This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that $f^{-}1(7)$ belongs to.

$$f(x) = e^{x+3} + 3$$

The solution is $f^{-1}(7) = -1.614$, which is option E.

A. $f^{-1}(7) \in [4.3, 4.7]$

This solution corresponds to distractor 3.

B. $f^{-1}(7) \in [4.4, 5.9]$

This solution corresponds to distractor 4.

C. $f^{-1}(7) \in [4.4, 5.9]$

This solution corresponds to distractor 2.

D. $f^{-1}(7) \in [4.3, 4.7]$

This solution corresponds to distractor 1.

E. $f^{-1}(7) \in [-2.8, -1.3]$

This is the solution.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

2. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 3x^2 + 5x + 8$$
 and $g(x) = \frac{2}{4x + 27}$

The solution is The domain is all Real numbers except x = -6.75, which is option B.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [-9.5, -2.5]$
- B. The domain is all Real numbers except x = a, where $a \in [-13.75, -4.75]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [-2, 5]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [3.33, 9.33]$ and $b \in [-3.2, -2.2]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

3. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -10 and choose the interval that $f^{-1}(-10)$ belongs to.

$$f(x) = \sqrt[3]{2x+5}$$

The solution is -502.5, which is option D.

A. $f^{-1}(-10) \in [-499.5, -496.5]$

Distractor 1: This corresponds to

B. $f^{-1}(-10) \in [501.1, 503.1]$

This solution corresponds to distractor 2.

C. $f^{-1}(-10) \in [495.1, 500.2]$

This solution corresponds to distractor 3.

- D. $f^{-1}(-10) \in [-503.9, -500.4]$
 - * This is the correct solution.
- E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

4. Determine whether the function below is 1-1.

$$f(x) = (5x - 35)^3$$

The solution is yes, which is option A.

- A. Yes, the function is 1-1.
 - * This is the solution.
- B. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

D. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

E. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

5. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{3}{6x + 37}$$
 and $g(x) = x + 7$

The solution is The domain is all Real numbers except x = -6.17, which is option B.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [-6.5, -2.5]$
- B. The domain is all Real numbers except x = a, where $a \in [-6.17, -2.17]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [0,3]$

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- D. The domain is all Real numbers except x = a and x = b, where $a \in [-3.8, 1.2]$ and $b \in [4.33, 8.33]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

6. Find the inverse of the function below. Then, evaluate the inverse at x = 10 and choose the interval that $f^{-}1(10)$ belongs to.

$$f(x) = \ln(x+4) - 5$$

The solution is $f^{-1}(10) = 3269013.372$, which is option C.

A. $f^{-1}(10) \in [142.41, 149.41]$

This solution corresponds to distractor 1.

B. $f^{-1}(10) \in [396.43, 399.43]$

This solution corresponds to distractor 2.

C. $f^{-1}(10) \in [3269012.37, 3269019.37]$

This is the solution.

D. $f^{-1}(10) \in [1202597.28, 1202600.28]$

This solution corresponds to distractor 4.

E. $f^{-1}(10) \in [3269019.37, 3269022.37]$

This solution corresponds to distractor 3.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

7. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = -2x^3 + x^2 + 2x$$
 and $g(x) = -x^3 - 2x^2 - 3x - 4$

The solution is 16.0, which is option A.

A. $(f \circ g)(-1) \in [13, 17]$

* This is the correct solution

B. $(f \circ g)(-1) \in [-16, -6]$

Distractor 1: Corresponds to reversing the composition.

C. $(f \circ g)(-1) \in [-8, -3]$

Distractor 3: Corresponds to being slightly off from the solution.

D. $(f \circ g)(-1) \in [5, 12]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

8. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -15 and choose the interval that $f^{-1}(-15)$ belongs to.

$$f(x) = 3x^2 - 4$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A. $f^{-1}(-15) \in [1.82, 1.95]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

B. $f^{-1}(-15) \in [6.9, 7.22]$

Distractor 4: This corresponds to both distractors 2 and 3.

C. $f^{-1}(-15) \in [3.76, 4.2]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

D. $f^{-1}(-15) \in [2.22, 2.55]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

- E. The function is not invertible for all Real numbers.
 - * This is the correct option.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

9. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = 2x^3 - 2x^2 + 2x + 3$$
 and $g(x) = x^3 + 2x^2 + 3x$

The solution is -25.0, which is option C.

A. $(f \circ g)(-1) \in [-18.39, -17.32]$

Distractor 1: Corresponds to reversing the composition.

B. $(f \circ g)(-1) \in [-13.09, -12.75]$

Distractor 3: Corresponds to being slightly off from the solution.

- C. $(f \circ g)(-1) \in [-25.46, -22.42]$
 - * This is the correct solution
- D. $(f \circ g)(-1) \in [-21.79, -18.43]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

10. Determine whether the function below is 1-1.

$$f(x) = (3x + 21)^3$$

The solution is yes, which is option D.

A. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

B. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

C. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

- D. Yes, the function is 1-1.
 - * This is the solution.
- E. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

11. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that $f^{-1}(7)$ belongs to.

$$f(x) = \ln(x+2) - 5$$

The solution is $f^{-1}(7) = 162752.791$, which is option A.

A. $f^{-1}(7) \in [162750.79, 162754.79]$

This is the solution.

B. $f^{-1}(7) \in [-0.61, 7.39]$

This solution corresponds to distractor 1.

C. $f^{-1}(7) \in [143.41, 144.41]$

This solution corresponds to distractor 2.

D. $f^{-1}(7) \in [162753.79, 162764.79]$

This solution corresponds to distractor 3.

E. $f^{-1}(7) \in [8098.08, 8102.08]$

This solution corresponds to distractor 4.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

12. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{2}{4x + 21}$$
 and $g(x) = \frac{2}{6x - 23}$

The solution is The domain is all Real numbers except x = -5.25 and x = 3.83, which is option D.

- A. The domain is all Real numbers except x = a, where $a \in [0.4, 11.4]$
- B. The domain is all Real numbers greater than or equal to x = a, where $a \in [1, 9]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [-6.67, -2.67]$
- D. The domain is all Real numbers except x=a and x=b, where $a\in[-7.25,-4.25]$ and $b\in[0.83,7.83]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

13. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 11 and choose the interval that $f^{-1}(11)$ belongs to.

$$f(x) = \sqrt[3]{2x+3}$$

The solution is 664.0, which is option A.

- A. $f^{-1}(11) \in [663.3, 664.8]$
 - * This is the correct solution.
- B. $f^{-1}(11) \in [664.9, 667.9]$

Distractor 1: This corresponds to

C. $f^{-1}(11) \in [-664.5, -661.8]$

This solution corresponds to distractor 2.

D. $f^{-1}(11) \in [-669.6, -664.4]$

This solution corresponds to distractor 3.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

14. Determine whether the function below is 1-1.

$$f(x) = -9x^2 + 15x + 234$$

The solution is no, which is option E.

A. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

B. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

C. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

D. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- E. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

15. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = x + 6$$
 and $g(x) = \frac{1}{4x - 13}$

The solution is The domain is all Real numbers except x = 3.25, which is option A.

- A. The domain is all Real numbers except x = a, where $a \in [2.25, 6.25]$
- B. The domain is all Real numbers less than or equal to x = a, where $a \in [-6.4, -2.4]$
- C. The domain is all Real numbers greater than or equal to x = a, where $a \in [-6.75, -2.75]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [-12.33, 2.67]$ and $b \in [-8.67, -3.67]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

16. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that $f^{-1}(7)$ belongs to.

$$f(x) = e^{x-4} + 5$$

The solution is $f^{-1}(7) = 4.693$, which is option B.

A.
$$f^{-1}(7) \in [6.02, 6.21]$$

This solution corresponds to distractor 4.

B.
$$f^{-1}(7) \in [4.66, 4.73]$$

This is the solution.

C.
$$f^{-1}(7) \in [7.35, 7.45]$$

This solution corresponds to distractor 3.

D.
$$f^{-1}(7) \in [-3.34, -3.28]$$

This solution corresponds to distractor 1.

E.
$$f^{-1}(7) \in [7.41, 7.5]$$

This solution corresponds to distractor 2.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

17. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = -2x^3 - 2x^2 + 2x$$
 and $g(x) = -2x^3 - 3x^2 + 3x + 1$

The solution is -2.0, which is option D.

A.
$$(f \circ g)(1) \in [-1.78, -0.74]$$

Distractor 1: Corresponds to reversing the composition.

B.
$$(f \circ g)(1) \in [2.64, 3.93]$$

Distractor 2: Corresponds to being slightly off from the solution.

C.
$$(f \circ g)(1) \in [-6.26, -5.68]$$

Distractor 3: Corresponds to being slightly off from the solution.

D.
$$(f \circ g)(1) \in [-2.2, -1.72]$$

* This is the correct solution

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

18. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 12 and choose the interval that $f^{-1}(12)$ belongs to.

$$f(x) = \sqrt[3]{3x+4}$$

The solution is 574.66666666666666666, which is option A.

- A. $f^{-1}(12) \in [574, 576.8]$
 - * This is the correct solution.
- B. $f^{-1}(12) \in [577.3, 578.8]$

Distractor 1: This corresponds to

C. $f^{-1}(12) \in [-580.7, -574.7]$

This solution corresponds to distractor 3.

D. $f^{-1}(12) \in [-575.6, -573.9]$

This solution corresponds to distractor 2.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

19. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = -3x^3 - 2x^2 + 3x + 4$$
 and $g(x) = x^3 - 2x^2 + 3x$

The solution is -22.0, which is option C.

A. $(f \circ g)(1) \in [-30, -24]$

Distractor 2: Corresponds to being slightly off from the solution.

B. $(f \circ g)(1) \in [6, 11]$

Distractor 1: Corresponds to reversing the composition.

- C. $(f \circ g)(1) \in [-26, -20]$
 - * This is the correct solution
- D. $(f \circ g)(1) \in [-6, 1]$

Distractor 3: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

20. Determine whether the function below is 1-1.

$$f(x) = (4x + 13)^3$$

The solution is yes, which is option C.

A. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

B. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

- C. Yes, the function is 1-1.
 - * This is the solution.
- D. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

E. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

21. Find the inverse of the function below. Then, evaluate the inverse at x = 8 and choose the interval that $f^{-1}(8)$ belongs to.

$$f(x) = \ln(x+5) + 2$$

The solution is $f^{-1}(8) = 398.429$, which is option E.

A. $f^{-1}(8) \in [22020.47, 22024.47]$

This solution corresponds to distractor 1.

B. $f^{-1}(8) \in [21.09, 27.09]$

This solution corresponds to distractor 2.

C. $f^{-1}(8) \in [442414.39, 442420.39]$

This solution corresponds to distractor 4.

D. $f^{-1}(8) \in [405.43, 413.43]$

This solution corresponds to distractor 3.

E. $f^{-1}(8) \in [388.43, 399.43]$

This is the solution.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

22. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \sqrt{6x - 28}$$
 and $g(x) = x + 6$

The solution is The domain is all Real numbers greater than or equal to x = 4.67., which is option B.

- A. The domain is all Real numbers except x = a, where $a \in [1.17, 5.17]$
- B. The domain is all Real numbers greater than or equal to x = a, where $a \in [0.67, 5.67]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [-5.5, -0.5]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [-1.67, 4.33]$ and $b \in [-4.2, -3.2]$

E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

23. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -15 and choose the interval that $f^{-1}(-15)$ belongs to.

$$f(x) = \sqrt[3]{3x+4}$$

A. $f^{-1}(-15) \in [1125.5, 1129.3]$

This solution corresponds to distractor 2.

B. $f^{-1}(-15) \in [1122.7, 1126]$

This solution corresponds to distractor 3.

C. $f^{-1}(-15) \in [-1125.4, -1122.4]$

Distractor 1: This corresponds to

- D. $f^{-1}(-15) \in [-1129, -1126.3]$
 - * This is the correct solution.
- E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

24. Determine whether the function below is 1-1.

$$f(x) = 9x^2 - 39x - 230$$

The solution is no, which is option B.

A. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

- B. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.
- C. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

D. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

E. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

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25. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{3}{3x - 16}$$
 and $g(x) = \frac{2}{3x + 16}$

The solution is The domain is all Real numbers except x = 5.33 and x = -5.33, which is option D.

- A. The domain is all Real numbers less than or equal to x = a, where $a \in [-6.6, 5.4]$
- B. The domain is all Real numbers except x = a, where $a \in [-8.25, -4.25]$
- C. The domain is all Real numbers greater than or equal to x=a, where $a \in [5,13]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [0.33, 6.33]$ and $b \in [-11.33, -1.33]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

26. Find the inverse of the function below. Then, evaluate the inverse at x = 4 and choose the interval that $f^{-}1(4)$ belongs to.

$$f(x) = e^{x+2} + 2$$

The solution is $f^{-1}(4) = -1.307$, which is option B.

A. $f^{-1}(4) \in [-0.7, 2.7]$

This solution corresponds to distractor 1.

B. $f^{-1}(4) \in [-3.5, -0.7]$

This is the solution.

C. $f^{-1}(4) \in [-0.7, 2.7]$

This solution corresponds to distractor 3.

D. $f^{-1}(4) \in [2.8, 5.5]$

This solution corresponds to distractor 4.

E. $f^{-1}(4) \in [2.8, 5.5]$

This solution corresponds to distractor 2.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

27. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = -4x^3 - 2x^2 + 4x - 1$$
 and $g(x) = -2x^3 - 2x^2 - x$

The solution is -3.0, which is option D.

A. $(f \circ g)(-1) \in [42, 47]$

Distractor 3: Corresponds to being slightly off from the solution.

B. $(f \circ g)(-1) \in [38, 40]$

Distractor 1: Corresponds to reversing the composition.

C. $(f \circ g)(-1) \in [4, 6]$

Distractor 2: Corresponds to being slightly off from the solution.

- D. $(f \circ g)(-1) \in [-12, 0]$
 - * This is the correct solution
- E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

28. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 13 and choose the interval that $f^{-1}(13)$ belongs to.

$$f(x) = \sqrt[3]{5x+3}$$

The solution is 438.8, which is option A.

- A. $f^{-1}(13) \in [438.67, 438.81]$
 - * This is the correct solution.
- B. $f^{-1}(13) \in [439.45, 441.34]$

Distractor 1: This corresponds to

C. $f^{-1}(13) \in [-439.21, -438.65]$

This solution corresponds to distractor 2.

D. $f^{-1}(13) \in [-440.29, -439.8]$

This solution corresponds to distractor 3.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

29. Choose the interval below that f composed with q at x = -1 is in.

$$f(x) = -2x^3 + 3x^2 + 4x$$
 and $g(x) = 3x^3 - 1x^2 - 2x$

The solution is 20.0, which is option B.

A. $(f \circ g)(-1) \in [24, 37]$

Distractor 2: Corresponds to being slightly off from the solution.

- B. $(f \circ g)(-1) \in [20, 21]$
 - * This is the correct solution
- C. $(f \circ g)(-1) \in [1, 14]$

Distractor 3: Corresponds to being slightly off from the solution.

D. $(f \circ g)(-1) \in [-5, 3]$

Distractor 1: Corresponds to reversing the composition.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

30. Determine whether the function below is 1-1.

$$f(x) = 15x^2 - 56x - 396$$

The solution is no, which is option A.

- A. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.
- B. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

D. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

E. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

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