This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Evaluate the limit below, if possible.

$$\lim_{x \to 4} \frac{\sqrt{6x - 8} - 4}{2x - 8}$$

The solution is 0.375, which is option C.

A.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

B. 1.225

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

- C. 0.375
  - \* This is the correct option.
- D. 0.125

You likely memorized how to solve the similar homework problem and used the same formula here.

E. None of the above

If you got a limit that does not match any of the above, please contact the coordinator.

General Comment: General comments: It is difficult to imagine the graph of this function, so you need to test values close to x = 4.

2. Based on the information below, which of the following statements is always true?

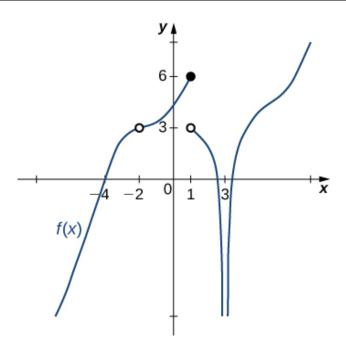
As x approaches 6, f(x) approaches 18.908.

The solution is f(x) is close to or exactly 18.908 when x is close to 6, which is option A.

- A. f(x) is close to or exactly 18.908 when x is close to 6
- B. f(x) = 6 when x is close to 18.908
- C. f(x) = 18.908 when x is close to 6
- D. f(x) is close to or exactly 6 when x is close to 18.908
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach 6. It says **absolutely nothing** about what is happening exactly at f(6)!

3. For the graph below, find the value(s) a that makes the statement true:  $\lim_{x\to a} f(x) = -\infty$ .

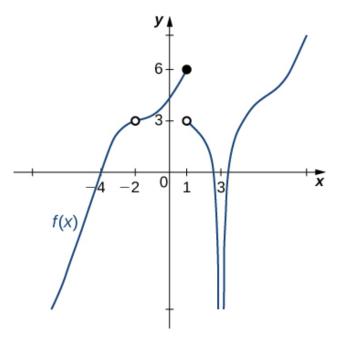


The solution is Multiple a make the statement true., which is option D.

- A. -2
- B.  $-\infty$
- C. 3
- D. Multiple a make the statement true.
- E. No a make the statement true.

General Comments: There can be multiple a values that make the statement true! For the limit, draw a horizontal line and determine if an x value makes the limit exist.

4. For the graph below, evaluate the limit:  $\lim_{x\to 1} f(x)$ .



The solution is The limit does not exist, which is option D.

- A.  $-\infty$
- B. 3
- C. 6
- D. The limit does not exist
- E. None of the above

**General Comments:** Remember that the limit does not exist if the left-hand and right-hand limits do not match.

5. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to -2^+} \frac{-3}{(x-2)^3} + 4$$

The solution is f(-2), which is option A.

- A. f(-2)
- B.  $-\infty$
- C.  $\infty$
- D. The limit does not exist
- E. None of the above

**General Comment: General comments:** You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

6. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to 8^+} \frac{2}{(x+8)^6} + 9$$

The solution is f(8), which is option B.

- A.  $-\infty$
- B. f(8)
- C.  $\infty$
- D. The limit does not exist
- E. None of the above

General Comment: General comments: You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

7. To estimate the one-sided limit of the function below as x approaches 5 from the left, which of the following sets of numbers should you use?

$$\frac{\frac{5}{x} - 1}{x - 5}$$

The solution is  $\{4.9000, 4.9900, 4.9990, 4.9999\}$ , which is option D.

A.  $\{5.0000, 4.9000, 4.9900, 4.9990\}$ 

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 5 doesn't help us estimate the limit.

B. {4.9000, 4.9900, 5.0100, 5.1000}

These values would estimate the limit at the point and not a one-sided limit.

C.  $\{5.1000, 5.0100, 5.0010, 5.0001\}$ 

These values would estimate the limit of 5 on the right.

D. {4.9000, 4.9900, 4.9990, 4.9999}

This is correct!

E.  $\{5.0000, 5.1000, 5.0100, 5.0010\}$ 

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 5 doesn't help us estimate the limit.

**General Comments:** To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

8. Based on the information below, which of the following statements is always true?

As 
$$x$$
 approaches 9,  $f(x)$  approaches 2.293.

The solution is f(x) is close to or exactly 2.293 when x is close to 9, which is option C.

- A. f(x) = 9 when x is close to 2.293
- B. f(x) = 2.293 when x is close to 9
- C. f(x) is close to or exactly 2.293 when x is close to 9
- D. f(x) is close to or exactly 9 when x is close to 2.293
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach 9. It says **absolutely nothing** about what is happening exactly at f(9)!

9. To estimate the one-sided limit of the function below as x approaches 10 from the right, which of the following sets of numbers should you use?

$$\frac{\frac{10}{x}-1}{x-10}$$

The solution is  $\{10.1000, 10.0100, 10.0010, 10.0001\}$ , which is option D.

A. {10.0000, 9.9000, 9.9900, 9.9990}

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 10 doesn't help us estimate the limit.

B. {9.9000, 9.9900, 9.9990, 9.9999}

These values would estimate the limit of 10 on the left.

C. {9.9000, 9.9900, 10.0100, 10.1000}

These values would estimate the limit at the point and not a one-sided limit.

D. {10.1000, 10.0100, 10.0010, 10.0001}

This is correct!

E.  $\{10.0000, 10.1000, 10.0100, 10.0010\}$ 

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 10 doesn't help us estimate the limit.

General Comments: To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

10. Evaluate the limit below, if possible.

$$\lim_{x \to 7} \frac{\sqrt{6x - 6} - 6}{3x - 21}$$

The solution is None of the above, which is option E.

A. 0.028

You likely learned L'Hospital's Rule in a previous course, but misapplied it here.

B. 0.816

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

C.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

D. 0.083

You likely memorized how to solve the similar homework problem and used the same formula here.

E. None of the above

\* This is the correct option as the limit is 0.167.

**General Comment: General comments:** It is difficult to imagine the graph of this function, so you need to test values close to x = 7.

11. Evaluate the limit below, if possible.

$$\lim_{x\to 8} \frac{\sqrt{7x-7}-7}{4x-32}$$

The solution is None of the above, which is option E.

A. 0.071

You likely memorized how to solve the similar homework problem and used the same formula here.

B.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

C. 0.661

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

D. 0.018

You likely learned L'Hospital's Rule in a previous course, but misapplied it here.

- E. None of the above
  - \* This is the correct option as the limit is 0.125.

General Comment: General comments: It is difficult to imagine the graph of this function, so you need to test values close to x = 8.

12. Based on the information below, which of the following statements is always true?

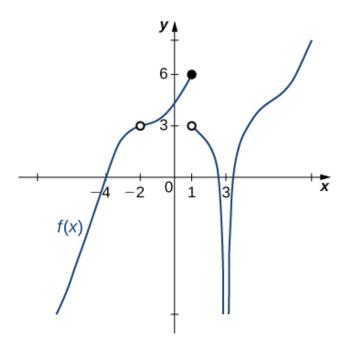
As x approaches 7, 
$$f(x)$$
 approaches  $\infty$ .

The solution is f(x) is undefined when x is close to or exactly 7., which is option C.

- A. f(x) is close to or exactly  $\infty$  when x is large enough.
- B. x is undefined when f(x) is close to or exactly  $\infty$ .
- C. f(x) is undefined when x is close to or exactly 7.
- D. f(x) is close to or exactly 7 when x is large enough.
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach 7. It says **absolutely nothing** about what is happening exactly at f(7)!

13. For the graph below, find the value(s) a that makes the statement true:  $\lim_{x\to a} f(x) = -\infty$ .

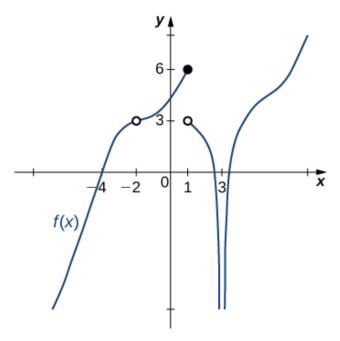


The solution is Multiple a make the statement true., which is option D.

- A.  $-\infty$
- B. -2
- C. 3
- D. Multiple a make the statement true.
- E. No a make the statement true.

General Comments: There can be multiple a values that make the statement true! For the limit, draw a horizontal line and determine if an x value makes the limit exist.

14. For the graph below, find the value(s) a that makes the statement true:  $\lim_{x\to a} f(x) = -\infty$ .



The solution is Multiple a make the statement true., which is option D.

- A. -2
- B.  $-\infty$
- C. 3
- D. Multiple a make the statement true.
- E. No a make the statement true.

General Comments: There can be multiple a values that make the statement true! For the limit, draw a horizontal line and determine if an x value makes the limit exist.

15. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to 8^{-}} \frac{-5}{(x+8)^8} + 2$$

The solution is f(8), which is option B.

- A.  $\infty$
- B. f(8)
- C.  $-\infty$
- D. The limit does not exist
- E. None of the above

**General Comment: General comments:** You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

16. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to 6^+} \frac{1}{(x+6)^4} + 7$$

The solution is f(6), which is option A.

- A. f(6)
- B.  $-\infty$
- C.  $\infty$
- D. The limit does not exist
- E. None of the above

**General Comment: General comments:** You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

17. To estimate the one-sided limit of the function below as x approaches 1 from the left, which of the following sets of numbers should you use?

$$\frac{\frac{1}{x}-1}{x-1}$$

The solution is  $\{0.9000, 0.9900, 0.9990, 0.9999\}$ , which is option C.

- A. {1.0000, 1.1000, 1.0100, 1.0010}
  - If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 1 doesn't help us estimate the limit.
- B. {0.9000, 0.9900, 1.0100, 1.1000}

These values would estimate the limit at the point and not a one-sided limit.

C. {0.9000, 0.9900, 0.9990, 0.9999}

This is correct!

- D. {1.0000, 0.9000, 0.9900, 0.9990}
  - If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 1 doesn't help us estimate the limit.
- E. {1.1000, 1.0100, 1.0010, 1.0001}

These values would estimate the limit of 1 on the right.

General Comments: To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

18. Based on the information below, which of the following statements is always true?

$$f(x)$$
 approaches 17.817 as x approaches 6.

The solution is None of the above are always true., which is option E.

- A. f(6) is close to or exactly 17
- B. f(17) = 6
- C. f(6) = 17
- D. f(17) is close to or exactly 6
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach 6. It says **absolutely nothing** about what is happening exactly at f(6)!

19. To estimate the one-sided limit of the function below as x approaches 5 from the right, which of the following sets of numbers should you use?

$$\frac{\frac{5}{x}-1}{x-5}$$

The solution is  $\{5.1000, 5.0100, 5.0010, 5.0001\}$ , which is option D.

A. {5.0000, 5.1000, 5.0100, 5.0010}

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 5 doesn't help us estimate the limit.

B. {5.0000, 4.9000, 4.9900, 4.9990}

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 5 doesn't help us estimate the limit.

C.  $\{4.9000, 4.9900, 5.0100, 5.1000\}$ 

These values would estimate the limit at the point and not a one-sided limit.

D. {5.1000, 5.0100, 5.0010, 5.0001}

This is correct!

E. {4.9000, 4.9900, 4.9990, 4.9999}

These values would estimate the limit of 5 on the left.

General Comments: To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

20. Evaluate the limit below, if possible.

$$\lim_{x \to 3} \frac{\sqrt{7x - 5} - 4}{6x - 18}$$

The solution is None of the above, which is option E.

A. 0.021

You likely learned L'Hospital's Rule in a previous course, but misapplied it here.

B. 0.441

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

C. 0.125

You likely memorized how to solve the similar homework problem and used the same formula here.

D.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

E. None of the above

<sup>\*</sup> This is the correct option as the limit is 0.146.

**General Comment: General comments:** It is difficult to imagine the graph of this function, so you need to test values close to x = 3.

21. Evaluate the limit below, if possible.

$$\lim_{x \to 6} \frac{\sqrt{5x - 14} - 4}{6x - 36}$$

The solution is None of the above, which is option E.

A. 0.373

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

B. 0.125

You likely memorized how to solve the similar homework problem and used the same formula here.

C.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

D. 0.021

You likely learned L'Hospital's Rule in a previous course, but misapplied it here.

- E. None of the above
  - \* This is the correct option as the limit is 0.104.

General Comment: General comments: It is difficult to imagine the graph of this function, so you need to test values close to x = 6.

22. Based on the information below, which of the following statements is always true?

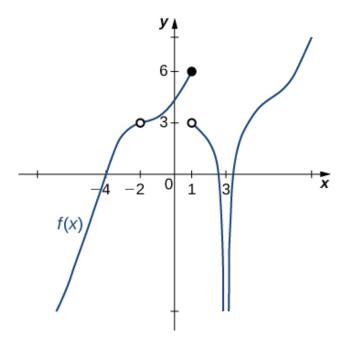
As x approaches 5, 
$$f(x)$$
 approaches  $\infty$ .

The solution is f(x) is undefined when x is close to or exactly 5., which is option A.

- A. f(x) is undefined when x is close to or exactly 5.
- B. f(x) is close to or exactly  $\infty$  when x is large enough.
- C. f(x) is close to or exactly 5 when x is large enough.
- D. x is undefined when f(x) is close to or exactly  $\infty$ .
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach 5. It says **absolutely nothing** about what is happening exactly at f(5)!

23. For the graph below, find the value(s) a that makes the statement true:  $\lim_{x\to a} f(x)$  does not exist.

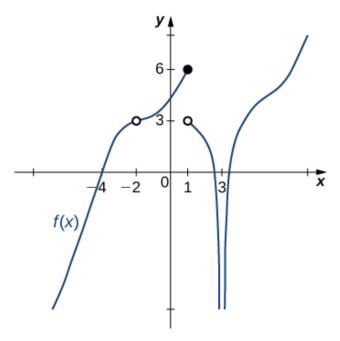


The solution is 1, which is option C.

- A. 3
- B. -2
- C. 1
- D. Multiple a make the statement true.
- E. No a make the statement true.

**General Comments:** Remember that the limit does not exist if the left-hand and right-hand limits do not match.

24. For the graph below, evaluate the limit:  $\lim_{x\to 3} f(x)$ .



The solution is  $-\infty$ , which is option C.

- A. -2
- B. 1
- C.  $-\infty$
- D. The limit does not exist
- E. None of the above

**General Comments:** Remember that the limit does not exist if the left-hand and right-hand limits do not match.

25. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to -3^{-}} \frac{4}{(x+3)^7} + 3$$

The solution is  $-\infty$ , which is option C.

- A. f(-3)
- B.  $\infty$
- C.  $-\infty$
- D. The limit does not exist
- E. None of the above

General Comment: General comments: You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

26. Evaluate the one-sided limit of the function f(x) below, if possible.

$$\lim_{x \to -3^+} \frac{4}{(x-3)^5} + 1$$

The solution is f(-3), which is option C.

- A.  $-\infty$
- B.  $\infty$
- C. f(-3)
- D. The limit does not exist
- E. None of the above

**General Comment: General comments:** You should be able to graph the rational function displayed. If not, go back to Module 7 to learn about the general shape of rational functions.

27. To estimate the one-sided limit of the function below as x approaches 4 from the right, which of the following sets of numbers should you use?

$$\frac{\frac{4}{x}-1}{x-4}$$

The solution is  $\{4.1000, 4.0100, 4.0010, 4.0001\}$ , which is option E.

A. {3.9000, 3.9900, 4.0100, 4.1000}

These values would estimate the limit at the point and not a one-sided limit.

B. {4.0000, 3.9000, 3.9900, 3.9990}

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 4 doesn't help us estimate the limit.

C.  $\{4.0000, 4.1000, 4.0100, 4.0010\}$ 

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 4 doesn't help us estimate the limit.

D. {3.9000, 3.9900, 3.9990, 3.9999}

These values would estimate the limit of 4 on the left.

E. {4.1000, 4.0100, 4.0010, 4.0001}

This is correct!

**General Comments:** To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

28. Based on the information below, which of the following statements is always true?

As x approaches 
$$\infty$$
,  $f(x)$  approaches 6.955.

The solution is f(x) is close to or exactly 6.955 when x is large enough., which is option B.

- A. x is undefined when f(x) is large enough.
- B. f(x) is close to or exactly 6.955 when x is large enough.
- C. f(x) is close to or exactly  $\infty$  when x is large enough.
- D. f(x) is undefined when x is large enough.
- E. None of the above are always true.

**General Comment:** The limit tells you what happens as the x-values approach  $\infty$ . It says **absolutely nothing** about what is happening exactly at  $f(\infty)$ !

29. To estimate the one-sided limit of the function below as x approaches 2 from the right, which of the following sets of numbers should you use?

$$\frac{\frac{2}{x}-1}{x-2}$$

The solution is  $\{2.1000, 2.0100, 2.0010, 2.0001\}$ , which is option A.

A. {2.1000, 2.0100, 2.0010, 2.0001}

This is correct!

B. {1.9000, 1.9900, 2.0100, 2.1000}

These values would estimate the limit at the point and not a one-sided limit.

C. {1.9000, 1.9900, 1.9990, 1.9999}

These values would estimate the limit of 2 on the left.

D. {2.0000, 1.9000, 1.9900, 1.9990}

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 2 doesn't help us estimate the limit.

 $E. \ \{2.0000, 2.1000, 2.0100, 2.0010\}$ 

If we get  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ , the value 2 doesn't help us estimate the limit.

General Comments: To evaluate a one-sided limit, we want to put numbers close to the limit. We can't use the limit value itself if it results in  $\frac{0}{0}$  or  $\frac{\infty}{\infty}$ 

30. Evaluate the limit below, if possible.

$$\lim_{x \to 7} \frac{\sqrt{7x - 33} - 4}{6x - 42}$$

The solution is None of the above, which is option E.

A. 0.021

You likely learned L'Hospital's Rule in a previous course, but misapplied it here.

B. 0.125

You likely memorized how to solve the similar homework problem and used the same formula here.

C.  $\infty$ 

You likely believed that since the denominator is equal to 0, the limit is infinity.

D. 0.441

You likely tried to use a shortcut to find the limit of a function that only works for when the numerator/denominator are polynomials.

E. None of the above

\* This is the correct option as the limit is 0.146.

General Comments: It is difficult to imagine the graph of this function, so you need to test values close to x = 7.