

1. Factor the polynomial below completely, knowing that $x + 4$ is a factor. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \leq z_2 \leq z_3 \leq z_4$. *To make the problem easier, all zeros are between -5 and 5.*

$$f(x) = 10x^4 - 7x^3 - 172x^2 + 112x + 192$$

- A. $z_1 \in [-5, -3]$, $z_2 \in [-1.44, -1.13]$, $z_3 \in [0.36, 0.71]$, and $z_4 \in [2, 6]$
- B. $z_1 \in [-5, -3]$, $z_2 \in [-0.37, -0.25]$, $z_3 \in [3.94, 4.03]$, and $z_4 \in [2, 6]$
- C. $z_1 \in [-5, -3]$, $z_2 \in [-1.65, -1.31]$, $z_3 \in [0.67, 0.93]$, and $z_4 \in [2, 6]$
- D. $z_1 \in [-5, -3]$, $z_2 \in [-0.99, -0.67]$, $z_3 \in [1.33, 1.68]$, and $z_4 \in [2, 6]$
- E. $z_1 \in [-5, -3]$, $z_2 \in [-0.75, -0.48]$, $z_3 \in [1.19, 1.42]$, and $z_4 \in [2, 6]$
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2. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where $z_1 \leq z_2 \leq z_3$. *To make the problem easier, all zeros are between -5 and 5.*

$$f(x) = 4x^3 - 24x^2 + 5x + 75$$

- A. $z_1 \in [-5.6, -3.7]$, $z_2 \in [-2.9, -2.3]$, and $z_3 \in [0.7, 2]$
- B. $z_1 \in [-5.6, -3.7]$, $z_2 \in [-0.8, -0.1]$, and $z_3 \in [0.6, 0.9]$
- C. $z_1 \in [-1.2, 0.2]$, $z_2 \in [-0.1, 1.3]$, and $z_3 \in [4.3, 6.5]$
- D. $z_1 \in [-3.1, -0.7]$, $z_2 \in [1.8, 4.1]$, and $z_3 \in [4.3, 6.5]$
- E. $z_1 \in [-5.6, -3.7]$, $z_2 \in [-1.8, -0.5]$, and $z_3 \in [2, 4.1]$
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3. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r .

$$\frac{12x^3 - 56x^2 + 12x + 84}{x - 4}$$

- A. $a \in [11, 13]$, $b \in [-13, -4]$, $c \in [-27, -16]$, and $r \in [-4, 8]$.
B. $a \in [41, 54]$, $b \in [132, 138]$, $c \in [553, 566]$, and $r \in [2307, 2309]$.
C. $a \in [11, 13]$, $b \in [-24, -16]$, $c \in [-53, -46]$, and $r \in [-62, -57]$.
D. $a \in [41, 54]$, $b \in [-254, -243]$, $c \in [999, 1006]$, and $r \in [-3936, -3929]$.
E. $a \in [11, 13]$, $b \in [-112, -92]$, $c \in [426, 437]$, and $r \in [-1631, -1620]$.
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4. Perform the division below. Then, find the intervals that correspond to the quotient in the form $ax^2 + bx + c$ and remainder r .

$$\frac{15x^3 + 65x^2 - 84}{x + 4}$$

- A. $a \in [13, 20]$, $b \in [122, 127]$, $c \in [492, 504]$, and $r \in [1910, 1918]$.
B. $a \in [13, 20]$, $b \in [4, 10]$, $c \in [-21, -18]$, and $r \in [-5, 3]$.
C. $a \in [-63, -59]$, $b \in [301, 309]$, $c \in [-1222, -1219]$, and $r \in [4792, 4797]$.
D. $a \in [-63, -59]$, $b \in [-181, -169]$, $c \in [-703, -698]$, and $r \in [-2886, -2879]$.
E. $a \in [13, 20]$, $b \in [-14, -5]$, $c \in [48, 54]$, and $r \in [-338, -329]$.
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5. What are the *possible Rational* roots of the polynomial below?

$$f(x) = 4x^3 + 3x^2 + 2x + 2$$

- A. $\pm 1, \pm 2$
B. $\pm 1, \pm 2, \pm 4$
C. All combinations of: $\frac{\pm 1, \pm 2, \pm 4}{\pm 1, \pm 2}$
D. All combinations of: $\frac{\pm 1, \pm 2}{\pm 1, \pm 2, \pm 4}$

E. There is no formula or theorem that tells us all possible Rational roots.
