This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8 + 7x > 8x$$
 or  $-6 + 7x < 9x$ 

The solution is  $(-\infty, -8.0)$  or  $(-3.0, \infty)$ , which is option D.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-9, -7]$  and  $b \in [-3, 0]$ 

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [3, 4]$  and  $b \in [7, 10]$ 

Corresponds to inverting the inequality and negating the solution.

C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [2, 8]$  and  $b \in [8, 11]$ 

Corresponds to including the endpoints AND negating.

- D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-10, -7]$  and  $b \in [-6, -2]$ 
  - \* Correct option.
- E.  $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

2. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 10 units from the number 8.

The solution is None of the above, which is option E.

A.  $(-\infty, 2] \cup [18, \infty)$ 

This describes the values no less than 8 from 10

B. [2, 18]

This describes the values no more than 8 from 10

C. (2,18)

This describes the values less than 8 from 10

D.  $(-\infty, 2) \cup (18, \infty)$ 

This describes the values more than 8 from 10

E. None of the above

Options A-D described the values [more/less than] 8 units from 10, which is the reverse of what the question asked.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3x + 4 < 6x + 9$$

The solution is  $[-0.556, \infty)$ , which is option A.

- A.  $[a, \infty)$ , where  $a \in [-1.69, -0.39]$ 
  - \*  $[-0.556, \infty)$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [-2.2, -0.2]$

 $(-\infty, -0.556]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

C.  $(-\infty, a]$ , where  $a \in [0.1, 1.9]$ 

 $(-\infty, 0.556]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- D.  $[a, \infty)$ , where  $a \in [0.35, 0.95]$ 
  - $[0.556, \infty)$ , which corresponds to negating the endpoint of the solution.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

4. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 6 units from the number -6.

The solution is [-12, 0], which is option B.

A. 
$$(-\infty, -12) \cup (0, \infty)$$

This describes the values more than 6 from -6

B. [-12, 0]

This describes the values no more than 6 from -6

C.  $(-\infty, -12] \cup [0, \infty)$ 

This describes the values no less than 6 from -6

D. (-12,0)

This describes the values less than 6 from -6

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{3}{6} - \frac{6}{4}x \le \frac{-4}{2}x - \frac{3}{3}$$

The solution is  $(-\infty, -3.0]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [-4, 0]$ 
  - \*  $(-\infty, -3.0]$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [2, 5]$

 $(-\infty, 3.0]$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [3, 5]$ 

 $[3.0, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- D.  $[a, \infty)$ , where  $a \in [-3, 0]$ 
  - $[-3.0, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 + 8x > 9x$$
 or  $3 + 9x < 12x$ 

The solution is  $(-\infty, -5.0)$  or  $(1.0, \infty)$ , which is option A.

- A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-10, -4]$  and  $b \in [1, 3]$ 
  - \* Correct option.
- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-1, 4]$  and  $b \in [5, 6]$

Corresponds to inverting the inequality and negating the solution.

C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-6, -4]$  and  $b \in [-3, 3]$ 

Corresponds to including the endpoints (when they should be excluded).

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-2, 0]$  and  $b \in [5, 6]$ 

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-9}{7} - \frac{5}{8}x < \frac{4}{6}x + \frac{5}{3}$$

The solution is  $(-2.286, \infty)$ , which is option B.

A.  $(a, \infty)$ , where  $a \in [-0.71, 3.29]$ 

 $(2.286, \infty)$ , which corresponds to negating the endpoint of the solution.

B.  $(a, \infty)$ , where  $a \in [-5.29, -1.29]$ 

\*  $(-2.286, \infty)$ , which is the correct option.

C.  $(-\infty, a)$ , where  $a \in [0.29, 5.29]$ 

 $(-\infty, 2.286)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(-\infty, a)$ , where  $a \in [-3.29, -0.29]$ 

 $(-\infty, -2.286)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3x - 3 \le 9x + 8$$

The solution is  $[-0.917, \infty)$ , which is option C.

A.  $(-\infty, a]$ , where  $a \in [0.1, 2.3]$ 

 $(-\infty, 0.917]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

B.  $[a, \infty)$ , where  $a \in [-0.08, 8.92]$ 

 $[0.917, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [-5.92, 0.08]$ 

\*  $[-0.917, \infty)$ , which is the correct option.

D.  $(-\infty, a]$ , where  $a \in [-2, 0.8]$ 

 $(-\infty, -0.917]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 6x \le \frac{56x + 6}{9} < -4 + 6x$$

The solution is [-34.50, -21.00), which is option C.

A.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-36.5, -32.5]$  and  $b \in [-25, -20]$ 

 $(-\infty, -34.50] \cup (-21.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

B. (a, b], where  $a \in [-34.5, -30.5]$  and  $b \in [-25, -20]$ 

(-34.50, -21.00], which corresponds to flipping the inequality.

C. [a, b), where  $a \in [-38.5, -33.5]$  and  $b \in [-21, -18]$ 

[-34.50, -21.00), which is the correct option.

D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-37.5, -33.5]$  and  $b \in [-22, -17]$ 

 $(-\infty, -34.50) \cup [-21.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8 - 7x \le \frac{-19x + 8}{3} < 8 - 9x$$

The solution is [-16.00, 2.00), which is option B.

A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-16, -12]$  and  $b \in [-1, 7]$ 

 $(-\infty, -16.00) \cup [2.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

B. [a, b), where  $a \in [-16, -15]$  and  $b \in [1, 3]$ 

[-16.00, 2.00), which is the correct option.

C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-21, -14]$  and  $b \in [0, 3]$ 

 $(-\infty, -16.00] \cup (2.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

D. (a, b], where  $a \in [-16, -15]$  and  $b \in [1.3, 4.5]$ 

(-16.00, 2.00], which corresponds to flipping the inequality.

E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.