This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$ .

Pringles wants to add 42 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 12 percent, which is option A.

- A. About 12 percent
  - \* This is the correct option.
- B. About 21 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

C. About 14 percent

This corresponds to not solving for the increase properly.

D. About 19 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

E. None of the above

If you chose this, please contact the coordinator to discus how you solved the problem.

**General Comment:** Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

2. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the square of the time, T (Earth years), required for a planet to orbit  $Sun \chi$  decreases as the square of the distance, d (AUs), that the planet is from  $Sun \chi$  decreases. For example, when Ea's average distance from  $Sun \chi$  is 5, it takes 94 Earth days to complete an orbit.

The solution is k = 353.440, which is option D.

A. k = 4.028

This copies the constant used in the homework.

B. k = 220900.000

This corresponds to the model  $T^2 = \frac{k}{d^2}$ .

C. k = 4.336

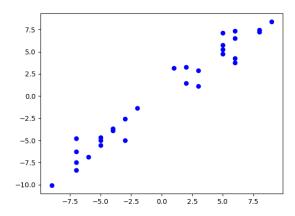
This corresponds to the model  $T^{1/2} = kd^{1/2}$ .

- D. k = 353.440
  - \* This is the correct option corresponding to the model  $T^2 = kd^2$ .
- E. Unable to compute the constant based on the information given.

This corresponds to believing you cannot determine the type of model from the information given.

**General Comment:** Since T decreases proportionally as d decreases, we know this is a direct variation model.

## 3. Determine the appropriate model for the graph of points below.



The solution is Linear model, which is option D.

### A. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

# B. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

# C. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

### D. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

#### E. None of the above

For this to be the correct option, we want to see no pattern in the points.

**General Comment:** This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

4. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has tripled every 4 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 45 days, which is option D.

A. About 22 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

B. About 21 days

You modeled the situation correctly but did not apply the properties of log correctly.

C. About 49 days

You modeled the situation with e as the base, but solved correctly otherwise.

- D. About 45 days
  - \* This is the correct option.
- E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

**General Comment:** Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

5. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 22 liter 20 percent solution of chemical  $\chi$  using two different solution percentages of chemical  $\chi$ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 15 percent and 38 percent solutions, what was the amount she used of the 38 percent solution?

The solution is 4.78, which is option C.

A. 7.03

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 17.22

This is the concentration of 15 percent solution.

C. 4.78

\*This is the correct option.

D. 11.00

This would be correct if Brittany used equal parts of each solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

**General Comment:** Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

6. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$ .

Pringles wants to add 22 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 7 percent, which is option D.

A. About 10 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

B. About 3 percent

This corresponds to not solving for the increase properly.

C. About 11 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

- D. About 7 percent
  - \* This is the correct option.
- E. None of the above

If you chose this, please contact the coordinator to discus how you solved the problem.

**General Comment:** Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

7. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 26 liter 25 percent solution of chemical  $\chi$  using two different solution percentages of chemical  $\chi$ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 13 percent and 38 percent solutions, what was the amount she used of the 38 percent solution?

The solution is 12.48, which is option B.

A. 13.52

This is the concentration of 13 percent solution.

B. 12.48

\*This is the correct option.

C. 12.00

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

D. 13.00

This would be correct if Brittany used equal parts of each solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

**General Comment:** Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

## 8. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has quadrupled every 2 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 18 days, which is option A.

- A. About 18 days
  - \* This is the correct option.
- B. About 11 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

C. About 25 days

You modeled the situation with e as the base, but solved correctly otherwise.

D. About 10 days

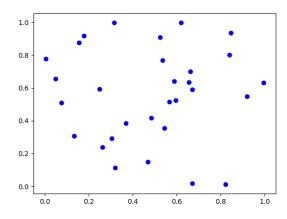
You modeled the situation correctly but did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

**General Comment:** Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

## 9. Determine the appropriate model for the graph of points below.



The solution is None of the above, which is option E.

A. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

B. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

D. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

**General Comment:** This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

10. Using the situation below, construct a linear model that describes the cost of the coffee beans C(h) in terms of the weight of the high-quality coffee beans h.

Veronica needs to prepare 190 of blended coffee beans selling for \$3.67 per pound. She has a high-quality bean that sells for \$4.43 a pound and a low-quality bean that sells for \$2.95 a pound.

The solution is C(h) = 1.48h + 560.50, which is option B.

A. C(h) = 3.69h

This assumes that exactly half of the high- and low- quality beans are mixed to create the blended coffee beans.

B. C(h) = 1.48h + 560.50

\* This is the correct option since the questions asked you to construct the cost model in terms of the weight of the high-quality bean.

C. C(h) = -1.48h + 841.70

This would be correct if the question asked you to construct the cost model in terms of the weight of the low-quality bean.

D. C(h) = 4.43h

This models the cost of the high-quality bean only, not the blended beans.

E. None of the above.

If you chose this option, please talk to the coordinator to discuss why.

**General Comment:** This is exactly like the chemistry mixture question from the homework! If you are having trouble with this problem, be sure to review the video for building linear models.