

Step-1

If P is any permutation matrix, we have to find a nonzero matrix x such that $(I - P)x = 0$

Given that $(I - P)x = 0$

$$\Rightarrow Ix - Px = 0$$

$$\Rightarrow Ix = Px$$

$$\Rightarrow x = Px$$

Since by matrices multiplication and because I is identity so $Ix = x$

This will happens if $x = (1, 1, \dots, 1)$

Step-2

Because for instance let $x = (1, 1, 1)$ and P be 3 by 3 permutation matrix equals to I then

$$Px = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

$$= \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$$

$$= x$$