

Step-1

Consider $x_1 = x_0 + y$. Here $LUy = r$, where $r = b - Ax_0$. We get

$$\begin{aligned}x_1 &= x_0 + y \\LUx_1 &= LUx_0 + LUy \\&= LUx_0 + r \\LUx_1 &= LUx_0 + b - Ax_0 \\&= (LU - A)x_0 + b\end{aligned}$$

Step-2

Comparing this with $Sx_1 = Tx_0 + b$, we get

$$\boxed{\begin{aligned}S &= LU \\T &= LU - A\end{aligned}}$$

It should be clear that T is very small.