This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = -2x^3 + 2x^2 - 3x$$
 and $g(x) = 2x^3 + 2x^2 - 2x$

The solution is -14.0, which is option B.

A. $(f \circ g)(1) \in [-36, -34]$

Distractor 3: Corresponds to being slightly off from the solution.

B. $(f \circ g)(1) \in [-19, -13]$

* This is the correct solution

C. $(f \circ g)(1) \in [-10, 3]$

Distractor 2: Corresponds to being slightly off from the solution.

D. $(f \circ q)(1) \in [-31, -29]$

Distractor 1: Corresponds to reversing the composition.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

2. Choose the interval below that f composed with g at x=-1 is in.

$$f(x) = x^3 - 4x^2 - 4x - 2$$
 and $g(x) = -4x^3 - 1x^2 + 2x + 2$

The solution is -23.0, which is option A.

A. $(f \circ g)(-1) \in [-24, -18]$

* This is the correct solution

B. $(f \circ g)(-1) \in [89, 99]$

Distractor 1: Corresponds to reversing the composition.

C. $(f \circ g)(-1) \in [97, 107]$

Distractor 3: Corresponds to being slightly off from the solution.

D. $(f \circ g)(-1) \in [-31, -26]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

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3. Determine whether the function below is 1-1.

$$f(x) = -16x^2 - 24x + 247$$

The solution is no, which is option B.

A. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

- B. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.
- C. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

D. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

E. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

4. Find the inverse of the function below. Then, evaluate the inverse at x = 10 and choose the interval that $f^{-}1(10)$ belongs to.

$$f(x) = e^{x+2} - 5$$

The solution is $f^{-1}(10) = 0.708$, which is option E.

A.
$$f^{-1}(10) \in [-3.55, -3.34]$$

This solution corresponds to distractor 2.

B.
$$f^{-1}(10) \in [-3.16, -2.67]$$

This solution corresponds to distractor 3.

C.
$$f^{-1}(10) \in [4.47, 4.86]$$

This solution corresponds to distractor 1.

D.
$$f^{-1}(10) \in [-2.54, -2.41]$$

This solution corresponds to distractor 4.

E.
$$f^{-1}(10) \in [0.55, 0.96]$$

This is the solution.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

5. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 10 and choose the interval that $f^{-1}(10)$ belongs to.

$$f(x) = 2x^2 - 4$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A. $f^{-1}(10) \in [1.77, 2.8]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

B. $f^{-1}(10) \in [2.88, 4.02]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

C. $f^{-1}(10) \in [6.38, 7.96]$

Distractor 4: This corresponds to both distractors 2 and 3.

D. $f^{-1}(10) \in [0.91, 2.03]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

E. The function is not invertible for all Real numbers.

* This is the correct option.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

6. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that $f^{-}1(7)$ belongs to.

$$f(x) = \ln(x+5) + 3$$

The solution is $f^{-1}(7) = 49.598$, which is option D.

A. $f^{-1}(7) \in [162755.79, 162763.79]$

This solution corresponds to distractor 4.

B. $f^{-1}(7) \in [58.6, 61.6]$

This solution corresponds to distractor 3.

C. $f^{-1}(7) \in [22020.47, 22024.47]$

This solution corresponds to distractor 1.

D. $f^{-1}(7) \in [47.6, 54.6]$

This is the solution.

E. $f^{-1}(7) \in [7.39, 11.39]$

This solution corresponds to distractor 2.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

7. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 14 and choose the interval that $f^{-1}(14)$ belongs to.

$$f(x) = \sqrt[3]{3x - 4}$$

The solution is 916.0, which is option C.

A. $f^{-1}(14) \in [-916.4, -914.3]$

This solution corresponds to distractor 2.

B. $f^{-1}(14) \in [-913.6, -911.7]$

This solution corresponds to distractor 3.

- C. $f^{-1}(14) \in [914.9, 919.4]$
 - * This is the correct solution.
- D. $f^{-1}(14) \in [911.6, 915.6]$

Distractor 1: This corresponds to

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

8. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{1}{4x + 25}$$
 and $g(x) = \frac{4}{6x - 29}$

The solution is The domain is all Real numbers except x = -6.25 and x = 4.83, which is option D.

- A. The domain is all Real numbers except x = a, where $a \in [5.67, 14.67]$
- B. The domain is all Real numbers less than or equal to x = a, where $a \in [0.33, 12.33]$
- C. The domain is all Real numbers greater than or equal to x = a, where $a \in [-8.5, -4.5]$
- D. The domain is all Real numbers except x=a and x=b, where $a\in[-15.25,-2.25]$ and $b\in[2.83,9.83]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

9. Determine whether the function below is 1-1.

$$f(x) = (4x - 18)^3$$

The solution is yes, which is option B.

A. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

- B. Yes, the function is 1-1.
 - * This is the solution.
- C. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

D. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

E. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

10. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 6x + 4$$
 and $g(x) = \frac{1}{4x - 21}$

The solution is The domain is all Real numbers except x = 5.25, which is option C.

- A. The domain is all Real numbers less than or equal to x = a, where $a \in [-1.5, 4.5]$
- B. The domain is all Real numbers greater than or equal to x = a, where $a \in [-6.67, -0.67]$
- C. The domain is all Real numbers except x = a, where $a \in [4.25, 8.25]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [2.83, 7.83]$ and $b \in [-7.33, 1.67]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

11. Choose the interval below that f composed with q at x = -1 is in.

$$f(x) = -x^3 + 3x^2 + 4x$$
 and $g(x) = -4x^3 - 4x^2 + 4x + 3$

The solution is 0.0, which is option B.

A. $(f \circ g)(-1) \in [-7, -4]$

Distractor 3: Corresponds to being slightly off from the solution.

- B. $(f \circ g)(-1) \in [-3, 1]$
 - * This is the correct solution
- C. $(f \circ g)(-1) \in [3, 10]$

Distractor 1: Corresponds to reversing the composition.

D. $(f \circ g)(-1) \in [-12, -8]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

12. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = -2x^3 + 2x^2 - 2x$$
 and $g(x) = x^3 - 2x^2 + x$

The solution is 0.0, which is option A.

- A. $(f \circ g)(1) \in [-0.7, 1.9]$
 - * This is the correct solution
- B. $(f \circ g)(1) \in [-16.8, -11.2]$

Distractor 3: Corresponds to being slightly off from the solution.

C. $(f \circ g)(1) \in [-5.9, -3.1]$

Distractor 2: Corresponds to being slightly off from the solution.

D. $(f \circ g)(1) \in [-19.7, -15.7]$

Distractor 1: Corresponds to reversing the composition.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

13. Determine whether the function below is 1-1.

$$f(x) = 15x^2 - 189x + 594$$

The solution is no, which is option D.

A. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

B. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

C. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

- D. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.
- E. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

14. Find the inverse of the function below. Then, evaluate the inverse at x = 8 and choose the interval that $f^{-}1(8)$ belongs to.

$$f(x) = \ln\left(x - 2\right) - 5$$

The solution is $f^{-1}(8) = 442415.392$, which is option A.

A. $f^{-1}(8) \in [442414.39, 442417.39]$

This is the solution.

B. $f^{-1}(8) \in [22016.47, 22027.47]$

This solution corresponds to distractor 2.

C. $f^{-1}(8) \in [15.09, 25.09]$

This solution corresponds to distractor 1.

D. $f^{-1}(8) \in [396.43, 399.43]$

This solution corresponds to distractor 4.

E. $f^{-1}(8) \in [442405.39, 442412.39]$

This solution corresponds to distractor 3.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

15. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 15 and choose the interval that $f^{-1}(15)$ belongs to.

$$f(x) = \sqrt[3]{4x - 3}$$

The solution is 844.5, which is option A.

- A. $f^{-1}(15) \in [843.5, 844.8]$
 - * This is the correct solution.
- B. $f^{-1}(15) \in [-847.1, -843.8]$

This solution corresponds to distractor 2.

C. $f^{-1}(15) \in [841.1, 843.1]$

Distractor 1: This corresponds to

D. $f^{-1}(15) \in [-843.1, -839.4]$

This solution corresponds to distractor 3.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

16. Find the inverse of the function below. Then, evaluate the inverse at x = 9 and choose the interval that $f^{-}1(9)$ belongs to.

$$f(x) = e^{x+4} - 3$$

The solution is $f^{-1}(9) = -1.515$, which is option B.

A. $f^{-1}(9) \in [-1.44, -1.23]$

This solution corresponds to distractor 3.

B. $f^{-1}(9) \in [-1.58, -1.46]$

This is the solution.

C. $f^{-1}(9) \in [-0.58, -0.38]$

This solution corresponds to distractor 4.

D. $f^{-1}(9) \in [-1.36, -1.19]$

This solution corresponds to distractor 2.

E. $f^{-1}(9) \in [6.47, 6.65]$

This solution corresponds to distractor 1.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

17. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -11 and choose the interval that $f^{-1}(-11)$ belongs to.

$$f(x) = \sqrt[3]{2x+4}$$

The solution is -667.5, which is option C.

A. $f^{-1}(-11) \in [-663.5, -660.5]$

Distractor 1: This corresponds to

B. $f^{-1}(-11) \in [662.5, 664.5]$

This solution corresponds to distractor 3.

- C. $f^{-1}(-11) \in [-674.5, -665.5]$
 - * This is the correct solution.
- D. $f^{-1}(-11) \in [664.5, 668.5]$

This solution corresponds to distractor 2.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

18. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 8x^2 + 8$$
 and $g(x) = \sqrt{3x + 15}$

The solution is The domain is all Real numbers greater than or equal to x = -5.0, which is option A.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [-6, -1]$
- B. The domain is all Real numbers except x = a, where $a \in [0.83, 5.83]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [-0.6, 8.4]$
- D. The domain is all Real numbers except x=a and x=b, where $a\in[-9.67,-1.67]$ and $b\in[-3.75,1.25]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

19. Determine whether the function below is 1-1.

$$f(x) = (5x - 18)^3$$

The solution is yes, which is option A.

- A. Yes, the function is 1-1.
 - * This is the solution.
- B. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

D. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

E. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

20. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 9x^3 + 8x^2 + 6x$$
 and $g(x) = \sqrt{-3x + 10}$

The solution is The domain is all Real numbers less than or equal to x = 3.33, which is option C.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [4.5, 10.5]$
- B. The domain is all Real numbers except x = a, where $a \in [-8.25, 0.75]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [3.33, 4.33]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [3.75, 5.75]$ and $b \in [-6.2, -3.2]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

21. Choose the interval below that f composed with g at x = -2 is in.

$$f(x) = -2x^3 - 4x^2 + x - 1$$
 and $g(x) = -2x^3 - 3x^2 + x$

The solution is -31.0, which is option B.

A. $(f \circ g)(-2) \in [31, 36]$

Distractor 3: Corresponds to being slightly off from the solution.

- B. $(f \circ g)(-2) \in [-34, -26]$
 - * This is the correct solution
- C. $(f \circ g)(-2) \in [24, 26]$

Distractor 1: Corresponds to reversing the composition.

D. $(f \circ g)(-2) \in [-38, -35]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

22. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = 4x^3 + 4x^2 - 2x$$
 and $g(x) = 2x^3 - 2x^2 - 3x - 1$

The solution is -12.0, which is option B.

A. $(f \circ g)(-1) \in [-2, 7]$

Distractor 1: Corresponds to reversing the composition.

B. $(f \circ g)(-1) \in [-17, -9]$

* This is the correct solution

C. $(f \circ g)(-1) \in [5, 16]$

Distractor 3: Corresponds to being slightly off from the solution.

D. $(f \circ g)(-1) \in [-8, -1]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

General Comment: f composed with g at x means f(g(x)). The order matters!

23. Determine whether the function below is 1-1.

$$f(x) = (5x - 26)^3$$

The solution is yes, which is option A.

A. Yes, the function is 1-1.

* This is the solution.

B. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

C. No, because there is a y-value that goes to 2 different x-values.

Corresponds to the Horizontal Line test, which this function passes.

D. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

E. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

24. Find the inverse of the function below. Then, evaluate the inverse at x = 10 and choose the interval that $f^{-1}(10)$ belongs to.

$$f(x) = e^{x-3} - 5$$

The solution is $f^{-1}(10) = 5.708$, which is option A.

A. $f^{-1}(10) \in [5.61, 5.73]$

This is the solution.

B. $f^{-1}(10) \in [-3.24, -2.83]$

This solution corresponds to distractor 4.

C. $f^{-1}(10) \in [-0.54, -0.06]$

This solution corresponds to distractor 1.

D. $f^{-1}(10) \in [-3.66, -3.28]$

This solution corresponds to distractor 2.

E. $f^{-1}(10) \in [-2.64, -2.19]$

This solution corresponds to distractor 3.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

25. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -14 and choose the interval that $f^{-1}(-14)$ belongs to.

$$f(x) = \sqrt[3]{2x - 5}$$

The solution is -1369.5, which is option A.

- A. $f^{-1}(-14) \in [-1373.5, -1362.5]$
 - * This is the correct solution.
- B. $f^{-1}(-14) \in [1371.5, 1375.5]$

This solution corresponds to distractor 3.

C. $f^{-1}(-14) \in [1369.5, 1370.5]$

This solution corresponds to distractor 2.

D. $f^{-1}(-14) \in [-1374.5, -1371.5]$

Distractor 1: This corresponds to

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

26. Find the inverse of the function below. Then, evaluate the inverse at x = 5 and choose the interval that $f^{-1}(5)$ belongs to.

$$f(x) = e^{x-2} - 2$$

The solution is $f^{-1}(5) = 3.946$, which is option A.

A. $f^{-1}(5) \in [3.7, 4.98]$

This is the solution.

B. $f^{-1}(5) \in [-0.07, 1.7]$

This solution corresponds to distractor 1.

C. $f^{-1}(5) \in [-0.93, -0.88]$

This solution corresponds to distractor 2.

D. $f^{-1}(5) \in [-0.93, -0.88]$

This solution corresponds to distractor 4.

E. $f^{-1}(5) \in [-0.07, 1.7]$

This solution corresponds to distractor 3.

General Comment: Natural log and exponential functions always have an inverse. Once you switch the x and y, use the conversion $e^y = x \leftrightarrow y = \ln(x)$.

27. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 10 and choose the interval that $f^{-1}(10)$ belongs to.

$$f(x) = 4x^2 - 5$$

The solution is The function is not invertible for all Real numbers. , which is option E.

A. $f^{-1}(10) \in [0.71, 1.71]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

B. $f^{-1}(10) \in [3.05, 4.01]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

C. $f^{-1}(10) \in [4.69, 5.8]$

Distractor 4: This corresponds to both distractors 2 and 3.

D. $f^{-1}(10) \in [1.81, 2.61]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

- E. The function is not invertible for all Real numbers.
 - * This is the correct option.

General Comment: Be sure you check that the function is 1-1 before trying to find the inverse!

28. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 9x + 7$$
 and $g(x) = \sqrt{-3x - 9}$

The solution is The domain is all Real numbers less than or equal to x = -3.0, which is option B.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [-6.33, -0.33]$
- B. The domain is all Real numbers less than or equal to x = a, where $a \in [-6, 0]$
- C. The domain is all Real numbers except x = a, where $a \in [2.33, 8.33]$
- D. The domain is all Real numbers except x=a and x=b, where $a\in[-7.83,-1.83]$ and $b\in[1.2,7.2]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.

29. Determine whether the function below is 1-1.

$$f(x) = -12x^2 - 167x - 575$$

The solution is no, which is option D.

A. No, because the domain of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the domain is all Real numbers.

B. No, because the range of the function is not $(-\infty, \infty)$.

Corresponds to believing 1-1 means the range is all Real numbers.

C. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- D. No, because there is a y-value that goes to 2 different x-values.
 - * This is the solution.
- E. No, because there is an x-value that goes to 2 different y-values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

General Comment: There are only two valid options: The function is 1-1 OR No because there is a y-value that goes to 2 different x-values.

30. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 3x^4 + 6x^3 + 4x^2 + 5x$$
 and $g(x) = \sqrt{-6x - 18}$

The solution is The domain is all Real numbers less than or equal to x = -3.0, which is option C.

- A. The domain is all Real numbers greater than or equal to x = a, where $a \in [-8.83, -0.83]$
- B. The domain is all Real numbers except x = a, where $a \in [5.33, 6.33]$
- C. The domain is all Real numbers less than or equal to x = a, where $a \in [-7, 1]$
- D. The domain is all Real numbers except x = a and x = b, where $a \in [-1.17, 4.83]$ and $b \in [5.25, 11.25]$
- E. The domain is all Real numbers.

General Comment: The new domain is the intersection of the previous domains.