This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

11. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6 + 6x > 9x$$
 or  $8 - 3x < 5x$ 

The solution is  $(-\infty, -2.0)$  or  $(1.0, \infty)$ 

A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-1.31, -0.19]$  and  $b \in [1.84, 2.65]$ 

Corresponds to inverting the inequality and negating the solution.

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-2.3, -1.1]$  and  $b \in [-0.43, 1.35]$ 

Corresponds to including the endpoints (when they should be excluded).

- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2.4, -1.81]$  and  $b \in [0.59, 1.56]$ 
  - \* Correct option.
- D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-1.8, -0.2]$  and  $b \in [1.13, 3.55]$

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comments: When multiplying or dividing by a negative, flip the sign.

12. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{7}{3} + \frac{3}{2}x < \frac{5}{6}x - \frac{8}{4}$$

The solution is  $(-\infty, -6.5)$ 

- A.  $(-\infty, a)$ , where  $a \in [-7, -5]$ 
  - \*  $(-\infty, -6.5)$ , which is the correct option.
- B.  $(-\infty, a)$ , where  $a \in [5, 7]$

 $(-\infty, 6.5)$ , which corresponds to negating the endpoint of the solution.

C.  $(a, \infty)$ , where  $a \in [4, 9]$ 

 $(6.5, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(a, \infty)$ , where  $a \in [-8, -4]$ 

 $(-6.5, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comments: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

13. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-4 + 4x < \frac{30x - 8}{7} \le -9 + 3x$$

The solution is None of the above.

- A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [5, 11]$  and  $b \in [1, 8]$ 
  - $(-\infty, 10.00) \cup [6.11, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.
- B.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [9, 11]$  and  $b \in [1, 7]$ 
  - $(-\infty, 10.00] \cup (6.11, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.
- C. [a, b), where  $a \in [9, 14]$  and  $b \in [5, 7]$ 
  - [10.00, 6.11), which corresponds to flipping the inequality and getting negatives of the actual endpoints.
- D. (a, b], where  $a \in [8, 11]$  and  $b \in [0, 13]$ 
  - (10.00, 6.11], which is the correct interval but negatives of the actual endpoints.
- E. None of the above.
  - \* This is correct as the answer should be (-10.00, -6.11].

To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

14. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

More than 8 units from the number 4.

The solution is  $(-\infty, -4) \cup (12, \infty)$ 

A. 
$$[-4, 12]$$

This describes the values no more than 8 from 4

B. 
$$(-4, 12)$$

This describes the values less than 8 from 4

C. 
$$(-\infty, -4) \cup (12, \infty)$$

This describes the values more than 8 from 4

D. 
$$(-\infty, -4] \cup [12, \infty)$$

This describes the values no less than 8 from 4

## E. None of the above

You likely thought the values in the interval were not correct.

## Answer Key for Module 3 - Inequalities Version C

General Comments: When thinking about this language, it helps to draw a number line and try points.

15. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8x + 5 < 7x + 6$$

The solution is  $(-0.067, \infty)$ 

A.  $(a, \infty)$ , where  $a \in [-0.05, 0.35]$ 

 $(0.067, \infty)$ , which corresponds to negating the endpoint of the solution.

- B.  $(a, \infty)$ , where  $a \in [-0.1, -0]$ 
  - \*  $(-0.067, \infty)$ , which is the correct option.
- C.  $(-\infty, a)$ , where  $a \in [0.02, 0.08]$

 $(-\infty, 0.067)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(-\infty, a)$ , where  $a \in [-0.17, -0.06]$ 

 $(-\infty, -0.067)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comments: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.