1. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{10x^3 - 42x^2 + 37}{x - 4}$$

- A.  $a \in [7, 15], b \in [-89, -81], c \in [325, 333], \text{ and } r \in [-1276, -1272].$
- B.  $a \in [7, 15], b \in [-3, 2], c \in [-8, -4], \text{ and } r \in [4, 9].$
- C.  $a \in [7, 15], b \in [-15, -10], c \in [-38, -35], \text{ and } r \in [-74, -67].$
- D.  $a \in [38, 46], b \in [117, 128], c \in [472, 476], \text{ and } r \in [1924, 1933].$
- E.  $a \in [38, 46], b \in [-204, -197], c \in [808, 817], \text{ and } r \in [-3200, -3192].$

2. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 3x^4 + 6x^3 + 6x^2 + 3x + 6$$

- A.  $\pm 1, \pm 3$
- B.  $\pm 1, \pm 2, \pm 3, \pm 6$
- C. All combinations of:  $\frac{\pm 1, \pm 3}{\pm 1, \pm 2, \pm 3, \pm 6}$
- D. All combinations of:  $\frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1, \pm 3}$
- E. There is no formula or theorem that tells us all possible Integer roots.
- 3. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{15x^3 - 33x^2 - 96x - 50}{x - 4}$$

- A.  $a \in [14, 16], b \in [24, 34], c \in [12, 16], and <math>r \in [-9, 0].$
- B.  $a \in [57, 64], b \in [207, 214], c \in [728, 736], and <math>r \in [2878, 2879].$
- C.  $a \in [14, 16], b \in [-97, -88], c \in [275, 283], and <math>r \in [-1160, -1151].$

- D.  $a \in [14, 16], b \in [11, 15], c \in [-65, -59], and r \in [-230, -226].$
- E.  $a \in [57, 64], b \in [-277, -269], c \in [996, 1002], and <math>r \in [-4037, -4026].$
- 4. Factor the polynomial below completely, knowing that x+5 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 15x^4 + 29x^3 - 233x^2 + 3x + 90$$

- A.  $z_1 \in [-4, 1], z_2 \in [-1.52, -1.5], z_3 \in [1.55, 1.68], \text{ and } z_4 \in [4, 8]$
- B.  $z_1 \in [-7, -4], z_2 \in [-1.72, -1.66], z_3 \in [1.46, 1.55], \text{ and } z_4 \in [1, 4]$
- C.  $z_1 \in [-7, -4], z_2 \in [-0.62, -0.57], z_3 \in [0.64, 0.75], \text{ and } z_4 \in [1, 4]$
- D.  $z_1 \in [-4, 1], z_2 \in [-0.15, -0.04], z_3 \in [2.95, 3.07], \text{ and } z_4 \in [4, 8]$
- E.  $z_1 \in [-4, 1], z_2 \in [-0.67, -0.65], z_3 \in [0.55, 0.64], \text{ and } z_4 \in [4, 8]$
- 5. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 10x^3 + 9x^2 - 28x - 12$$

- A.  $z_1 \in [-3.33, -2.61], z_2 \in [-0.02, 0.32], \text{ and } z_3 \in [1.78, 2.21]$
- B.  $z_1 \in [-2.82, -2.12], z_2 \in [-2.05, -1.75], \text{ and } z_3 \in [0.04, 0.93]$
- C.  $z_1 \in [-2.38, -1.94], z_2 \in [-0.71, -0.38], \text{ and } z_3 \in [1.45, 1.66]$
- D.  $z_1 \in [-0.73, -0.52], z_2 \in [1.91, 2.19], \text{ and } z_3 \in [2.48, 2.61]$
- E.  $z_1 \in [-1.57, -1.33], z_2 \in [0.32, 0.59], \text{ and } z_3 \in [1.78, 2.21]$
- 6. Factor the polynomial below completely, knowing that x-5 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where

 $z_1 \le z_2 \le z_3 \le z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 10x^4 - 99x^3 + 308x^2 - 333x + 90$$

- A.  $z_1 \in [-5.14, -4.51], z_2 \in [-3.1, -2.9], z_3 \in [-2.91, -2.29], \text{ and } z_4 \in [-0.78, -0.64]$
- B.  $z_1 \in [0.57, 0.97], z_2 \in [1.9, 3.4], z_3 \in [2.25, 3.29], \text{ and } z_4 \in [4.93, 5.07]$
- C.  $z_1 \in [-5.14, -4.51], z_2 \in [-3.1, -2.9], z_3 \in [-1.97, -1.46], \text{ and } z_4 \in [-0.44, -0.38]$
- D.  $z_1 \in [-5.14, -4.51], z_2 \in [-3.1, -2.9], z_3 \in [-2.01, -1.57], \text{ and } z_4 \in [-0.3, -0.06]$
- E.  $z_1 \in [0.25, 0.54], z_2 \in [0.4, 2.2], z_3 \in [2.25, 3.29], \text{ and } z_4 \in [4.93, 5.07]$
- 7. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{9x^3 + 39x^2 - 44}{x + 4}$$

- A.  $a \in [-39, -33], b \in [182, 186], c \in [-735, -729], \text{ and } r \in [2880, 2888].$
- B.  $a \in [-39, -33], b \in [-106, -102], c \in [-420, -411], \text{ and } r \in [-1728, -1723].$
- C.  $a \in [7, 16], b \in [-8, -5], c \in [28, 34], \text{ and } r \in [-196, -188].$
- D.  $a \in [7, 16], b \in [71, 80], c \in [298, 307], \text{ and } r \in [1148, 1157].$
- E.  $a \in [7, 16], b \in [0, 11], c \in [-14, -9], \text{ and } r \in [2, 10].$
- 8. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^3 - 19x^2 - 9x + 36$$

- A.  $z_1 \in [-1.96, -1.17], z_2 \in [1.18, 1.64], \text{ and } z_3 \in [2, 3.4]$
- B.  $z_1 \in [-3.26, -2.9], z_2 \in [-0.79, -0.65], \text{ and } z_3 \in [0.2, 0.8]$

C. 
$$z_1 \in [-1.13, -0.74], z_2 \in [0.49, 0.98], \text{ and } z_3 \in [2, 3.4]$$

D. 
$$z_1 \in [-3.26, -2.9], z_2 \in [-0.57, -0.38], \text{ and } z_3 \in [3.7, 5]$$

E. 
$$z_1 \in [-3.26, -2.9], z_2 \in [-1.57, -1.18], \text{ and } z_3 \in [1.2, 1.4]$$

9. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{20x^3 + 113x^2 + 142x + 42}{x + 4}$$

- A.  $a \in [15, 21], b \in [29, 34], c \in [9, 12], and r \in [2, 3].$
- B.  $a \in [15, 21], b \in [191, 198], c \in [907, 915], and <math>r \in [3697, 3699].$
- C.  $a \in [-84, -78], b \in [-207, -203], c \in [-694, -681], and r \in [-2708, -2700].$
- D.  $a \in [15, 21], b \in [10, 14], c \in [73, 85], and r \in [-347, -336].$
- E.  $a \in [-84, -78], b \in [429, 434], c \in [-1591, -1588], and r \in [6401, 6406].$

10. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 7x^4 + 2x^3 + 4x^2 + 3x + 5$$

- A.  $\pm 1, \pm 5$
- B. All combinations of:  $\frac{\pm 1, \pm 5}{\pm 1, \pm 7}$
- C.  $\pm 1, \pm 7$
- D. All combinations of:  $\frac{\pm 1, \pm 7}{\pm 1, \pm 5}$
- E. There is no formula or theorem that tells us all possible Integer roots.
- 11. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{15x^3 - 65x^2 + 82}{x - 4}$$

A. 
$$a \in [13, 16], b \in [-24, -15], c \in [-60, -55], \text{ and } r \in [-99, -97].$$

B. 
$$a \in [13, 16], b \in [-11, -1], c \in [-25, -13], \text{ and } r \in [-5, 4].$$

C. 
$$a \in [60, 61], b \in [175, 181], c \in [697, 708], \text{ and } r \in [2882, 2889].$$

D. 
$$a \in [13, 16], b \in [-125, -123], c \in [495, 504], \text{ and } r \in [-1919, -1912].$$

E. 
$$a \in [60, 61], b \in [-309, -304], c \in [1220, 1223], \text{ and } r \in [-4803, -4794].$$

12. What are the *possible Rational* roots of the polynomial below?

$$f(x) = 6x^2 + 5x + 2$$

A. 
$$\pm 1, \pm 2$$

B. All combinations of: 
$$\frac{\pm 1, \pm 2}{\pm 1, \pm 2, \pm 3, \pm 6}$$

C. All combinations of: 
$$\frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1, \pm 2}$$

D. 
$$\pm 1, \pm 2, \pm 3, \pm 6$$

E. There is no formula or theorem that tells us all possible Rational roots.

13. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{10x^3 - 38x^2 - 16x + 34}{x - 4}$$

A.  $a \in [37, 41], b \in [119, 126], c \in [468, 475], and <math>r \in [1922, 1924].$ 

B.  $a \in [5, 14], b \in [-78, -74], c \in [296, 303], and <math>r \in [-1152, -1147].$ 

C.  $a \in [5, 14], b \in [-3, 4], c \in [-11, -3], and <math>r \in [-1, 3].$ 

D.  $a \in [37, 41], b \in [-201, -193], c \in [776, 778], and <math>r \in [-3074, -3063].$ 

E.  $a \in [5, 14], b \in [-10, -2], c \in [-42, -39], and r \in [-86, -82].$ 

14. Factor the polynomial below completely, knowing that x+4 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 20x^4 + 13x^3 - 253x^2 + 78x + 72$$

- A.  $z_1 \in [-3.3, -2.6], z_2 \in [-1.16, -0.5], z_3 \in [0.23, 0.44], \text{ and } z_4 \in [3.1, 4.6]$
- B.  $z_1 \in [-3.3, -2.6], z_2 \in [-1.59, -1.31], z_3 \in [2.3, 2.69], \text{ and } z_4 \in [3.1, 4.6]$
- C.  $z_1 \in [-4.7, -3.5], z_2 \in [-2.67, -2.31], z_3 \in [1.2, 1.91], \text{ and } z_4 \in [1.5, 3.2]$
- D.  $z_1 \in [-3.3, -2.6], z_2 \in [-3.23, -2.61], z_3 \in [-0.05, 0.12], \text{ and } z_4 \in [3.1, 4.6]$
- E.  $z_1 \in [-4.7, -3.5], z_2 \in [-0.5, 0.04], z_3 \in [0.72, 0.88], \text{ and } z_4 \in [1.5, 3.2]$
- 15. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^3 - 1x^2 - 39x - 36$$

- A.  $z_1 \in [-0.79, -0.48], z_2 \in [-0.68, -0.58], \text{ and } z_3 \in [2.6, 3.4]$
- B.  $z_1 \in [-3.4, -2.82], z_2 \in [1.28, 1.47], \text{ and } z_3 \in [1, 1.6]$
- C.  $z_1 \in [-3.4, -2.82], z_2 \in [0.56, 0.82], \text{ and } z_3 \in [-0.2, 1.1]$
- D.  $z_1 \in [-3.4, -2.82], z_2 \in [0.36, 0.66], \text{ and } z_3 \in [3.4, 5.4]$
- E.  $z_1 \in [-2.03, -1.3], z_2 \in [-1.4, -1.18], \text{ and } z_3 \in [2.6, 3.4]$
- 16. Factor the polynomial below completely, knowing that x-4 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 8x^4 - 6x^3 - 189x^2 + 265x + 300$$

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A.  $z_1 \in [-5.9, -4.4], z_2 \in [-0.82, -0.46], z_3 \in [2.49, 2.51], \text{ and } z_4 \in [2.7, 4.9]$ 

- B.  $z_1 \in [-4.7, -2.8], z_2 \in [-0.5, -0.38], z_3 \in [1.33, 1.35], \text{ and } z_4 \in [4.7, 5.3]$
- C.  $z_1 \in [-5.9, -4.4], z_2 \in [-4.11, -3.8], z_3 \in [0.35, 0.38], \text{ and } z_4 \in [4.7, 5.3]$
- D.  $z_1 \in [-4.7, -2.8], z_2 \in [-2.96, -2.39], z_3 \in [0.74, 0.76], \text{ and } z_4 \in [4.7, 5.3]$
- E.  $z_1 \in [-5.9, -4.4], z_2 \in [-1.42, -1.05], z_3 \in [0.39, 0.41], \text{ and } z_4 \in [2.7, 4.9]$
- 17. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{10x^3 - 70x + 65}{x + 3}$$

- A.  $a \in [7, 12], b \in [30, 33], c \in [20, 26], \text{ and } r \in [124, 130].$
- B.  $a \in [-38, -25], b \in [90, 93], c \in [-344, -335], \text{ and } r \in [1078, 1091].$
- C.  $a \in [-38, -25], b \in [-91, -85], c \in [-344, -335], \text{ and } r \in [-958, -953].$
- D.  $a \in [7, 12], b \in [-40, -39], c \in [89, 91], \text{ and } r \in [-298, -294].$
- E.  $a \in [7, 12], b \in [-35, -29], c \in [20, 26], \text{ and } r \in [2, 13].$
- 18. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 20x^3 - 33x^2 - 20x + 12$$

- A.  $z_1 \in [-2.02, -1.65], z_2 \in [-2.77, -1.28], \text{ and } z_3 \in [0.09, 0.38]$
- B.  $z_1 \in [-1.2, -0.31], z_2 \in [0.22, 0.44], \text{ and } z_3 \in [1.92, 2.22]$
- C.  $z_1 \in [-1.63, -1.11], z_2 \in [1.83, 2.91], \text{ and } z_3 \in [2.28, 2.58]$

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D. 
$$z_1 \in [-2.55, -2.31], z_2 \in [-2.77, -1.28], \text{ and } z_3 \in [1.1, 1.38]$$

E. 
$$z_1 \in [-2.02, -1.65], z_2 \in [-0.52, -0.21], \text{ and } z_3 \in [0.69, 0.98]$$

19. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{15x^3 + 67x^2 + 94x + 35}{x + 2}$$

A. 
$$a \in [13, 18], b \in [37, 39], c \in [16, 24], and  $r \in [-11, -3].$$$

B. 
$$a \in [-31, -28], b \in [6, 13], c \in [104, 113], and  $r \in [251, 257].$$$

C. 
$$a \in [-31, -28], b \in [125, 129], c \in [-161, -159], and  $r \in [354, 357].$$$

D. 
$$a \in [13, 18], b \in [92, 101], c \in [284, 289], and  $r \in [606, 615].$$$

E. 
$$a \in [13, 18], b \in [20, 23], c \in [24, 34], and r \in [-50, -46].$$

20. What are the *possible Integer* roots of the polynomial below?

$$f(x) = 6x^4 + 4x^3 + 7x^2 + 4x + 7$$

A. All combinations of: 
$$\frac{\pm 1, \pm 2, \pm 3, \pm 6}{\pm 1, \pm 7}$$

B. 
$$\pm 1, \pm 7$$

C. 
$$\pm 1, \pm 2, \pm 3, \pm 6$$

D. All combinations of: 
$$\frac{\pm 1, \pm 7}{\pm 1, \pm 2, \pm 3, \pm 6}$$

E. There is no formula or theorem that tells us all possible Integer roots.

21. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{9x^3 + 21x^2 - 7}{x + 2}$$

- A.  $a \in [8, 17], b \in [36, 48], c \in [77, 84], \text{ and } r \in [149, 151].$
- B.  $a \in [8, 17], b \in [-8, -2], c \in [13, 21], \text{ and } r \in [-65, -60].$
- C.  $a \in [-18, -14], b \in [54, 60], c \in [-114, -113], \text{ and } r \in [219, 224].$
- D.  $a \in [8, 17], b \in [3, 8], c \in [-11, -3], \text{ and } r \in [4, 14].$
- E.  $a \in [-18, -14], b \in [-17, -10], c \in [-32, -25], \text{ and } r \in [-69, -66].$
- 22. What are the *possible Rational* roots of the polynomial below?

$$f(x) = 4x^4 + 6x^3 + 3x^2 + 7x + 2$$

- A. All combinations of:  $\frac{\pm 1, \pm 2, \pm 4}{\pm 1, \pm 2}$
- B. All combinations of:  $\frac{\pm 1, \pm 2}{\pm 1, \pm 2, \pm 4}$
- C.  $\pm 1, \pm 2, \pm 4$
- D.  $\pm 1, \pm 2$
- E. There is no formula or theorem that tells us all possible Rational roots.
- 23. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{20x^3 - 48x^2 - 116x - 43}{x - 4}$$

- A.  $a \in [19, 24], b \in [12, 13], c \in [-85, -79], and <math>r \in [-284, -280].$
- B.  $a \in [19, 24], b \in [-131, -125], c \in [391, 398], and <math>r \in [-1632, -1622].$
- C.  $a \in [19, 24], b \in [31, 38], c \in [8, 19], and r \in [2, 9].$
- D.  $a \in [80, 86], b \in [-370, -364], c \in [1356, 1360], and <math>r \in [-5472, -5466].$
- E.  $a \in [80, 86], b \in [269, 275], c \in [969, 975], and <math>r \in [3842, 3846].$

24. Factor the polynomial below completely, knowing that x+5 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 25x^4 + 210x^3 + 507x^2 + 434x + 120$$

- A.  $z_1 \in [1.24, 1.46], z_2 \in [1.6, 1.94], z_3 \in [1.3, 2.2], \text{ and } z_4 \in [4.71, 5.09]$
- B.  $z_1 \in [0.1, 0.33], z_2 \in [1.89, 2.8], z_3 \in [2.8, 4.5], \text{ and } z_4 \in [4.71, 5.09]$
- C.  $z_1 \in [-5.19, -4.79], z_2 \in [-2.35, -1.49], z_3 \in [-2, -1], \text{ and } z_4 \in [-1.56, -1.17]$
- D.  $z_1 \in [-5.19, -4.79], z_2 \in [-2.35, -1.49], z_3 \in [-1.1, 1.6], \text{ and } z_4 \in [-0.93, 0.31]$
- E.  $z_1 \in [0.5, 0.72], z_2 \in [-0.1, 0.82], z_3 \in [1.3, 2.2], \text{ and } z_4 \in [4.71, 5.09]$
- 25. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 6x^3 + 5x^2 - 22x - 24$$

- A.  $z_1 \in [-1.67, -1.39], z_2 \in [-1.42, -1.18], \text{ and } z_3 \in [1.7, 2.6]$
- B.  $z_1 \in [-2.13, -1.96], z_2 \in [0.46, 0.55], \text{ and } z_3 \in [3.7, 4.4]$
- C.  $z_1 \in [-2.13, -1.96], z_2 \in [0.62, 0.81], \text{ and } z_3 \in [-0.5, 1.2]$
- D.  $z_1 \in [-2.13, -1.96], z_2 \in [1.22, 1.4], \text{ and } z_3 \in [1, 1.9]$
- E.  $z_1 \in [-1.04, -0.67], z_2 \in [-0.83, -0.6], \text{ and } z_3 \in [1.7, 2.6]$
- 26. Factor the polynomial below completely, knowing that x-4 is a factor. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3 \leq z_4$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 12x^4 - 53x^3 - 23x^2 + 202x - 120$$

A.  $z_1 \in [-3.4, -1.4], z_2 \in [0.68, 0.95], z_3 \in [1.54, 1.71], \text{ and } z_4 \in [4, 6]$ 

B. 
$$z_1 \in [-3.4, -1.4], z_2 \in [0.52, 0.7], z_3 \in [1.2, 1.38], \text{ and } z_4 \in [4, 6]$$

- C.  $z_1 \in [-5.6, -4.6], z_2 \in [-4.05, -3.87], z_3 \in [-0.43, -0.2], \text{ and } z_4 \in [0, 3]$
- D.  $z_1 \in [-4.7, -3.1], z_2 \in [-1.44, -1.16], z_3 \in [-0.71, -0.32], \text{ and } z_4 \in [0, 3]$
- E.  $z_1 \in [-4.7, -3.1], z_2 \in [-1.75, -1.65], z_3 \in [-0.85, -0.62], \text{ and } z_4 \in [0, 3]$
- 27. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{8x^3 + 28x^2 - 33}{x+3}$$

- A.  $a \in [5, 12], b \in [4, 6], c \in [-13, -3], \text{ and } r \in [0, 8].$
- B.  $a \in [5, 12], b \in [52, 57], c \in [156, 158], \text{ and } r \in [435, 437].$
- C.  $a \in [5, 12], b \in [-6, 1], c \in [13, 19], \text{ and } r \in [-104, -92].$
- D.  $a \in [-24, -23], b \in [97, 102], c \in [-300, -290], \text{ and } r \in [864, 875].$
- E.  $a \in [-24, -23], b \in [-48, -40], c \in [-135, -124], \text{ and } r \in [-432, -427].$
- 28. Factor the polynomial below completely. Then, choose the intervals the zeros of the polynomial belong to, where  $z_1 \leq z_2 \leq z_3$ . To make the problem easier, all zeros are between -5 and 5.

$$f(x) = 10x^3 - 41x^2 - 54x + 45$$

- A.  $z_1 \in [-6, -4.8], z_2 \in [-0.8, -0.3], \text{ and } z_3 \in [1, 1.6]$
- B.  $z_1 \in [-6, -4.8], z_2 \in [-3.3, -2.7], \text{ and } z_3 \in [-0.7, 0.6]$
- C.  $z_1 \in [-6, -4.8], z_2 \in [-2.9, -1.5], \text{ and } z_3 \in [0.6, 0.9]$
- D.  $z_1 \in [-1, -0.1], z_2 \in [0.8, 2.1], \text{ and } z_3 \in [4.4, 5.9]$
- E.  $z_1 \in [-1.9, -1.1], z_2 \in [-0.1, 1.2], \text{ and } z_3 \in [4.4, 5.9]$

29. Perform the division below. Then, find the intervals that correspond to the quotient in the form  $ax^2 + bx + c$  and remainder r.

$$\frac{12x^3 + 45x^2 - 21x - 39}{x + 4}$$

- A.  $a \in [8, 13], b \in [90, 102], c \in [342, 359], and <math>r \in [1363, 1367].$
- B.  $a \in [-49, -44], b \in [-152, -144], c \in [-611, -607], \text{ and } r \in [-2475, -2471].$
- C.  $a \in [-49, -44], b \in [232, 242], c \in [-970, -961], and <math>r \in [3834, 3839].$
- D.  $a \in [8, 13], b \in [-16, -10], c \in [53, 55], and r \in [-310, -305].$
- E.  $a \in [8, 13], b \in [-3, 4], c \in [-19, -8], and <math>r \in [-5, 4].$
- 30. What are the *possible Rational* roots of the polynomial below?

$$f(x) = 3x^2 + 6x + 5$$

- A. All combinations of:  $\frac{\pm 1, \pm 3}{\pm 1, \pm 5}$
- B. All combinations of:  $\frac{\pm 1, \pm 5}{\pm 1, \pm 3}$
- C.  $\pm 1, \pm 5$
- D.  $\pm 1, \pm 3$
- E. There is no formula or theorem that tells us all possible Rational roots.