This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$7x + 3 < 8x - 9$$

The solution is  $(12.0, \infty)$ , which is option D.

A.  $(-\infty, a)$ , where  $a \in [-13, -10]$ 

 $(-\infty, -12.0)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

B.  $(a, \infty)$ , where  $a \in [-18, -8]$ 

 $(-12.0, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(-\infty, a)$ , where  $a \in [7, 13]$ 

 $(-\infty, 12.0)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $(a, \infty)$ , where  $a \in [9, 14]$ 
  - \*  $(12.0, \infty)$ , which is the correct option.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

2. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

Less than 4 units from the number -4.

The solution is (-8,0), which is option C.

A. [-8,0]

This describes the values no more than 4 from -4

B.  $(-\infty, -8) \cup (0, \infty)$ 

This describes the values more than 4 from -4

C. (-8,0)

This describes the values less than 4 from -4

D.  $(-\infty, -8] \cup [0, \infty)$ 

This describes the values no less than 4 from -4

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8 + 8x > 9x$$
 or  $4 + 9x < 10x$ 

The solution is  $(-\infty, -8.0)$  or  $(4.0, \infty)$ , which is option C.

A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-5, -2]$  and  $b \in [5, 9]$ 

Corresponds to inverting the inequality and negating the solution.

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-8, -7]$  and  $b \in [2, 6]$ 

Corresponds to including the endpoints (when they should be excluded).

- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-9, -7]$  and  $b \in [3, 6]$ 
  - \* Correct option.
- D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-5, -1]$  and  $b \in [7, 12]$

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$5x + 5 \ge 10x - 3$$

The solution is  $(-\infty, 1.6]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [-1.4, 6.6]$ 
  - \*  $(-\infty, 1.6]$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [-1.6, -0.6]$

 $(-\infty, -1.6]$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [-0.6, 3.4]$ 

 $[1.6, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D.  $[a, \infty)$ , where  $a \in [-3.4, -0.4]$ 

 $[-1.6, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

5. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

Less than 8 units from the number -1.

The solution is (-9,7), which is option A.

A. (-9,7)

This describes the values less than 8 from -1

B.  $(-\infty, -9] \cup [7, \infty)$ 

This describes the values no less than 8 from -1

C. [-9, 7]

This describes the values no more than 8 from -1

D.  $(-\infty, -9) \cup (7, \infty)$ 

This describes the values more than 8 from -1

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{4}{8} - \frac{6}{9}x \ge \frac{-3}{3}x + \frac{7}{6}$$

The solution is  $[2.0, \infty)$ , which is option C.

A.  $[a, \infty)$ , where  $a \in [-2, -1]$ 

 $[-2.0,\infty)$ , which corresponds to negating the endpoint of the solution.

B.  $(-\infty, a]$ , where  $a \in [2, 7]$ 

 $(-\infty, 2.0]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

C.  $[a, \infty)$ , where  $a \in [2, 3]$ 

\*  $[2.0, \infty)$ , which is the correct option.

D.  $(-\infty, a]$ , where  $a \in [-3, -1]$ 

 $(-\infty, -2.0]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-9 + 6x < \frac{56x + 9}{9} \le -7 + 6x$$

The solution is None of the above., which is option E.

A. (a, b], where  $a \in [42, 47]$  and  $b \in [33, 41]$ 

(45.00, 36.00], which is the correct interval but negatives of the actual endpoints.

B.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [42, 49]$  and  $b \in [35, 41]$ 

 $(-\infty, 45.00) \cup [36.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

C. [a, b), where  $a \in [45, 51]$  and  $b \in [36, 39]$ 

[45.00, 36.00), which corresponds to flipping the inequality and getting negatives of the actual endpoints.

D.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [44, 50]$  and  $b \in [34, 39]$ 

 $(-\infty, 45.00] \cup (36.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be (-45.00, -36.00].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-4 + 8x < \frac{76x + 9}{9} \le 9 + 3x$$

The solution is None of the above., which is option E.

A. (a, b], where  $a \in [10.25, 13.25]$  and  $b \in [-1.47, -0.47]$ 

(11.25, -1.47], which is the correct interval but negatives of the actual endpoints.

B. [a, b), where  $a \in [11.25, 13.25]$  and  $b \in [-4.47, -0.47]$ 

[11.25, -1.47), which corresponds to flipping the inequality and getting negatives of the actual endpoints.

C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [9.25, 19.25]$  and  $b \in [-4.47, 0.53]$ 

 $(-\infty, 11.25] \cup (-1.47, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [10.25, 13.25]$  and  $b \in [-3.47, -0.47]$ 

 $(-\infty, 11.25) \cup [-1.47, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be (-11.25, 1.47].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6 + 3x > 5x$$
 or  $-5 + 3x < 6x$ 

The solution is  $(-\infty, -3.0)$  or  $(-1.667, \infty)$ , which is option B.

A. 
$$(-\infty, a] \cup [b, \infty)$$
, where  $a \in [-5, 0]$  and  $b \in [-6.67, -0.67]$ 

Corresponds to including the endpoints (when they should be excluded).

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-5, -1]$  and  $b \in [-4.67, 0.33]$ 
  - \* Correct option.
- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-0.33, 5.67]$  and  $b \in [-1, 6]$

Corresponds to inverting the inequality and negating the solution.

D. 
$$(-\infty, a] \cup [b, \infty)$$
, where  $a \in [-2.33, 2.67]$  and  $b \in [3, 5]$ 

Corresponds to including the endpoints AND negating.

E. 
$$(-\infty, \infty)$$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{5}{9} - \frac{6}{4}x < \frac{-5}{8}x - \frac{4}{5}$$

The solution is  $(1.549, \infty)$ , which is option D.

- A.  $(a, \infty)$ , where  $a \in [-1.55, 1.45]$ 
  - $(-1.549, \infty)$ , which corresponds to negating the endpoint of the solution.
- B.  $(-\infty, a)$ , where  $a \in [-4.55, 0.45]$

 $(-\infty, -1.549)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

C.  $(-\infty, a)$ , where  $a \in [0.55, 4.55]$ 

 $(-\infty, 1.549)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $(a, \infty)$ , where  $a \in [0.55, 3.55]$ 
  - \*  $(1.549, \infty)$ , which is the correct option.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.