## Step-1

We have to fill the following blanks:

Multiplying the rank 1 matrices,  $A = uv^T$  and  $B = wz^T$  gives  $uz^T$  times the number ----.

AB has rank 1 unless ---- = 0.

## Step-2

$$A = uv^{T}$$
 and  $B = wz^{T}$ , and rank  $A = 1$ , rank  $B = 1$ .

Rank 
$$(AB)$$
 = rank of  $(uv^T .wz^T)$   
= rank of  $(u(v^T .w)z^T)$ 

Multiplying the rank 1 matrices A,B gives  $uz^T$  times  $v^T.w$ .

And hence rank of AB = 1 unless  $v^T w = 0$ .