

Step-1

Given that $A.B = I = B.A$ (i)

$BC = I = CB$ (ii)

Let $(AB)C = A(BC)$ [Since by associative law]

$= A.I$ [Since by given $BC = I$]

$= A$ (a)

Step-2

Let $A(BC) = (AB).C$ [Since by associative law]

$= I.C$ [Since by given $AB = I$]

$= C$

We have $(AB)C = A(BC)$

$$\Rightarrow \boxed{A = C}$$

Hence proved.