

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

1. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 6x^2 + x + 6 \text{ and } g(x) = \sqrt{4x + 25}$$

The solution is The domain is all Real numbers greater than or equal to  $x = -6.25$ , which is option B.

- A. The domain is all Real numbers except  $x = a$ , where  $a \in [2.4, 11.4]$
- B. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-9.25, -4.25]$
- C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-2.5, 10.5]$
- D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [5.67, 11.67]$  and  $b \in [-7.83, -0.83]$
- E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

2. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = 3x^3 + 2x^2 - x - 4 \text{ and } g(x) = 2x^3 - 4x^2 + 2x + 2$$

The solution is 26.0, which is option D.

- A.  $(f \circ g)(1) \in [34, 39]$   
Distractor 2: Corresponds to being slightly off from the solution.
- B.  $(f \circ g)(1) \in [2, 4]$   
Distractor 1: Corresponds to reversing the composition.
- C.  $(f \circ g)(1) \in [8, 18]$   
Distractor 3: Corresponds to being slightly off from the solution.
- D.  $(f \circ g)(1) \in [21, 31]$   
\* This is the correct solution
- E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

3. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = 2x^3 + 3x^2 - 2x \text{ and } g(x) = -3x^3 - 3x^2 + 4x$$

The solution is 0.0, which is option C.

A.  $(f \circ g)(1) \in [1, 11]$

Distractor 2: Corresponds to being slightly off from the solution.

B.  $(f \circ g)(1) \in [-109, -103]$

Distractor 3: Corresponds to being slightly off from the solution.

C.  $(f \circ g)(1) \in [-1, 1]$

\* This is the correct solution

D.  $(f \circ g)(1) \in [-102, -90]$

Distractor 1: Corresponds to reversing the composition.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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4. Find the inverse of the function below. Then, evaluate the inverse at  $x = 6$  and choose the interval that  $f^{-1}(6)$  belongs to.

$$f(x) = \ln(x + 4) + 4$$

The solution is  $f^{-1}(6) = 3.389$ , which is option A.

A.  $f^{-1}(6) \in [1.39, 5.39]$

This is the solution.

B.  $f^{-1}(6) \in [22019.47, 22024.47]$

This solution corresponds to distractor 1.

C.  $f^{-1}(6) \in [9.39, 14.39]$

This solution corresponds to distractor 2.

D.  $f^{-1}(6) \in [22029.47, 22035.47]$

This solution corresponds to distractor 4.

E.  $f^{-1}(6) \in [9.39, 14.39]$

This solution corresponds to distractor 3.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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5. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = 15$  and choose the interval that  $f^{-1}(15)$  belongs to.

$$f(x) = 2x^2 - 3$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A.  $f^{-1}(15) \in [5.93, 6.5]$

Distractor 4: This corresponds to both distractors 2 and 3.

B.  $f^{-1}(15) \in [2.58, 3.53]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

C.  $f^{-1}(15) \in [4.86, 5.77]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

D.  $f^{-1}(15) \in [2.06, 2.97]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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6. Find the inverse of the function below. Then, evaluate the inverse at  $x = 8$  and choose the interval that  $f^{-1}(8)$  belongs to.

$$f(x) = e^{x-5} - 2$$

The solution is  $f^{-1}(8) = 7.303$ , which is option D.

A.  $f^{-1}(8) \in [-0.01, 1.1]$

This solution corresponds to distractor 3.

B.  $f^{-1}(8) \in [-3.28, -2.68]$

This solution corresponds to distractor 1.

C.  $f^{-1}(8) \in [-2.24, -0.83]$

This solution corresponds to distractor 4.

D.  $f^{-1}(8) \in [7.11, 8.12]$

This is the solution.

E.  $f^{-1}(8) \in [-0.33, 0.41]$

This solution corresponds to distractor 2.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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7. Determine whether the function below is 1-1.

$$f(x) = 36x^2 - 204x + 289$$

The solution is no, which is option C.

A. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

B. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

C. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

D. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

E. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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8. Determine whether the function below is 1-1.

$$f(x) = 9x^2 - 21x - 228$$

The solution is no, which is option B.

- A. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

- B. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

- C. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

- D. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- E. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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9. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \sqrt{-6x + 22} \text{ and } g(x) = 8x + 3$$

The solution is The domain is all Real numbers less than or equal to  $x = 3.67$ ., which is option C.

- A. The domain is all Real numbers except  $x = a$ , where  $a \in [-4.4, 2.6]$

- B. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [4.25, 6.25]$

- C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [1.67, 4.67]$

- D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-5.83, -0.83]$  and  $b \in [4.83, 12.83]$

- E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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10. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = 15$  and choose the interval that  $f^{-1}(15)$  belongs to.

$$f(x) = \sqrt[3]{5x - 2}$$

The solution is 675.4, which is option B.

- A.  $f^{-1}(15) \in [-675.69, -675.24]$

This solution corresponds to distractor 2.

B.  $f^{-1}(15) \in [675.16, 675.65]$

\* This is the correct solution.

C.  $f^{-1}(15) \in [673.87, 674.67]$

Distractor 1: This corresponds to

D.  $f^{-1}(15) \in [-675.01, -674.59]$

This solution corresponds to distractor 3.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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11. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 4x^2 + 4x + 4 \text{ and } g(x) = 5x^2 + 8x + 2$$

The solution is  $(-\infty, \infty)$ , which is option E.

A. The domain is all Real numbers except  $x = a$ , where  $a \in [-12.67, -3.67]$

B. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [0.25, 6.25]$

C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-5.4, 0.6]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [3.67, 9.67]$  and  $b \in [-4.33, 0.67]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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12. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = -x^3 - 2x^2 + x \text{ and } g(x) = -4x^3 - 4x^2 + 4x + 3$$

The solution is  $-2.0$ , which is option A.

A.  $(f \circ g)(1) \in [-3.2, 0.5]$

\* This is the correct solution

B.  $(f \circ g)(1) \in [9.5, 11.2]$

Distractor 1: Corresponds to reversing the composition.

C.  $(f \circ g)(1) \in [4.5, 8]$

Distractor 3: Corresponds to being slightly off from the solution.

D.  $(f \circ g)(1) \in [2.6, 4.9]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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13. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = -3x^3 + 4x^2 + 4x \text{ and } g(x) = x^3 - 1x^2 - 3x + 1$$

The solution is 32.0, which is option B.

A.  $(f \circ g)(1) \in [81, 89]$

Distractor 1: Corresponds to reversing the composition.

B.  $(f \circ g)(1) \in [28, 36]$

\* This is the correct solution

C.  $(f \circ g)(1) \in [35, 42]$

Distractor 2: Corresponds to being slightly off from the solution.

D.  $(f \circ g)(1) \in [88, 96]$

Distractor 3: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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14. Find the inverse of the function below. Then, evaluate the inverse at  $x = 7$  and choose the interval that  $f^{-1}(7)$  belongs to.

$$f(x) = e^{x-2} - 2$$

The solution is  $f^{-1}(7) = 4.197$ , which is option E.

A.  $f^{-1}(7) \in [-1.06, 0.03]$

This solution corresponds to distractor 4.

B.  $f^{-1}(7) \in [-0.08, 0.39]$

This solution corresponds to distractor 1.

C.  $f^{-1}(7) \in [-1.06, 0.03]$

This solution corresponds to distractor 2.

D.  $f^{-1}(7) \in [-0.08, 0.39]$

This solution corresponds to distractor 3.

E.  $f^{-1}(7) \in [3.32, 4.75]$

This is the solution.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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15. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -12$  and choose the interval that  $f^{-1}(-12)$  belongs to.

$$f(x) = \sqrt[3]{2x - 5}$$

The solution is  $-861.5$ , which is option A.

A.  $f^{-1}(-12) \in [-863.5, -860.5]$

\* This is the correct solution.

B.  $f^{-1}(-12) \in [-866.5, -865.5]$

Distractor 1: This corresponds to

C.  $f^{-1}(-12) \in [866.5, 870.5]$

This solution corresponds to distractor 3.

D.  $f^{-1}(-12) \in [855.5, 862.5]$

This solution corresponds to distractor 2.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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16. Find the inverse of the function below. Then, evaluate the inverse at  $x = 9$  and choose the interval that  $f^{-1}(9)$  belongs to.

$$f(x) = e^{x-5} + 2$$

The solution is  $f^{-1}(9) = 6.946$ , which is option A.

A.  $f^{-1}(9) \in [6.88, 7.09]$

This is the solution.

B.  $f^{-1}(9) \in [-3.15, -2.83]$

This solution corresponds to distractor 1.

C.  $f^{-1}(9) \in [4.54, 4.85]$

This solution corresponds to distractor 3.

D.  $f^{-1}(9) \in [4.28, 4.42]$

This solution corresponds to distractor 2.

E.  $f^{-1}(9) \in [3.38, 3.42]$

This solution corresponds to distractor 4.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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17. Determine whether the function below is 1-1.

$$f(x) = 25x^2 - 90x - 319$$

The solution is no, which is option C.

A. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

B. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

C. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

D. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

E. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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18. Determine whether the function below is 1-1.

$$f(x) = 9x^2 - 60x + 100$$

The solution is no, which is option A.

A. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

B. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

D. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

E. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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19. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{5}{3x - 20} \text{ and } g(x) = 7x + 3$$

The solution is The domain is all Real numbers except  $x = 6.67$ , which is option C.

A. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-7.4, 3.6]$

B. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [2, 4]$

C. The domain is all Real numbers except  $x = a$ , where  $a \in [5.67, 7.67]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-0.33, 8.67]$  and  $b \in [2.83, 11.83]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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20. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = 14$  and choose the interval that  $f^{-1}(14)$  belongs to.

$$f(x) = 5x^2 - 4$$

The solution is The function is not invertible for all Real numbers. , which is option E.



A.  $f^{-1}(14) \in [2.69, 3.04]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

B.  $f^{-1}(14) \in [5.7, 5.94]$

Distractor 4: This corresponds to both distractors 2 and 3.

C.  $f^{-1}(14) \in [0.88, 1.83]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

D.  $f^{-1}(14) \in [1.81, 2.14]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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21. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 4x^3 + x^2 + 5x + 3 \text{ and } g(x) = \frac{4}{6x + 19}$$

The solution is The domain is all Real numbers except  $x = -3.17$ , which is option A.

A. The domain is all Real numbers except  $x = a$ , where  $a \in [-3.17, 2.83]$

B. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-10.2, -0.2]$

C. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-13.5, -6.5]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-6.6, -5.6]$  and  $b \in [-7.33, -3.33]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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22. Choose the interval below that  $f$  composed with  $g$  at  $x = -1$  is in.

$$f(x) = 2x^3 - 3x^2 - 4x - 1 \text{ and } g(x) = 3x^3 - 1x^2 - 3x + 3$$

The solution is  $-5.0$ , which is option A.

A.  $(f \circ g)(-1) \in [-9, -3]$

\* This is the correct solution

B.  $(f \circ g)(-1) \in [0, 4]$

Distractor 2: Corresponds to being slightly off from the solution.

C.  $(f \circ g)(-1) \in [-21, -12]$

Distractor 1: Corresponds to reversing the composition.

D.  $(f \circ g)(-1) \in [-29, -26]$

Distractor 3: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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23. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = 4x^3 - 1x^2 - 2x \text{ and } g(x) = x^3 + x^2 - x + 2$$

The solution is 93.0, which is option A.

A.  $(f \circ g)(1) \in [88, 97]$

\* This is the correct solution

B.  $(f \circ g)(1) \in [-5, -4]$

Distractor 3: Corresponds to being slightly off from the solution.

C.  $(f \circ g)(1) \in [2, 6]$

Distractor 1: Corresponds to reversing the composition.

D.  $(f \circ g)(1) \in [100, 103]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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24. Find the inverse of the function below. Then, evaluate the inverse at  $x = 8$  and choose the interval that  $f^{-1}(8)$  belongs to.

$$f(x) = e^{x-4} - 4$$

The solution is  $f^{-1}(8) = 6.485$ , which is option C.

A.  $f^{-1}(8) \in [-4.61, -1.61]$

This solution corresponds to distractor 4.

B.  $f^{-1}(8) \in [-1.52, -0.52]$

This solution corresponds to distractor 1.

C.  $f^{-1}(8) \in [1.48, 11.48]$

This is the solution.

D.  $f^{-1}(8) \in [-4.61, -1.61]$

This solution corresponds to distractor 2.

E.  $f^{-1}(8) \in [-1.52, -0.52]$

This solution corresponds to distractor 3.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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25. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -13$  and choose the interval that  $f^{-1}(-13)$  belongs to.

$$f(x) = 4x^2 - 3$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A.  $f^{-1}(-13) \in [2.52, 3.29]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

B.  $f^{-1}(-13) \in [3.81, 4.71]$

Distractor 4: This corresponds to both distractors 2 and 3.

C.  $f^{-1}(-13) \in [1.81, 2.5]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

D.  $f^{-1}(-13) \in [1.15, 1.95]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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26. Find the inverse of the function below. Then, evaluate the inverse at  $x = 9$  and choose the interval that  $f^{-1}(9)$  belongs to.

$$f(x) = e^{x+5} - 2$$

The solution is  $f^{-1}(9) = -2.602$ , which is option E.

A.  $f^{-1}(9) \in [-0.77, -0.59]$

This solution corresponds to distractor 3.

B.  $f^{-1}(9) \in [7.29, 7.8]$

This solution corresponds to distractor 1.

C.  $f^{-1}(9) \in [0.07, 0.74]$

This solution corresponds to distractor 4.

D.  $f^{-1}(9) \in [-0.08, 0.22]$

This solution corresponds to distractor 2.

E.  $f^{-1}(9) \in [-2.69, -2.51]$

This is the solution.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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27. Determine whether the function below is 1-1.

$$f(x) = 9x^2 - 60x + 100$$

The solution is no, which is option E.

A. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

B. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

D. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

E. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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28. Determine whether the function below is 1-1.

$$f(x) = (3x - 18)^3$$

The solution is yes, which is option B.

A. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

B. Yes, the function is 1-1.

\* This is the solution.

C. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

Corresponds to the Horizontal Line test, which this function passes.

D. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

E. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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29. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{2}{3x - 13} \text{ and } g(x) = \frac{2}{3x - 19}$$

The solution is The domain is all Real numbers except  $x = 4.33$  and  $x = 6.33$ , which is option D.

A. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-4.17, -2.17]$

B. The domain is all Real numbers except  $x = a$ , where  $a \in [-8.8, -1.8]$

C. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [3.33, 10.33]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [2.33, 8.33]$  and  $b \in [4.33, 10.33]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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30. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -12$  and choose the interval that  $f^{-1}(-12)$  belongs to.

$$f(x) = 4x^2 - 3$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A.  $f^{-1}(-12) \in [1.56, 2.12]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

B.  $f^{-1}(-12) \in [4.48, 4.58]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

C.  $f^{-1}(-12) \in [7.34, 7.65]$

Distractor 4: This corresponds to both distractors 2 and 3.

D.  $f^{-1}(-12) \in [1.37, 1.68]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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