This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$ to find the coefficient for the model of the new volume $V_{\text{new}} = kr^2 h$.

Pepsi wants to increase the volume of soda in their cans. They've decided to increase the radius by 11 percent and increase the height by 18 percent. They want to model the new volume based on the radius and height of the original cans.

The solution is k = 4.56749, which is option B.

A. k = 0.00684

This corresponds to the model: $V = \pi (0.11r)^2 (0.18h)$.

B. k = 4.56749

* This is the correct option and corresponds to the model: $V = \pi (1.11r)^2 (1.18h)$.

C. k = 1.45388

This corresponds to the model: $V = (1.11r)^2(1.18h)$.

D. k = 0.00218

This corresponds to the model: $V = (0.11r)^2(0.18h)$.

E. None of the above.

If you chose this, please talk with the coordinator to discuss why you believe none of the options are correct.

General Comment: When calculating the new dimensions, you need to add/subtract from 100%. For example, a 10% increase in height would result in 110% of the original height: $1.1h_{old} = h_{new}$.

2. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string ω increases as the quartic length of the string decreases. For example, when string ω is 3 mm long, the rate of vibration is 24 cm/s.

The solution is k = 0.19, which is option C.

A. k = 1944.00

This option uses the correct model, $R = \frac{k}{l^4}$, but does not convert from mm to cm so that the units match.

B. k = 0.30

This option uses the model $R = kl^4$ as if this is a direct variation AND does not convert from mm to cm so that the units match.

C. k = 0.19

* This is the correct option, which corresponds to the model $R = \frac{k}{l^4}$ AND converts from mm to cm.

D. k = 2962.96

This option uses the model $R = kl^4$ as if this is a direct variation.

E. None of the above.

Talk with the coordinator if you chose this option.

General Comment: The most common mistake on this question is to not convert mm to cm! When modeling, you need to make sure all of the units for your variables are compatible.

3. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string ω increases as the square length of the string decreases. For example, when string ω is 3 mm long, the rate of vibration is 36 cm/s.

The solution is k = 3.24, which is option A.

A. k = 3.24

* This is the correct option, which corresponds to the model $R = \frac{k}{l^2}$ AND converts from mm to cm.

B. k = 324.00

This option uses the correct model, $R = \frac{k}{l^2}$, but does not convert from mm to cm so that the units match.

C. k = 400.00

This option uses the model $R = kl^2$ as if this is a direct variation.

D. k = 4.00

This option uses the model $R = kl^2$ as if this is a direct variation AND does not convert from mm to cm so that the units match.

E. None of the above.

Talk with the coordinator if you chose this option.

General Comment: The most common mistake on this question is to not convert mm to cm! When modeling, you need to make sure all of the units for your variables are compatible.

4. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$ to find the coefficient for the model of the new volume $V_{\text{new}} = kr^2 h$.

Pepsi wants to increase the volume of soda in their cans. They've decided to increase the radius by 18 percent and increase the height by 13 percent. They want to model the new volume based on the radius and height of the original cans.

The solution is k = 4.94302, which is option D.

A. k = 1.57341

This corresponds to the model: $V = (1.18r)^2(1.13h)$.

B. k = 0.00421

This corresponds to the model: $V = (0.18r)^2(0.13h)$.

C. k = 0.01323

This corresponds to the model: $V = \pi (0.18r)^2 (0.13h)$.

D. k = 4.94302

* This is the correct option and corresponds to the model: $V = \pi (1.18r)^2 (1.13h)$.

E. None of the above.

If you chose this, please talk with the coordinator to discuss why you believe none of the options are correct.

General Comment: When calculating the new dimensions, you need to add/subtract from 100%. For example, a 10% increase in height would result in 110% of the original height: $1.1h_{old} = h_{new}$.

5. A town has an initial population of 100000. The town's population for the next 9 years is provided below. Which type of function would be most appropriate to model the town's population?

$\mathbf{Y}\mathbf{e}\mathbf{a}\mathbf{r}$	1	2	3	4	5	6	7	8	9	The solution is Exponential, which
Pop	99800	99200	96800	87200	48800	0	0	0	0	-The solution is Exponential, which
is option	'nВ.									

A. Non-Linear Power

This suggests a growth faster than constant but slower than exponential.

B. Exponential

This suggests the fastest of growths that we know.

C. Logarithmic

This suggests the slowest of growths that we know.

D. Linear

This suggests a constant growth. You would be able to add or subtract the same amount year-to-year if this is the correct answer.

E. None of the above

Please contact the coordinator to discuss why you believe none of the options model the population.

General Comment: We are trying to compare the growth rate of the population. Growth rates can be characterized from slowest to fastest as: logarithmic, indirect, linear, direct, exponential. The best way to approach this is to first compare it to linear (is it linear, faster than linear, or slower than linear)? If faster, is it as fast as exponential? If slower, is it as slow as logarithmic?

6. A town has an initial population of 80000. The town's population for the next 9 years is provided below. Which type of function would be most appropriate to model the town's population?

Year	1	2	3	4	5	6	7	8	9	-The solution is Linear,
Pop	80030	80060	80090	80120	80150	80180	80210	80240	80270	
Year 1 2 3 4 5 6 7 8 9 The solution is Linear, Pop 80030 80060 80090 80120 80150 80180 80210 80240 80270 The solution is Linear, which is option C.										

A. Non-Linear Power

This suggests a growth faster than constant but slower than exponential.

B. Exponential

This suggests the fastest of growths that we know.

C. Linear

This suggests a constant growth. You would be able to add or subtract the same amount year-to-year if this is the correct answer.

D. Logarithmic

This suggests the slowest of growths that we know.

E. None of the above

Please contact the coordinator to discuss why you believe none of the options model the population.

General Comment: We are trying to compare the growth rate of the population. Growth rates can be characterized from slowest to fastest as: logarithmic, indirect, linear, direct, exponential. The best way to approach this is to first compare it to linear (is it linear, faster than linear, or slower than linear)? If faster, is it as fast as exponential? If slower, is it as slow as logarithmic?

7. Choose the model type that would best describe the scenario below.

Big O notation is common in computer science to describe how fast a program can solve a particular problem. Big O notation categorizes functions according to their growth rates, the same way we have categorized modeling real-world problems by certain types of functions. When analyzing a particular program, a student found the computer to need x^x time to complete, where x was the number of inputs into the program.

The solution is None of the above, which is option D.

- A. Direct variation
- B. Joint variation
- C. Indirect variation
- D. None of the above

General Comment: We have been modeling real-world problems according to the growth rates of functions. So far, we've seen logarithmics to be the slowest, then power functions, then exponentials as the fastest. But, there are far more types of functions than the ones we've looked at! One such function is x^x , also known as a power tower. This function class grows significantly faster than exponentials. Remember for power variation, we need the exponent to be a constant.

8. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the square of the time, T (Earth years), required for a planet to orbit $Sun \chi$ decreases as the square of the distance, d (AUs), that the planet is from $Sun \chi$ decreases. For example, when Ea's average distance from $Sun \chi$ is 3, it takes 70 Earth days to complete an orbit.

The solution is k = 544.444, which is option A.

A. k = 544.444

* This is the correct option corresponding to the model $T^2 = kd^2$.

B. k = 44100.000

This corresponds to the model $T^2 = \frac{k}{d^2}$.

C. k = 4.830

This corresponds to the model $T^{1/2} = kd^{1/2}$.

D. k = 4.028

This copies the constant used in the homework.

E. Unable to compute the constant based on the information given.

This corresponds to believing you cannot determine the type of model from the information given.

General Comment: Since T decreases proportionally as d decreases, we know this is a direct variation model.

9. Choose the model type that would best describe the scenario below.

Big O notation is common in computer science to describe how fast a program can solve a particular problem. Big O notation categorizes functions according to their growth rates, the same way we have categorized modeling real-world problems by certain types of functions. When analyzing a particular program, a student found the computer to need x^x time to complete, where x was the number of inputs into the program.

The solution is None of the above, which is option D.

- A. Direct variation
- B. Indirect variation
- C. Joint variation
- D. None of the above

General Comment: We have been modeling real-world problems according to the growth rates of functions. So far, we've seen logarithmics to be the slowest, then power functions, then exponentials as the fastest. But, there are far more types of functions than the ones we've looked at! One such function is x^x , also known as a power tower. This function class grows significantly faster than exponentials. Remember for power variation, we need the exponent to be a constant.

10. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the cube of the time, T (Earth years), required for a planet to orbit $Sun \chi$ increases as the quartic of the distance, d (AUs), that the planet is from $Sun \chi$ increases. For example, when Ea's average distance from $Sun \chi$ is 9, it takes 64 Earth days to complete an orbit.

The solution is k = 39.955, which is option B.

A. k = 1719926784.000

This corresponds to the model $T^3 = \frac{k}{d^4}$.

B. k = 39.955

* This is the correct option corresponding to the model $T^3 = kd^4$.

C. k = 2.309

This corresponds to the model $T^{1/3} = kd^{1/4}$.

D. k = 4.028

This copies the constant used in the homework.

E. Unable to compute the constant based on the information given.

This corresponds to believing you cannot determine the type of model from the information given.

General Comment: Since T increases proportionally as d increases, we know this is a direct variation model.