

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

26. Construct the lowest-degree polynomial given the zeros below. Then, choose the intervals that contain the coefficients of the polynomial in the form  $x^3 + bx^2 + cx + d$ .

$$-5 + 4i \text{ and } -5 - 4i$$

The solution is  $x^3 + 14x^2 + 81x + 164$

A.  $b \in [13, 20]$ ,  $c \in [77, 87]$ , and  $d \in [161, 165]$

\*  $x^3 + 14x^2 + 81x + 164$ , which is the correct option.

B.  $b \in [-22, -9]$ ,  $c \in [77, 87]$ , and  $d \in [-169, -163]$

$x^3 - 14x^2 + 81x - 164$ , which corresponds to multiplying out  $(x - (-5 + 4i))(x - (-5 - 4i))(x - 4)$ .

C.  $b \in [-5, 7]$ ,  $c \in [-2, 4]$ , and  $d \in [-17, -8]$

$x^3 + x^2 - 16$ , which corresponds to multiplying out  $(x - 4)(x + 4)$ .

D.  $b \in [-5, 7]$ ,  $c \in [7, 11]$ , and  $d \in [19, 22]$

$x^3 + x^2 + 9x + 20$ , which corresponds to multiplying out  $(x + 5)(x + 4)$ .

E. None of the above.

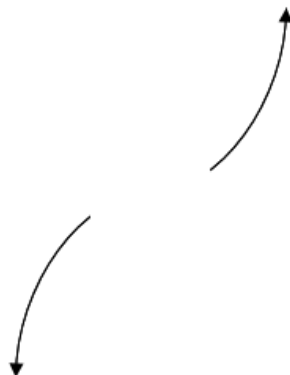
This corresponds to making an unanticipated error or not understanding how to use nonreal complex numbers to create the lowest-degree polynomial. If you chose this and are not sure what you did wrong, please contact the coordinator for help.

General Comments: Remember that the conjugate of  $a + bi$  is  $a - bi$ . Since these zeros always come in pairs, we need to multiply out  $(x - (-5 + 4i))(x - (-5 - 4i))(x - (-4))$ .

27. Describe the end behavior of the polynomial below.

$$f(x) = 9(x - 6)^3(x + 6)^4(x + 5)^2(x - 5)^4$$

The solution is



<p><b>A.</b></p> <p>A graph of a cubic function on a Cartesian coordinate system. The curve starts from the bottom-left, rises to a local maximum, falls to a local minimum, and then rises again towards the top-right. Arrows at both ends indicate the direction of the curve as it continues infinitely.</p>	<p><b>B.</b></p> <p>A graph of a cubic function on a Cartesian coordinate system. The curve starts from the bottom-left, rises to a local maximum, falls to a local minimum, and then rises again towards the top-right. Arrows at both ends indicate the direction of the curve as it continues infinitely.</p>
<p><b>C.</b></p> <p>A graph of a cubic function on a Cartesian coordinate system. The curve starts from the bottom-left, rises to a local maximum, falls to a local minimum, and then rises again towards the top-right. Arrows at both ends indicate the direction of the curve as it continues infinitely.</p>	<p><b>D.</b></p> <p>A graph of a cubic function on a Cartesian coordinate system. The curve starts from the bottom-left, rises to a local maximum, falls to a local minimum, and then rises again towards the top-right. Arrows at both ends indicate the direction of the curve as it continues infinitely.</p>
<p>E. None of the figures above.</p>	

**General Comments:** Remember that end behavior is determined by the leading coefficient AND whether the **sum** of the multiplicities is positive or negative.

28. Construct the lowest-degree polynomial given the zeros below. Then, choose the intervals that contain the coefficients of the polynomial in the form  $ax^3 + bx^2 + cx + d$ .

$$\frac{-1}{2}, 6, \text{ and } \frac{-1}{4}$$

The solution is  $8x^3 - 42x^2 - 35x - 6$

A.  $a \in [0, 16], b \in [43, 49], c \in [-17, -4],$  and  $d \in [-15, -3]$

$8x^3 + 46x^2 - 13x - 6$ , which corresponds to multiplying out  $(2x + 2)(x + 1)(4x - 4)$ .

B.  $a \in [0, 16], b \in [-49, -38], c \in [-41, -25],$  and  $d \in [-15, -3]$

\*  $8x^3 - 42x^2 - 35x - 6$ , which is the correct option.

C.  $a \in [0, 16], b \in [-49, -38], c \in [-41, -25],$  and  $d \in [1, 9]$

$8x^3 - 42x^2 - 35x + 6$ , which corresponds to multiplying everything correctly except the constant term.

D.  $a \in [0, 16], b \in [41, 44], c \in [-41, -25],$  and  $d \in [1, 9]$

$8x^3 + 42x^2 - 35x + 6$ , which corresponds to multiplying out  $(2x - 1)(x + 6)(4x - 1)$ .

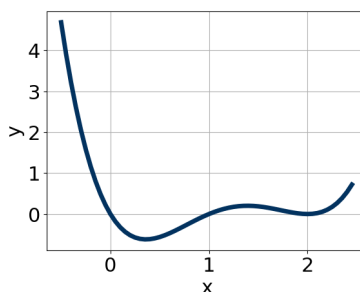
E.  $a \in [0, 16], b \in [-57, -48], c \in [10, 13],$  and  $d \in [1, 9]$

$8x^3 - 50x^2 + 11x + 6$ , which corresponds to multiplying out  $(2x + 2)(x - 1)(4x - 4)$ .

General Comments: To construct the lowest-degree polynomial, you want to multiply out  $(2x + 1)(x - 6)(4x + 1)$

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29. Which of the following equations *could* be of the graph presented below?



The solution is  $7x^9(x - 2)^8(x - 1)^9$

A.  $-14x^7(x - 2)^6(x - 1)^5$

This corresponds to the leading coefficient being the opposite value than it should be.

B.  $-3x^8(x - 2)^4(x - 1)^7$

The factor  $x$  should have an odd power and the leading coefficient should be the opposite sign.

C.  $7x^9(x - 2)^8(x - 1)^9$

\* This is the correct option.

D.  $19x^9(x - 2)^7(x - 1)^4$

The factor 2 should have an even power and the factor 1 should have an odd power.

E.  $9x^7(x - 2)^{10}(x - 1)^8$

The factor  $(x - 1)$  should have an odd power.

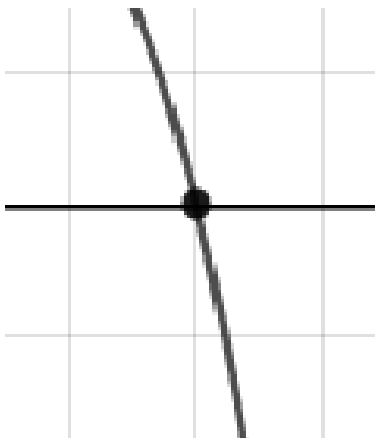
General Comments: Draw the x-axis to determine which zeros are touching (and so have even multiplicity) or cross (and have odd multiplicity).

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30. Describe the zero behavior of the zero  $x = -6$  of the polynomial below.

$$f(x) = 6(x + 6)^3(x - 6)^4(x + 3)^4(x - 3)^7$$

The solution is



<p>A.</p>	<p>B.</p>
<p>C.</p>	<p>D.</p>
<p>E. None of the figures above.</p>	

**General Comments:** You will need to sketch the entire graph, then zoom in on the zero the question asks about.