This key should allow you to understand why you choose the option you did (beyond just getting a question right or wrong). More instructions on how to use this key can be found here.

If you have a suggestion to make the keys better, please fill out the short survey here.

Note: This key is auto-generated and may contain issues and/or errors. The keys are reviewed after each exam to ensure grading is done accurately. If there are issues (like duplicate options), they are noted in the offline gradebook. The keys are a work-in-progress to give students as many resources to improve as possible.

1. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-5x - 10 > -4x - 7$$

The solution is  $(-\infty, -3.0)$ , which is option D.

A.  $(a, \infty)$ , where  $a \in [-3, -1]$ 

 $(-3.0, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $(-\infty, a)$ , where  $a \in [1, 4]$ 

 $(-\infty, 3.0)$ , which corresponds to negating the endpoint of the solution.

C.  $(a, \infty)$ , where  $a \in [2, 13]$ 

 $(3.0, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

- D.  $(-\infty, a)$ , where  $a \in [-9, -1]$ 
  - \*  $(-\infty, -3.0)$ , which is the correct option.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

2. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-3 + 6x < \frac{26x + 8}{4} \le 8 + 5x$$

The solution is None of the above., which is option E.

A. [a, b), where  $a \in [6, 10.5]$  and  $b \in [-6, -3]$ 

[10.00, -4.00), which corresponds to flipping the inequality and getting negatives of the actual endpoints.

B.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [9, 16.5]$  and  $b \in [-4.5, -3]$ 

 $(-\infty, 10.00) \cup [-4.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.

- C.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [6.75, 15]$  and  $b \in [-9.75, -1.5]$ 
  - $(-\infty, 10.00] \cup (-4.00, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.
- D. (a, b], where  $a \in [8.25, 15]$  and  $b \in [-6, -3]$

(10.00, -4.00], which is the correct interval but negatives of the actual endpoints.

- E. None of the above.
  - \* This is correct as the answer should be (-10.00, 4.00].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

3. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No less than 9 units from the number -9.

The solution is  $(-\infty, -18] \cup [0, \infty)$ , which is option D.

A. [-18, 0]

This describes the values no more than 9 from -9

B. (-18,0)

This describes the values less than 9 from -9

C.  $(-\infty, -18) \cup (0, \infty)$ 

This describes the values more than 9 from -9

D.  $(-\infty, -18] \cup [0, \infty)$ 

This describes the values no less than 9 from -9

E. None of the above

You likely thought the values in the interval were not correct.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

4. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-6 + 8x < \frac{37x + 7}{4} \le -9 + 5x$$

The solution is None of the above, which is option E.

- A. [a, b), where  $a \in [4.5, 9]$  and  $b \in [1.5, 7.5]$ 
  - [6.20, 2.53), which corresponds to flipping the inequality and getting negatives of the actual endpoints.
- B.  $(-\infty, a] \cup (b, \infty)$ , where  $a \in [3.75, 7.5]$  and  $b \in [1.5, 3.75]$ 
  - $(-\infty, 6.20] \cup (2.53, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality AND flipping the inequality AND getting negatives of the actual endpoints.
- C. (a, b], where  $a \in [4.5, 7.5]$  and  $b \in [0.75, 4.5]$

(6.20, 2.53], which is the correct interval but negatives of the actual endpoints.

- D.  $(-\infty, a) \cup [b, \infty)$ , where  $a \in [3, 7.5]$  and  $b \in [-0.75, 3]$ 
  - $(-\infty, 6.20) \cup [2.53, \infty)$ , which corresponds to displaying the and-inequality as an or-inequality and getting negatives of the actual endpoints.
- E. None of the above.
  - \* This is correct as the answer should be (-6.20, -2.53].

**General Comment:** To solve, you will need to break up the compound inequality into two inequalities. Be sure to keep track of the inequality! It may be best to draw a number line and graph your solution.

5. Using an interval or intervals, describe all the x-values within or including a distance of the given values.

No less than 3 units from the number 5.

The solution is None of the above, which is option E.

A.  $(-\infty, -2) \cup (8, \infty)$ 

This describes the values more than 5 from 3

B. (-2,8)

This describes the values less than 5 from 3

C. [-2, 8]

This describes the values no more than 5 from 3

D.  $(-\infty, -2] \cup [8, \infty)$ 

This describes the values no less than 5 from 3

E. None of the above

Options A-D described the values [more/less than] 5 units from 3, which is the reverse of what the question asked.

**General Comment:** When thinking about this language, it helps to draw a number line and try points.

6. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{4}{4} - \frac{6}{8}x > \frac{4}{9}x - \frac{9}{5}$$

The solution is  $(-\infty, 2.344)$ , which is option D.

- A.  $(a, \infty)$ , where  $a \in [-1.5, 4.5]$ 
  - $(2.344, \infty)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!
- B.  $(a, \infty)$ , where  $a \in [-3, 1.5]$

 $(-2.344, \infty)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

C.  $(-\infty, a)$ , where  $a \in [-5.25, -2.25]$ 

 $(-\infty, -2.344)$ , which corresponds to negating the endpoint of the solution.

- D.  $(-\infty, a)$ , where  $a \in [0, 5.25]$ 
  - \*  $(-\infty, 2.344)$ , which is the correct option.
- E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

7. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-7 + 8x > 10x$$
 or  $9 + 5x < 7x$ 

The solution is  $(-\infty, -3.5)$  or  $(4.5, \infty)$ , which is option C.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-4.06, -2.92]$  and  $b \in [4.46, 5.05]$ 

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-4.65, -3.6]$  and  $b \in [2.25, 3.6]$ 

Corresponds to inverting the inequality and negating the solution.

- C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-3.6, -2.4]$  and  $b \in [3.52, 6.38]$ 
  - \* Correct option.
- D.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-5.65, -4.13]$  and  $b \in [3.42, 3.78]$

Corresponds to including the endpoints AND negating.

E.  $(-\infty, \infty)$ 

Corresponds to the variable canceling, which does not happen in this instance.

**General Comment:** When multiplying or dividing by a negative, flip the sign.

8. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$\frac{10}{8} - \frac{5}{2}x < \frac{4}{9}x - \frac{6}{3}$$

The solution is  $(1.104, \infty)$ , which is option D.

- A.  $(-\infty, a)$ , where  $a \in [-2.25, 0]$ 
  - $(-\infty, -1.104)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.
- B.  $(-\infty, a)$ , where  $a \in [0, 3]$

 $(-\infty, 1.104)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

- C.  $(a, \infty)$ , where  $a \in [-1.88, -0.97]$ 
  - $(-1.104, \infty)$ , which corresponds to negating the endpoint of the solution.
- D.  $(a, \infty)$ , where  $a \in [1.05, 2.4]$ 
  - \*  $(1.104, \infty)$ , which is the correct option.

## E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

9. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$-9x - 9 < 4x + 5$$

The solution is  $(-1.077, \infty)$ , which is option C.

A.  $(-\infty, a)$ , where  $a \in [-2.6, -0.4]$ 

 $(-\infty, -1.077)$ , which corresponds to switching the direction of the interval. You likely did this if you did not flip the inequality when dividing by a negative!

B.  $(a, \infty)$ , where  $a \in [-0.5, 1.63]$ 

 $(1.077, \infty)$ , which corresponds to negating the endpoint of the solution.

C.  $(a, \infty)$ , where  $a \in [-1.14, -0.06]$ 

\*  $(-1.077, \infty)$ , which is the correct option.

D.  $(-\infty, a)$ , where  $a \in [-0.4, 2.9]$ 

 $(-\infty, 1.077)$ , which corresponds to switching the direction of the interval AND negating the endpoint. You likely did this if you did not flip the inequality when dividing by a negative as well as not moving values over to a side properly.

E. None of the above.

You may have chosen this if you thought the inequality did not match the ends of the intervals.

**General Comment:** Remember that less/greater than or equal to includes the endpoint, while less/greater do not. Also, remember that you need to flip the inequality when you multiply or divide by a negative.

10. Solve the linear inequality below. Then, choose the constant and interval combination that describes the solution set.

$$5 + 4x > 7x$$
 or  $8 + 5x < 6x$ 

The solution is  $(-\infty, 1.667)$  or  $(8.0, \infty)$ , which is option D.

A.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-2.25, 6]$  and  $b \in [3.75, 11.25]$ 

Corresponds to including the endpoints (when they should be excluded).

B.  $(-\infty, a] \cup [b, \infty)$ , where  $a \in [-11.25, -5.25]$  and  $b \in [-2.25, 0]$ 

Corresponds to including the endpoints AND negating.

C.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [-9, -5.25]$  and  $b \in [-3, 3]$ 

Corresponds to inverting the inequality and negating the solution.

D.  $(-\infty, a) \cup (b, \infty)$ , where  $a \in [0.75, 5.25]$  and  $b \in [3.75, 9]$ 

\* Correct option.

## E. $(-\infty, \infty)$

Corresponds to the variable canceling, which does not happen in this instance.

General Comment: When multiplying or dividing by a negative, flip the sign.