

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

1. Choose the interval below that  $f$  composed with  $g$  at  $x = -1$  is in.

$$f(x) = x^3 - 3x^2 - 2x + 1 \text{ and } g(x) = 4x^3 + 4x^2 - x$$

The solution is  $-3.0$ , which is option B.

- A.  $(f \circ g)(-1) \in [9.3, 10.38]$

Distractor 3: Corresponds to being slightly off from the solution.

- B.  $(f \circ g)(-1) \in [-3.32, -2.98]$

\* This is the correct solution

- C.  $(f \circ g)(-1) \in [1.64, 2.57]$

Distractor 2: Corresponds to being slightly off from the solution.

- D.  $(f \circ g)(-1) \in [-0.35, 1.66]$

Distractor 1: Corresponds to reversing the composition.

- E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

2. Determine whether the function below is 1-1.

$$f(x) = 36x^2 + 480x + 1600$$

The solution is no, which is option A.

- A. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

- B. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- C. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

- D. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

- E. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

3. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \sqrt{-4x + 11} \text{ and } g(x) = 6x + 4$$

The solution is The domain is all Real numbers less than or equal to  $x = 2.75$ ., which is option A.

- A. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-0.25, 5.75]$
- B. The domain is all Real numbers except  $x = a$ , where  $a \in [-6.8, -0.8]$
- C. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-12.4, -2.4]$
- D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-9.4, -1.4]$  and  $b \in [2.33, 14.33]$
- E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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4. Find the inverse of the function below. Then, evaluate the inverse at  $x = 10$  and choose the interval that  $f^{-1}(10)$  belongs to.

$$f(x) = e^{x-5} + 2$$

The solution is  $f^{-1}(10) = 7.079$ , which is option B.

- A.  $f^{-1}(10) \in [3.11, 3.77]$

This solution corresponds to distractor 4.

- B.  $f^{-1}(10) \in [6.93, 7.45]$

This is the solution.

- C.  $f^{-1}(10) \in [-2.94, -2.59]$

This solution corresponds to distractor 1.

- D.  $f^{-1}(10) \in [4.02, 4.57]$

This solution corresponds to distractor 2.

- E.  $f^{-1}(10) \in [4.57, 4.97]$

This solution corresponds to distractor 3.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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5. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -13$  and choose the interval that  $f^{-1}(-13)$  belongs to.

$$f(x) = \sqrt[3]{3x + 5}$$

The solution is  $-734.0$ , which is option C.

- A.  $f^{-1}(-13) \in [722.67, 732.67]$

This solution corresponds to distractor 3.

- B.  $f^{-1}(-13) \in [734, 740]$

This solution corresponds to distractor 2.

- C.  $f^{-1}(-13) \in [-735, -733]$

\* This is the correct solution.

D.  $f^{-1}(-13) \in [-732.67, -723.67]$

Distractor 1: This corresponds to

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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6. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = 2x^3 - 1x^2 + 4x - 4 \text{ and } g(x) = -2x^3 + x^2 + 2x + 1$$

The solution is 16.0, which is option A.

A.  $(f \circ g)(1) \in [15, 25]$

\* This is the correct solution

B.  $(f \circ g)(1) \in [-8, -5]$

Distractor 3: Corresponds to being slightly off from the solution.

C.  $(f \circ g)(1) \in [-1, 3]$

Distractor 1: Corresponds to reversing the composition.

D.  $(f \circ g)(1) \in [23, 36]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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7. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 8x^4 + 8x^3 + 4x^2 + x \text{ and } g(x) = \frac{5}{5x + 22}$$

The solution is The domain is all Real numbers except  $x = -4.4$ , which is option A.

A. The domain is all Real numbers except  $x = a$ , where  $a \in [-6.4, 0.6]$

B. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-8.33, -0.33]$

C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [-1.17, 6.83]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [3.67, 16.67]$  and  $b \in [-9.17, -5.17]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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8. Find the inverse of the function below. Then, evaluate the inverse at  $x = 8$  and choose the interval that  $f^{-1}(8)$  belongs to.

$$f(x) = e^{x+2} + 5$$

The solution is  $f^{-1}(8) = -0.901$ , which is option C.

A.  $f^{-1}(8) \in [6.73, 6.89]$

This solution corresponds to distractor 3.

B.  $f^{-1}(8) \in [7.35, 7.89]$

This solution corresponds to distractor 2.

C.  $f^{-1}(8) \in [-1.17, -0.58]$

This is the solution.

D.  $f^{-1}(8) \in [2.92, 3.25]$

This solution corresponds to distractor 1.

E.  $f^{-1}(8) \in [6.92, 7.48]$

This solution corresponds to distractor 4.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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9. Determine whether the function below is 1-1.

$$f(x) = 20x^2 - 68x - 736$$

The solution is no, which is option C.

- A. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- B. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

- C. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

- D. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

- E. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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10. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -10$  and choose the interval that  $f^{-1}(-10)$  belongs to.

$$f(x) = 4x^2 - 5$$

The solution is The function is not invertible for all Real numbers. , which is option E.

- A.  $f^{-1}(-10) \in [1.26, 2.12]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

- B.  $f^{-1}(-10) \in [2.98, 3.66]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

- C.  $f^{-1}(-10) \in [1.05, 1.21]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

D.  $f^{-1}(-10) \in [3.84, 4.42]$

Distractor 4: This corresponds to both distractors 2 and 3.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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11. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = 2x^3 + x^2 - 3x \text{ and } g(x) = -x^3 + 2x^2 - 3x$$

The solution is  $-6.0$ , which is option A.

A.  $(f \circ g)(1) \in [-8, -5]$

\* This is the correct solution

B.  $(f \circ g)(1) \in [-8, -5]$

Distractor 3: Corresponds to being slightly off from the solution.

C.  $(f \circ g)(1) \in [-3, 2]$

Distractor 1: Corresponds to reversing the composition.

D.  $(f \circ g)(1) \in [-16, -10]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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12. Determine whether the function below is 1-1.

$$f(x) = 16x^2 - 80x + 100$$

The solution is no, which is option D.

A. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

B. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

C. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

D. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

E. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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13. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \sqrt{-3x + 12} \text{ and } g(x) = 5x + 5$$

The solution is The domain is all Real numbers less than or equal to  $x = 4.0$ , which is option C.

- A. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-6.25, -2.25]$
- B. The domain is all Real numbers except  $x = a$ , where  $a \in [-6.4, 0.6]$
- C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [4, 6]$
- D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [-7.8, -0.8]$  and  $b \in [3.75, 7.75]$
- E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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14. Find the inverse of the function below. Then, evaluate the inverse at  $x = 8$  and choose the interval that  $f^{-1}(8)$  belongs to.

$$f(x) = e^{x+4} - 2$$

The solution is  $f^{-1}(8) = -1.697$ , which is option D.

- A.  $f^{-1}(8) \in [-0.66, -0.48]$

This solution corresponds to distractor 3.

- B.  $f^{-1}(8) \in [6.02, 6.73]$

This solution corresponds to distractor 1.

- C.  $f^{-1}(8) \in [-0.35, -0.08]$

This solution corresponds to distractor 2.

- D.  $f^{-1}(8) \in [-1.75, -1.28]$

This is the solution.

- E.  $f^{-1}(8) \in [0.38, 0.63]$

This solution corresponds to distractor 4.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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15. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -12$  and choose the interval that  $f^{-1}(-12)$  belongs to.

$$f(x) = 4x^2 - 3$$

The solution is The function is not invertible for all Real numbers. , which is option E.

- A.  $f^{-1}(-12) \in [3.32, 4.02]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

- B.  $f^{-1}(-12) \in [1.6, 2.66]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

- C.  $f^{-1}(-12) \in [5.18, 5.92]$

Distractor 4: This corresponds to both distractors 2 and 3.

D.  $f^{-1}(-12) \in [1.28, 1.69]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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16. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = -2x^3 + 2x^2 + 3x - 1 \text{ and } g(x) = -x^3 + 2x^2 - 2x + 4$$

The solution is  $-28.0$ , which is option B.

A.  $(f \circ g)(1) \in [-7, 5]$

Distractor 1: Corresponds to reversing the composition.

B.  $(f \circ g)(1) \in [-28, -27]$

\* This is the correct solution

C.  $(f \circ g)(1) \in [-14, -6]$

Distractor 3: Corresponds to being slightly off from the solution.

D.  $(f \circ g)(1) \in [-26, -22]$

Distractor 2: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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17. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 5x^2 + 3x + 3 \text{ and } g(x) = 2x^4 + x^3 + 7x^2 + 8x + 9$$

The solution is  $(-\infty, \infty)$ , which is option E.

A. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [3.5, 8.5]$

B. The domain is all Real numbers except  $x = a$ , where  $a \in [4.8, 6.8]$

C. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-12.67, -5.67]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [4.2, 8.2]$  and  $b \in [-10.6, -2.6]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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18. Find the inverse of the function below. Then, evaluate the inverse at  $x = 5$  and choose the interval that  $f^{-1}(5)$  belongs to.

$$f(x) = e^{x+2} - 3$$

The solution is  $f^{-1}(5) = 0.079$ , which is option C.

A.  $f^{-1}(5) \in [-2.77, -1.99]$

This solution corresponds to distractor 2.

B.  $f^{-1}(5) \in [-1.09, -0.58]$

This solution corresponds to distractor 4.

C.  $f^{-1}(5) \in [-0.74, 0.63]$

This is the solution.

D.  $f^{-1}(5) \in [-1.97, -1.86]$

This solution corresponds to distractor 3.

E.  $f^{-1}(5) \in [3.78, 4.92]$

This solution corresponds to distractor 1.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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19. Determine whether the function below is 1-1.

$$f(x) = 12x^2 - 114x + 252$$

The solution is no, which is option B.

- A. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

- B. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

- C. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

- D. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

- E. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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20. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -13$  and choose the interval that  $f^{-1}(-13)$  belongs to.

$$f(x) = \sqrt[3]{5x + 4}$$

The solution is  $-440.2$ , which is option C.

A.  $f^{-1}(-13) \in [438.59, 439.36]$

This solution corresponds to distractor 3.

B.  $f^{-1}(-13) \in [-439.72, -437.92]$

Distractor 1: This corresponds to

C.  $f^{-1}(-13) \in [-440.63, -439.67]$

\* This is the correct solution.



D.  $f^{-1}(-13) \in [439.31, 440.26]$

This solution corresponds to distractor 2.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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21. Choose the interval below that  $f$  composed with  $g$  at  $x = -1$  is in.

$$f(x) = 3x^3 + 3x^2 - 2x \text{ and } g(x) = -2x^3 - 3x^2 - 2x - 3$$

The solution is  $-8.0$ , which is option B.

A.  $(f \circ g)(-1) \in [-35.4, -34.9]$

Distractor 1: Corresponds to reversing the composition.

B.  $(f \circ g)(-1) \in [-11.2, -7.5]$

\* This is the correct solution

C.  $(f \circ g)(-1) \in [-4.3, 0.9]$

Distractor 2: Corresponds to being slightly off from the solution.

D.  $(f \circ g)(-1) \in [-33.6, -28.9]$

Distractor 3: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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22. Determine whether the function below is 1-1.

$$f(x) = (5x - 18)^3$$

The solution is yes, which is option A.

A. Yes, the function is 1-1.

\* This is the solution.

B. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

Corresponds to the Horizontal Line test, which this function passes.

C. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

D. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

E. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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23. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 5x^4 + 9x^3 + 3x^2 + 4x + 8 \text{ and } g(x) = 2x + 2$$

The solution is  $(-\infty, \infty)$ , which is option E.

- A. The domain is all Real numbers except  $x = a$ , where  $a \in [-9.2, -1.2]$
- B. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [1.5, 7.5]$
- C. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-11.33, 0.67]$
- D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [3.25, 6.25]$  and  $b \in [-10.2, -3.2]$
- E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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24. Find the inverse of the function below. Then, evaluate the inverse at  $x = 7$  and choose the interval that  $f^{-1}(7)$  belongs to.

$$f(x) = \ln(x - 3) + 5$$

The solution is  $f^{-1}(7) = 10.389$ , which is option A.

- A.  $f^{-1}(7) \in [8.39, 11.39]$

This is the solution.

- B.  $f^{-1}(7) \in [162757.79, 162759.79]$

This solution corresponds to distractor 1.

- C.  $f^{-1}(7) \in [22027.47, 22034.47]$

This solution corresponds to distractor 2.

- D.  $f^{-1}(7) \in [56.6, 63.6]$

This solution corresponds to distractor 4.

- E.  $f^{-1}(7) \in [-0.61, 5.39]$

This solution corresponds to distractor 3.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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25. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -11$  and choose the interval that  $f^{-1}(-11)$  belongs to.

$$f(x) = 3x^2 - 4$$

The solution is The function is not invertible for all Real numbers. , which is option E.

- A.  $f^{-1}(-11) \in [1.94, 2.92]$

Distractor 2: This corresponds to finding the (nonexistent) inverse and not subtracting by the vertical shift.

- B.  $f^{-1}(-11) \in [7.43, 7.82]$

Distractor 4: This corresponds to both distractors 2 and 3.

- C.  $f^{-1}(-11) \in [1.19, 1.93]$

Distractor 1: This corresponds to trying to find the inverse even though the function is not 1-1.

D.  $f^{-1}(-11) \in [4.35, 5.19]$

Distractor 3: This corresponds to finding the (nonexistent) inverse and dividing by a negative.

E. The function is not invertible for all Real numbers.

\* This is the correct option.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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26. Choose the interval below that  $f$  composed with  $g$  at  $x = 1$  is in.

$$f(x) = -x^3 - 2x^2 + 2x + 3 \text{ and } g(x) = -4x^3 - 1x^2 + 2x + 2$$

The solution is 0.0, which is option A.

A.  $(f \circ g)(1) \in [0, 6]$

\* This is the correct solution

B.  $(f \circ g)(1) \in [-30, -25]$

Distractor 1: Corresponds to reversing the composition.

C.  $(f \circ g)(1) \in [-5, -2]$

Distractor 2: Corresponds to being slightly off from the solution.

D.  $(f \circ g)(1) \in [-25, -22]$

Distractor 3: Corresponds to being slightly off from the solution.

E. It is not possible to compose the two functions.

**General Comment:**  $f$  composed with  $g$  at  $x$  means  $f(g(x))$ . The order matters!

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27. Multiply the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 4x^4 + 2x^3 + 2x + 9 \text{ and } g(x) = 4x + 3$$

The solution is  $(-\infty, \infty)$ , which is option E.

A. The domain is all Real numbers greater than or equal to  $x = a$ , where  $a \in [-7, 1]$

B. The domain is all Real numbers except  $x = a$ , where  $a \in [-4.4, 0.6]$

C. The domain is all Real numbers less than or equal to  $x = a$ , where  $a \in [1.67, 3.67]$

D. The domain is all Real numbers except  $x = a$  and  $x = b$ , where  $a \in [7.2, 15.2]$  and  $b \in [-7.6, -1.6]$

E. The domain is all Real numbers.

**General Comment:** The new domain is the intersection of the previous domains.

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28. Find the inverse of the function below. Then, evaluate the inverse at  $x = 7$  and choose the interval that  $f^{-1}(7)$  belongs to.

$$f(x) = e^{x-2} - 3$$

The solution is  $f^{-1}(7) = 4.303$ , which is option C.

A.  $f^{-1}(7) \in [-0.52, 1.86]$

This solution corresponds to distractor 1.

B.  $f^{-1}(7) \in [-1.47, -0.87]$

This solution corresponds to distractor 4.

C.  $f^{-1}(7) \in [3.95, 4.49]$

This is the solution.

D.  $f^{-1}(7) \in [-1, -0.76]$

This solution corresponds to distractor 3.

E.  $f^{-1}(7) \in [-2.16, -1.55]$

This solution corresponds to distractor 2.

**General Comment:** Natural log and exponential functions always have an inverse. Once you switch the  $x$  and  $y$ , use the conversion  $e^y = x \leftrightarrow y = \ln(x)$ .

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29. Determine whether the function below is 1-1.

$$f(x) = 16x^2 + 128x + 256$$

The solution is no, which is option A.

- A. No, because there is a  $y$ -value that goes to 2 different  $x$ -values.

\* This is the solution.

- B. No, because the range of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the range is all Real numbers.

- C. No, because the domain of the function is not  $(-\infty, \infty)$ .

Corresponds to believing 1-1 means the domain is all Real numbers.

- D. No, because there is an  $x$ -value that goes to 2 different  $y$ -values.

Corresponds to the Vertical Line test, which checks if an expression is a function.

- E. Yes, the function is 1-1.

Corresponds to believing the function passes the Horizontal Line test.

**General Comment:** There are only two valid options: The function is 1-1 OR No because there is a  $y$ -value that goes to 2 different  $x$ -values.

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30. Find the inverse of the function below (if it exists). Then, evaluate the inverse at  $x = -15$  and choose the interval that  $f^{-1}(-15)$  belongs to.

$$f(x) = \sqrt[3]{2x-3}$$

The solution is  $-1686.0$ , which is option D.

A.  $f^{-1}(-15) \in [1684, 1688.7]$

This solution corresponds to distractor 2.

B.  $f^{-1}(-15) \in [1686.8, 1691.3]$

This solution corresponds to distractor 3.

C.  $f^{-1}(-15) \in [-1691.2, -1687.3]$

Distractor 1: This corresponds to

D.  $f^{-1}(-15) \in [-1687.2, -1683.8]$

\* This is the correct solution.

E. The function is not invertible for all Real numbers.

This solution corresponds to distractor 4.

**General Comment:** Be sure you check that the function is 1-1 before trying to find the inverse!

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