

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-5}{4} - \frac{9}{8}x \leq \frac{-5}{6}x + \frac{7}{9}$$

The solution is $[-6.952, \infty)$, which is option D.

- A. $(-\infty, a]$, where $a \in [3, 7.5]$

$(-\infty, 6.952]$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- B. $[a, \infty)$, where $a \in [3.75, 10.5]$

$[6.952, \infty)$, which corresponds to negating the endpoint of the solution.

- C. $(-\infty, a]$, where $a \in [-8.25, -6.75]$

$(-\infty, -6.952]$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D. $[a, \infty)$, where $a \in [-11.25, -4.5]$

* $[-6.952, \infty)$, which is the correct option.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

2. Using an interval or intervals, describe all the x -values within or including a distance of the given values.

Less than 5 units from the number -6 .

The solution is $(-11, -1)$, which is option C.

- A. $(-\infty, -11] \cup [-1, \infty)$

This describes the values no less than 5 from -6

- B. $(-\infty, -11) \cup (-1, \infty)$

This describes the values more than 5 from -6

- C. $(-11, -1)$

This describes the values less than 5 from -6

D. $[-11, -1]$

This describes the values no more than 5 from -6

E. None of the above

You likely thought the values in the interval were not correct.

General Comment: When thinking about this language, it helps to draw a number line and try points.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$3 + 7x > 10x \text{ or } 8 + 9x < 11x$$

The solution is $(-\infty, 1.0)$ or $(4.0, \infty)$, which is option A.

A. $(-\infty, a) \cup (b, \infty)$, where $a \in [-2.25, 3]$ and $b \in [3, 5.25]$

* Correct option.

B. $(-\infty, a] \cup [b, \infty)$, where $a \in [0.75, 5.25]$ and $b \in [3.75, 9]$

Corresponds to including the endpoints (when they should be excluded).

C. $(-\infty, a] \cup [b, \infty)$, where $a \in [-7.5, -3]$ and $b \in [-3, 1.5]$

Corresponds to including the endpoints AND negating.

D. $(-\infty, a) \cup (b, \infty)$, where $a \in [-5.25, 0.75]$ and $b \in [-6, 0.75]$

Corresponds to inverting the inequality and negating the solution.

E. $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 - 8x \leq \frac{-61x - 9}{8} < -3 - 9x$$

The solution is None of the above., which is option E.

A. $(-\infty, a] \cup (b, \infty)$, where $a \in [6.75, 13.5]$ and $b \in [-0.75, 5.25]$

$(-\infty, 10.33] \cup (1.36, \infty)$, which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

B. $[a, b)$, where $a \in [5.25, 12.75]$ and $b \in [0.3, 2.02]$

$[10.33, 1.36)$, which is the correct interval but negatives of the actual endpoints.

C. $(a, b]$, where $a \in [9.75, 11.25]$ and $b \in [0, 6.75]$

$(10.33, 1.36]$, which corresponds to flipping the inequality and getting negatives of the actual endpoints.

D. $(-\infty, a) \cup [b, \infty)$, where $a \in [9, 13.5]$ and $b \in [-0.38, 3.38]$

$(-\infty, 10.33) \cup [1.36, \infty)$, which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

E. None of the above.

* This is correct as the answer should be $[-10.33, -1.36)$.

General Comment: To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$6x + 9 \geq 10x - 8$$

The solution is $(-\infty, 4.25]$, which is option A.

A. $(-\infty, a]$, where $a \in [3.25, 10.25]$

* $(-\infty, 4.25]$, which is the correct option.

B. $(-\infty, a]$, where $a \in [-5.25, 0.75]$

$(-\infty, -4.25]$, which corresponds to negating the endpoint of the solution.

C. $[a, \infty)$, where $a \in [4.25, 9.25]$

$[4.25, \infty)$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D. $[a, \infty)$, where $a \in [-10.25, 1.75]$

$[-4.25, \infty)$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-9 + 4x > 5x \text{ or } 6 + 3x < 4x$$

The solution is $(-\infty, -9.0)$ or $(6.0, \infty)$, which is option A.

A. $(-\infty, a) \cup (b, \infty)$, where $a \in [-9.6, -7.88]$ and $b \in [2.92, 7.95]$

* Correct option.

B. $(-\infty, a) \cup (b, \infty)$, where $a \in [-7.65, -5.7]$ and $b \in [6.75, 10.12]$

Corresponds to inverting the inequality and negating the solution.

C. $(-\infty, a] \cup [b, \infty)$, where $a \in [-7.5, -0.75]$ and $b \in [6.75, 11.25]$

Corresponds to including the endpoints AND negating.

D. $(-\infty, a] \cup [b, \infty)$, where $a \in [-11.25, -8.25]$ and $b \in [1.5, 6.75]$

Corresponds to including the endpoints (when they should be excluded).

E. $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 - 4x \leq \frac{-33x - 4}{9} < 9 - 6x$$

The solution is None of the above., which is option E.

- A. $[a, b]$, where $a \in [9.75, 19.5]$ and $b \in [-7.5, -1.5]$

$[13.67, -4.05]$, which is the correct interval but negatives of the actual endpoints.

- B. $(a, b]$, where $a \in [10.5, 18]$ and $b \in [-5.25, 3]$

$(13.67, -4.05]$, which corresponds to flipping the inequality and getting negatives of the actual endpoints.

- C. $(-\infty, a] \cup (b, \infty)$, where $a \in [8.25, 14.25]$ and $b \in [-6, -1.5]$

$(-\infty, 13.67] \cup (-4.05, \infty)$, which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

- D. $(-\infty, a) \cup [b, \infty)$, where $a \in [10.5, 18.75]$ and $b \in [-6.75, 1.5]$

$(-\infty, 13.67) \cup [-4.05, \infty)$, which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

- E. None of the above.

* This is correct as the answer should be $[-13.67, 4.05)$.

General Comment: To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

8. Using an interval or intervals, describe all the x -values within or including a distance of the given values.

More than 7 units from the number 3.

The solution is None of the above, which is option E.

- A. $(4, 10)$

This describes the values less than 3 from 7

- B. $[4, 10]$

This describes the values no more than 3 from 7

- C. $(-\infty, 4] \cup [10, \infty)$

This describes the values no less than 3 from 7

- D. $(-\infty, 4) \cup (10, \infty)$

This describes the values more than 3 from 7

- E. None of the above

Options A-D described the values [more/less than] 3 units from 7, which is the reverse of what the question asked.

General Comment: When thinking about this language, it helps to draw a number line and try points.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{9}{2} - \frac{7}{4}x \leq \frac{7}{6}x - \frac{10}{3}$$

The solution is $[2.686, \infty)$, which is option B.

- A. $(-\infty, a]$, where $a \in [-3.75, -2.25]$

$(-\infty, -2.686]$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- B. $[a, \infty)$, where $a \in [1.5, 3.75]$

* $[2.686, \infty)$, which is the correct option.

- C. $(-\infty, a]$, where $a \in [0, 5.25]$

$(-\infty, 2.686]$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D. $[a, \infty)$, where $a \in [-7.5, 0.75]$

$[-2.686, \infty)$, which corresponds to negating the endpoint of the solution.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-10x + 8 < -8x + 7$$

The solution is $(0.5, \infty)$, which is option D.

- A. (a, ∞) , where $a \in [-2.1, -0.2]$

$(-0.5, \infty)$, which corresponds to negating the endpoint of the solution.

- B. $(-\infty, a)$, where $a \in [-2.98, -0.08]$

$(-\infty, -0.5)$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- C. $(-\infty, a)$, where $a \in [0.18, 1.43]$

$(-\infty, 0.5)$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D. (a, ∞) , where $a \in [0.4, 4]$

* $(0.5, \infty)$, which is the correct option.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.
