

## Step-1

We have to show that  $A = 4 * eye(4) - ones(4,4)$  is not invertible.

## Step-2

Given that  $A = 4 * eye(4) - ones(4,4)$

$$= 4 * \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 0 & 0 & 0 \\ 0 & 4 & 0 & 0 \\ 0 & 0 & 4 & 0 \\ 0 & 0 & 0 & 4 \end{bmatrix} - \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 3 & -1 & -1 & -1 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 3 & -1 \\ -1 & -1 & -1 & 3 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & -1 & -1 & -1 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 3 & -1 \\ -1 & -1 & -1 & 3 \end{bmatrix}$$

Therefore,

## Step-3

Now we have to multiply  $A * ones(4,1)$ .

Now

$$\begin{aligned}
\begin{bmatrix} 3 & -1 & -1 & -1 \\ -1 & 3 & -1 & -1 \\ -1 & -1 & 3 & -1 \\ -1 & -1 & -1 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} &= \begin{bmatrix} 3(1)+(-1)1+(-1)1+(-1)1 \\ (-1)(1)+(3)1+(-1)1+(-1)1 \\ (-1)(1)+(-1)1+(3)1+(-1)1 \\ (-1)(1)+(-1)1+(-1)1+(3)1 \end{bmatrix} \\
&= \begin{bmatrix} 3-1-1-1 \\ -1+3-1-1 \\ -1-1+3-1 \\ -1-1-1+3 \end{bmatrix} \\
&= \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}
\end{aligned}$$

Therefore, the system  $Ax = 0$  has zero solution.

Hence  $A$  is not invertible.