

1. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder  $r$ .

$$\frac{12x^3 - 16x^2 - 108x - 75}{x - 4}$$

- A.  $a \in [47, 51]$ ,  $b \in [-209, -207]$ ,  $c \in [717, 728]$ , and  $r \in [-2976, -2965]$ .  
B.  $a \in [8, 17]$ ,  $b \in [17, 21]$ ,  $c \in [-52, -46]$ , and  $r \in [-220, -216]$ .  
C.  $a \in [8, 17]$ ,  $b \in [31, 40]$ ,  $c \in [16, 23]$ , and  $r \in [2, 10]$ .  
D.  $a \in [8, 17]$ ,  $b \in [-67, -62]$ ,  $c \in [145, 149]$ , and  $r \in [-670, -662]$ .  
E.  $a \in [47, 51]$ ,  $b \in [173, 177]$ ,  $c \in [587, 598]$ , and  $r \in [2305, 2313]$ .
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2. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . *To make the problem easier, all zeros are between -5 and 5.*

$$f(x) = 6x^3 + 13x^2 - 40x - 75$$

- A.  $z_1 \in [-1.05, -0.83]$ ,  $z_2 \in [2.61, 3.51]$ , and  $z_3 \in [4.84, 5.5]$   
B.  $z_1 \in [-2.55, -2.4]$ ,  $z_2 \in [1, 2.02]$ , and  $z_3 \in [2.54, 3.31]$   
C.  $z_1 \in [-0.59, -0.3]$ ,  $z_2 \in [0.53, 0.84]$ , and  $z_3 \in [2.54, 3.31]$   
D.  $z_1 \in [-3.02, -2.94]$ ,  $z_2 \in [-0.92, -0.12]$ , and  $z_3 \in [0.06, 0.76]$   
E.  $z_1 \in [-3.02, -2.94]$ ,  $z_2 \in [-2.29, -1.21]$ , and  $z_3 \in [2.31, 2.87]$
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3. Factor the polynomial below completely, knowing that  $x - 2$  is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . *To make the problem easier, all zeros are between -5 and 5.*

$$f(x) = 9x^4 - 63x^3 + 74x^2 + 112x - 160$$

- A.  $z_1 \in [-6.6, -2.9]$ ,  $z_2 \in [-3.01, -1.54]$ ,  $z_3 \in [-0.7, -0.27]$ , and  $z_4 \in [3.8, 4.1]$
- B.  $z_1 \in [-6.6, -2.9]$ ,  $z_2 \in [-3.01, -1.54]$ ,  $z_3 \in [-1.52, -0.93]$ , and  $z_4 \in [0.9, 1.7]$
- C.  $z_1 \in [-2, -1.1]$ ,  $z_2 \in [1.09, 1.58]$ ,  $z_3 \in [1.9, 2.44]$ , and  $z_4 \in [4.1, 5.1]$
- D.  $z_1 \in [-6.6, -2.9]$ ,  $z_2 \in [-3.01, -1.54]$ ,  $z_3 \in [-1.03, -0.53]$ , and  $z_4 \in [0.3, 1.3]$
- E.  $z_1 \in [-0.8, 0.5]$ ,  $z_2 \in [0.42, 0.86]$ ,  $z_3 \in [1.9, 2.44]$ , and  $z_4 \in [4.1, 5.1]$
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4. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder  $r$ .

$$\frac{20x^3 - 60x + 42}{x + 2}$$

- A.  $a \in [18, 24]$ ,  $b \in [31, 44]$ ,  $c \in [16, 24]$ , and  $r \in [80, 87]$ .
- B.  $a \in [18, 24]$ ,  $b \in [-65, -55]$ ,  $c \in [118, 121]$ , and  $r \in [-324, -317]$ .
- C.  $a \in [-41, -37]$ ,  $b \in [79, 84]$ ,  $c \in [-222, -211]$ , and  $r \in [477, 488]$ .
- D.  $a \in [18, 24]$ ,  $b \in [-47, -37]$ ,  $c \in [16, 24]$ , and  $r \in [-2, 3]$ .
- E.  $a \in [-41, -37]$ ,  $b \in [-83, -76]$ ,  $c \in [-222, -211]$ , and  $r \in [-399, -397]$ .
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5. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 6x^2 + 3x + 3$$

- A.  $\pm 1, \pm 3$
- B. All combinations of:  $\frac{\pm 1, \pm 3}{\pm 1, \pm 2, \pm 3, \pm 6}$
- C.  $\pm 1, \pm 2, \pm 3, \pm 6$
- D. All combinations of:  $\frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1, \pm 3}$

E. There is no formula or theorem that tells us all possible Integer roots.

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