

Step-1

Suppose that A^2 is the inverse of the matrix B .

The objective is to show that the inverse of A is AB .

Step-2

Use the result that if M is the inverse of N then $NM^{-1} = M^{-1}N = I$ (1)

Since A^2 is the inverse of the matrix B , so

$$A^2B = BA^2 = I.$$

Use the equation $A^2B = I$ to get the result.

$$\begin{array}{ll} A^2B = I & \\ (AA)B = I & \text{Use } A^2 = AA \\ A(AB) = I & \text{Associative law holds for matrix multiplication.} \end{array}$$

By the result in (1), the product AB is the inverse of the matrix A .