

Step-1

a) If $Ax = b$ has two solutions x_1 and x_2 , then we have to find two solutions to $Ax = 0$.

If $Ax = b$ has two solutions x_1 and x_2 then

$$Ax_1 = b \text{ and } Ax_2 = b$$

Now consider $A(x_1 - x_2)$

$$= Ax_1 - Ax_2$$

$$= b - b$$

$$= 0$$

Therefore $x_1 - x_2$ is a solution of $Ax = 0$

Step-2

If we consider $A(2x_1 - 2x_2)$

$$= 2(Ax_1 - Ax_2)$$

$$= 2(b - b)$$

$$= 0$$

Therefore $2(x_1 - x_2)$ is also a solution of $Ax = 0$

Step-3

b) We have to find another solution to $Ax = b$

If we consider

$$A(2x_1 - x_2) = 2Ax_1 - Ax_2$$

$$= 2b - b$$

$$= b$$

Therefore $A(2x_1 - x_2) = b$

Hence $2x_1 - x_2$ is another solution of $Ax = b$