

Step-1

Given matrix $\begin{vmatrix} 4 & 4 & 4 & 4 \\ 1 & 2 & 0 & 1 \\ 2 & 0 & 1 & 2 \\ 1 & 1 & 0 & 2 \end{vmatrix}$

So, consider

$$\begin{vmatrix} 4 & 4 & 4 & 4 \\ 1 & 2 & 0 & 1 \\ 2 & 0 & 1 & 2 \\ 1 & 1 & 0 & 2 \end{vmatrix} \\ = 4 \begin{vmatrix} 2 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 0 & 2 \end{vmatrix} - 4 \begin{vmatrix} 1 & 0 & 1 \\ 2 & 1 & 2 \\ 1 & 0 & 2 \end{vmatrix} + 4 \begin{vmatrix} 1 & 2 & 1 \\ 2 & 0 & 2 \\ 1 & 1 & 2 \end{vmatrix} - 4 \begin{vmatrix} 1 & 2 & 0 \\ 2 & 0 & 1 \\ 1 & 1 & 0 \end{vmatrix}$$

Step-2

On solving

$$= 4[2(2) + 1(-1)] - 4[1(2) + (-1)] + 4[(-2) - 2(2) + 2] - 4[0 - 1 - 2(-1)] \\ = 4(3) - 4(1) + 4(-4) - 4(1) \\ = 4(3 - 1 - 4 - 1) \\ = 4(-3) \\ = \boxed{-12}$$

Step-3

b) We recomputed the same determinant by subtracting 1st column from other columns.

$$\begin{vmatrix} 4 & 4 & 4 & 4 \\ 1 & 2 & 0 & 1 \\ 2 & 0 & 1 & 2 \\ 1 & 1 & 0 & 2 \end{vmatrix} = \begin{vmatrix} 4 & 0 & 0 & 0 \\ 1 & 1 & -1 & 0 \\ 2 & -2 & -1 & 0 \\ 1 & 0 & -1 & 1 \end{vmatrix} \text{ subtracting 1st column from remaining columns}$$

$$= 4 \begin{vmatrix} 1 & -1 & 0 \\ -2 & -1 & 0 \\ 0 & -1 & 1 \end{vmatrix}$$

Step-4

On solving

$$= 4 \begin{vmatrix} 1 & -1 \\ -2 & -1 \end{vmatrix} \text{expanding by last columns}$$

$$= 4(-1-2)$$

$$= \boxed{-12}$$