This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No less than 2 units from the number 9.

The solution is  $(-\infty, 7] \cup [11, \infty)$ , which is option D.

A. (7,11)

This describes the values less than 2 from 9

B. [7, 11]

This describes the values no more than 2 from 9

C.  $(-\infty, 7) \cup (11, \infty)$ 

This describes the values more than 2 from 9

D.  $(-\infty, 7] \cup [11, \infty)$ 

This describes the values no less than 2 from 9

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

2. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$4x + 5 \le 5x - 8$$

The solution is  $[13.0, \infty)$ , which is option A.

A.  $[a, \infty)$ , where  $a \in [12, 14]$ 

\*  $[13.0, \infty)$ , which is the correct option.

B.  $[a, \infty)$ , where  $a \in [-16, -12]$ 

 $[-13.0, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(-\infty, a]$ , where  $a \in [-15, -12]$ 

 $(-\infty, -13.0]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(-\infty, a]$ , where  $a \in [6, 15]$ 

 $(-\infty, 13.0]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-4 - 6x < \frac{-46x + 8}{8} \le -7 - 8x$$

The solution is (-20.00, -3.56], which is option D.

A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-25.5, -17.25]$  and  $b \in [-5.25, -1.5]$  $(-\infty, -20.00) \cup [-3.56, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

B. [a, b), where  $a \in [-21, -15.75]$  and  $b \in [-4.5, 0.75]$  [-20.00, -3.56), which corresponds to flipping the inequality.

C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-21, -18]$  and  $b \in [-6, -3]$ 

 $(-\infty, -20.00] \cup (-3.56, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

- D. (a, b], where  $a \in [-21.75, -16.5]$  and  $b \in [-6.75, -0.75]$ 
  - \* (-20.00, -3.56], which is the correct option.
- E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6 + 8x \le \frac{26x - 9}{3} < 4 + 4x$$

The solution is [-4.50, 1.50), which is option C.

A.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-9.75, -1.5]$  and  $b \in [-0.75, 5.25]$ 

 $(-\infty, -4.50) \cup [1.50, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

B. (a, b], where  $a \in [-5.25, -0.75]$  and  $b \in [-0.75, 9.75]$ 

(-4.50, 1.50], which corresponds to flipping the inequality.

C. [a, b), where  $a \in [-5.25, -2.25]$  and  $b \in [0.22, 1.72]$ 

[-4.50, 1.50), which is the correct option.

D.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-7.5, -3]$  and  $b \in [1.05, 1.8]$ 

 $(-\infty, -4.50] \cup (1.50, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{9}{8} + \frac{4}{7}x \le \frac{7}{3}x - \frac{3}{4}$$

The solution is  $[1.064, \infty)$ , which is option A.

A.  $[a, \infty)$ , where  $a \in [0, 2.25]$ 

\*  $[1.064, \infty)$ , which is the correct option.

B.  $[a, \infty)$ , where  $a \in [-4.5, 0]$ 

 $[-1.064, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(-\infty, a]$ , where  $a \in [-4.5, 0.75]$ 

 $(-\infty, -1.064]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(-\infty, a]$ , where  $a \in [0.75, 2.25]$ 

 $(-\infty, 1.064]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 3x > 5x$$
 or  $7 + 5x < 8x$ 

The solution is  $(-\infty, -3.5)$  or  $(2.333, \infty)$ , which is option B.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-4.65, -2.4]$  and  $b \in [1.95, 2.48]$ 

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-3.96, -3.48]$  and  $b \in [1.74, 3.01]$ 

\* Correct option.

C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2.75, -2.24]$  and  $b \in [3.05, 4.35]$ 

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-3, -1.12]$  and  $b \in [3.15, 5.77]$ 

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-8}{7} - \frac{5}{8}x \le \frac{5}{6}x + \frac{8}{9}$$

The solution is  $[-1.393, \infty)$ , which is option C.

A.  $(-\infty, a]$ , where  $a \in [0, 4.5]$ 

 $(-\infty, 1.393]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

B.  $[a, \infty)$ , where  $a \in [0.75, 2.25]$ 

 $[1.393, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [-2.25, 0.75]$ 

\*  $[-1.393, \infty)$ , which is the correct option.

D.  $(-\infty, a]$ , where  $a \in [-2.25, 0.75]$ 

 $(-\infty, -1.393]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 - 3x > 4x$$
 or  $6 + 9x < 10x$ 

The solution is  $(-\infty, -1.0)$  or  $(6.0, \infty)$ , which is option B.

A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-8.25, -4.5]$  and  $b \in [-0.75, 3.75]$ 

Corresponds to inverting the inequality and negating the solution.

B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-3.75, 0]$  and  $b \in [1.5, 8.25]$ 

\* Correct option.

C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-9.75, -3]$  and  $b \in [0, 4.5]$ 

Corresponds to including the endpoints AND negating.

D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-5.25, 2.25]$  and  $b \in [3.75, 9]$ 

Corresponds to including the endpoints (when they should be excluded).

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

9. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 5 units from the number 4.

The solution is [-1, 9], which is option A.

A. [-1, 9]

This describes the values no more than 5 from 4

B. (-1,9)

This describes the values less than 5 from 4

C.  $(-\infty, -1) \cup (9, \infty)$ 

This describes the values more than 5 from 4

D.  $(-\infty, -1] \cup [9, \infty)$ 

This describes the values no less than 5 from 4

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8x - 3 < 5x + 4$$

The solution is  $[-0.538, \infty)$ , which is option B.

A.  $[a, \infty)$ , where  $a \in [0.06, 1.26]$ 

 $[0.538, \infty)$ , which corresponds to negating the endpoint of the solution.

B.  $[a, \infty)$ , where  $a \in [-1.23, -0.26]$ 

\*  $[-0.538, \infty)$ , which is the correct option.

C.  $(-\infty, a]$ , where  $a \in [-1.54, 0.46]$ 

 $(-\infty, -0.538]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D.  $(-\infty, a]$ , where  $a \in [-0.46, 5.54]$ 

 $(-\infty, 0.538]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.