

## Step-1

Consider the following:

$$Bx = \mu x$$

$$(I - A)x = \mu x$$

$$Ix - Ax = \mu x$$

$$x - \lambda x = \mu x$$

$$(1 - \lambda)x = \mu x$$

Thus,  $1 - \lambda = \mu$ . Therefore, eigenvalue of  $B$  is  $\boxed{1 - \lambda}$ .

## Step-2

Suppose the absolute value of eigenvalue of  $B$  is less than 1.

Thus, we have  $|1 - \lambda| < 1$ .

This is same as  $|\lambda - 1| < 1$

## Step-3

We know the following property of the absolute value function:

$$|x| < a \Rightarrow -a < x < a$$

By using the above property, we get

$$\begin{aligned} |\lambda - 1| < 1 \\ -1 < \lambda - 1 < 1 \end{aligned}$$

Adding 1 through the inequality, we get

$$0 < \lambda < 2$$

## Step-4

Thus, if the absolute value of eigenvalue of  $B$  is less than 1, the absolute value of the eigenvalue of  $A$  must lie between  $\boxed{0 \text{ and } 2}$ .