

Step-1

If A is an m by n matrix, using row operations, we can reduce A to r non zero rows and $m - r$ zero rows. Then

1. $C(A)$ = Column space of A ; dimension r
2. $N(A)$ = null space of A ; dimension $n - r$
3. $C(A^T)$ = row space of A ; dimension r
4. $N(A^T)$ = left null space of A ; dimension $m - r$

Step-2

If A is an n by $n - 1$ matrix and rank is $n - 2$

We know that $\text{rank } A + \dim N(A) = \text{Number of columns}$

$$n - 2 + \dim(N(A)) = n - 1$$

$$\dim(N(A)) = 1$$

Therefore, the dimension of null space = 1