1. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r.

$$\frac{4x^3 - 12x + 5}{x + 2}$$

- A. $a \in [0, 5], b \in [3, 9], c \in [1, 7], \text{ and } r \in [11, 17].$
- B. $a \in [-14, -6], b \in [15, 20], c \in [-48, -39], \text{ and } r \in [91, 94].$
- C. $a \in [0, 5], b \in [-10, -2], c \in [1, 7], \text{ and } r \in [-7, -1].$
- D. $a \in [-14, -6], b \in [-18, -13], c \in [-48, -39], \text{ and } r \in [-84, -78].$
- E. $a \in [0, 5], b \in [-13, -10], c \in [23, 26], \text{ and } r \in [-69, -66].$
- 2. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \leq z_2 \leq z_3$. To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^3 - 5x^2 - 22x + 24$$

- A. $z_1 \in [-2.82, -1.65], z_2 \in [-0.5, 0.9], \text{ and } z_3 \in [0.25, 1.03]$
- B. $z_1 \in [-3.34, -2.54], z_2 \in [-1, -0.3], \text{ and } z_3 \in [1.94, 2.41]$
- C. $z_1 \in [-2.82, -1.65], z_2 \in [1.2, 2.2], \text{ and } z_3 \in [1.45, 1.52]$
- D. $z_1 \in [-1.57, -1.04], z_2 \in [-1.9, -1.2], \text{ and } z_3 \in [1.94, 2.41]$
- E. $z_1 \in [-0.93, -0.6], z_2 \in [-1, -0.3], \text{ and } z_3 \in [1.94, 2.41]$
- 3. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r.

$$\frac{6x^3 + 43x^2 + 86x + 38}{x + 4}$$

- A. $a \in [2, 10], b \in [17, 21], c \in [8, 17], and <math>r \in [-3, 0].$
- B. $a \in [-33, -18], b \in [134, 145], c \in [-473, -467], and r \in [1917, 1919].$

- C. $a \in [2, 10], b \in [65, 70], c \in [349, 360], and <math>r \in [1451, 1462].$
- D. $a \in [2, 10], b \in [11, 15], c \in [19, 25], and <math>r \in [-75, -65].$
- E. $a \in [-33, -18], b \in [-57, -51], c \in [-131, -118], and r \in [-469, -465].$
- 4. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 2x^4 + 4x^3 + 3x^2 + 7x + 7$$

- A. All combinations of: $\frac{\pm 1, \pm 7}{\pm 1, \pm 2}$
- B. $\pm 1, \pm 2$
- C. $\pm 1, \pm 7$
- D. All combinations of: $\frac{\pm 1, \pm 2}{\pm 1, \pm 7}$
- E. There is no formula or theorem that tells us all possible Integer roots.
- 5. Factor the polynomial below completely, knowing that x + 5 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \le z_2 \le z_3 \le z_4$. To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 10x^4 + 33x^3 - 165x^2 - 448x - 240$$

- A. $z_1 \in [-4.2, -1.2], z_2 \in [0.22, 0.43], z_3 \in [2.96, 3.09], \text{ and } z_4 \in [4.04, 5.73]$
- B. $z_1 \in [-7.3, -4.2], z_2 \in [-1.53, -1.46], z_3 \in [-0.94, -0.78], \text{ and } z_4 \in [3.87, 4.67]$
- C. $z_1 \in [-4.2, -1.2], z_2 \in [0.47, 0.77], z_3 \in [0.9, 1.27], \text{ and } z_4 \in [4.04, 5.73]$
- D. $z_1 \in [-7.3, -4.2], z_2 \in [-1.39, -1.22], z_3 \in [-0.72, -0.65], \text{ and } z_4 \in [3.87, 4.67]$
- E. $z_1 \in [-4.2, -1.2], z_2 \in [0.74, 1], z_3 \in [1.36, 1.51], \text{ and } z_4 \in [4.04, 5.73]$

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