1. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{9x^3 - 21x^2 + 10}{x - 2}$$

- A.  $a \in [3, 12], b \in [-40, -38], c \in [73, 83], \text{ and } r \in [-151, -144].$
- B.  $a \in [3, 12], b \in [-16, -10], c \in [-13, -10], \text{ and } r \in [-5, 1].$
- C.  $a \in [15, 20], b \in [14, 20], c \in [29, 38], \text{ and } r \in [62, 75].$
- D.  $a \in [15, 20], b \in [-59, -54], c \in [113, 120], \text{ and } r \in [-220, -210].$
- E.  $a \in [3, 12], b \in [-8, -2], c \in [-11, -1], \text{ and } r \in [-5, 1].$
- 2. Factor the polynomial below completely, knowing that x-2 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^4 + 31x^3 + 5x^2 - 122x - 120$$

- A.  $z_1 \in [-3, 2], z_2 \in [0.56, 0.81], z_3 \in [0.47, 1], \text{ and } z_4 \in [3.2, 4.6]$
- B.  $z_1 \in [-8, -3], z_2 \in [-0.8, -0.41], z_3 \in [-0.66, -0.15], \text{ and } z_4 \in [1.8, 3.3]$
- C.  $z_1 \in [-3, 2], z_2 \in [0.66, 0.85], z_3 \in [2.76, 4.17], \text{ and } z_4 \in [3.2, 4.6]$
- D.  $z_1 \in [-3, 2], z_2 \in [1.5, 1.54], z_3 \in [0.96, 2.43], \text{ and } z_4 \in [3.2, 4.6]$
- E.  $z_1 \in [-8, -3], z_2 \in [-1.78, -1.63], z_3 \in [-1.97, -1.17], \text{ and } z_4 \in [1.8, 3.3]$
- 3. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{6x^3 - 38x^2 + 76x - 50}{x - 3}$$

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A. 
$$a \in [15, 20], b \in [9, 20], c \in [123, 131], and  $r \in [319, 324].$$$

B. 
$$a \in [4, 8], b \in [-29, -21], c \in [20, 26], and r \in [-3, 3].$$

C. 
$$a \in [15, 20], b \in [-99, -91], c \in [347, 355], and  $r \in [-1112, -1102].$$$

D. 
$$a \in [4, 8], b \in [-24, -19], c \in [14, 22], and  $r \in [-3, 3].$$$

E. 
$$a \in [4, 8], b \in [-59, -54], c \in [243, 247], and  $r \in [-783, -777].$$$

4. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 9x^3 + 9x^2 - 28x - 20$$

A. 
$$z_1 \in [-1.92, -1.5], z_2 \in [0.54, 0.69], \text{ and } z_3 \in [1.89, 2.3]$$

B. 
$$z_1 \in [-5.17, -4.86], z_2 \in [0.01, 0.57], \text{ and } z_3 \in [1.89, 2.3]$$

C. 
$$z_1 \in [-2.19, -1.97], z_2 \in [-1.64, -1.25], \text{ and } z_3 \in [0.37, 0.66]$$

D. 
$$z_1 \in [-0.88, -0.21], z_2 \in [1.24, 1.7], \text{ and } z_3 \in [1.89, 2.3]$$

E. 
$$z_1 \in [-2.19, -1.97], z_2 \in [-1.1, -0.25], \text{ and } z_3 \in [1.49, 1.7]$$

5. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 2x^2 + 5x + 4$$

A. 
$$\pm 1, \pm 2$$

B. 
$$\pm 1, \pm 2, \pm 4$$

C. All combinations of: 
$$\frac{\pm 1, \pm 2}{\pm 1, \pm 2, \pm 4}$$

D. All combinations of: 
$$\frac{\pm 1, \pm 2, \pm 4}{\pm 1, \pm 2}$$

E. There is no formula or theorem that tells us all possible Integer roots.