This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$ .

Pringles wants to add 35 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 11 percent, which is option C.

A. About 16 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

B. About 3 percent

This corresponds to not solving for the increase properly.

- C. About 11 percent
  - \* This is the correct option.
- D. About 18 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

E. None of the above

If you chose this, please contact the coordinator to discus how you solved the problem.

**General Comment:** Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

2. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$ .

Pringles wants to add 24 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 7 percent, which is option D.

A. About 11 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

B. About 3 percent

This corresponds to not solving for the increase properly.

C. About 12 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

## D. About 7 percent

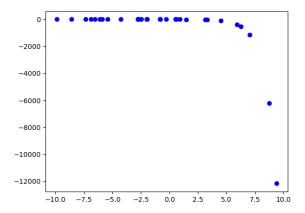
\* This is the correct option.

#### E. None of the above

If you chose this, please contact the coordinator to discus how you solved the problem.

**General Comment:** Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

# 3. Determine the appropriate model for the graph of points below.



The solution is Exponential model, which is option A.

## A. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

#### B. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

#### C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

## D. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

#### E. None of the above

For this to be the correct option, we want to see no pattern in the points.

**General Comment:** This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

4. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 8 many cases reported, but the number of confirmed cases has doubled every 3 days. How long will it be until there are at least 100000 confirmed cases?

The solution is About 41 days, which is option A.

- A. About 41 days
  - \* This is the correct option.
- B. About 29 days

You modeled the situation with e as the base, but solved correctly otherwise.

C. About 12 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

D. About 13 days

You modeled the situation correctly but did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

**General Comment:** Set up the model the same as in Module 11M. Then, plug in 100000 and solve for d in your model.

5. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 23 liter 11 percent solution of chemical  $\chi$  using two different solution percentages of chemical  $\chi$ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 9 percent and 22 percent solutions, what was the amount she used of the 22 percent solution?

The solution is 3.54 liters, which is option A.

A. 3.54 liters

\*This is the correct option.

B. 11.50liters

This would be correct if Brittany used equal parts of each solution.

C. 19.46 *liters* 

This is the concentration of 9 percent solution.

D. 7.88liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

**General Comment:** Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

6. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the quartic of the time, T (Earth years), required for a planet to orbit Sun  $\chi$  decreases as the square of the distance, d (AUs), that the planet is from Sun  $\chi$  decreases. For example, when Ea's average distance from Sun  $\chi$  is 8, it takes 89 Earth days to complete an orbit.

The solution is k = 980347.516, which is option A.

A. k = 980347.516

\* This is the correct option corresponding to the model  $T^4 = kd^2$ .

B. k = 4.028

This copies the constant used in the homework.

C. k = 4015503424.000

This corresponds to the model  $T^4 = \frac{k}{d^2}$ 

D. k = 1.086

This corresponds to the model  $T^{1/4} = kd^{1/2}$ .

E. Unable to compute the constant based on the information given.

This corresponds to believing you cannot determine the type of model from the information given.

**General Comment:** Since T decreases proportionally as d decreases, we know this is a direct variation model.

7. Using the situation below, construct a linear model that describes the cost of the coffee beans C(h) in terms of the weight of the low-quality coffee beans h.

Veronica needs to prepare 120 of blended coffee beans selling for \$6.11 per pound. She has a high-quality bean that sells for \$7.57 a pound and a low-quality bean that sells for \$4.86 a pound.

The solution is C(h) = -2.71h + 908.40, which is option C.

A. 
$$C(h) = 6.21h$$

This assumes that exactly half of the high- and low- quality beans are mixed to create the blended coffee beans.

B. 
$$C(h) = 2.71h + 583.20$$

This would be correct if the question asked you to construct the cost model in terms of the weight of the high-quality bean.

C. 
$$C(h) = -2.71h + 908.40$$

\* This is the correct option since the questions asked you to construct the cost model in terms of the weight of the low-quality bean.

D. 
$$C(h) = 4.86h$$

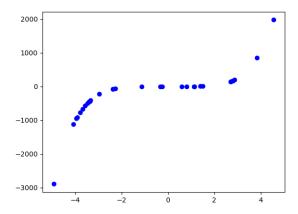
This models the cost of the low-quality bean only, not the blended beans.

E. None of the above.

If you chose this option, please talk to the coordinator to discuss why.

**General Comment:** This is exactly like the chemistry mixture question from the homework! If you are having trouble with this problem, be sure to review the video for building linear models.

# 8. Determine the appropriate model for the graph of points below.



The solution is Non-linear Power model, which is option C.

## A. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

#### B. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

#### C. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

## D. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

# E. None of the above

For this to be the correct option, we want to see no pattern in the points.

**General Comment:** This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

#### 9. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has quadrupled every 3 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 17 days, which is option C.

## A. About 23 days

You modeled the situation with e as the base, but solved correctly otherwise.

## B. About 10 days

You modeled the situation correctly but did not apply the properties of log correctly.

- C. About 17 days
  - \* This is the correct option.
- D. About 11 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

**General Comment:** Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

10. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 29 liter 27 percent solution of chemical  $\chi$  using two different solution percentages of chemical  $\chi$ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 17 percent and 39 percent solutions, what was the amount she used of the 39 percent solution?

The solution is 13.18 liters, which is option D.

A. 13.63liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 14.50liters

This would be correct if Brittany used equal parts of each solution.

C. 15.82liters

This is the concentration of 17 percent solution.

D. 13.18liters

\*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

**General Comment:** Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.