This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$4 + 8x > 11x \text{ or } 5 + 3x < 5x$$

The solution is  $(-\infty, 1.333)$  or  $(2.5, \infty)$ , which is option C.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-2.25, 3.75]$  and  $b \in [0, 5.25]$ 

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-7.5, -2.25]$  and  $b \in [-6.75, 0.75]$ 

Corresponds to including the endpoints AND negating.

- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-0.75, 3.75]$  and  $b \in [2.25, 3.75]$ 
  - \* Correct option.
- D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-4.5, -1.5]$  and  $b \in [-5.25, 2.25]$

Corresponds to inverting the inequality and negating the solution.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.

2. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-6}{9} - \frac{7}{7}x \le \frac{-5}{2}x + \frac{8}{8}$$

The solution is  $(-\infty, 1.111]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [0.6, 1.65]$ 
  - \*  $(-\infty, 1.111]$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [-2.48, -0.67]$

 $(-\infty, -1.111]$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [0, 2.25]$ 

 $[1.111, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D.  $[a, \infty)$ , where  $a \in [-2.25, 0]$ 

 $[-1.111, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

3. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No more than 2 units from the number 3.

The solution is [1, 5], which is option A.

A. [1, 5]

This describes the values no more than 2 from 3

B.  $(-\infty, 1] \cup [5, \infty)$ 

This describes the values no less than 2 from 3

C. (1,5)

This describes the values less than 2 from 3

D.  $(-\infty,1)\cup(5,\infty)$ 

This describes the values more than 2 from 3

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5 - 6x \le \frac{-20x - 9}{4} < 8 - 6x$$

The solution is None of the above., which is option E.

A.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [1.5, 4.5]$  and  $b \in [-12, -9]$ 

 $(-\infty, 2.75] \cup (-10.25, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

B. [a, b), where  $a \in [1.5, 3.75]$  and  $b \in [-12, -9]$ 

[2.75, -10.25), which is the correct interval but negatives of the actual endpoints.

C.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [1.5, 6]$  and  $b \in [-11.25, -6]$ 

 $(-\infty, 2.75) \cup [-10.25, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

D. (a, b], where  $a \in [2.25, 7.5]$  and  $b \in [-12.75, -6.75]$ 

(2.75, -10.25], which corresponds to flipping the inequality and getting negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be [-2.75, 10.25).

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-8 + 4x > 6x$$
 or  $-3 + 3x < 4x$ 

The solution is  $(-\infty, -4.0)$  or  $(-3.0, \infty)$ , which is option C.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [2.25, 7.5]$  and  $b \in [3.75, 4.5]$ 

Corresponds to including the endpoints AND negating.

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-6, -1.5]$  and  $b \in [-3.75, -2.25]$ 

Corresponds to including the endpoints (when they should be excluded).

- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-10.5, -3]$  and  $b \in [-6, -2.25]$ 
  - \* Correct option.
- D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-1.5, 3.75]$  and  $b \in [1.5, 6]$

Corresponds to inverting the inequality and negating the solution.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-10x - 6 \le -9x + 5$$

The solution is  $[-11.0, \infty)$ , which is option B.

A.  $(-\infty, a]$ , where  $a \in [-13, -8]$ 

 $(-\infty, -11.0]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $[a, \infty)$ , where  $a \in [-11, -4]$ 

\*  $[-11.0, \infty)$ , which is the correct option.

C.  $[a, \infty)$ , where  $a \in [10, 14]$ 

 $[11.0,\infty)$ , which corresponds to negating the endpoint of the solution.

D.  $(-\infty, a]$ , where  $a \in [9, 12]$ 

 $(-\infty, 11.0]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6x - 4 \le 3x + 10$$

The solution is  $[-1.556, \infty)$ , which is option C.

A.  $[a, \infty)$ , where  $a \in [0.56, 6.56]$ 

 $[1.556, \infty)$ , which corresponds to negating the endpoint of the solution.

B.  $(-\infty, a]$ , where  $a \in [-4.56, 0.44]$ 

 $(-\infty, -1.556]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

C.  $[a, \infty)$ , where  $a \in [-1.56, -0.56]$ 

\*  $[-1.556, \infty)$ , which is the correct option.

D.  $(-\infty, a]$ , where  $a \in [-0.44, 8.56]$ 

 $(-\infty, 1.556]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 - 9x \le \frac{-15x + 9}{3} < 7 - 6x$$

The solution is None of the above., which is option E.

A.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [2.25, 6]$  and  $b \in [-6, -2.25]$ 

 $(-\infty, 2.50] \cup (-4.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

B. [a, b), where  $a \in [-1.5, 8.25]$  and  $b \in [-4.5, -1.5]$ 

[2.50, -4.00), which is the correct interval but negatives of the actual endpoints.

C. (a, b], where  $a \in [0.75, 5.25]$  and  $b \in [-7.5, -2.25]$ 

(2.50, -4.00], which corresponds to flipping the inequality and getting negatives of the actual endpoints.

D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-2.25, 3]$  and  $b \in [-5.25, -3]$ 

 $(-\infty, 2.50) \cup [-4.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be [-2.50, 4.00).

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

9. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

Less than 4 units from the number -10.

The solution is (-14, -6), which is option D.

A. 
$$(-\infty, -14] \cup [-6, \infty)$$

This describes the values no less than 4 from -10

B. 
$$(-\infty, -14) \cup (-6, \infty)$$

This describes the values more than 4 from -10

C. 
$$[-14, -6]$$

This describes the values no more than 4 from -10

D. 
$$(-14, -6)$$

This describes the values less than 4 from -10

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{-9}{2} - \frac{5}{8}x \ge \frac{6}{4}x + \frac{10}{6}$$

The solution is  $(-\infty, -2.902]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [-6.75, -2.25]$ 
  - \*  $(-\infty, -2.902]$ , which is the correct option.
- B.  $(-\infty, a]$ , where  $a \in [2.25, 6.75]$

 $(-\infty, 2.902]$ , which corresponds to negating the endpoint of the solution.

C.  $[a, \infty)$ , where  $a \in [-6, -0.75]$ 

 $[-2.902, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

D.  $[a, \infty)$ , where  $a \in [-0.75, 6.75]$ 

 $[2.902, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.