

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

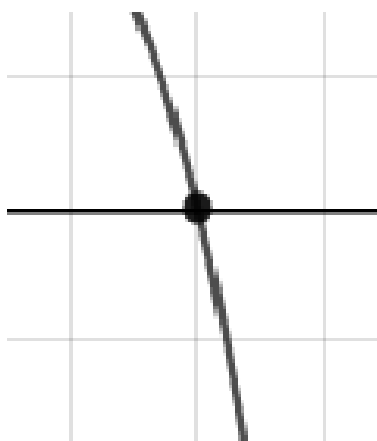
If you have a suggestion to make the keys better, please fill out the short survey [here](#).

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Describe the zero behavior of the zero $x = -2$ of the polynomial below.

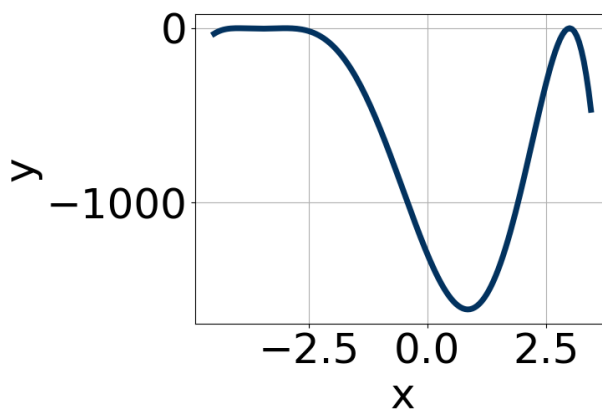
$$f(x) = 6(x - 5)^7(x + 5)^4(x + 2)^9(x - 2)^6$$

The solution is the graph below.



General Comment: You will need to sketch the entire graph, then zoom in on the zero the question asks about.

2. Write an equation that *could* represent the graph below.



The solution is $-19(x + 3)^4(x + 4)^{10}(x - 3)^8$.

Plausible alternative answers include:* This is the correct option. The factor $(x - 3)$ should have an even power and the leading coefficient should be the opposite sign. This corresponds to the leading coefficient being the opposite value than it should be. The factors $(x + 4)$ and $(x - 3)$ should both have even powers. The factor $(x - 3)$ should have an even power.

General Comment: General Comments: Draw the x-axis to determine which zeros are touching (and so have even multiplicity) or cross (and have odd multiplicity).

3. Construct the lowest-degree polynomial given the zeros below.

$$\frac{-4}{3}, \frac{-5}{3}, \text{ and } -7$$

The solution is $9x^3 + 90x^2 + 209x + 140$.

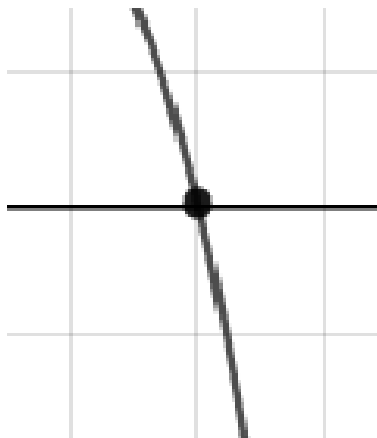
Plausible alternative answers include: $9x^3 + 66x^2 + x - 140$, which corresponds to multiplying out $(3x - 4)(3x + 5)(x + 7)$. $9x^3 - 90x^2 + 209x - 140$, which corresponds to multiplying out $(3x - 4)(3x - 5)(x - 7)$. * $9x^3 + 90x^2 + 209x + 140$, which is the correct option. $9x^3 + 36x^2 - 169x + 140$, which corresponds to multiplying out $(3x - 4)(3x - 5)(x + 7)$. $9x^3 + 90x^2 + 209x - 140$, which corresponds to multiplying everything correctly except the constant term.

General Comment: To construct the lowest-degree polynomial, you want to multiply out $(3x + 4)(3x + 5)(x + 7)$

4. Describe the zero behavior of the zero $x = -8$ of the polynomial below.

$$f(x) = -6(x + 2)^{11}(x - 2)^7(x + 8)^3(x - 8)^2$$

The solution is the graph below.



General Comment: You will need to sketch the entire graph, then zoom in on the zero the question asks about.

5. Construct the lowest-degree polynomial given the zeros below.

$$\frac{1}{2}, \frac{3}{4}, \text{ and } 4$$

The solution is $8x^3 - 42x^2 + 43x - 12$.

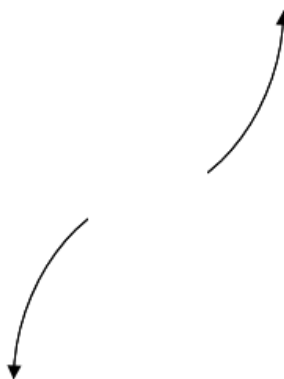
Plausible alternative answers include: $8x^3 - 34x^2 + 5x + 12$, which corresponds to multiplying out $(2x + 1)(4x - 3)(x - 4)$. $8x^3 - 22x^2 - 37x - 12$, which corresponds to multiplying out $(2x + 1)(4x + 3)(x - 4)$. * $8x^3 - 42x^2 + 43x - 12$, which is the correct option. $8x^3 - 42x^2 + 43x + 12$, which corresponds to multiplying everything correctly except the constant term. $8x^3 + 42x^2 + 43x + 12$, which corresponds to multiplying out $(2x + 1)(4x + 3)(x + 4)$.

General Comment: To construct the lowest-degree polynomial, you want to multiply out $(2x - 1)(4x - 3)(x - 4)$

6. Describe the end behavior of the polynomial below.

$$f(x) = 2(x + 7)^4(x - 7)^9(x - 4)^2(x + 4)^2$$

The solution is the graph below.



General Comment: Remember that end behavior is determined by the leading coefficient AND whether the **sum** of the multiplicities is positive or negative.

7. Construct the lowest-degree polynomial given the zeros below.

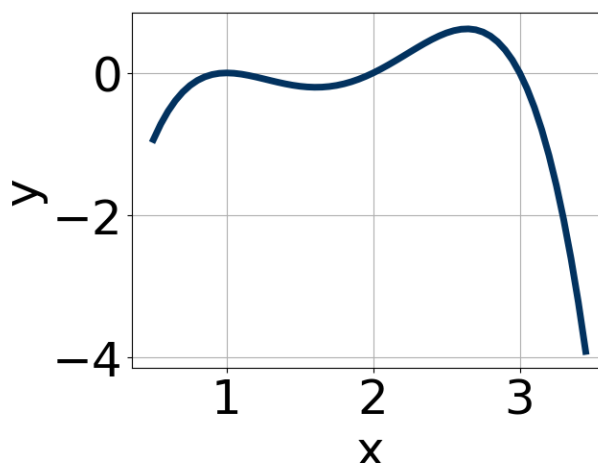
$$-2 + 2i \text{ and } -2$$

The solution is $x^3 + 6x^2 + 16x + 16$.

Plausible alternative answers include:* $x^3 + 6x^2 + 16x + 16$, which is the correct option. $x^3 - 6x^2 + 16x - 16$, which corresponds to multiplying out $(x - (-2 + 2i))(x - (-2 - 2i))(x - 2)$. $x^3 + x^2 + 0x - 4$, which corresponds to multiplying out $(x - 2)(x + 2)$. $x^3 + x^2 + 4x + 4$, which corresponds to multiplying out $(x + 2)(x + 2)$. This corresponds to making an unanticipated error or not understanding how to use nonreal complex numbers to create the lowest-degree polynomial. If you chose this and are not sure what you did wrong, please contact the coordinator for help.

General Comment: Remember that the conjugate of $a + bi$ is $a - bi$. Since these zeros always come in pairs, we need to multiply out $(x - (-2 + 2i))(x - (-2 - 2i))(x - (-2))$.

8. Write an equation that *could* represent the graph below.



The solution is $-8(x-1)^8(x-3)^7(x-2)^5$.

Plausible alternative answers include:* This is the correct option. This corresponds to the leading coefficient being the opposite value than it should be. The factor 1 should have an even power and the factor 3 should have an odd power. The factor $(x-3)$ should have an odd power. The factor $(x-2)$ should have an odd power and the leading coefficient should be the opposite sign.

General Comment: General Comments: Draw the x-axis to determine which zeros are touching (and so have even multiplicity) or cross (and have odd multiplicity).

9. Construct the lowest-degree polynomial given the zeros below.

$$-2 + 2i \text{ and } 3$$

The solution is $x^3 + x^2 - 4x - 24$.

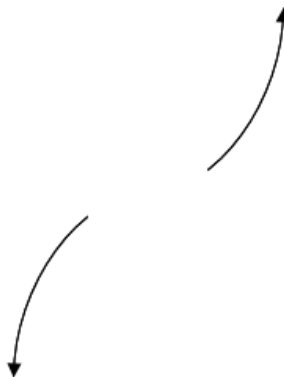
Plausible alternative answers include: $x^3 + x^2 - x - 6$, which corresponds to multiplying out $(x+2)(x-3)$. $x^3 + x^2 - 5x + 6$, which corresponds to multiplying out $(x-2)(x-3)$. * $x^3 + x^2 - 4x - 24$, which is the correct option. $x^3 - 1x^2 - 4x + 24$, which corresponds to multiplying out $(x - (-2 + 2i))(x - (-2 - 2i))(x + 3)$. This corresponds to making an unanticipated error or not understanding how to use nonreal complex numbers to create the lowest-degree polynomial. If you chose this and are not sure what you did wrong, please contact the coordinator for help.

General Comment: Remember that the conjugate of $a + bi$ is $a - bi$. Since these zeros always come in pairs, we need to multiply out $(x - (-2 + 2i))(x - (-2 - 2i))(x - (3))$.

10. Describe the end behavior of the polynomial below.

$$f(x) = 5(x+9)^4(x-9)^7(x-7)^4(x+7)^4$$

The solution is the graph below.



General Comment: Remember that end behavior is determined by the leading coefficient AND whether the **sum** of the multiplicities is positive or negative.
