

This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found [here](#).

If you have a suggestion to make the keys better, please fill out the short survey [here](#).

*Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.*

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$5 + 3x \leq \frac{15x + 9}{3} < 8 + 4x$$

The solution is None of the above., which is option E.

- A.  $[a, b]$ , where  $a \in [-9, -0.75]$  and  $b \in [-7.5, -1.5]$

$[-1.00, -5.00]$ , which is the correct interval but negatives of the actual endpoints.

- B.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [-2.55, -0.45]$  and  $b \in [-5.25, -4.5]$

$(-\infty, -1.00] \cup (-5.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

- C.  $(a, b]$ , where  $a \in [-2.48, -0.22]$  and  $b \in [-8.25, -2.25]$

$(-1.00, -5.00]$ , which corresponds to flipping the inequality and getting negatives of the actual endpoints.

- D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [-2.25, -0.07]$  and  $b \in [-6, -2.25]$

$(-\infty, -1.00) \cup [-5.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.

- E. None of the above.

\* This is correct as the answer should be  $[1.00, 5.00]$ .

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

2. Using an interval or intervals, describe all the  $x$ -values within or including a distance of the given values.

No more than 5 units from the number 4.

The solution is  $[-1, 9]$ , which is option B.

- A.  $(-1, 9)$

This describes the values less than 5 from 4

- B.  $[-1, 9]$

This describes the values no more than 5 from 4

- C.  $(-\infty, -1] \cup [9, \infty)$

This describes the values no less than 5 from 4

- D.  $(-\infty, -1) \cup (9, \infty)$

This describes the values more than 5 from 4

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

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3. Using an interval or intervals, describe all the  $x$ -values within or including a distance of the given values.

No more than 5 units from the number 7.

The solution is  $[2, 12]$ , which is option A.

A.  $[2, 12]$

This describes the values no more than 5 from 7

B.  $(2, 12)$

This describes the values less than 5 from 7

C.  $(-\infty, 2) \cup (12, \infty)$

This describes the values more than 5 from 7

D.  $(-\infty, 2] \cup [12, \infty)$

This describes the values no less than 5 from 7

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

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4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{9}{4} - \frac{10}{8}x < \frac{-6}{9}x + \frac{7}{2}$$

The solution is  $(-2.143, \infty)$ , which is option C.

A.  $(-\infty, a)$ , where  $a \in [-3.75, 1.5]$

$(-\infty, -2.143)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $(a, \infty)$ , where  $a \in [0.75, 3.75]$

$(2.143, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(a, \infty)$ , where  $a \in [-7.5, -0.75]$

\*  $(-2.143, \infty)$ , which is the correct option.

D.  $(-\infty, a)$ , where  $a \in [0, 3]$

$(-\infty, 2.143)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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5. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7x + 5 < 3x - 3$$

The solution is  $(0.8, \infty)$ , which is option C.

- A.  $(-\infty, a)$ , where  $a \in [0.8, 7.8]$

$(-\infty, 0.8)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- B.  $(-\infty, a)$ , where  $a \in [-1.8, 0.2]$

$(-\infty, -0.8)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- C.  $(a, \infty)$ , where  $a \in [-0.33, 1.28]$

\*  $(0.8, \infty)$ , which is the correct option.

- D.  $(a, \infty)$ , where  $a \in [-2.07, -0.39]$

$(-0.8, \infty)$ , which corresponds to negating the endpoint of the solution.

- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$7x - 5 \geq 9x + 6$$

The solution is  $(-\infty, -5.5]$ , which is option A.

- A.  $(-\infty, a]$ , where  $a \in [-6.5, -4.5]$

\*  $(-\infty, -5.5]$ , which is the correct option.

- B.  $(-\infty, a]$ , where  $a \in [3.5, 9.5]$

$(-\infty, 5.5]$ , which corresponds to negating the endpoint of the solution.

- C.  $[a, \infty)$ , where  $a \in [-5.5, 0.5]$

$[-5.5, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- D.  $[a, \infty)$ , where  $a \in [0.5, 6.5]$

$[5.5, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-9 + 6x > 9x \text{ or } 9 + 6x < 7x$$

The solution is  $(-\infty, -3.0)$  or  $(9.0, \infty)$ , which is option C.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-7.5, -1.5]$  and  $b \in [4.5, 9.75]$

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-9.75, -3.75]$  and  $b \in [2.25, 5.25]$

Corresponds to including the endpoints AND negating.

C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-3.75, 5.25]$  and  $b \in [6.75, 12]$

\* Correct option.

D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-10.5, -7.5]$  and  $b \in [0, 6]$

Corresponds to inverting the inequality and negating the solution.

E.  $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

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8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{4}{6} - \frac{8}{4}x \leq \frac{-3}{7}x - \frac{7}{3}$$

The solution is  $[1.909, \infty)$ , which is option A.

A.  $[a, \infty)$ , where  $a \in [0.75, 3.75]$

\*  $[1.909, \infty)$ , which is the correct option.

B.  $[a, \infty)$ , where  $a \in [-3.75, 0.75]$

$[-1.909, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(-\infty, a]$ , where  $a \in [-4.5, 0]$

$(-\infty, -1.909]$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

D.  $(-\infty, a]$ , where  $a \in [-0.75, 3.75]$

$(-\infty, 1.909]$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

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9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$8 - 3x > 5x \text{ or } 9 + 3x < 6x$$

The solution is  $(-\infty, 1.0)$  or  $(3.0, \infty)$ , which is option B.

- A.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-5.25, -0.75]$  and  $b \in [-3, 0.75]$

Corresponds to inverting the inequality and negating the solution.

- B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-2.25, 3]$  and  $b \in [0.75, 4.5]$

\* Correct option.

- C.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-4.5, 0.75]$  and  $b \in [-3, 2.25]$

Corresponds to including the endpoints AND negating.

- D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [0, 5.25]$  and  $b \in [2.25, 8.25]$

Corresponds to including the endpoints (when they should be excluded).

- E.  $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

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10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$7 + 3x < \frac{29x + 7}{9} \leq 9 + 3x$$

The solution is  $(28.00, 37.00]$ , which is option D.

- A.  $[a, b]$ , where  $a \in [26.25, 31.5]$  and  $b \in [35.25, 37.5]$

$[28.00, 37.00]$ , which corresponds to flipping the inequality.

- B.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [27.75, 33.75]$  and  $b \in [34.5, 38.25]$

$(-\infty, 28.00) \cup [37.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality.

- C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [27, 29.25]$  and  $b \in [36.75, 38.25]$

$(-\infty, 28.00] \cup (37.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality.

- D.  $(a, b]$ , where  $a \in [27, 33]$  and  $b \in [36.75, 37.5]$

\*  $(28.00, 37.00]$ , which is the correct option.

- E. None of the above.

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

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