## Step-1

The relation between  $F_{-k}$  and  $F_{k}$  is as follows:  $F_{-k} = (-1)^{k+1} F_{k}$ .

## Step-2

Since the difference equation of the Fibonacci series is  $F_{k+2} = F_{k+1} + F_k$ , we can write  $F_k = F_{k+2} - F_{k+1}$ . Thus, we get

$$\begin{split} F_0 &= F_2 - F_1 \\ &= 0 \\ F_{-1} &= F_1 - F_0 \end{split}$$

$$F_{-2} = F_0 - F_{-1}$$
$$= -1$$

$$F_{-3} = F_{-1} - F_{-2}$$
$$= 2$$

## Step-3

Thus, we can obtain the further terms of the Fibonacci series. It is as follows:

0, 1, â€"1, 2, â€"3, 5, â€"8 13, â€"21, â€"34, 55, â€"89,...

Thus, the numerical values of the terms remain the same and the terms are alternately positive and negative.

Thus, note the following:

$$F_{-1} = F_1$$

$$F_{-2} = -F_2$$

$$F_{-3} = F_3$$

$$F_{-4} = -F_4$$

And so on!