1. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$  to find the coefficient for the model of the new volume  $V_{\text{new}} = kr^2 h$ .

Pepsi wants to increase the volume of soda in their cans. They've decided to increase the radius by 16 percent and increase the height by 10 percent. They want to model the new volume based on the radius and height of the original cans.

- A. k = 0.00256
- B. k = 0.00804
- C. k = 4.65006
- D. k = 1.48016
- E. None of the above.
- 2. Choose the model type that would best describe the scenario below.

Big O notation is common in computer science to describe how fast a program can solve a particular problem. Big O notation categorizes functions according to their growth rates, the same way we have categorized modeling real-world problems by certain types of functions. When analyzing a particular program, a student found the computer to need  $x^x$  time to complete, where x was the number of inputs into the program.

- A. Indirect variation
- B. Direct variation
- C. Joint variation
- D. None of the above
- 3. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the quartic of the time, T (Earth years), required for a planet to orbit  $Sun \chi$  decreases as the square of the

distance, d (AUs), that the planet is from Sun  $\chi$  decreases. For example, when Ea's average distance from Sun  $\chi$  is 2, it takes 94 Earth days to complete an orbit.

A. 
$$k = 2.202$$

B. 
$$k = 19518724.000$$

C. 
$$k = 312299584.000$$

D. 
$$k = 4.028$$

- E. Unable to compute the constant based on the information given.
- 4. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string  $\omega$  decreases as the cube length of the string increases. For example, when string  $\omega$  is 5 mm long, the rate of vibration is 21 cm/s.

A. 
$$k = 2.62$$

B. 
$$k = 0.17$$

C. 
$$k = 168.00$$

D. 
$$k = 2625.00$$

- E. None of the above.
- 5. For the scenario below, model the rate of vibration (cm/s) of the string in terms of the length of the string. Then determine the variation constant k of the model (if possible). The constant should be in terms of cm and s.

The rate of vibration of a string under constant tension varies based on the type of string and the length of the string. The rate of vibration of string  $\omega$  increases as the quartic length of the string decreases. For example, when string  $\omega$  is 2 mm long, the rate of vibration is 38 cm/s.

- A. k = 608.00
- B. k = 2.38
- C. k = 0.06
- D. k = 23750.00
- E. None of the above.
- 6. A town has an initial population of 70000. The town's population for the next 9 years is provided below. Which type of function would be most appropriate to model the town's population?

Year	1	2	3	4	5	6	7	8	9
Pop	70000	70013	70021	70027	70032	70035	70038	70041	70043

- A. Logarithmic
- B. Exponential
- C. Linear
- D. Non-Linear Power
- E. None of the above
- 7. A town has an initial population of 30000. The town's population for the next 9 years is provided below. Which type of function would be most appropriate to model the town's population?

Year	1	2	3	4	5	6	7	8	9
Pop	30052	30098	30144	30206	30252	30298	30344	30406	30452

- A. Exponential
- B. Non-Linear Power
- C. Linear
- D. Logarithmic

- E. None of the above
- 8. For the scenario below, use the model for the volume of a cylinder as  $V = \pi r^2 h$  to find the coefficient for the model of the new volume  $V_{\text{new}} = kr^2 h$ .

Pepsi wants to increase the volume of soda in their cans. They've decided to increase the radius by 11 percent and increase the height by 17 percent. They want to model the new volume based on the radius and height of the original cans.

- A. k = 1.44156
- B. k = 0.00206
- C. k = 0.00646
- D. k = 4.52878
- E. None of the above.
- 9. For the scenario below, find the variation constant k of the model (if possible).

In an alternative galaxy, the quartic of the time, T (Earth years), required for a planet to orbit  $Sun\ \chi$  increases as the square of the distance, d (AUs), that the planet is from  $Sun\ \chi$  increases. For example, when Ea's average distance from  $Sun\ \chi$  is 8, it takes 51 Earth days to complete an orbit.

- A. k = 432972864.000
- B. k = 4.028
- C. k = 0.945
- D. k = 105706.266
- E. Unable to compute the constant based on the information given.
- 10. Choose the model type that would best describe the scenario below.

In economics, there are two common equations to model interest earned. The compound interest formula is  $A = P(1 + \frac{r}{n})^{nt}$ , where A is the amount of money you end up with, P is your starting money, r is the interest rate, n is the number of times compounded in a year, and t is the total number of years. For example, if you were a parent and wanted to save \$10,000 in 3 years-time at 3.5% interest compounded monthly, you would need to invest about \$9,000.

- A. Direct variation
- B. Indirect variation
- C. Joint variation
- D. None of the above

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