1. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r.

$$\frac{9x^3 - 28x - 13}{x - 2}$$

- A. $a \in [14, 20], b \in [29, 40], c \in [36, 45], \text{ and } r \in [71, 77].$
- B. $a \in [2, 10], b \in [6, 13], c \in [-22, -14], \text{ and } r \in [-37, -30].$
- C. $a \in [14, 20], b \in [-42, -35], c \in [36, 45], \text{ and } r \in [-104, -95].$
- D. $a \in [2, 10], b \in [15, 20], c \in [6, 10], \text{ and } r \in [2, 5].$
- E. $a \in [2, 10], b \in [-22, -16], c \in [6, 10], \text{ and } r \in [-31, -23].$
- 2. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r.

$$\frac{6x^3 + 9x^2 - 51x + 34}{x + 4}$$

- A. $a \in [-2, 9], b \in [-24, -18], c \in [48, 56], and <math>r \in [-238, -229].$
- B. $a \in [-2, 9], b \in [-17, -13], c \in [3, 12], and r \in [-5, 3].$
- C. $a \in [-30, -21], b \in [-90, -86], c \in [-402, -396], and <math>r \in [-1563, -1558].$
- D. $a \in [-2, 9], b \in [28, 36], c \in [76, 85], and <math>r \in [354, 359].$
- E. $a \in [-30, -21], b \in [104, 113], c \in [-472, -465], and r \in [1913, 1924].$
- 3. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 2x^3 + 3x^2 + 7x + 3$$

- A. $\pm 1, \pm 3$
- B. All combinations of: $\frac{\pm 1, \pm 3}{\pm 1, \pm 2}$

- C. All combinations of: $\frac{\pm 1, \pm 2}{\pm 1, \pm 3}$
- D. $\pm 1, \pm 2$
- E. There is no formula or theorem that tells us all possible Integer roots.
- 4. Factor the polynomial below completely, knowing that x + 5 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \le z_2 \le z_3 \le z_4$. To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^4 + 55x^3 + 117x^2 - 88x - 240$$

- A. $z_1 \in [-5.54, -4.65], z_2 \in [-4.26, -3.9], z_3 \in [-2.14, -0.83], \text{ and } z_4 \in [1.27, 1.9]$
- B. $z_1 \in [-1.37, -1.22], z_2 \in [1.32, 1.6], z_3 \in [3.23, 4.14], \text{ and } z_4 \in [4.12, 5.15]$
- C. $z_1 \in [-1.05, -0.46], z_2 \in [0.66, 0.73], z_3 \in [3.23, 4.14], \text{ and } z_4 \in [4.12, 5.15]$
- D. $z_1 \in [-4.96, -3.52], z_2 \in [0.44, 0.51], z_3 \in [3.23, 4.14], \text{ and } z_4 \in [4.12, 5.15]$
- E. $z_1 \in [-5.54, -4.65], z_2 \in [-4.26, -3.9], z_3 \in [-1.49, -0.16], \text{ and } z_4 \in [-0.12, 1.25]$
- 5. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \leq z_2 \leq z_3$. To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 4x^3 - 4x^2 - 33x + 45$$

- A. $z_1 \in [-2.7, -2.1], z_2 \in [-2.08, -0.87], \text{ and } z_3 \in [2.7, 3.47]$
- B. $z_1 \in [-3.8, -2.9], z_2 \in [0.15, 0.55], \text{ and } z_3 \in [0.49, 0.74]$
- C. $z_1 \in [-1.8, 0.2], z_2 \in [-0.49, -0.08], \text{ and } z_3 \in [2.7, 3.47]$

D. $z_1 \in [-3.8, -2.9], z_2 \in [1.25, 1.89], \text{ and } z_3 \in [1.76, 2.8]$

E.
$$z_1 \in [-5.1, -4.8], z_2 \in [-1.25, -0.55], \text{ and } z_3 \in [2.7, 3.47]$$

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