This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

26. Construct the lowest-degree polynomial given the zeros below. Then, choose the intervals that contain the coefficients of the polynomial in the form $ax^3 + bx^2 + cx + d$.

$$\frac{4}{5}, \frac{-7}{4}, \text{ and } \frac{5}{3}$$

The solution is $60x^3 - 43x^2 - 179x + 140$

A. $a \in [57, 68], b \in [52, 55], c \in [-173, -166], \text{ and } d \in [-143, -138]$

 $60x^3 + 53x^2 - 171x - 140$, which corresponds to multiplying out (5x + 5)(4x - 4)(3x - 3).

B. $a \in [57, 68], b \in [42, 47], c \in [-186, -177], \text{ and } d \in [-143, -138]$

 $60x^3 + 43x^2 - 179x - 140$, which corresponds to multiplying out (5x + 4)(4x - 7)(3x + 5).

C. $a \in [57, 68], b \in [-48, -38], c \in [-186, -177], \text{ and } d \in [137, 145]$

* $60x^3 - 43x^2 - 179x + 140$, which is the correct option.

D. $a \in [57, 68], b \in [-48, -38], c \in [-186, -177], \text{ and } d \in [-143, -138]$

 $60x^3 - 43x^2 - 179x - 140$, which corresponds to multiplying everything correctly except the constant term.

E. $a \in [57, 68], b \in [-165, -155], c \in [8, 12], \text{ and } d \in [137, 145]$

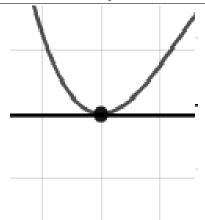
 $60x^3 - 157x^2 + 11x + 140$, which corresponds to multiplying out (5x + 5)(4x + 4)(3x - 3).

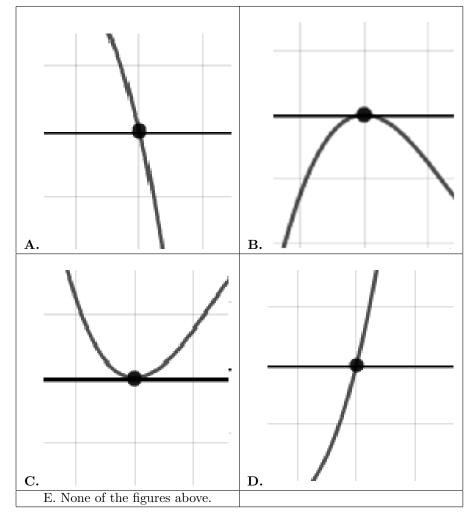
General Comments: To construct the lowest-degree polynomial, you want to multiply out (5x - 4)(4x + 7)(3x - 5)

27. Describe the zero behavior of the zero x = 5 of the polynomial below.

$$f(x) = 2(x+6)^{11}(x-6)^8(x+5)^9(x-5)^8$$

The solution is

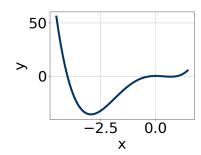




- A.
- В.
- C.
- D.

General Comments: You will need to sketch the entire graph, then zoom in on the zero the question asks about.

28. Which of the following equations *could* be of the graph presented below?



The solution is $19x^{8}(x-1)^{7}(x+4)^{5}$

A.
$$19x^8(x-1)^7(x+4)^5$$

* This is the correct option.

B.
$$-18x^{10}(x-1)^9(x+4)^{11}$$

This corresponds to the leading coefficient being the opposite value than it should be.

C.
$$19x^{10}(x-1)^4(x+4)^7$$

The factor (x-1) should have an odd power.

D.
$$-15x^6(x-1)^9(x+4)^4$$

The factor (x + 4) should have an odd power and the leading coefficient should be the opposite sign.

E.
$$17x^7(x-1)^6(x+4)^7$$

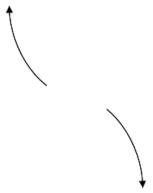
The factor 0 should have an even power and the factor 1 should have an odd power.

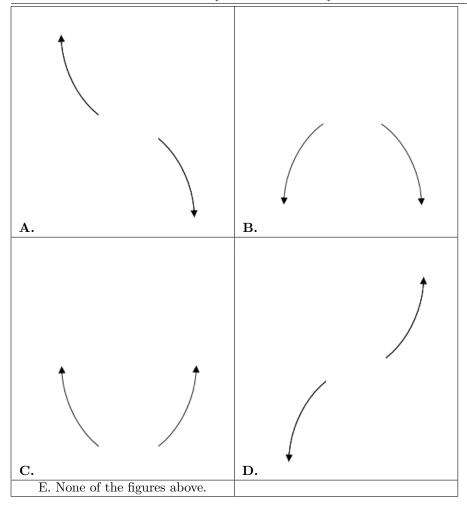
General Comments: Draw the x-axis to determine which zeros are touching (and so have even multiplicity) or cross (and have odd multiplicity).

29. Describe the end behavior of the polynomial below.

$$f(x) = -3(x-9)^{2}(x+9)^{3}(x+2)^{4}(x-2)^{6}$$

The solution is





- A. The function is above the x-axis, then passes through.
- B. The function is below the x-axis, then touches.
- C. The function is above the x-axis, then touches.
- D. The function is below the x-axis, then passes through.

General Comments: Remember that end behavior is determined by the leading coefficient AND whether the **sum** of the multiplicities is positive or negative.

30. Construct the lowest-degree polynomial given the zeros below. Then, choose the intervals that contain the coefficients of the polynomial in the form $x^3 + bx^2 + cx + d$.

$$3 + 4i \text{ and } -4$$

The solution is $x^3 - 2x^2 + x + 100$

A. $b \in [0.9, 1.29], c \in [0.57, 2.03]$, and $d \in [-15, -9]$ $x^3 + x^2 + x - 12$, which corresponds to multiplying out (x - 3)(x + 4).

B.
$$b \in [0.9, 1.29], c \in [-0.81, 0.51]$$
, and $d \in [-23, -14]$
 $x^3 + x^2 - 16$, which corresponds to multiplying out $(x - 4)(x + 4)$.

Answer Key for Module 6 - Polynomial Functions Version A

- C. $b \in [-2.11, -1.02], c \in [0.57, 2.03], \text{ and } d \in [98, 102]$ * $x^3 - 2x^2 + x + 100$, which is the correct option.
- D. $b \in [1.03, 2.65], c \in [0.57, 2.03], \text{ and } d \in [-101, -98]$ $x^3 + 2x^2 + x - 100, \text{ which corresponds to multiplying out } (x - (3 + 4i))(x - (3 - 4i))(x - 4).$
- E. None of the above.

This corresponds to making an unanticipated error or not understanding how to use nonreal complex numbers to create the lowest-degree polynomial. If you chose this and are not sure what you did wrong, please contact the coordinator for help.

General Comments: Remember that the conjugate of a + bi is a - bi. Since these zeros always come in pairs, we need to multiply out (x - (3 + 4i))(x - (3 - 4i))(x - (-4)).

 $\operatorname{Summer} \operatorname{C} 2020$