ :

$$y = \frac{|B_2|}{\det A}$$

$$= \frac{fg - id}{D}$$

Hence,  $\boxed{y = \frac{fg - id}{D}}$