This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$3x - 4 > 10x + 8$$

The solution is  $(-\infty, -1.714)$ , which is option B.

A.  $(a, \infty)$ , where  $a \in [1.71, 2.71]$ 

 $(1.714, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- B.  $(-\infty, a)$ , where  $a \in [-6.71, 1.29]$ 
  - \*  $(-\infty, -1.714)$ , which is the correct option.
- C.  $(a, \infty)$ , where  $a \in [-5.71, 0.29]$

 $(-1.714, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $(-\infty, a)$ , where  $a \in [0.71, 5.71]$ 
  - $(-\infty, 1.714)$ , which corresponds to negating the endpoint of the solution.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

2. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

Less than 10 units from the number 7.

The solution is (-3, 17), which is option C.

A.  $(-\infty, -3] \cup [17, \infty)$ 

This describes the values no less than 10 from 7

B. [-3, 17]

This describes the values no more than 10 from 7

C. (-3, 17)

This describes the values less than 10 from 7

D.  $(-\infty, -3) \cup (17, \infty)$ 

This describes the values more than 10 from 7

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6-3x \le \frac{-22x-3}{9} < 4-3x$$

The solution is None of the above., which is option E.

A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [10.2, 11.2]$  and  $b \in [-11.8, -3.8]$ 

 $(-\infty, 10.20) \cup [-7.80, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

B. [a, b), where  $a \in [7.2, 13.2]$  and  $b \in [-8.8, -3.8]$ 

[10.20, -7.80), which is the correct interval but negatives of the actual endpoints.

C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [5.2, 12.2]$  and  $b \in [-9.8, -6.8]$ 

 $(-\infty, 10.20] \cup (-7.80, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

D. (a, b], where  $a \in [6.2, 14.2]$  and  $b \in [-7.8, -4.8]$ 

(10.20, -7.80], which corresponds to flipping the inequality and getting negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be [-10.20, 7.80).

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-5}{3} - \frac{10}{5}x \le \frac{-3}{4}x - \frac{3}{9}$$

The solution is  $[-1.067, \infty)$ , which is option B.

A.  $(-\infty, a]$ , where  $a \in [-2.9, -0.9]$ 

 $(-\infty, -1.067]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- B.  $[a, \infty)$ , where  $a \in [-3.07, 0.93]$ 
  - \*  $[-1.067, \infty)$ , which is the correct option.
- C.  $[a, \infty)$ , where  $a \in [0.07, 2.07]$

 $[1.067, \infty)$ , which corresponds to negating the endpoint of the solution.

D.  $(-\infty, a]$ , where  $a \in [0.4, 3.1]$ 

 $(-\infty, 1.067]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3 + 8x > 9x$$
 or  $-6 + 7x < 10x$ 

The solution is  $(-\infty, -3.0)$  or  $(-2.0, \infty)$ , which is option B.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-3, 0]$  and  $b \in [-2, 2]$ 

Corresponds to including the endpoints (when they should be excluded).

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-3, 1]$  and  $b \in [-4, -1]$ 
  - \* Correct option.
- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [2, 9]$  and  $b \in [-1, 4]$

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [1, 4]$  and  $b \in [2, 4]$ 

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 7x > 8x$$
 or  $3 + 3x < 6x$ 

The solution is  $(-\infty, -7.0)$  or  $(1.0, \infty)$ , which is option D.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-4, 1]$  and  $b \in [7, 10]$ 

Corresponds to including the endpoints AND negating.

B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2, 1]$  and  $b \in [7, 12]$ 

Corresponds to inverting the inequality and negating the solution.

C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-9, -6]$  and  $b \in [-2, 4]$ 

Corresponds to including the endpoints (when they should be excluded).

D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-7, -6]$  and  $b \in [-2, 3]$ 

\* Correct option.

E. 
$$(-\infty, \infty)$$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 + 6x \le \frac{40x + 9}{6} < -7 + 4x$$

The solution is [-9.75, -3.19), which is option A.

A. [a, b), where  $a \in [-9.75, -7.75]$  and  $b \in [-7.19, -2.19]$ 

[-9.75, -3.19), which is the correct option.

B.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-12.75, -6.75]$  and  $b \in [-6.19, 0.81]$ 

 $(-\infty, -9.75) \cup [-3.19, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

C. (a, b], where  $a \in [-10.75, -7.75]$  and  $b \in [-7.19, -1.19]$ 

(-9.75, -3.19], which corresponds to flipping the inequality.

D.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-9.75, -8.75]$  and  $b \in [-7.19, 1.81]$ 

 $(-\infty, -9.75] \cup (-3.19, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

8. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 5 units from the number 7.

The solution is [2, 12], which is option A.

A. [2, 12]

This describes the values no more than 5 from 7

B.  $(-\infty, 2] \cup [12, \infty)$ 

This describes the values no less than 5 from 7

C.  $(-\infty, 2) \cup (12, \infty)$ 

This describes the values more than 5 from 7

D. (2, 12)

This describes the values less than 5 from 7

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{6}{5} - \frac{6}{8}x \le \frac{-5}{6}x - \frac{9}{4}$$

The solution is  $(-\infty, -41.4]$ , which is option B.

A.  $(-\infty, a]$ , where  $a \in [40.4, 43.4]$ 

 $(-\infty, 41.4]$ , which corresponds to negating the endpoint of the solution.

B.  $(-\infty, a]$ , where  $a \in [-42.4, -39.4]$ 

\*  $(-\infty, -41.4]$ , which is the correct option.

C.  $[a, \infty)$ , where  $a \in [40.4, 43.4]$ 

 $[41.4, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $[a, \infty)$ , where  $a \in [-43.4, -39.4]$ 

 $[-41.4, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$3x - 5 < 6x - 3$$

The solution is  $(-0.667, \infty)$ , which is option D.

A.  $(-\infty, a)$ , where  $a \in [-4.5, -0.5]$ 

 $(-\infty, -0.667)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $(-\infty, a)$ , where  $a \in [0.3, 3.3]$ 

 $(-\infty, 0.667)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

C.  $(a, \infty)$ , where  $a \in [-0.24, 1.18]$ 

 $(0.667, \infty)$ , which corresponds to negating the endpoint of the solution.

D.  $(a, \infty)$ , where  $a \in [-2.11, -0.11]$ 

\*  $(-0.667, \infty)$ , which is the correct option.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.