This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 - 3x < \frac{-13x - 3}{6} \le 9 - 3x$$

The solution is None of the above., which is option E.

- A. (a, b], where  $a \in [0.4, 9.4]$  and  $b \in [-12.4, -7.4]$ 
  - (5.40, -11.40], which is the correct interval but negatives of the actual endpoints.
- B.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [5.4, 9.4]$  and  $b \in [-11.4, -9.4]$ 
  - $(-\infty, 5.40] \cup (-11.40, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.
- C. [a, b), where  $a \in [2.4, 7.4]$  and  $b \in [-12.4, -6.4]$ 
  - [5.40, -11.40), which corresponds to flipping the inequality and getting negatives of the actual endpoints.
- D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [4.4, 7.4]$  and  $b \in [-11.4, -10.4]$ 
  - $(-\infty, 5.40) \cup [-11.40, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.
- E. None of the above.
  - \* This is correct as the answer should be (-5.40, 11.40].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

2. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{6}{3} - \frac{8}{8}x > \frac{-3}{5}x - \frac{9}{6}$$

The solution is  $(-\infty, 8.75)$ , which is option D.

- A.  $(a, \infty)$ , where  $a \in [8.75, 9.75]$ 
  - $(8.75, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- B.  $(a, \infty)$ , where  $a \in [-8.75, -5.75]$ 
  - $(-8.75, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.
- C.  $(-\infty, a)$ , where  $a \in [-10.75, -7.75]$

 $(-\infty, -8.75)$ , which corresponds to negating the endpoint of the solution.

- D.  $(-\infty, a)$ , where  $a \in [6.75, 10.75]$ 
  - \*  $(-\infty, 8.75)$ , which is the correct option.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$7 + 8x > 9x$$
 or  $8 + 4x < 5x$ 

The solution is  $(-\infty, 7.0)$  or  $(8.0, \infty)$ , which is option B.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-8, -6]$  and  $b \in [-8, -4]$ 

Corresponds to including the endpoints AND negating.

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [3, 8]$  and  $b \in [8, 11]$ 
  - \* Correct option.
- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-8, -5]$  and  $b \in [-9, -1]$

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [4, 9]$  and  $b \in [8, 11]$ 

Corresponds to including the endpoints (when they should be excluded).

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$8x + 5 \ge 10x + 3$$

The solution is  $(-\infty, 1.0]$ , which is option C.

A.  $(-\infty, a]$ , where  $a \in [-2.8, 0.7]$ 

 $(-\infty, -1.0]$ , which corresponds to negating the endpoint of the solution.

B.  $[a, \infty)$ , where  $a \in [-0.7, 3.3]$ 

 $[1.0, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

C.  $(-\infty, a]$ , where  $a \in [-0.6, 5.4]$ 

\*  $(-\infty, 1.0]$ , which is the correct option.

D.  $[a, \infty)$ , where  $a \in [-1.6, 0.9]$ 

 $[-1.0, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

5. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No less than 6 units from the number -3.

The solution is  $(-\infty, -9] \cup [3, \infty)$ , which is option A.

A. 
$$(-\infty, -9] \cup [3, \infty)$$

This describes the values no less than 6 from -3

B. [-9, 3]

This describes the values no more than 6 from -3

C. (-9,3)

This describes the values less than 6 from -3

D.  $(-\infty, -9) \cup (3, \infty)$ 

This describes the values more than 6 from -3

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{8}{8} - \frac{8}{4}x \ge \frac{-7}{5}x - \frac{6}{9}$$

The solution is  $(-\infty, 2.778]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [-1.22, 3.78]$ 
  - \*  $(-\infty, 2.778]$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [-4.78, 0.22]$

 $(-\infty, -2.778]$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [-3.78, 0.22]$ 

 $[-2.778, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $[a, \infty)$ , where  $a \in [1.78, 5.78]$ 

 $[2.778, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

7. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No less than 9 units from the number 5.

The solution is  $(-\infty, -4] \cup [14, \infty)$ , which is option D.

A. 
$$(-\infty, -4) \cup (14, \infty)$$

This describes the values more than 9 from 5

B. [-4, 14]

This describes the values no more than 9 from 5

C. (-4, 14)

This describes the values less than 9 from 5

D. 
$$(-\infty, -4] \cup [14, \infty)$$

This describes the values no less than 9 from 5

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 8x < \frac{66x + 4}{8} \le 3 + 8x$$

The solution is None of the above., which is option E.

A. [a, b), where  $a \in [29, 34]$  and  $b \in [-11, -3]$ 

[30.00, -10.00), which corresponds to flipping the inequality and getting negatives of the actual endpoints.

B.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [30, 34]$  and  $b \in [-12, -8]$ 

 $(-\infty, 30.00] \cup (-10.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

C.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [29, 32]$  and  $b \in [-13, -4]$ 

 $(-\infty, 30.00) \cup [-10.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

D. (a, b], where  $a \in [30, 31]$  and  $b \in [-12, -7]$ 

(30.00, -10.00], which is the correct interval but negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be (-30.00, 10.00].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 + 4x > 7x$$
 or  $9 + 9x < 12x$ 

The solution is  $(-\infty, -1.667)$  or  $(3.0, \infty)$ , which is option B.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-6, -2]$  and  $b \in [-0.33, 2.67]$ 

Corresponds to including the endpoints AND negating.

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-1.67, 2.33]$  and  $b \in [2.68, 3.81]$ 
  - \* Correct option.
- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-4, -2]$  and  $b \in [1.04, 2.06]$

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-1.67, 0.33]$  and  $b \in [2, 6]$ 

Corresponds to including the endpoints (when they should be excluded).

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-9x - 7 > 8x - 10$$

The solution is  $(-\infty, 0.176)$ , which is option C.

A.  $(a, \infty)$ , where  $a \in [-0.02, 0.51]$ 

 $(0.176, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $(-\infty, a)$ , where  $a \in [-0.46, 0.14]$ 

 $(-\infty, -0.176)$ , which corresponds to negating the endpoint of the solution.

C.  $(-\infty, a)$ , where  $a \in [0.11, 1.05]$ 

\*  $(-\infty, 0.176)$ , which is the correct option.

D.  $(a, \infty)$ , where  $a \in [-0.47, -0.17]$ 

 $(-0.176, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.