

Step-1

Let A be a 3×3 matrix such that $\det A = -1$.

a) We have to find $\det\left(\frac{1}{2}A\right)$.

We know that if A is an $n \times n$ matrix then $\det(kA) = k^n \det A$.

Now

$$\begin{aligned}\det\left(\frac{1}{2}A\right) &= \left(\frac{1}{2}\right)^n \det(A) \\ &= \left(\frac{1}{2}\right)^3 (-1) \quad (\text{Since } n=3) \\ &= -\frac{1}{8}\end{aligned}$$

Thus, $\boxed{\det\left(\frac{1}{2}A\right) = -\frac{1}{8}}$

Step-2

b) We have to find $\det(-A)$.

Now

$$\begin{aligned}\det(-A) &= -\det(A) \\ &= -(-1) \\ &= 1\end{aligned}$$

Thus, $\boxed{\det(-A) = 1}$

Step-3

c) We have to find $\det(A^2)$.

We know that $\det(A^n) = (\det A)^n$.

Now

$$\det(A^2) = (\det(A))^2$$

$$= (-1)^2$$

$$= 1$$

Thus, $\boxed{\det(A^2) = 1}$

Step-4

d) We have to find $\det(A^{-1})$.

Now

$$\det(A^{-1}) = \frac{1}{\det(A)}$$

$$= \frac{1}{-1}$$

$$= -1$$

Thus, $\boxed{\det(A^{-1}) = -1}$