

## Step-1

Thus, we have

$$\begin{vmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{vmatrix} = \begin{vmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{vmatrix} \begin{vmatrix} 1 & 2 \\ 4 & 5 \\ 7 & 8 \end{vmatrix}$$

The elements along the diagonal are  $(1,5,9)$ ,  $(2,6,7)$ , and  $(3,4,8)$ . The elements along the anti diagonal are  $(2,4,9)$ ,  $(1,6,8)$ , and  $(3,5,7)$ .

Therefore,  $\det(A) = (1 \times 5 \times 9 + 2 \times 6 \times 7 + 3 \times 4 \times 8) - (2 \times 4 \times 9 + 1 \times 6 \times 8 + 3 \times 5 \times 7)$ .

## Step-2

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

Consider the matrix

Observe that  $\boxed{2A - \text{Row } 2 \hat{=} \text{Row } 3 = \text{Row } 1}$ .

Therefore, the rows of the above matrix are not linearly independent. Therefore, this matrix is not invertible.

## Step-3

Also, note the following:

$$\begin{aligned} \det(A) &= (1 \times 5 \times 9 + 2 \times 6 \times 7 + 3 \times 4 \times 8) - (2 \times 4 \times 9 + 1 \times 6 \times 8 + 3 \times 5 \times 7) \\ &= (45 + 84 + 96) - (72 + 48 + 105) \\ &= 225 - 225 \\ &= \boxed{0} \end{aligned}$$

This also tells us that the matrix  $\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$  is not invertible.