

## Step-1

We have to find what matrix represents multiplication by  $2+3t$  from the cubics  $\mathbf{P}_3$  to the fourth degree polynomials  $\mathbf{P}_4$ .

## Step-2

We know that the standard basis of  $\mathbf{P}_3$  is  $1, t, t^2, t^3$  and the standard basis of  $\mathbf{P}_4$  is  $1, t, t^2, t^3, t^4$ .

Therefore,

$$\begin{aligned}1(2+3t) &= 2+3t \\ &= 2.1 + 3.t + 0.t^2 + 0.t^3 + 0.t^4\end{aligned}$$

$$\begin{aligned}t(2+3t) &= 2t+3t^2 \\ &= 0.1 + 2.t + 3.t^2 + 0.t^3 + 0.t^4\end{aligned}$$

## Step-3

And

$$\begin{aligned}t^2(2+3t) &= 2t^2+3t^3 \\ &= 0.1 + 0.t + 2.t^2 + 3.t^3 + 0.t^4\end{aligned}$$

$$\begin{aligned}t^3(2+3t) &= 2t^3+3t^4 \\ &= 0.1 + 0.t + 0.t^2 + 2.t^3 + 3.t^4\end{aligned}$$

Therefore, the required matrix is 
$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 3 & 2 & 0 & 0 \\ 0 & 3 & 2 & 0 \\ 0 & 0 & 3 & 2 \\ 0 & 0 & 0 & 3 \end{bmatrix}.$$

$$\begin{bmatrix} 2 & 0 & 0 & 0 \\ 3 & 2 & 0 & 0 \\ 0 & 3 & 2 & 0 \\ 0 & 0 & 3 & 2 \\ 0 & 0 & 0 & 3 \end{bmatrix}$$

Hence the matrix that represents the multiplication by  $2+3t$  in  $\mathbf{P}_4$  is