

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 31 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 9 percent, which is option A.

- A. About 9 percent

* This is the correct option.

- B. About 3 percent

This corresponds to not solving for the increase properly.

- C. About 16 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

- D. About 14 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

- E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

2. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has doubled every 3 days. How long will it be until there are at least 100000 confirmed cases?

The solution is About 43 days, which is option A.

- A. About 43 days

* This is the correct option.

- B. About 14 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

- C. About 30 days

You modeled the situation with e as the base, but solved correctly otherwise.

D. About 15 days

You modeled the situation correctly but did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 100000 and solve for d in your model.

3. The temperature of an object, T , in a different surrounding temperature T_s will behave according to the formula $T(t) = Ae^{kt} + T_s$, where t is minutes, A is a constant, and k is a constant. Use this formula and the situation below to construct a model that describes the uranium's temperature, T , based on the amount of time t (in minutes) that have passed. Choose the correct constant k from the options below.

Uranium is taken out of the reactor with a temperature of 190°C and is placed into a 15°C bath to cool. After 28 minutes, the uranium has cooled to 130°C .

The solution is None of the above, which is option E.

A. $k = -0.01793$

This uses A as the initial temperature and solves for k correctly.

B. $k = -0.02749$

This uses A correctly and solves for k incorrectly.

C. $k = -0.04570$

This uses A as the bath temperature and solves for k incorrectly.

D. $k = -0.02713$

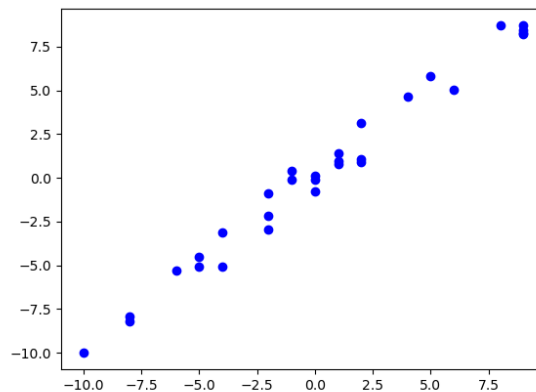
This uses A as the initial temperature and solves for k incorrectly.

E. None of the above

* This is the correct answer as $k = -0.01499$.

General Comment: The initial temperature is when $t = 0$. Unlike power models, that means A is not the initial temperature!

4. Determine the appropriate model for the graph of points below.



The solution is Linear model, which is option D.

A. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

B. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

D. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

5. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 38 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 11 percent, which is option A.

A. About 11 percent

* This is the correct option.

B. About 19 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

C. About 3 percent

This corresponds to not solving for the increase properly.

D. About 17 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

6. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 29 liter 23 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 19 percent and 43 percent solutions, what was the amount she used of the 43 percent solution?

The solution is 4.83liters, which is option C.

A. 20.16liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 14.50liters

This would be correct if Brittany used equal parts of each solution.

C. 4.83liters

*This is the correct option.

D. 24.17liters

This is the concentration of 19 percent solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

7. Using the situation below, construct a linear model that describes the cost of the coffee beans $C(h)$ in terms of the weight of the high-quality coffee beans h .

Veronica needs to prepare 210 of blended coffee beans selling for \$5.34 per pound. She has a high-quality bean that sells for \$6.02 a pound and a low-quality bean that sells for \$4.47 a pound.

The solution is $C(h) = 1.55h + 938.70$, which is option B.

A. $C(h) = 6.02h$

This models the cost of the high-quality bean only, not the blended beans.

B. $C(h) = 1.55h + 938.70$

* This is the correct option since the questions asked you to construct the cost model in terms of the weight of the high-quality bean.

C. $C(h) = -1.55h + 1264.20$

This would be correct if the question asked you to construct the cost model in terms of the weight of the low-quality bean.

D. $C(h) = 5.24h$

This assumes that exactly half of the high- and low- quality beans are mixed to create the blended coffee beans.

E. None of the above.

If you chose this option, please talk to the coordinator to discuss why.

General Comment: This is exactly like the chemistry mixture question from the homework! If you are having trouble with this problem, be sure to review the video for building linear models.

8. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 27 liter 31 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 16 percent and 40 percent solutions, what was the amount she used of the 40 percent solution?

The solution is 16.88liters, which is option C.

A. 10.12liters

This is the concentration of 16 percent solution.

B. 13.50liters

This would be correct if Brittany used equal parts of each solution.

C. 16.88liters

*This is the correct option.

D. 15.73liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

9. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 3 many cases reported, but the number of confirmed cases has quadrupled every 4 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 37 days, which is option C.

A. About 51 days

You modeled the situation with e as the base, but solved correctly otherwise.

B. About 23 days

You modeled the situation correctly but did not apply the properties of log correctly.

C. About 37 days

* This is the correct option.

D. About 27 days

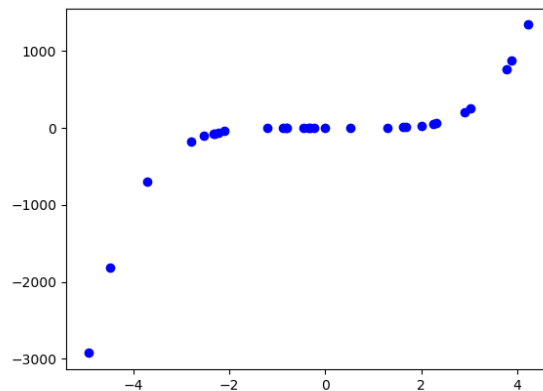
You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

10. Determine the appropriate model for the graph of points below.



The solution is Non-linear Power model, which is option A.

A. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

B. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

D. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

11. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 33 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 10 percent, which is option B.

- A. About 15 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

- B. About 10 percent

* This is the correct option.

- C. About 11 percent

This corresponds to not solving for the increase properly.

- D. About 16 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

- E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

12. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 4 many cases reported, but the number of confirmed cases has doubled every 1 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 12 days, which is option C.

- A. About 4 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

- B. About 5 days

You modeled the situation correctly but did not apply the properties of log correctly.

- C. About 12 days

* This is the correct option.

- D. About 8 days

You modeled the situation with e as the base, but solved correctly otherwise.

- E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

13. The temperature of an object, T , in a different surrounding temperature T_s will behave according to the formula $T(t) = Ae^{kt} + T_s$, where t is minutes, A is a constant, and k is a constant. Use this formula and the situation below to construct a model that describes the uranium's temperature, T , based on the amount of time t (in minutes) that have passed. Choose the correct constant k from the options below.

Uranium is taken out of the reactor with a temperature of 120°C and is placed into a 13°C bath to cool. After 18 minutes, the uranium has cooled to 60°C .

The solution is $k = -0.04570$, which is option C.

- A. $k = -0.03696$

This uses A as the initial temperature and solves for k incorrectly.

- B. $k = -0.05207$

This uses A as the initial temperature and solves for k correctly.

- C. $k = -0.04570$

* This is the correct option.

- D. $k = -0.03771$

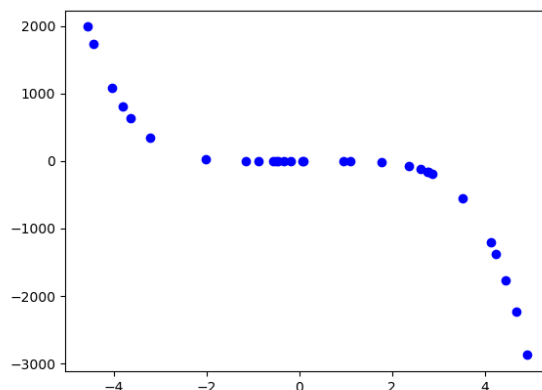
This uses A correctly but solves for k incorrectly.

- E. None of the above

If you chose this, please contact the coordinator to discuss why you believe none of the other answers are correct.

General Comment: The initial temperature is when $t = 0$. Unlike power models, that means A is not the initial temperature!

14. Determine the appropriate model for the graph of points below.



The solution is Non-linear Power model, which is option D.

- A. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

B. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

C. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

D. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

15. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 49 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 14 percent, which is option D.

A. About 22 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

B. About 24 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

C. About 4 percent

This corresponds to not solving for the increase properly.

D. About 14 percent

* This is the correct option.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

16. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 29 liter 23 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 17 percent and 33 percent solutions, what was the amount she used of the 17 percent solution?

The solution is 18.12liters, which is option D.

A. 14.50*liters*

This would be correct if Brittany used equal parts of each solution.

B. 13.10*liters*

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

C. 10.88*liters*

This is the concentration of 33 percent solution.

D. 18.12*liters*

*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

17. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$ to find the coefficient for the model of the new volume $V_{\text{new}} = k r^2 h$.

Pepsi wants to increase the volume of soda in their cans. They've decided to decrease the radius by 20 percent and increase the height by 16 percent. They want to model the new volume based on the radius and height of the original cans.

The solution is $k = 2.33232$, which is option B.

A. $k = 0.74240$

This corresponds to the model: $V = (0.80r)^2(1.16h)$.

B. $k = 2.33232$

* This is the correct option and corresponds to the model: $V = \pi(0.80r)^2(1.16h)$.

C. $k = 0.02011$

This corresponds to the model: $V = \pi(0.20r)^2(0.16h)$.

D. $k = 0.00640$

This corresponds to the model: $V = (0.20r)^2(0.16h)$.

E. None of the above.

If you chose this, please talk with the coordinator to discuss why you believe none of the options are correct.

General Comment: When calculating the new dimensions, you need to add/subtract from 100%. For example, a 10% increase in height would result in 110% of the original height: $1.1h_{\text{old}} = h_{\text{new}}$.

18. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 28 liter 22 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to

write the amount of each solution she used! If she remembers she used 5 percent and $3\frac{1}{4}$ percent solutions, what was the amount she used of the $3\frac{1}{4}$ percent solution?

The solution is 16.41*liters*, which is option C.

A. 12.23*liters*

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 14.00*liters*

This would be correct if Brittany used equal parts of each solution.

C. 16.41*liters*

*This is the correct option.

D. 11.59*liters*

This is the concentration of 5 percent solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

19. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has tripled every 2 days. How long will it be until there are at least 100000 confirmed cases?

The solution is About 18 days, which is option C.

A. About 8 days

You modeled the situation correctly but did not apply the properties of log correctly.

B. About 20 days

You modeled the situation with e as the base, but solved correctly otherwise.

C. About 18 days

* This is the correct option.

D. About 9 days

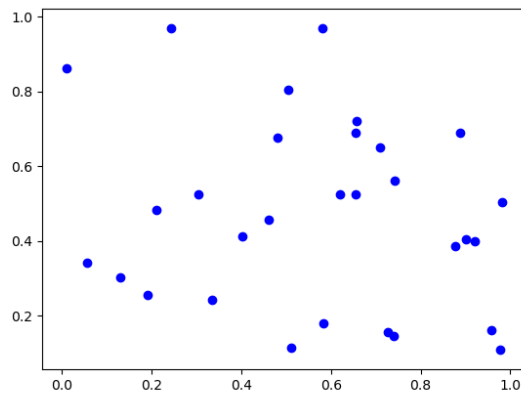
You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 100000 and solve for d in your model.

20. Determine the appropriate model for the graph of points below.



The solution is None of the above, which is option E.

A. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

B. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

D. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

21. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 42 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 12 percent, which is option B.

A. About 21 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

B. About 12 percent

* This is the correct option.

C. About 19 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

D. About 3 percent

This corresponds to not solving for the increase properly.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

22. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has quadrupled every 2 days. How long will it be until there are at least 100000 confirmed cases?

The solution is About 15 days, which is option B.

A. About 8 days

You modeled the situation correctly but did not apply the properties of log correctly.

B. About 15 days

* This is the correct option.

C. About 9 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

D. About 20 days

You modeled the situation with e as the base, but solved correctly otherwise.

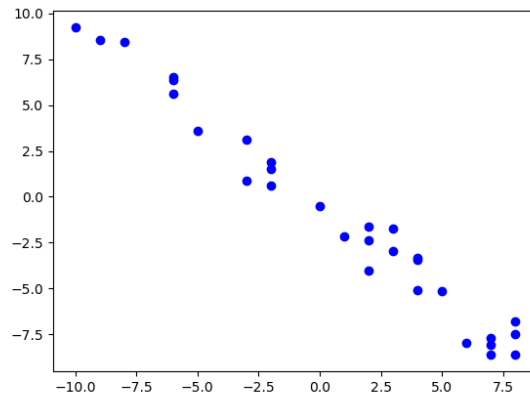
E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 100000 and solve for d in your model.

23. **General Comment:** None

24. Determine the appropriate model for the graph of points below.



The solution is Linear model, which is option B.

A. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

B. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

C. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

D. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

25. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 47 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 14 percent, which is option C.

A. About 24 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

B. About 21 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

C. About 14 percent

* This is the correct option.

D. About 4 percent

This corresponds to not solving for the increase properly.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

26. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 30 liter 9 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 5 percent and 33 percent solutions, what was the amount she used of the 33 percent solution?

The solution is 4.29liters, which is option B.

A. 15.00liters

This would be correct if Brittany used equal parts of each solution.

B. 4.29liters

*This is the correct option.

C. 16.92liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

D. 25.71liters

This is the concentration of 5 percent solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

27. Using the scenario below, model the population of bacteria α in terms of the number of minutes, t that pass. Then, choose the correct approximate (*rounded to the nearest minute*) replication rate of bacteria- α .

A newly discovered bacteria, α , is being examined in a lab. The lab started with a petri dish of 3 bacteria- α . After 1 hours, the petri dish has 105 bacteria- α . Based on similar bacteria, the lab believes bacteria- α quadruples after some undetermined number of minutes.

The solution is None of the above, which is option E.

A. About 70 minutes

This uses the wrong base and solves for the constant correctly but converted incorrectly.

B. About 138 minutes

This uses the wrong base, does not solve for the constant correctly, AND converted incorrectly.

C. About 23 minutes

This uses the wrong base and does not solve for the constant correctly.

D. About 11 minutes

This uses the wrong base.

E. None of the above

* This is the correct option as all other options used the wrong base in their model.

General Comment: Your model should be $P(t) = P_0(b)^{kt}$, where $P(t)$ is the population at some time t , P_0 is the initial population, and k is the replication rate. Be sure you convert the hours into minutes!

28. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 28 liter 25 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 17 percent and 32 percent solutions, what was the amount she used of the 32 percent solution?

The solution is 14.93liters, which is option A.

A. 14.93liters

*This is the correct option.

B. 13.70liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

C. 13.07liters

This is the concentration of 17 percent solution.

D. 14.00liters

This would be correct if Brittany used equal parts of each solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

29. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 8 many cases reported, but the number of confirmed cases has quadrupled every 5 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 26 days, which is option B.

A. About 36 days

You modeled the situation with e as the base, but solved correctly otherwise.

B. About 26 days

* This is the correct option.

C. About 15 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

D. About 14 days

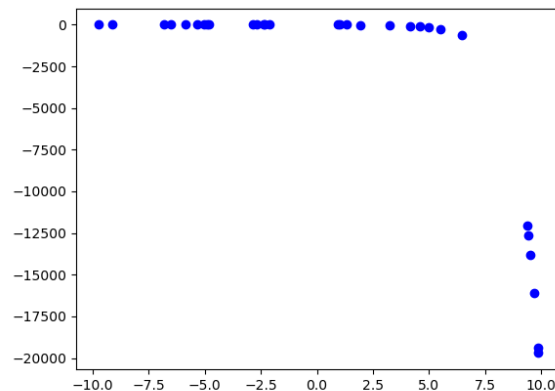
You modeled the situation correctly but did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

30. Determine the appropriate model for the graph of points below.



The solution is Exponential model, which is option C.

A. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

B. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

C. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

D. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.
