This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$5 + 6x < \frac{36x + 4}{4} \le 4 + 8x$$

The solution is None of the above., which is option E.

- A. $(-\infty, a) \cup [b, \infty)$, where $a \in [-4.5, 0.75]$ and $b \in [-5.25, 2.25]$
 - $(-\infty, -1.33) \cup [-3.00, \infty)$, which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.
- B. $(-\infty, a] \cup (b, \infty)$, where $a \in [-2.55, 0.38]$ and $b \in [-6.75, -1.5]$
 - $(-\infty, -1.33] \cup (-3.00, \infty)$, which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.
- C. [a, b), where $a \in [-1.72, -0.22]$ and $b \in [-5.25, 2.25]$
 - [-1.33, -3.00), which corresponds to flipping the inequality and getting negatives of the actual endpoints.
- D. (a, b], where $a \in [-4.5, -0.75]$ and $b \in [-7.5, 0]$
 - (-1.33, -3.00], which is the correct interval but negatives of the actual endpoints.
- E. None of the above.
 - * This is correct as the answer should be (1.33, 3.00].

General Comment: To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

2. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-5}{4} - \frac{7}{8}x \le \frac{-4}{5}x + \frac{8}{3}$$

The solution is $[-52.222, \infty)$, which is option C.

- A. $(-\infty, a]$, where $a \in [51.75, 54.75]$
 - $(-\infty, 52.222]$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.
- B. $[a, \infty)$, where $a \in [51, 53.25]$

 $[52.222, \infty)$, which corresponds to negating the endpoint of the solution.

- C. $[a, \infty)$, where $a \in [-54.75, -51.75]$
 - * $[-52.222, \infty)$, which is the correct option.

- D. $(-\infty, a]$, where $a \in [-54, -46.5]$
 - $(-\infty, -52.222]$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

3. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-10x + 8 > 6x - 5$$

The solution is $(-\infty, 0.812)$, which is option C.

- A. (a, ∞) , where $a \in [-0.3, 1.8]$
 - $(0.812, \infty)$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- B. (a, ∞) , where $a \in [-1.8, -0.1]$
 - $(-0.812, \infty)$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.
- C. $(-\infty, a)$, where $a \in [-0.4, 2.4]$
 - * $(-\infty, 0.812)$, which is the correct option.
- D. $(-\infty, a)$, where $a \in [-1.5, 0.2]$
 - $(-\infty, -0.812)$, which corresponds to negating the endpoint of the solution.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-10x + 4 < 7x + 7$$

The solution is $[-0.176, \infty)$, which is option B.

- A. $(-\infty, a]$, where $a \in [-0.27, -0.05]$
 - $(-\infty, -0.176]$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- B. $[a, \infty)$, where $a \in [-0.38, -0]$
 - * $[-0.176, \infty)$, which is the correct option.
- C. $[a, \infty)$, where $a \in [0.03, 0.36]$

 $[0.176, \infty)$, which corresponds to negating the endpoint of the solution.

D. $(-\infty, a]$, where $a \in [-0.06, 0.27]$

 $(-\infty, 0.176]$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

5. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 5 units from the number -10.

The solution is [-15, -5], which is option C.

A. (-15, -5)

This describes the values less than 5 from -10

B. $(-\infty, -15) \cup (-5, \infty)$

This describes the values more than 5 from -10

C. [-15, -5]

This describes the values no more than 5 from -10

D. $(-\infty, -15] \cup [-5, \infty)$

This describes the values no less than 5 from -10

E. None of the above

You likely thought the values in the interval were not correct.

General Comment: When thinking about this language, it helps to draw a number line and try points.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-4 - 3x < \frac{-22x + 6}{9} \le -7 - 5x$$

The solution is None of the above., which is option E

A. $(-\infty, a] \cup (b, \infty)$, where $a \in [6, 13.5]$ and $b \in [-1.5, 6]$

 $(-\infty, 8.40] \cup (3.00, \infty)$, which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

B. [a, b), where $a \in [3, 9.75]$ and $b \in [2.25, 5.25]$

[8.40, 3.00), which corresponds to flipping the inequality and getting negatives of the actual endpoints.

C. (a, b], where $a \in [3.75, 9.75]$ and $b \in [-0.75, 5.25]$

(8.40, 3.00], which is the correct interval but negatives of the actual endpoints.

- D. $(-\infty, a) \cup [b, \infty)$, where $a \in [6.75, 13.5]$ and $b \in [2.25, 6]$
 - $(-\infty, 8.40) \cup [3.00, \infty)$, which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.
- E. None of the above.
 - * This is correct as the answer should be (-8.40, -3.00].

General Comment: To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3 + 4x > 7x$$
 or $5 + 9x < 10x$

The solution is $(-\infty, -1.0)$ or $(5.0, \infty)$, which is option D.

A. $(-\infty, a] \cup [b, \infty)$, where $a \in [-2.25, 1.5]$ and $b \in [4.5, 6.75]$

Corresponds to including the endpoints (when they should be excluded).

B. $(-\infty, a) \cup (b, \infty)$, where $a \in [-7.95, -3.23]$ and $b \in [-0.75, 4.5]$

Corresponds to inverting the inequality and negating the solution.

C. $(-\infty, a] \cup [b, \infty)$, where $a \in [-8.25, -3]$ and $b \in [-1.5, 3]$

Corresponds to including the endpoints AND negating.

- D. $(-\infty, a) \cup (b, \infty)$, where $a \in [-1.43, 1.43]$ and $b \in [3, 10.5]$
 - * Correct option.
- E. $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$5 + 4x > 7x$$
 or $7 + 4x < 5x$

The solution is $(-\infty, 1.667)$ or $(7.0, \infty)$, which is option D.

A. $(-\infty, a] \cup [b, \infty)$, where $a \in [-2.25, 6]$ and $b \in [4.5, 9.75]$

Corresponds to including the endpoints (when they should be excluded).

B. $(-\infty, a] \cup [b, \infty)$, where $a \in [-10.5, -6]$ and $b \in [-4.5, 0]$

Corresponds to including the endpoints AND negating.

C. $(-\infty, a) \cup (b, \infty)$, where $a \in [-9.75, -3]$ and $b \in [-5.25, -1.5]$

Corresponds to inverting the inequality and negating the solution.

- D. $(-\infty, a) \cup (b, \infty)$, where $a \in [0.75, 4.5]$ and $b \in [3, 10.5]$
 - * Correct option.
- E. $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{8}{2} - \frac{10}{3}x > \frac{5}{6}x - \frac{9}{5}$$

The solution is $(-\infty, 1.392)$, which is option A.

A. $(-\infty, a)$, where $a \in [-0.75, 3.75]$

* $(-\infty, 1.392)$, which is the correct option.

B. $(-\infty, a)$, where $a \in [-6.75, 0]$

 $(-\infty, -1.392)$, which corresponds to negating the endpoint of the solution.

C. (a, ∞) , where $a \in [0, 3.75]$

 $(1.392, \infty)$, which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D. (a, ∞) , where $a \in [-2.25, 0]$

 $(-1.392, \infty)$, which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

General Comment: Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

10. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

Less than 9 units from the number 6.

The solution is (-3, 15), which is option D.

A.
$$(-\infty, -3) \cup (15, \infty)$$

This describes the values more than 9 from 6

B. [-3, 15]

This describes the values no more than 9 from 6

C. $(-\infty, -3] \cup [15, \infty)$

This describes the values no less than 9 from 6

D. (-3, 15)

This describes the values less than 9 from 6

E. None of the above

You likely thought the values in the interval were not correct.

General Comment: When thinking about this language, it helps to draw a number line and try points.