

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

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51. Using the scenario below, model the situation using an exponential function and a base of  $\frac{1}{2}$ . Then, solve for the half-life of the element, rounding to the nearest day. The half-life of an element is the amount of time it takes for the element to decay to half of its initial starting amount. There is initially 680 grams of element  $X$  and after 20 years there is 97 grams remaining. The solution is About 2555 days

A. About 2555 days

\* This is the correct option.

B. About 9125 days

This uses the correct model but solves for the exponential constant incorrectly.

C. About 730 days

This models half-life as a linear function.

D. About 3650 days

This uses the correct model but a base of  $e$  rather than  $\frac{1}{2}$ .

E. None of the above

Please contact the coordinator if you believe all the options above are incorrect.

**General comments:** The model should be  $A(t) = A_0(\frac{1}{2})^{kt}$ , where  $A(t)$  is the amount after  $t$  years,  $A_0$  is the initial amount, and  $k$  is decay constant. To find the half-life, you need to solve for  $k$  by using the amount after  $x$  years, then solve for the time  $t$  when  $A = \frac{A_0}{2}$ . Your answer would be in years, so convert to days.

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52. The temperature of an object,  $T$ , in a different surrounding temperature  $T_s$  will behave according to the formula  $T(t) = Ae^{kt} + T_s$ , where  $t$  is minutes,  $A$  is a constant, and  $k$  is a constant. Use this formula and the situation below to construct a model that describes the uranium's temperature,  $T$ , based on the amount of time  $t$  (in minutes) that have passed. Choose the correct constant  $k$  from the options below. Uranium is taken out of the reactor with a temperature of  $120^\circ\text{C}$  and is placed into a  $16^\circ\text{C}$  bath to cool. After 35 minutes, the uranium has cooled to  $55^\circ\text{C}$ . The solution is None of the above

A.  $k = -0.03211$

This uses  $A$  as the initial temperature and solves for  $k$  correctly.

B.  $k = -0.03211$

This uses  $A$  as the initial temperature and solves for  $k$  incorrectly.

C.  $k = -0.01809$

This uses  $A$  as the initial temperature and solves for  $k$  incorrectly.

D.  $k = -0.01854$

This uses  $A$  correctly and solves for  $k$  incorrectly.

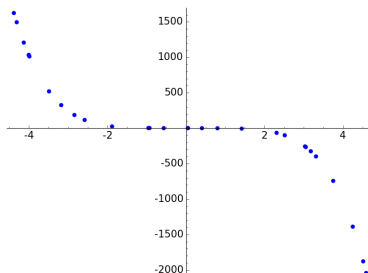
E. None of the above

\* This is the correct answer as  $k = -0.02802$ .

**General comments:** The initial temperature is when  $t = 0$ . Unlike power models, that means  $A$  is not the initial temperature!

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53. Determine the appropriate model for the graph of points below.



The solution is Non-linear Power model

A. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

B. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

C. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

D. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

**General comments:** This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

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54. Using the scenario below, model the population of bacteria  $\alpha$  in terms of the number of minutes,  $t$  that pass. Then, choose the correct approximate (*rounded to the nearest minute*) replication rate of bacteria- $\alpha$ . A newly discovered bacteria,  $\alpha$ , is being examined in a lab. The lab started with a petri dish of 2 bacteria- $\alpha$ . After 1 hours, the petri dish has 24 bacteria- $\alpha$ . Based on similar bacteria, the lab believes bacteria- $\alpha$  triples after some undetermined number of minutes. The solution is None of the above

A. About 155 minutes

This uses the wrong base, does not solve for the constant correctly, AND converted incorrectly.

B. About 25 minutes

This uses the wrong base and does not solve for the constant correctly.

C. About 99 minutes

This uses the wrong base and solves for the constant correctly but converted incorrectly.

D. About 16 minutes

This uses the wrong base.

E. None of the above

\* This is the correct option as all other options used the wrong base in their model.

**General comments:** Your model should be  $P(t) = P_0(b)^{kt}$ , where  $P(t)$  is the population at some time  $t$ ,  $P_0$  is the initial population, and  $k$  is the replication rate. Be sure you convert the hours into minutes!

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55. A town has an initial population of 80000. The town's population for the next 10 years is provided below. Which type of function would be most appropriate to model the town's population? Check for table in main PDF. The solution is Linear

A. Linear

This suggests a constant growth. You would be able to add or subtract the same amount year-to-year if this is the correct answer.

B. Non-Linear Power

This suggests a growth faster than constant but slower than exponential.

C. Logarithmic

This suggests the slowest of growths that we know.

D. Exponential

This suggests the fastest of growths that we know.

E. None of the above

Please contact the coordinator to discuss why you believe none of the options model the population.

**General Comments:** We are trying to compare the growth rate of the population. Growth rates can be characterized from slowest to fastest as: logarithmic, indirect, linear, direct, exponential. The best way to approach this is to first compare it to linear (is it linear, faster than linear, or slower than linear)? If faster, is it as fast as exponential? If slower, is it as slow as logarithmic?

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