

Step-1

Consider the following equations:

$$x + y = 4$$

$$2x - 2y = 4$$

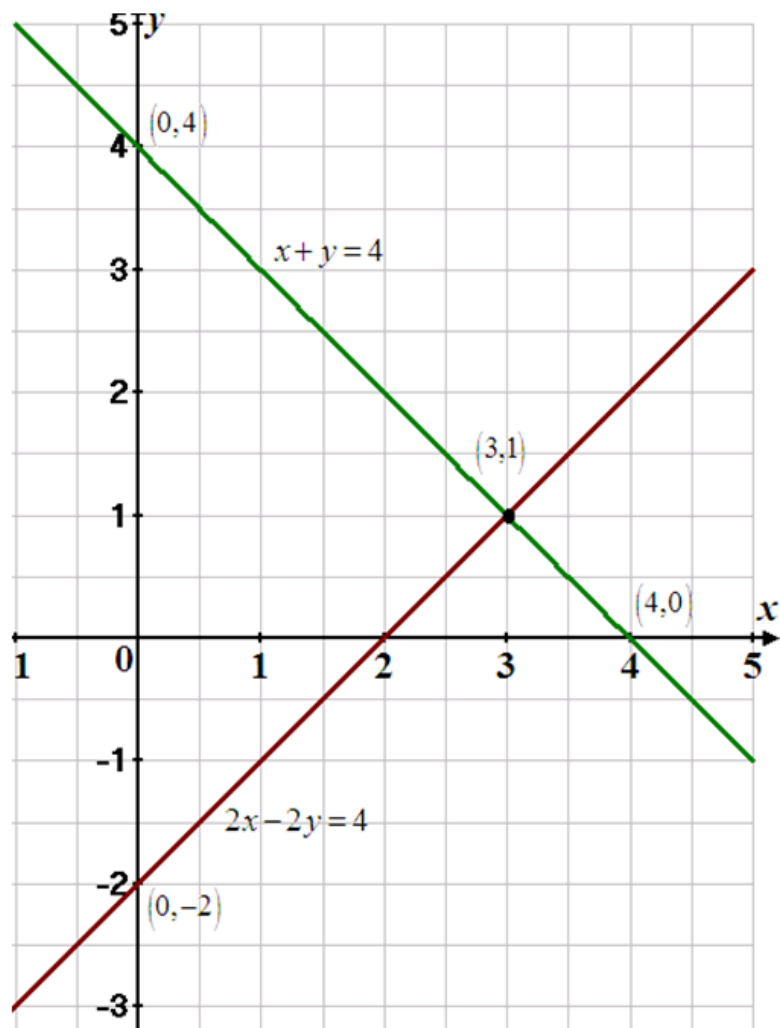
The equation $x + y = 4$ represented by a straight line in the x - y plane. The line goes through the points $x = 2, y = 2$ and $x = 4, y = 0$.

The second equation $2x - 2y = 4$ is also represented by a straight line in the x - y plane.

This line goes through the points $x = 0, y = -2$ and it crosses the first line at the solution.

Draw the row picture and the column picture for the equations $x + y = 4, 2x - 2y = 4$

The required diagram is shown as follows:



The two lines are intersecting at the point $(3, 1)$.

Step-2

Column form of the given equations as follows

$$x \begin{pmatrix} 1 \\ 2 \end{pmatrix} + y \begin{pmatrix} 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 4 \\ 4 \end{pmatrix}$$

Now consider

$$\begin{aligned}
 3\begin{pmatrix} 1 \\ 2 \end{pmatrix} + 1\begin{pmatrix} 1 \\ -2 \end{pmatrix} &= \begin{pmatrix} 3 \\ 6 \end{pmatrix} + \begin{pmatrix} 1 \\ -2 \end{pmatrix} \\
 &= \begin{pmatrix} 3+1 \\ 6-2 \end{pmatrix} \\
 &= \begin{pmatrix} 4 \\ 4 \end{pmatrix}
 \end{aligned}$$

Therefore $3(\text{column1}) + 1(\text{column2}) = (4, 4)$

Sketch the column picture as shown below.

