

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 5x < \frac{17x - 4}{3} \leq -8 + 3x$$

The solution is  $(-8.50, -2.50]$ , which is option B.

- A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-9.75, -2.25]$  and  $b \in [-4.5, -1.5]$

$(-\infty, -8.50) \cup [-2.50, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

- B.  $(a, b]$ , where  $a \in [-12, -8.25]$  and  $b \in [-6, 2.25]$

\*  $(-8.50, -2.50]$ , which is the correct option.

- C.  $[a, b)$ , where  $a \in [-9, -1.5]$  and  $b \in [-8.25, -2.25]$

$[-8.50, -2.50)$ , which corresponds to flipping the inequality.

- D.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-11.25, -5.25]$  and  $b \in [-7.5, 0]$

$(-\infty, -8.50] \cup (-2.50, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

- E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

2. Using an interval or intervals, describe all the  $x$ -values within or including a distance of the given values.

No more than 5 units from the number 1.

The solution is  $[-4, 6]$ , which is option A.

- A.  $[-4, 6]$

This describes the values no more than 5 from 1

- B.  $(-4, 6)$

This describes the values less than 5 from 1

- C.  $(-\infty, -4) \cup (6, \infty)$

This describes the values more than 5 from 1

- D.  $(-\infty, -4] \cup [6, \infty)$

This describes the values no less than 5 from 1

- E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

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3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{4}{8} - \frac{6}{9}x \geq \frac{6}{4}x - \frac{10}{2}$$

The solution is  $(-\infty, 2.538]$ , which is option B.

- A.  $(-\infty, a]$ , where  $a \in [-3, 0.75]$

$(-\infty, -2.538]$ , which corresponds to negating the endpoint of the solution.

- B.  $(-\infty, a]$ , where  $a \in [-0.75, 5.25]$

\*  $(-\infty, 2.538]$ , which is the correct option.

- C.  $[a, \infty)$ , where  $a \in [-0.75, 5.25]$

$[2.538, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $[a, \infty)$ , where  $a \in [-3, 0]$

$[-2.538, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6 + 8x \leq \frac{39x + 9}{4} < 8 + 9x$$

The solution is None of the above., which is option E.

- A.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [3, 9]$  and  $b \in [-11.25, -2.25]$

$(-\infty, 4.71] \cup (-7.67, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

- B.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [4.5, 8.25]$  and  $b \in [-8.25, -6]$

$(-\infty, 4.71) \cup [-7.67, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

- C.  $[a, b]$ , where  $a \in [3.75, 5.25]$  and  $b \in [-9.75, -1.5]$

$[4.71, -7.67]$ , which is the correct interval but negatives of the actual endpoints.

- D.  $(a, b]$ , where  $a \in [2.25, 6.75]$  and  $b \in [-9.75, -4.5]$

$(4.71, -7.67]$ , which corresponds to flipping the inequality and getting negatives of the actual endpoints.

E. None of the above.

\* This is correct as the answer should be  $[-4.71, 7.67]$ .

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

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5. Using an interval or intervals, describe all the  $x$ -values within or including a distance of the given values.

No more than 4 units from the number 2.

The solution is  $[-2, 6]$ , which is option C.

A.  $(-\infty, -2] \cup [6, \infty)$

This describes the values no less than 4 from 2

B.  $(-\infty, -2) \cup (6, \infty)$

This describes the values more than 4 from 2

C.  $[-2, 6]$

This describes the values no more than 4 from 2

D.  $(-2, 6)$

This describes the values less than 4 from 2

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

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6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3 + 6x > 8x \text{ or } 8 + 9x < 11x$$

The solution is  $(-\infty, -1.5)$  or  $(4.0, \infty)$ , which is option A.

A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2.25, 0.75]$  and  $b \in [3.52, 6]$

\* Correct option.

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-2.02, 0.67]$  and  $b \in [3, 7.5]$

Corresponds to including the endpoints (when they should be excluded).

C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-6, -3.75]$  and  $b \in [0.9, 3.9]$

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-4.65, -3.67]$  and  $b \in [0.75, 3.75]$

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

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7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 4x > 5x \text{ or } 3 + 3x < 5x$$

The solution is  $(-\infty, -7.0)$  or  $(1.5, \infty)$ , which is option A.

- A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-8.25, -3]$  and  $b \in [0, 2.25]$

\* Correct option.

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2.25, 1.5]$  and  $b \in [4.5, 10.5]$

Corresponds to inverting the inequality and negating the solution.

- C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-9.75, -6.75]$  and  $b \in [-4.5, 3]$

Corresponds to including the endpoints (when they should be excluded).

- D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-3, 1.5]$  and  $b \in [6, 12]$

Corresponds to including the endpoints AND negating.

- E.  $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

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8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7x + 10 > -4x - 4$$

The solution is  $(-\infty, 4.667)$ , which is option C.

- A.  $(a, \infty)$ , where  $a \in [2.67, 10.67]$

$(4.667, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- B.  $(a, \infty)$ , where  $a \in [-6.67, -0.67]$

$(-4.667, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- C.  $(-\infty, a)$ , where  $a \in [1.67, 5.67]$

\*  $(-\infty, 4.667)$ , which is the correct option.

- D.  $(-\infty, a)$ , where  $a \in [-4.67, 1.33]$

$(-\infty, -4.667)$ , which corresponds to negating the endpoint of the solution.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{4}{8} - \frac{4}{3}x < \frac{-3}{9}x - \frac{6}{7}$$

The solution is  $(1.357, \infty)$ , which is option B.

- A.  $(-\infty, a)$ , where  $a \in [-3.75, 0]$

$(-\infty, -1.357)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- B.  $(a, \infty)$ , where  $a \in [0, 4.5]$

\*  $(1.357, \infty)$ , which is the correct option.

- C.  $(-\infty, a)$ , where  $a \in [0.75, 4.5]$

$(-\infty, 1.357)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $(a, \infty)$ , where  $a \in [-3, -0.75]$

$(-1.357, \infty)$ , which corresponds to negating the endpoint of the solution.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-10x + 7 \leq 7x + 6$$

The solution is  $[0.059, \infty)$ , which is option C.

- A.  $(-\infty, a]$ , where  $a \in [-0.04, 0.12]$

$(-\infty, 0.059]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- B.  $(-\infty, a]$ , where  $a \in [-0.07, -0.01]$

$(-\infty, -0.059]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- C.  $[a, \infty)$ , where  $a \in [0.04, 0.16]$

\*  $[0.059, \infty)$ , which is the correct option.

- D.  $[a, \infty)$ , where  $a \in [-0.09, -0.05]$

$[-0.059, \infty)$ , which corresponds to negating the endpoint of the solution.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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