

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

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1. Determine the domain of the function below.

$$f(x) = \frac{4}{20x^2 - 9x - 20}$$

The solution is All Real numbers except  $x = -0.800$  and  $x = 1.250$ ., which is option D.

- A. All Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-22, -15]$  and  $b \in [17, 21]$

All Real numbers except  $x = -20.000$  and  $x = 20.000$ , which corresponds to not factoring the denominator correctly.

- B. All Real numbers except  $x = a$ , where  $a \in [-22, -15]$

All Real numbers except  $x = -20.000$ , which corresponds to removing a distractor value from the denominator.

- C. All Real numbers except  $x = a$ , where  $a \in [-0.8, 0.2]$

All Real numbers except  $x = -0.800$ , which corresponds to removing only 1 value from the denominator.

- D. All Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-0.8, 0.2]$  and  $b \in [1.25, 2.25]$

All Real numbers except  $x = -0.800$  and  $x = 1.250$ , which is the correct option.

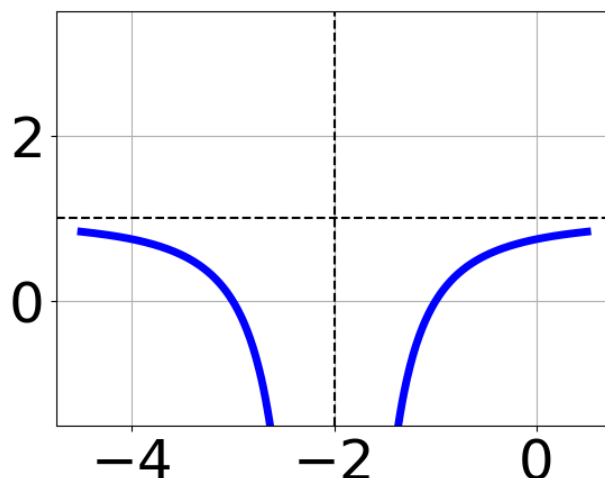
- E. All Real numbers.

This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers.

**General Comment:** Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

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2. Choose the equation of the function graphed below.



The solution is None of the above as it should be  $f(x) = \frac{-1}{(x+2)^2} + 1$ , which is option E.

A.  $f(x) = \frac{1}{x-2} + 7$

Corresponds to thinking the graph was a shifted version of  $\frac{1}{x}$ , using the general form  $f(x) = \frac{a}{(x+h)^2} + k$ , the opposite leading coefficient, AND not noticing the  $y$ -value was wrong.

B.  $f(x) = \frac{1}{(x-2)^2} + 7$

Corresponds to using the general form  $f(x) = \frac{a}{(x+h)^2} + k$ , the opposite leading coefficient, AND not noticing the  $y$ -value was wrong.

C.  $f(x) = \frac{-1}{x+2} + 7$

Corresponds to thinking the graph was a shifted version of  $\frac{1}{x}$  AND not noticing the  $y$ -value was wrong.

D.  $f(x) = \frac{-1}{(x+2)^2} + 7$

The  $y$ -value of the equation does not match the graph.

E. None of the above

None of the equation options were the correct equation.

**General Comment:** Remember that the general form of a basic rational equation is  $f(x) = \frac{a}{(x-h)^n} + k$ , where  $a$  is the leading coefficient (and in this case, we assume is either 1 or  $-1$ ),  $n$  is the degree (in this case, either 1 or 2), and  $(h, k)$  is the intersection of the asymptotes.

3. Solve the rational equation below. Then, choose the interval(s) that the solution(s) belongs to.

$$\frac{-4}{9x-4} + 7 = \frac{-6}{72x-32}$$

The solution is  $x = 0.496$ , which is option A.

A.  $x \in [0.5, 2.5]$

\*  $x = 0.496$ , which is the correct option.

B.  $x \in [-0.42, -0.29]$

$x = -0.393$ , which corresponds to not distributing the factor  $9x - 4$  correctly when trying to eliminate the fraction.

C.  $x_1 \in [-0.42, -0.29]$  and  $x_2 \in [-0.5, 1.5]$

$x = -0.393$  and  $x = 0.496$ , which corresponds to getting the correct solution and believing there should be a second solution to the equation.

D. All solutions lead to invalid or complex values in the equation.

This corresponds to thinking  $x = 0.496$  leads to dividing by zero in the original equation, which it does not.

E.  $x_1 \in [0.41, 0.48]$  and  $x_2 \in [-0.5, 1.5]$

$x = 0.413$  and  $x = 0.496$ , which corresponds to getting the correct solution and believing there should be a second solution to the equation.

**General Comment:** Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

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4. Determine the domain of the function below.

$$f(x) = \frac{4}{18x^2 + 18x - 36}$$

The solution is All Real numbers except  $x = -2.000$  and  $x = 1.000$ ., which is option C.

A. All Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-19, -16]$  and  $b \in [33, 38]$

All Real numbers except  $x = -18.000$  and  $x = 36.000$ , which corresponds to not factoring the denominator correctly.

B. All Real numbers.

This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers.

C. All Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-4, -1]$  and  $b \in [0, 4]$

All Real numbers except  $x = -2.000$  and  $x = 1.000$ , which is the correct option.

D. All Real numbers except  $x = a$ , where  $a \in [-4, -1]$

All Real numbers except  $x = -2.000$ , which corresponds to removing only 1 value from the denominator.

E. All Real numbers except  $x = a$ , where  $a \in [-19, -16]$

All Real numbers except  $x = -18.000$ , which corresponds to removing a distractor value from the denominator.

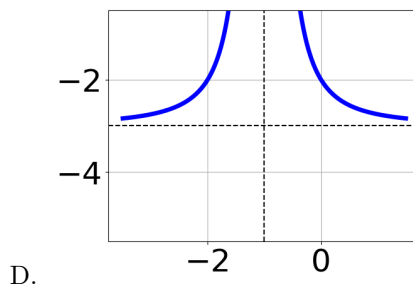
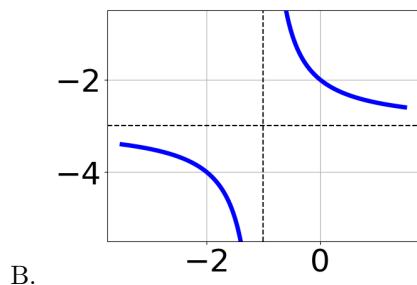
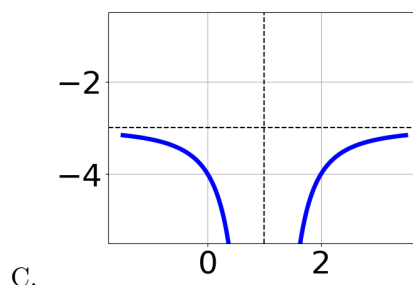
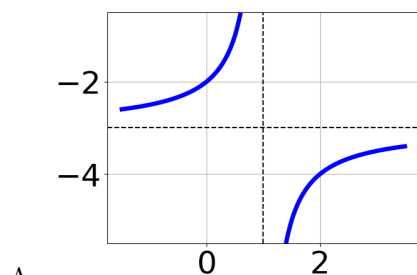
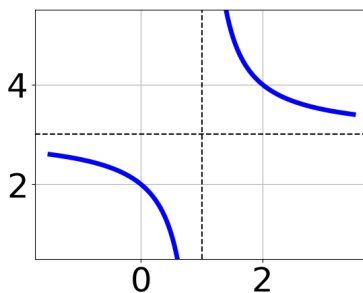
**General Comment:** Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

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5. Choose the graph of the equation below.

$$f(x) = \frac{1}{x-1} + 3$$

The solution is the graph below, which is option E.



- E. None of the above.

**General Comment:** Remember that the general form of a basic rational equation is  $f(x) = \frac{a}{(x-h)^n} + k$ , where  $a$  is the leading coefficient (and in this case, we assume is either 1 or  $-1$ ),  $n$  is the degree (in this case, either 1 or 2), and  $(h, k)$  is the intersection of the asymptotes.

6. Solve the rational equation below. Then, choose the interval(s) that the solution(s) belongs to.

$$\frac{56}{28x+56} + 1 = \frac{56}{28x+56}$$

The solution is all solutions are invalid or lead to complex values in the equation., which is option A.

- A. All solutions lead to invalid or complex values in the equation.

\* $x = -2.000$  leads to dividing by 0 in the original equation and thus is not a valid solution, which is the correct option.

B.  $x_1 \in [-3, 1]$  and  $x_2 \in [-2, -1]$

$x = -2.000$  and  $x = -2.000$ , which corresponds to getting the correct solution and believing there should be a second solution to the equation.

C.  $x \in [-3.0, -1.0]$

$x = -2.000$ , which corresponds to not checking if this value leads to dividing by 0 in the original equation and thus is not a valid solution.

D.  $x_1 \in [-3, 1]$  and  $x_2 \in [1, 6]$

$x = -2.000$  and  $x = 2.000$ , which corresponds to getting the correct solution and believing there should be a second solution to the equation.

E.  $x \in [2, 4]$

$x = 2.000$ , which corresponds to not distributing the factor  $28x + 56$  correctly when trying to eliminate the fraction.

**General Comment:** Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

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7. Solve the rational equation below. Then, choose the interval(s) that the solution(s) belongs to.

$$\frac{6x}{4x-6} + \frac{-4x^2}{28x^2-58x+24} = \frac{-5}{7x-4}$$

The solution is There are two solutions:  $x = -0.837$  and  $x = 0.943$ , which is option B.

A. All solutions lead to invalid or complex values in the equation.

B.  $x_1 \in [-1.15, 0.02]$  and  $x_2 \in [0.91, 1.23]$

\*  $x = -0.837$  and  $x = 0.943$ , which is the correct option.

C.  $x \in [0.93, 1.79]$

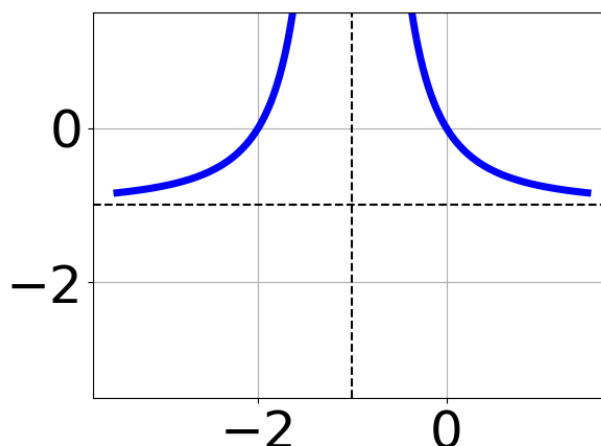
D.  $x \in [0.54, 0.72]$

E.  $x_1 \in [-1.15, 0.02]$  and  $x_2 \in [1.09, 1.6]$

**General Comment:** Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

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8. Choose the equation of the function graphed below.



The solution is  $f(x) = \frac{1}{(x+1)^2} - 1$ , which is option D.

A.  $f(x) = \frac{1}{x+1} - 1$

Corresponds to thinking the graph was a shifted version of  $\frac{1}{x}$ .

B.  $f(x) = \frac{-1}{x-1} - 1$

Corresponds to thinking the graph was a shifted version of  $\frac{1}{x}$ , using the general form  $f(x) = \frac{a}{(x+h)^2} + k$ , and the opposite leading coefficient.

C.  $f(x) = \frac{-1}{(x-1)^2} - 1$

Corresponds to using the general form  $f(x) = \frac{a}{(x+h)^2} + k$  and the opposite leading coefficient.

D.  $f(x) = \frac{1}{(x+1)^2} - 1$

This is the correct option.

E. None of the above

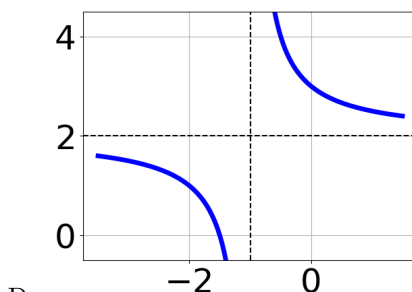
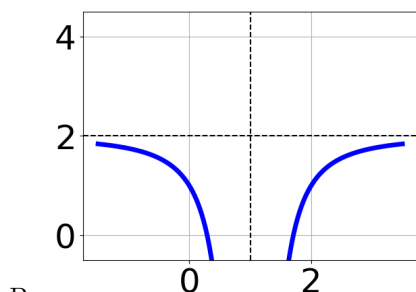
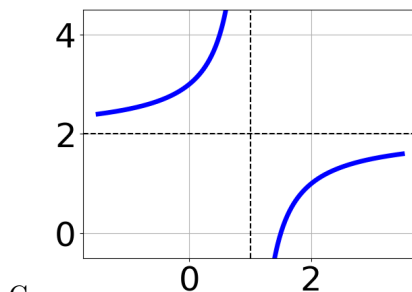
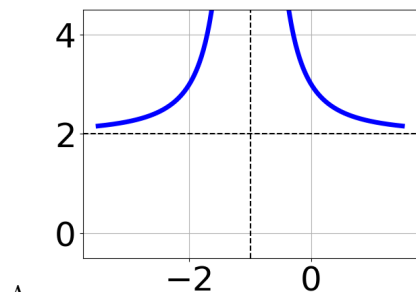
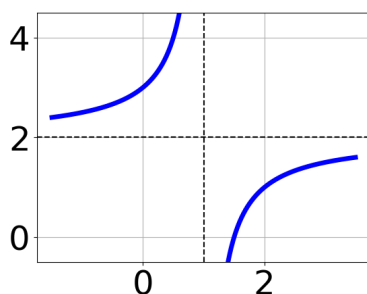
This corresponds to believing the vertex of the graph was not correct.

**General Comment:** Remember that the general form of a basic rational equation is  $f(x) = \frac{a}{(x-h)^n} + k$ , where  $a$  is the leading coefficient (and in this case, we assume is either 1 or  $-1$ ),  $n$  is the degree (in this case, either 1 or 2), and  $(h, k)$  is the intersection of the asymptotes.

9. Choose the graph of the equation below.

$$f(x) = \frac{-1}{x-1} + 2$$

The solution is the graph below, which is option C.



E. None of the above.

**General Comment:** Remember that the general form of a basic rational equation is  $f(x) = \frac{a}{(x-h)^n} + k$ , where  $a$  is the leading coefficient (and in this case, we assume is either 1 or  $-1$ ),  $n$  is the degree (in this case, either 1 or 2), and  $(h, k)$  is the intersection of the asymptotes.

10. Solve the rational equation below. Then, choose the interval(s) that the solution(s) belongs to.

$$\frac{5x}{-2x-5} + \frac{-4x^2}{-6x^2-x+35} = \frac{3}{3x-7}$$

The solution is There are two solutions:  $x = 0.707$  and  $x = 1.930$ , which is option E.

A.  $x \in [2.16, 2.42]$

B.  $x_1 \in [0.44, 1.31]$  and  $x_2 \in [-3.2, -1.4]$

C. All solutions lead to invalid or complex values in the equation.

D.  $x \in [0.76, 2.18]$

E.  $x_1 \in [0.44, 1.31]$  and  $x_2 \in [-0.6, 2.8]$

\*  $x = 0.707$  and  $x = 1.930$ , which is the correct option.

**General Comment:** Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

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