**This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.**

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

---

1. Determine the appropriate model for the graph of points below.
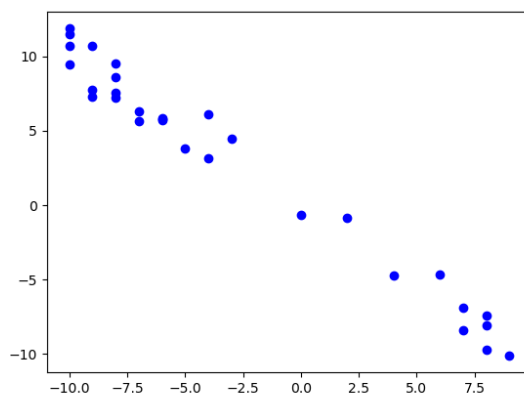
The solution is Linear model, which is option A.

   A. Linear model

   For this to be the correct option, we need to see a mostly straight line of points.

   B. Exponential model

   For this to be the correct option, we want an extremely slow change early, then a rapid change later.

   C. Logarithmic model

   For this to be the correct option, we want a rapid change early, then an extremely slow change later.

   D. Non-linear Power model

   For this to be the correct option, we need to see a polynomial or rational shape.

   E. None of the above

   For this to be the correct option, we want to see no pattern in the points.

   General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

---

2. Solve the modeling problem below, if possible.

   In CHM2045L, Brittany created a 15 liter 19 percent solution of chemical χ using two different solution percentages of chemical χ. When she went to write her lab report, she realized she forgot to

write the amount of each solution she used! If she remembers she used 16 percent and 26 percent solutions, what was the amount she used of the 26 percent solution?

The solution is 4.50, which is option D.

A. 7.50

This would be correct if Brittany used equal parts of each solution.

B. 10.50

This is the concentration of 16 percent solution.

C. 5.54

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

D. 4.50

*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

---

3. Determine the appropriate model for the graph of points below.
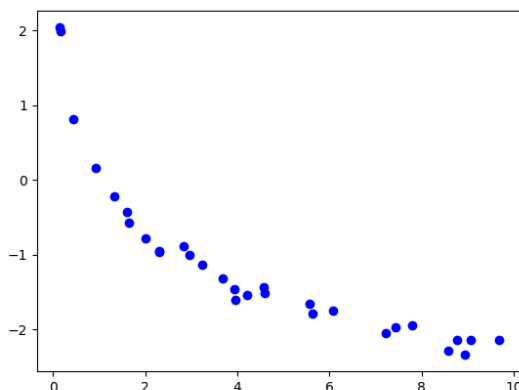
The solution is Logarithmic model, which is option D.

A. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

B. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

C. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

D. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

---

4. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 7 many cases reported, but the number of confirmed cases has doubled every 5 days. How long will it be until there are at least 100000 confirmed cases?

The solution is About 70 days, which is option C.

A. About 22 days

You modeled the situation correctly but did not apply the properties of log correctly.

B. About 48 days

You modeled the situation with e as the base, but solved correctly otherwise.

C. About 70 days

* This is the correct option.

D. About 20 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 100000 and solve for d in your model.

---

5. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 36 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 11 percent, which is option D.

A. About 3 percent

This corresponds to not solving for the increase properly.

B. About 17 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

C. About 18 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

D. About 11 percent

   * This is the correct option.

E. None of the above

   If you chose this, please contact the coordinator to discus how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

---

6. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

   The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string ω decreases as the square length of the string increases. For example, when string ω is 4 mm long, the rate of vibration is 20 cm/s.

The solution is $k = 3.20$, which is option D.

A. $k = 125.00$

   This option uses the model $R = kl^2$ as if this is a direct variation.

B. $k = 320.00$

   This option uses the correct model, $R = \dfrac{k}{l^2}$, but does not convert from mm to cm so that the units match.

C. $k = 1.25$

   This option uses the model $R = kl^2$ as if this is a direct variation AND does not convert from mm to cm so that the units match.

D. $k = 3.20$

   * This is the correct option, which corresponds to the model $R = \dfrac{k}{l^2}$ AND converts from mm to cm.

E. None of the above.

   Talk with the coordinator if you chose this option.

General Comment: The most common mistake on this question is to not convert mm to cm! When modeling, you need to make sure all of the units for your variables are compatible.

---

7. Solve the modeling problem below, if possible.

   In CHM2045L, Brittany created a 16 liter 7 percent solution of chemical χ using two different solution percentages of chemical χ. When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 5 percent and 19 percent solutions, what was the amount she used of the 5 percent solution?

The solution is 13.71, which is option C.

A. 2.29

   This is the concentration of 19 percent solution.

B. 8.00

   This would be correct if Brittany used equal parts of each solution.

 C. 13.71

  *This is the correct option.

 D. 10.13

  This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

 E. There is not enough information to solve the problem.

  You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

---

8. Solve the modeling problem below, if possible.

 A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has quadrupled every 4 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 35 days, which is option D.

 A. About 20 days

  You modeled the situation with e as the base and did not apply the properties of log correctly.

 B. About 18 days

  You modeled the situation correctly but did not apply the properties of log correctly.

 C. About 49 days

  You modeled the situation with e as the base, but solved correctly otherwise.

 D. About 35 days

  * This is the correct option.

 E. There is not enough information to solve the problem.

  If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

---

9. The temperature of an object, T, in a different surrounding temperature T_s will behave according to the formula $T(t) = Ae^{kt} + T_s$, where t is minutes, A is a constant, and k is a constant. Use this formula and the situation below to construct a model that describes the uranium's temperature, T, based on the amount of time t (in minutes) that have passed. Choose the correct constant k from the options below.

 Uranium is taken out of the reactor with a temperature of $100°$ C and is placed into a $19°$ C bath to cool. After 38 minutes, the uranium has cooled to $60°$ C.

The solution is $k = -0.01792$, which is option D.

 A. $k = -0.02346$

  This uses A as the initial temperature and solves for k incorrectly.

B. $k = -0.01743$

This uses A as the initial temperature and solves for k correctly.

C. $k = -0.01812$

This uses A correctly but solves for k incorrectly.

D. $k = -0.01792$

* This is the correct option.

E. None of the above

If you chose this, please contact the coordinator to discuss why you believe none of the other answers are correct.

General Comment: The initial temperature is when $t = 0$. Unlike power models, that means A is not the initial temperature!

---

10. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 39 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 12 percent, which is option B.

A. About 18 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

B. About 12 percent

* This is the correct option.

C. About 20 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

D. About 3 percent

This corresponds to not solving for the increase properly.

E. None of the above

If you chose this, please contact the coordinator to discus how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.