

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 42 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 12 percent, which is option C.

- A. About 21 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

- B. About 3 percent

This corresponds to not solving for the increase properly.

- C. About 12 percent

* This is the correct option.

- D. About 19 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

- E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

2. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 33 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 10 percent, which is option B.

- A. About 3 percent

This corresponds to not solving for the increase properly.

- B. About 10 percent

* This is the correct option.

- C. About 15 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

D. About 16 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

3. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has doubled every 4 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 43 days, which is option A.

A. About 43 days

* This is the correct option.

B. About 15 days

You modeled the situation correctly but did not apply the properties of log correctly.

C. About 30 days

You modeled the situation with e as the base, but solved correctly otherwise.

D. About 14 days

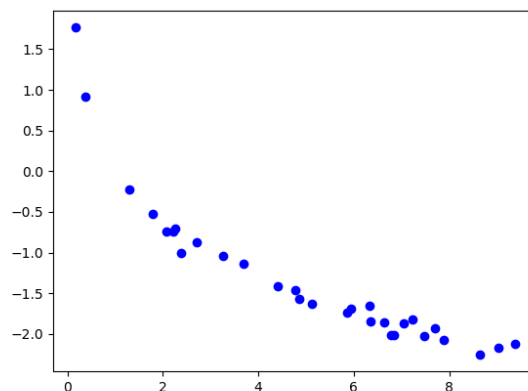
You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

4. Determine the appropriate model for the graph of points below.



The solution is Logarithmic model, which is option A.

A. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

B. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

C. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

D. Linear model

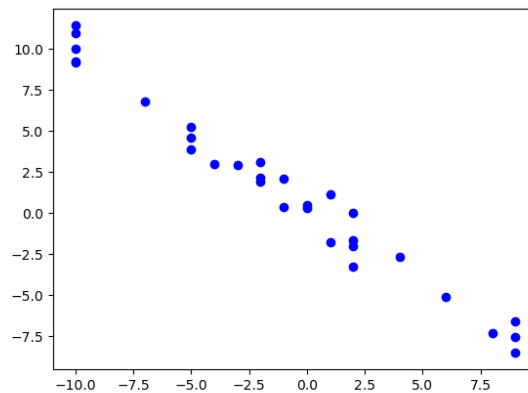
For this to be the correct option, we need to see a mostly straight line of points.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

5. Determine the appropriate model for the graph of points below.



The solution is Linear model, which is option B.

A. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

B. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

C. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

D. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

6. **General Comment:** None

7. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 18 liter 31 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 15 percent and 37 percent solutions, what was the amount she used of the 37 percent solution?

The solution is 13.09liters, which is option D.

A. 9.00liters

This would be correct if Brittany used equal parts of each solution.

B. 7.93liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

C. 4.91liters

This is the concentration of 15 percent solution.

D. 13.09liters

*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

8. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 5 many cases reported, but the number of confirmed cases has tripled every 4 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 28 days, which is option C.

A. About 31 days

You modeled the situation with e as the base, but solved correctly otherwise.

B. About 15 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

C. About 28 days

* This is the correct option.

D. About 14 days

You modeled the situation correctly but did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

9. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 16 liter 26 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 20 percent and 38 percent solutions, what was the amount she used of the 38 percent solution?

The solution is 5.33liters, which is option D.

A. 10.67liters

This is the concentration of 20 percent solution.

B. 8.00liters

This would be correct if Brittany used equal parts of each solution.

C. 5.26liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

D. 5.33liters

*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

10. For the information below, construct a linear model that describes the total time T spent on the path in terms of the distance of a particular part of the path *if we know that all parts of the path are equal length.*

A bicyclist is training for a race on a hilly path. Their bike keeps track of their speed at any time, but not the distance traveled. Their speed traveling up a hill is 6 mph, 10 mph when traveling down a hill, and 8 mph when traveling along a flat portion.

The solution is $0.392D$, which is option C.

A. $24.000D$

The coefficient here is calculated as if you were trying to model the distance on the total path.

B. $480.000D$

The coefficient here is calculated by multiplying the distances together rather than adding.

C. $0.392D$

* This is the correct option.

D. The model can be found with the information provided, but isn't options 1-3.

Since we know all parts of the path are equal length, we can treat all distance variables as the same variable, D .

E. The model cannot be found with the information provided.

If you chose this option, please contact the coordinator to discuss why you think we cannot model the situation.

General Comment: Be sure you pay attention to the variable we are writing the model in terms of. To create the model with a single variable, we have to know that variable is the same throughout each path!

11. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 26 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 8 percent, which is option A.

A. About 8 percent

* This is the correct option.

B. About 3 percent

This corresponds to not solving for the increase properly.

C. About 12 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

D. About 13 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

12. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 38 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 11 percent, which is option C.

A. About 19 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

B. About 3 percent

This corresponds to not solving for the increase properly.

C. About 11 percent

* This is the correct option.

D. About 17 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

13. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has doubled every 2 days. How long will it be until there are at least 1000 confirmed cases?

The solution is About 15 days, which is option A.

A. About 15 days

* This is the correct option.

B. About 6 days

You modeled the situation correctly but did not apply the properties of log correctly.

C. About 11 days

You modeled the situation with e as the base, but solved correctly otherwise.

D. About 5 days

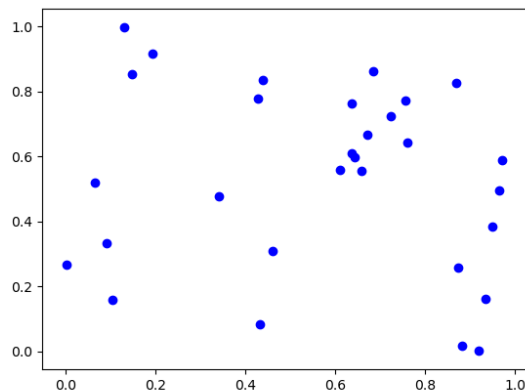
You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 1000 and solve for d in your model.

14. Determine the appropriate model for the graph of points below.



The solution is None of the above, which is option E.

A. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

B. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

C. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

D. Exponential model

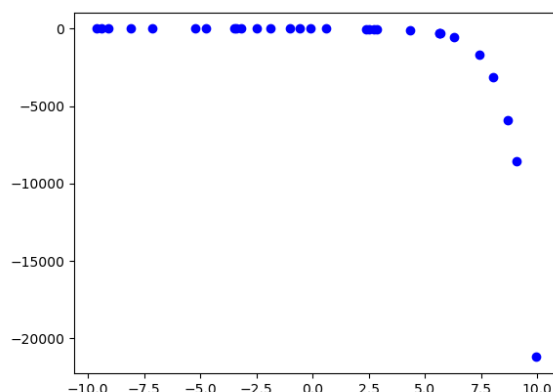
For this to be the correct option, we want an extremely slow change early, then a rapid change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

15. Determine the appropriate model for the graph of points below.



The solution is Exponential model, which is option D.

A. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

B. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

C. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

D. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

16. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string ω decreases as the quartic length of the string increases. For example, when string ω is 4 mm long, the rate of vibration is 29 cm/s.

The solution is $k = 0.74$, which is option B.

A. $k = 1132.81$

This option uses the model $R = kl^4$ as if this is a direct variation.

B. $k = 0.74$

* This is the correct option, which corresponds to the model $R = \frac{k}{l^4}$ AND converts from mm to cm.

C. $k = 7424.00$

This option uses the correct model, $R = \frac{k}{l^4}$, but does not convert from mm to cm so that the units match.

D. $k = 0.11$

This option uses the model $R = kl^4$ as if this is a direct variation AND does not convert from mm to cm so that the units match.

E. None of the above.

Talk with the coordinator if you chose this option.

General Comment: The most common mistake on this question is to not convert mm to cm! When modeling, you need to make sure all of the units for your variables are compatible.

17. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 25 liter 34 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 15 percent and 45 percent solutions, what was the amount she used of the 15 percent solution?

The solution is 9.17liters, which is option C.

A. 11.27liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 12.50liters

This would be correct if Brittany used equal parts of each solution.

C. 9.17liters

*This is the correct option.

D. 15.83liters

This is the concentration of 45 percent solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

18. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 4 many cases reported, but the number of confirmed cases has quadrupled every 2 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 18 days, which is option A.

A. About 18 days

* This is the correct option.

B. About 12 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

C. About 10 days

You modeled the situation correctly but did not apply the properties of log correctly.

D. About 25 days

You modeled the situation with e as the base, but solved correctly otherwise.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

19. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 15 liter 9 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 7 percent and 28 percent solutions, what was the amount she used of the 28 percent solution?

The solution is 1.43liters, which is option C.

A. 2.11liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

B. 13.57liters

This is the concentration of 7 percent solution.

C. 1.43liters

*This is the correct option.

D. 7.50liters

This would be correct if Brittany used equal parts of each solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

20. **General Comment:** None

21. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 45 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 13 percent, which is option D.

A. About 22 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

B. About 4 percent

This corresponds to not solving for the increase properly.

C. About 20 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

D. About 13 percent

* This is the correct option.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

22. For the scenario below, use the model for the volume of a cylinder as $V = \pi r^2 h$.

Pringles wants to add 41 percent more chips to their cylinder cans and minimize the design change of their cans. They've decided that the best way to minimize the design change is to increase the radius and height by the same percentage. What should this increase be?

The solution is About 12 percent, which is option B.

A. About 20 percent

This corresponds to treating both radius and height as equal contributors and not solving correctly.

B. About 12 percent

* This is the correct option.

C. About 14 percent

This corresponds to not solving for the increase properly.

D. About 19 percent

This corresponds to solving correctly but treating both radius and height as equal contributors to the volume.

E. None of the above

If you chose this, please contact the coordinator to discuss how you solved the problem.

General Comment: Remember that when plugging the increases of values in, you need to treat it as that percentage above 100. For example, a 5 percent increase means 105 percent.

23. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has tripled every 4 days. How long will it be until there are at least 10000 confirmed cases?

The solution is About 28 days, which is option D.

A. About 14 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

B. About 30 days

You modeled the situation with e as the base, but solved correctly otherwise.

C. About 13 days

You modeled the situation correctly but did not apply the properties of log correctly.

D. About 28 days

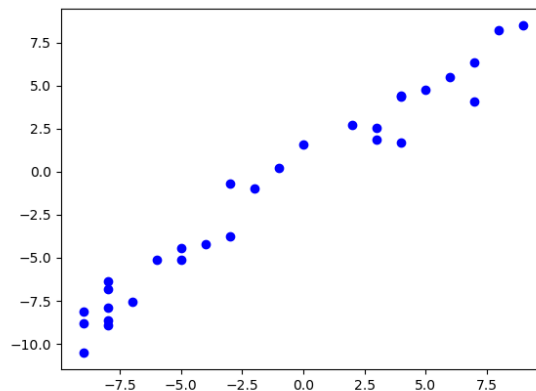
* This is the correct option.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 10000 and solve for d in your model.

24. Determine the appropriate model for the graph of points below.



The solution is Linear model, which is option A.

A. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

B. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

C. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

D. Non-linear Power model

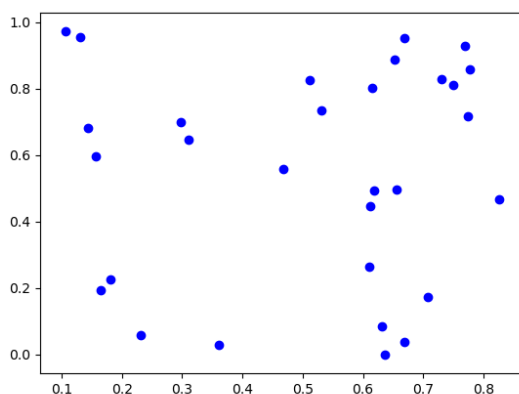
For this to be the correct option, we need to see a polynomial or rational shape.

E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

25. Determine the appropriate model for the graph of points below.



The solution is None of the above, which is option E.

- A. Logarithmic model

For this to be the correct option, we want a rapid change early, then an extremely slow change later.

- B. Non-linear Power model

For this to be the correct option, we need to see a polynomial or rational shape.

- C. Linear model

For this to be the correct option, we need to see a mostly straight line of points.

- D. Exponential model

For this to be the correct option, we want an extremely slow change early, then a rapid change later.

- E. None of the above

For this to be the correct option, we want to see no pattern in the points.

General Comment: This question is testing if you can associate the models with their graphical representation. If you are having trouble, go back to the corresponding Core module to learn about the specific function you are having trouble recognizing.

26. For the information below, construct a linear model that describes the total time T spent on the path in terms of the distance of a particular part of the path *if we know that all parts of the path are equal length*.

A bicyclist is training for a race on a hilly path. Their bike keeps track of their speed at any time, but not the distance traveled. Their speed traveling up a hill is 6 mph, 11 mph when traveling down a hill, and 8 mph when traveling along a flat portion.

The solution is $0.383D$, which is option C.

A. $25.000D$

The coefficient here is calculated as if you were trying to model the distance on the total path.

B. $528.000D$

The coefficient here is calculated by multiplying the distances together rather than adding.

C. $0.383D$

* This is the correct option.

D. The model can be found with the information provided, but isn't options 1-3.

Since we know all parts of the path are equal length, we can treat all distance variables as the same variable, D .

E. The model cannot be found with the information provided.

If you chose this option, please contact the coordinator to discuss why you think we cannot model the situation.

General Comment: Be sure you pay attention to the variable we are writing the model in terms of. To create the model with a single variable, we have to know that variable is the same throughout each path!

27. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 15 liter 14 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 9 percent and 26 percent solutions, what was the amount she used of the 9 percent solution?

The solution is 10.59liters, which is option D.

A. 4.41liters

This is the concentration of 26 percent solution.

B. 4.66liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

C. 7.50liters

This would be correct if Brittany used equal parts of each solution.

D. 10.59liters

*This is the correct option.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

28. Solve the modeling problem below, if possible.

A new virus is spreading throughout the world. There were initially 6 many cases reported, but the number of confirmed cases has quadrupled every 3 days. How long will it be until there are at least 1000000 confirmed cases?

The solution is About 27 days, which is option B.

A. About 14 days

You modeled the situation correctly but did not apply the properties of log correctly.

B. About 27 days

* This is the correct option.

C. About 37 days

You modeled the situation with e as the base, but solved correctly otherwise.

D. About 15 days

You modeled the situation with e as the base and did not apply the properties of log correctly.

E. There is not enough information to solve the problem.

If you chose this option, please contact the coordinator to discuss why you think this is the case.

General Comment: Set up the model the same as in Module 11M. Then, plug in 1000000 and solve for d in your model.

29. Solve the modeling problem below, if possible.

In CHM2045L, Brittany created a 24 liter 11 percent solution of chemical χ using two different solution percentages of chemical χ . When she went to write her lab report, she realized she forgot to write the amount of each solution she used! If she remembers she used 10 percent and 40 percent solutions, what was the amount she used of the 40 percent solution?

The solution is 0.80liters, which is option B.

A. 12.00liters

This would be correct if Brittany used equal parts of each solution.

B. 0.80liters

*This is the correct option.

C. 21.49liters

This was a random value. If this was not a guess, contact the coordinator to talk about how you got this value.

D. 23.20liters

This is the concentration of 10 percent solution.

E. There is not enough information to solve the problem.

You may have chose this if you thought you needed to know how much of the second solution was used in the problem. Remember that the total minus the first solution would give you the second amount used.

General Comment: Build the model exactly as you did in Module 9M. Then, solve for the volume you are looking for.

30. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the square of the time, T (Earth years), required for a planet to orbit Sun χ increases as the cube of the distance, d (AUs), that the planet is from Sun χ increases. For example, when Ea's average distance from Sun χ is 5, it takes 73 Earth days to complete an orbit.

The solution is $k = 42.632$, which is option B.

- A. $k = 666125.000$

This corresponds to the model $T^2 = \frac{k}{d^3}$.

- B. $k = 42.632$

* This is the correct option corresponding to the model $T^2 = kd^3$.

- C. $k = 4.997$

This corresponds to the model $T^{1/2} = kd^{1/3}$.

- D. $k = 4.028$

This copies the constant used in the homework.

- E. Unable to compute the constant based on the information given.

This corresponds to believing you cannot determine the type of model from the information given.

General Comment: Since T increases proportionally as d increases, we know this is a direct variation model.
