

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the rational equation below.

$$\frac{6x}{-3x+4} + \frac{-7x^2}{-6x^2-13x+28} = \frac{2}{2x+7}$$

The solution is There are two solutions: $x = 0.164$ and $x = -9.764$.

Plausible alternative answers include: * $x = 0.164$ and $x = -9.764$, which is the correct option.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

2. Determine the domain of the function below.

$$f(x) = \frac{4}{25x^2 - 9}$$

The solution is All Real numbers except $x = -0.600$ and $x = 0.600$.

Plausible alternative answers include: All Real numbers except $x = -0.600$ and $x = 0.600$, which is the correct option. All Real numbers except $x = -15.000$, which corresponds to removing a distractor value from the denominator. All Real numbers except $x = -0.600$, which corresponds to removing only 1 value from the denominator. This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = -15.000$ and $x = 15.000$, which corresponds to not factoring the denominator correctly.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

3. Solve the rational equation below.

$$\frac{3}{-9x-2} + -3 = \frac{-4}{81x+18}$$

The solution is $x = -0.317$.

Plausible alternative answers include: * $x = -0.317$, which is the correct option. This corresponds to thinking $x = -0.317$ leads to dividing by zero in the original equation, which it does not. $x = -0.481$ and $x = -0.317$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = 0.128$, which corresponds to not distributing the factor $-9x - 2$ correctly when trying to eliminate the fraction. $x = -0.317$ and $x = 0.128$, which corresponds to getting the correct solution and believing there should be a second solution to the equation.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

4. Solve the rational equation below.

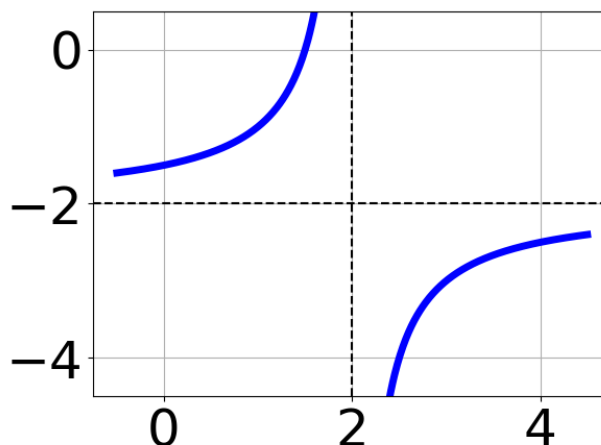
$$\frac{36}{24x - 108} + 1 = \frac{36}{24x - 108}$$

The solution is all solutions are invalid or lead to complex values in the equation..

Plausible alternative answers include: $x = 4.500$ leads to dividing by 0 in the original equation and thus is not a valid solution, which is the correct option. $x = 4.500$ and $x = 4.500$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = -4.500$ and $x = 4.500$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = 4.500$, which corresponds to not checking if this value leads to dividing by 0 in the original equation and thus is not a valid solution. $x = -4.500$, which corresponds to not distributing the factor $24x - 108$ correctly when trying to eliminate the fraction.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

5. Write an equation that can represent the function graphed below.



The solution is $f(x) = \frac{-1}{x-2} - 2$.

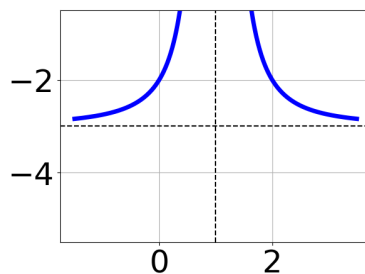
Plausible alternative answers include: Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$, using the general form $f(x) = \frac{a}{x+h} + k$, and the opposite leading coefficient. Corresponds to using the general form $f(x) = \frac{a}{x+h} + k$ and the opposite leading coefficient. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$. This is the correct option. This corresponds to believing the vertex of the graph was not correct.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

6. Sketch a graph that represents the equation below.

$$f(x) = \frac{1}{(x-1)^2} - 3$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

7. Determine the domain of the function below.

$$f(x) = \frac{5}{30x^2 - 30}$$

The solution is All Real numbers except $x = -1.000$ and $x = 1.000$.

Plausible alternative answers include: All Real numbers except $x = -36.000$ and $x = 25.000$, which corresponds to not factoring the denominator correctly. All Real numbers except $x = -36.000$, which corresponds to removing a distractor value from the denominator. All Real numbers except $x = -1.000$ and $x = 1.000$, which is the correct option. This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = -1.000$, which corresponds to removing only 1 value from the denominator.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

8. Solve the rational equation below.

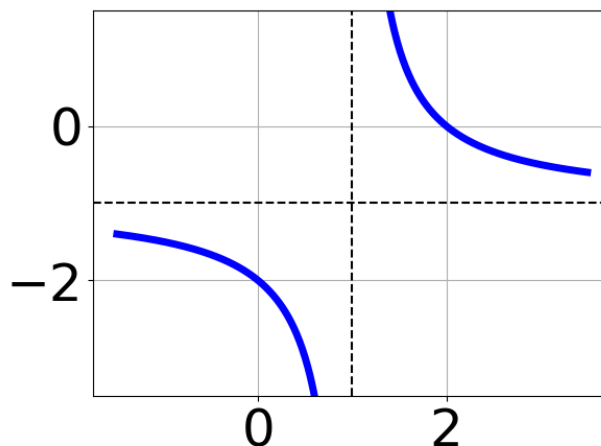
$$\frac{4x}{2x+5} + \frac{-7x^2}{4x^2+16x+15} = \frac{3}{2x+3}$$

The solution is There are two solutions: $x = 1.899$ and $x = -7.899$.

Plausible alternative answers include: * $x = 1.899$ and $x = -7.899$, which is the correct option.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

9. Write an equation that can represent the function graphed below.



The solution is $f(x) = \frac{1}{x-1} - 1$.

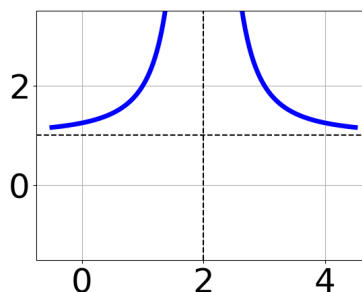
Plausible alternative answers include: Corresponds to using the general form $f(x) = \frac{a}{x+h} + k$ and the opposite leading coefficient. This is the correct option. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$, using the general form $f(x) = \frac{a}{x+h} + k$, and the opposite leading coefficient. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$. This corresponds to believing the vertex of the graph was not correct.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

10. Sketch a graph that represents the equation below.

$$f(x) = \frac{1}{(x-2)^2} + 1$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

11. Solve the rational equation below.

$$\frac{-4x}{-2x+7} + \frac{-3x^2}{-14x^2+35x+49} = \frac{3}{7x+7}$$

The solution is All solutions are invalid or lead to complex values in the equation..

Plausible alternative answers include: $x = -1.000$, which corresponds to solving $7x + 7 = 0$ and treating it as a solution to the equation. $x = 0.364$ and $x = -1.244$, which corresponds to making the discriminant from the Quadratic Formula positive to avoid complex solutions. $x = 3.500$ and $x = -1.000$, which corresponds to solving $-2x + 7 = 0$ and $7x + 7 = 0$ and treating them as solutions to the equation. * The equation leads to solving $-25x^2 - 22x - 21 = 0$, which leads to complex solutions. This is the correct option. $x = 3.500$, which corresponds to solving $-2x + 7 = 0$ and treating it as a solution to the equation.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

12. Determine the domain of the function below.

$$f(x) = \frac{4}{25x^2 - 5x - 12}$$

The solution is All Real numbers except $x = -0.600$ and $x = 0.800$..

Plausible alternative answers include: This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = -15.000$, which corresponds to removing a distractor value from the denominator. All Real numbers except $x = -0.600$ and $x = 0.800$, which is the correct option. All Real numbers except $x = -15.000$ and $x = 20.000$, which corresponds to not factoring the denominator correctly. All Real numbers except $x = -0.600$, which corresponds to removing only 1 value from the denominator.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

13. Solve the rational equation below.

$$\frac{3}{8x+7} + 5 = \frac{3}{-32x-28}$$

The solution is $x = -0.969$.

Plausible alternative answers include: This corresponds to thinking $x = -0.969$ leads to dividing by zero in the original equation, which it does not. $x = 0.781$, which corresponds to not distributing the factor $8x + 7$ correctly when trying to eliminate the fraction. $x = -0.969$ and $x = 0.781$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. * $x = -0.969$, which is the correct option. $x = -0.969$ and $x = -0.875$, which corresponds to getting the correct solution and believing there should be a second solution to the equation.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

14. Solve the rational equation below.

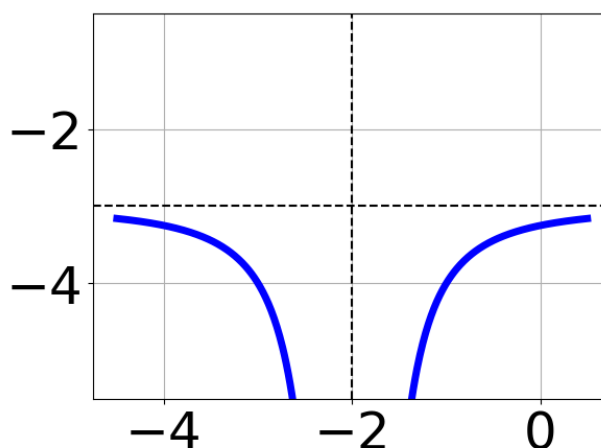
$$\frac{-98}{-42x+42} + 1 = \frac{-98}{-42x+42}$$

The solution is all solutions are invalid or lead to complex values in the equation..

Plausible alternative answers include: $x = 1.000$ and $x = 1.000$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = 1.000$, which corresponds to not checking if this value leads to dividing by 0 in the original equation and thus is not a valid solution. $x = -1.000$, which corresponds to not distributing the factor $-42x + 42$ correctly when trying to eliminate the fraction. $x = -1.000$ and $x = 1.000$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = 1.000$ leads to dividing by 0 in the original equation and thus is not a valid solution, which is the correct option.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

15. Write an equation that can represent the function graphed below.



The solution is $f(x) = \frac{-1}{(x+2)^2} - 3$.

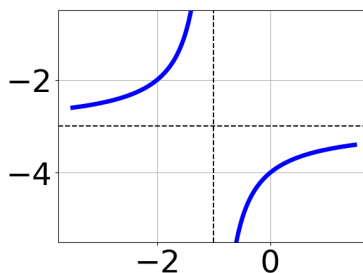
Plausible alternative answers include: Corresponds to thinking the graph was a shifted version of $\frac{1}{x}$, using the general form $f(x) = \frac{a}{(x+h)^2} + k$, and the opposite leading coefficient. Corresponds to using the general form $f(x) = \frac{a}{(x+h)^2} + k$ and the opposite leading coefficient. Corresponds to thinking the graph was a shifted version of $\frac{1}{x}$. This is the correct option. This corresponds to believing the vertex of the graph was not correct.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

16. Sketch a graph that represents the equation below.

$$f(x) = \frac{-1}{x+1} - 3$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

17. Determine the domain of the function below.

$$f(x) = \frac{4}{9x^2 - 27x + 20}$$

The solution is All Real numbers except $x = 1.333$ and $x = 1.667$.

Plausible alternative answers include: All Real numbers except $x = 12.000$ and $x = 15.000$, which corresponds to not factoring the denominator correctly. This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = 1.333$, which corresponds to removing only 1 value from the denominator. All Real numbers except $x = 1.333$ and $x = 1.667$, which is the correct option. All Real numbers except $x = 12.000$, which corresponds to removing a distractor value from the denominator.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

18. Solve the rational equation below.

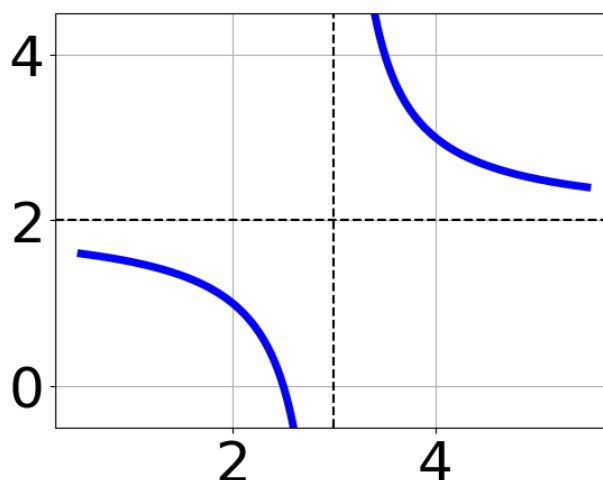
$$\frac{-2x}{-6x+5} + \frac{-5x^2}{30x^2-43x+15} = \frac{-4}{-5x+3}$$

The solution is There are two solutions: $x = 0.764$ and $x = 5.236$.

Plausible alternative answers include: $x = 0.764$ and $x = 5.236$, which is the correct option.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

19. Write an equation that can represent the function graphed below.



The solution is $f(x) = \frac{1}{x-3} + 2$.

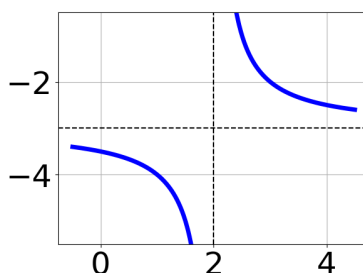
Plausible alternative answers include: This is the correct option. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$, using the general form $f(x) = \frac{a}{x+h} + k$, and the opposite leading coefficient. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$. Corresponds to using the general form $f(x) = \frac{a}{x+h} + k$ and the opposite leading coefficient. This corresponds to believing the vertex of the graph was not correct.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

20. Sketch a graph that represents the equation below.

$$f(x) = \frac{1}{x-2} - 3$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

21. Solve the rational equation below.

$$\frac{7x}{3x+7} + \frac{-6x^2}{15x^2+44x+21} = \frac{-6}{5x+3}$$

The solution is All solutions are invalid or lead to complex values in the equation..

Plausible alternative answers include:* The equation leads to solving $41x^2 + 39x + 42 = 0$, which leads to complex solutions. This is the correct option. $x = -2.333$, which corresponds to solving $3x + 7 = 0$ and treating it as a solution to the equation. $x = -2.333$ and $x = -0.600$, which corresponds to solving $3x + 7 = 0$ and $5x + 3 = 0$ and treating them as solutions to the equation. $x = -0.600$, which corresponds to solving $5x + 3 = 0$ and treating it as a solution to the equation. $x = -1.369$ and $x = 0.418$, which corresponds to making the discriminant from the Quadratic Formula positive to avoid complex solutions.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

22. Determine the domain of the function below.

$$f(x) = \frac{6}{15x^2 + 43x + 30}$$

The solution is All Real numbers except $x = -1.667$ and $x = -1.200$..

Plausible alternative answers include:This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = -1.667$, which corresponds to removing only 1 value from the denominator. All Real numbers except $x = -30.000$ and $x = -15.000$, which corresponds to not factoring the denominator correctly. All Real numbers except $x = -1.667$ and $x = -1.200$, which is the correct option. All Real numbers except $x = -30.000$, which corresponds to removing a distractor value from the denominator.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

23. Solve the rational equation below.

$$\frac{63}{-56x+28} + 1 = \frac{63}{-56x+28}$$

The solution is all solutions are invalid or lead to complex values in the equation..

Plausible alternative answers include: $x = 0.500$ and $x = 0.500$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $x = 0.500$, which corresponds to not checking if this value leads to dividing by 0 in the original equation and thus is not a valid solution. $x = -0.500$ and $x = 0.500$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. $*x = 0.500$ leads to dividing by 0 in the original equation and thus is not a valid solution, which is the correct option. $x = -0.500$, which corresponds to not distributing the factor $-56x + 28$ correctly when trying to eliminate the fraction.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

24. Solve the rational equation below.

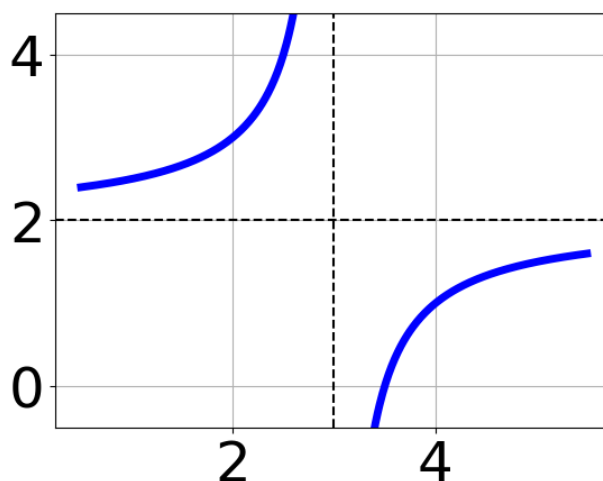
$$\frac{2}{-6x+9} + 3 = \frac{4}{18x-27}$$

The solution is $x = 1.685$.

Plausible alternative answers include: This corresponds to thinking $x = 1.685$ leads to dividing by zero in the original equation, which it does not. $x = -1.315$, which corresponds to not distributing the factor $-6x + 9$ correctly when trying to eliminate the fraction. $x = -1.315$ and $x = 1.685$, which corresponds to getting the correct solution and believing there should be a second solution to the equation. * $x = 1.685$, which is the correct option. $x = 1.389$ and $x = 1.685$, which corresponds to getting the correct solution and believing there should be a second solution to the equation.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

25. Write an equation that can represent the function graphed below.



The solution is $f(x) = \frac{-1}{x-3} + 2$.

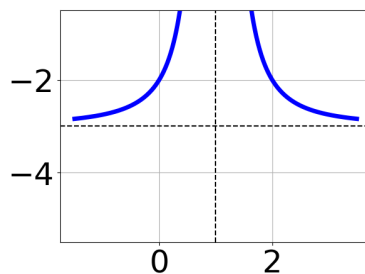
Plausible alternative answers include: Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$. This is the correct option. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$, using the general form $f(x) = \frac{a}{x+h} + k$, and the opposite leading coefficient. Corresponds to using the general form $f(x) = \frac{a}{x+h} + k$ and the opposite leading coefficient. This corresponds to believing the vertex of the graph was not correct.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

26. Sketch a graph that represents the equation below.

$$f(x) = \frac{1}{(x-1)^2} - 3$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

27. Determine the domain of the function below.

$$f(x) = \frac{3}{20x^2 + 3x - 9}$$

The solution is All Real numbers except $x = -0.750$ and $x = 0.600$.

Plausible alternative answers include: All Real numbers except $x = -0.750$, which corresponds to removing only 1 value from the denominator. All Real numbers except $x = -12.000$, which corresponds to removing a distractor value from the denominator. This corresponds to thinking the denominator has complex roots or that rational functions have a domain of all Real numbers. All Real numbers except $x = -0.750$ and $x = 0.600$, which is the correct option. All Real numbers except $x = -12.000$ and $x = 15.000$, which corresponds to not factoring the denominator correctly.

General Comment: Recall that dividing by zero is not a real number. Therefore the domain is all real numbers **except** those that make the denominator 0.

28. Solve the rational equation below.

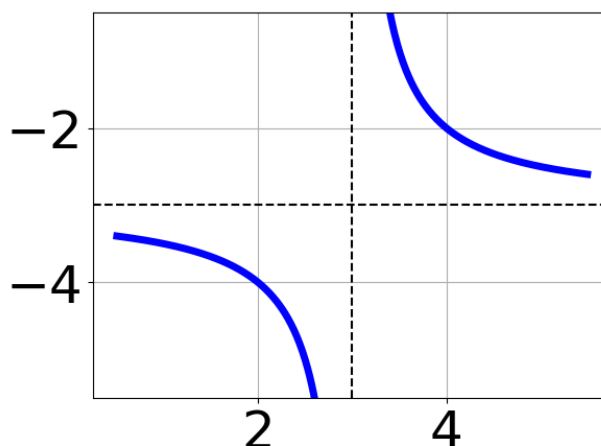
$$\frac{-5x}{-3x-5} + \frac{-4x^2}{-9x^2-24x-15} = \frac{5}{3x+3}$$

The solution is There are two solutions: $x = -1.147$ and $x = 1.147$.

Plausible alternative answers include: * $x = -1.147$ and $x = 1.147$, which is the correct option.

General Comment: Distractors are different based on the number of solutions. Remember that after solving, we need to make sure our solution does not make the original equation divide by zero!

29. Write an equation that can represent the function graphed below.



The solution is None of the above as it should be $f(x) = \frac{1}{x-3} - 3$.

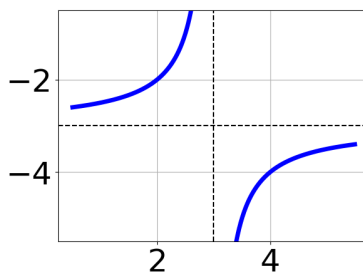
Plausible alternative answers include: Corresponds to using the general form $f(x) = \frac{a}{x-h} + k$ and the opposite leading coefficient. The x -value of the equation does not match the graph. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$, using the general form $f(x) = \frac{a}{x-h} + k$, and the opposite leading coefficient. Corresponds to thinking the graph was a shifted version of $\frac{1}{x^2}$. None of the equation options were the correct equation.

General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.

30. Sketch a graph that represents the equation below.

$$f(x) = \frac{-1}{x-3} - 3$$

The solution is the graph below.



General Comment: Remember that the general form of a basic rational equation is $f(x) = \frac{a}{(x-h)^n} + k$, where a is the leading coefficient (and in this case, we assume is either 1 or -1), n is the degree (in this case, either 1 or 2), and (h, k) is the intersection of the asymptotes.