1. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 3x^3 + 8x + 5$$
 and  $g(x) = \sqrt{-5x - 18}$ 

- A. The domain is all Real numbers less than or equal to x = a, where  $a \in [-7.6, 1.4]$
- B. The domain is all Real numbers except x = a, where  $a \in [-8.6, -3.6]$
- C. The domain is all Real numbers greater than or equal to x = a, where  $a \in [4, 9]$
- D. The domain is all Real numbers except x = a and x = b, where  $a \in [3.75, 10.75]$  and  $b \in [1.2, 8.2]$
- E. The domain is all Real numbers.
- 2. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that  $f^{-}1(7)$  belongs to.

$$f(x) = \ln(x - 5) - 3$$

- A.  $f^{-1}(7) \in [22026.47, 22032.47]$
- B.  $f^{-1}(7) \in [162748.79, 162754.79]$
- C.  $f^{-1}(7) \in [58.6, 62.6]$
- D.  $f^{-1}(7) \in [22015.47, 22023.47]$
- E.  $f^{-1}(7) \in [-2.61, 10.39]$
- 3. Determine whether the function below is 1-1.

$$f(x) = (4x + 22)^3$$

- A. No, because the domain of the function is not  $(-\infty, \infty)$ .
- B. Yes, the function is 1-1.
- C. No, because the range of the function is not  $(-\infty, \infty)$ .

- D. No, because there is an x-value that goes to 2 different y-values.
- E. No, because there is a y-value that goes to 2 different x-values.
- 4. Find the inverse of the function below. Then, evaluate the inverse at x = 4 and choose the interval that  $f^{-}1(4)$  belongs to.

$$f(x) = e^{x-2} - 2$$

- A.  $f^{-1}(4) \in [-0.26, 0.56]$
- B.  $f^{-1}(4) \in [-2.74, -0.56]$
- C.  $f^{-1}(4) \in [-0.26, 0.56]$
- D.  $f^{-1}(4) \in [-2.74, -0.56]$
- E.  $f^{-1}(4) \in [3.68, 4.18]$
- 5. Determine whether the function below is 1-1.

$$f(x) = 9x^2 + 126x + 441$$

- A. No, because there is a y-value that goes to 2 different x-values.
- B. No, because the range of the function is not  $(-\infty, \infty)$ .
- C. No, because there is an x-value that goes to 2 different y-values.
- D. No, because the domain of the function is not  $(-\infty, \infty)$ .
- E. Yes, the function is 1-1.
- 6. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = 3x^3 + 2x^2 - 4x$$
 and  $g(x) = 3x^3 + 2x^2 - 4x + 1$ 

- A.  $(f \circ g)(1) \in [-13, -3]$
- B.  $(f \circ g)(1) \in [21, 25]$
- C.  $(f \circ g)(1) \in [16, 21]$

D. 
$$(f \circ g)(1) \in [1, 4]$$

E. It is not possible to compose the two functions.

7. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = x^3 - 2x^2 - x + 2$$
 and  $g(x) = -x^3 + 4x^2 + x$ 

A. 
$$(f \circ g)(-1) \in [35, 40]$$

B. 
$$(f \circ g)(-1) \in [29, 31]$$

C. 
$$(f \circ g)(-1) \in [-4, 1]$$

D. 
$$(f \circ g)(-1) \in [7, 18]$$

E. It is not possible to compose the two functions.

8. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -14 and choose the interval that  $f^{-1}(-14)$  belongs to.

$$f(x) = \sqrt[3]{5x - 4}$$

A. 
$$f^{-1}(-14) \in [547, 548.6]$$

B. 
$$f^{-1}(-14) \in [-551.3, -548.6]$$

C. 
$$f^{-1}(-14) \in [-548.6, -546.7]$$

D. 
$$f^{-1}(-14) \in [549, 552.1]$$

E. The function is not invertible for all Real numbers.

9. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -15 and choose the interval that  $f^{-1}(-15)$  belongs to.

$$f(x) = 3x^2 - 4$$

A. 
$$f^{-1}(-15) \in [2.27, 2.72]$$

B. 
$$f^{-1}(-15) \in [2.73, 3.19]$$

C. 
$$f^{-1}(-15) \in [5.61, 6.24]$$

D. 
$$f^{-1}(-15) \in [1.77, 2.01]$$

- E. The function is not invertible for all Real numbers.
- 10. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \frac{3}{3x - 14}$$
 and  $g(x) = 2x^2 + 3x + 7$ 

- A. The domain is all Real numbers except x = a, where  $a \in [3.67, 13.67]$
- B. The domain is all Real numbers greater than or equal to x=a, where  $a \in [-8.67, -1.67]$
- C. The domain is all Real numbers less than or equal to x = a, where  $a \in [-3, 0]$
- D. The domain is all Real numbers except x = a and x = b, where  $a \in [2.67, 6.67]$  and  $b \in [-4.67, 1.33]$
- E. The domain is all Real numbers.
- 11. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = x^4 + 8x^3 + 7x + 7$$
 and  $g(x) = \frac{1}{5x + 36}$ 

- A. The domain is all Real numbers greater than or equal to x=a, where  $a \in [-7, -3]$
- B. The domain is all Real numbers less than or equal to x = a, where  $a \in [-6.33, -0.33]$
- C. The domain is all Real numbers except x = a, where  $a \in [-11.2, -2.2]$
- D. The domain is all Real numbers except x = a and x = b, where  $a \in [-6.33, -3.33]$  and  $b \in [1.2, 8.2]$
- E. The domain is all Real numbers.

12. Find the inverse of the function below. Then, evaluate the inverse at x = 9 and choose the interval that  $f^{-}1(9)$  belongs to.

$$f(x) = \ln\left(x - 2\right) - 5$$

- A.  $f^{-1}(9) \in [1090.63, 1098.63]$
- B.  $f^{-1}(9) \in [59866.14, 59873.14]$
- C.  $f^{-1}(9) \in [1202600.28, 1202606.28]$
- D.  $f^{-1}(9) \in [1202603.28, 1202608.28]$
- E.  $f^{-1}(9) \in [51.6, 59.6]$

13. Determine whether the function below is 1-1.

$$f(x) = -25x^2 + 30x + 391$$

- A. No, because there is an x-value that goes to 2 different y-values.
- B. No, because there is a y-value that goes to 2 different x-values.
- C. No, because the domain of the function is not  $(-\infty, \infty)$ .
- D. No, because the range of the function is not  $(-\infty, \infty)$ .
- E. Yes, the function is 1-1.

14. Find the inverse of the function below. Then, evaluate the inverse at x = 8 and choose the interval that  $f^{-}1(8)$  belongs to.

$$f(x) = \ln(x+5) - 2$$

- A.  $f^{-1}(8) \in [22019.47, 22022.47]$
- B.  $f^{-1}(8) \in [442411.39, 442413.39]$
- C.  $f^{-1}(8) \in [22029.47, 22035.47]$
- D.  $f^{-1}(8) \in [13.09, 22.09]$

E. 
$$f^{-1}(8) \in [395.43, 399.43]$$

15. Determine whether the function below is 1-1.

$$f(x) = 9x^2 - 78x + 169$$

- A. Yes, the function is 1-1.
- B. No, because there is an x-value that goes to 2 different y-values.
- C. No, because there is a y-value that goes to 2 different x-values.
- D. No, because the range of the function is not  $(-\infty, \infty)$ .
- E. No, because the domain of the function is not  $(-\infty, \infty)$ .
- 16. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = x^3 + 2x^2 - 3x - 3$$
 and  $g(x) = -2x^3 - 2x^2 + 3x + 2$ 

- A.  $(f \circ g)(-1) \in [0.74, 1.77]$
- B.  $(f \circ g)(-1) \in [0.74, 1.77]$
- C.  $(f \circ g)(-1) \in [-6.62, -4.63]$
- D.  $(f \circ g)(-1) \in [-4.38, -3.54]$
- E. It is not possible to compose the two functions.
- 17. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = -3x^3 + 4x^2 + x - 3$$
 and  $g(x) = -2x^3 + 3x^2 + 3x - 2$ 

- A.  $(f \circ g)(-1) \in [-4, 1]$
- B.  $(f \circ g)(-1) \in [-13, -6]$
- C.  $(f \circ g)(-1) \in [1, 7]$
- D.  $(f \circ g)(-1) \in [-29, -19]$
- E. It is not possible to compose the two functions.

18. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 15 and choose the interval that  $f^{-1}(15)$  belongs to.

$$f(x) = 4x^2 + 3$$

- A.  $f^{-1}(15) \in [1.41, 1.79]$
- B.  $f^{-1}(15) \in [2.37, 2.82]$
- C.  $f^{-1}(15) \in [5.29, 6]$
- D.  $f^{-1}(15) \in [2.06, 2.37]$
- E. The function is not invertible for all Real numbers.
- 19. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = 11 and choose the interval that  $f^{-1}(11)$  belongs to.

$$f(x) = 2x^2 + 5$$

- A.  $f^{-1}(11) \in [2.52, 2.9]$
- B.  $f^{-1}(11) \in [1.19, 2.72]$
- C.  $f^{-1}(11) \in [5.06, 7.17]$
- D.  $f^{-1}(11) \in [2.97, 4.59]$
- E. The function is not invertible for all Real numbers.
- 20. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 5x^3 + 9x^2 + 3x + 3$$
 and  $g(x) = \frac{5}{5x - 34}$ 

- A. The domain is all Real numbers greater than or equal to x=a, where  $a\in[7,13]$
- B. The domain is all Real numbers less than or equal to x=a, where  $a\in[-0.8,5.2]$

- C. The domain is all Real numbers except x = a, where  $a \in [5.8, 8.8]$
- D. The domain is all Real numbers except x = a and x = b, where  $a \in [-14.67, -1.67]$  and  $b \in [-6.17, 4.83]$
- E. The domain is all Real numbers.
- 21. Add the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = \sqrt{-3x - 16}$$
 and  $g(x) = 3x^3 + 9x$ 

- A. The domain is all Real numbers except x = a, where  $a \in [4.2, 12.2]$
- B. The domain is all Real numbers less than or equal to x = a, where  $a \in [-7.33, 0.67]$
- C. The domain is all Real numbers greater than or equal to x=a, where  $a \in [5.33, 11.33]$
- D. The domain is all Real numbers except x = a and x = b, where  $a \in [5.67, 8.67]$  and  $b \in [4.6, 12.6]$
- E. The domain is all Real numbers.
- 22. Find the inverse of the function below. Then, evaluate the inverse at x = 7 and choose the interval that  $f^{-1}(7)$  belongs to.

$$f(x) = \ln(x - 5) - 2$$

- A.  $f^{-1}(7) \in [153.41, 157.41]$
- B.  $f^{-1}(7) \in [8107.08, 8112.08]$
- C.  $f^{-1}(7) \in [2.39, 7.39]$
- D.  $f^{-1}(7) \in [8096.08, 8099.08]$
- E.  $f^{-1}(7) \in [162748.79, 162755.79]$

3510-5252 Summer C 2021

23. Determine whether the function below is 1-1.

$$f(x) = 25x^2 + 220x + 484$$

- A. Yes, the function is 1-1.
- B. No, because the range of the function is not  $(-\infty, \infty)$ .
- C. No, because there is an x-value that goes to 2 different y-values.
- D. No, because there is a y-value that goes to 2 different x-values.
- E. No, because the domain of the function is not  $(-\infty, \infty)$ .
- 24. Find the inverse of the function below. Then, evaluate the inverse at x = 10 and choose the interval that  $f^{-}1(10)$  belongs to.

$$f(x) = e^{x+5} - 3$$

- A.  $f^{-1}(10) \in [-1.1, -0.84]$
- B.  $f^{-1}(10) \in [7.32, 8.32]$
- C.  $f^{-1}(10) \in [-0.32, 0.71]$
- D.  $f^{-1}(10) \in [-2.55, -1.81]$
- E.  $f^{-1}(10) \in [-2.19, -1.3]$
- 25. Determine whether the function below is 1-1.

$$f(x) = (5x + 17)^3$$

- A. No, because the range of the function is not  $(-\infty, \infty)$ .
- B. Yes, the function is 1-1.
- C. No, because there is a y-value that goes to 2 different x-values.
- D. No, because there is an x-value that goes to 2 different y-values.
- E. No, because the domain of the function is not  $(-\infty, \infty)$ .

3510-5252 Summer C 2021

26. Choose the interval below that f composed with g at x = -1 is in.

$$f(x) = -4x^3 - 2x^2 + 4x$$
 and  $g(x) = -3x^3 - 4x^2 - x - 3$ 

- A.  $(f \circ g)(-1) \in [10, 23]$
- B.  $(f \circ g)(-1) \in [83, 91]$
- C.  $(f \circ g)(-1) \in [75, 84]$
- D.  $(f \circ g)(-1) \in [3, 15]$
- E. It is not possible to compose the two functions.

27. Choose the interval below that f composed with g at x = 1 is in.

$$f(x) = 2x^3 + 2x^2 - 3x$$
 and  $g(x) = -4x^3 + x^2 + 2x - 3$ 

- A.  $(f \circ g)(1) \in [-9, -3]$
- B.  $(f \circ g)(1) \in [1, 4]$
- C.  $(f \circ q)(1) \in [-84, -83]$
- D.  $(f \circ g)(1) \in [-76, -73]$
- E. It is not possible to compose the two functions.

28. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -10 and choose the interval that  $f^{-1}(-10)$  belongs to.

$$f(x) = \sqrt[3]{4x - 3}$$

- A.  $f^{-1}(-10) \in [-250, -247]$
- B.  $f^{-1}(-10) \in [246.4, 250.6]$
- C.  $f^{-1}(-10) \in [249.9, 253]$
- D.  $f^{-1}(-10) \in [-250.9, -249.9]$
- E. The function is not invertible for all Real numbers.

29. Find the inverse of the function below (if it exists). Then, evaluate the inverse at x = -15 and choose the interval that  $f^{-1}(-15)$  belongs to.

$$f(x) = 5x^2 - 2$$

- A.  $f^{-1}(-15) \in [5.33, 5.75]$
- B.  $f^{-1}(-15) \in [1.81, 2.05]$
- C.  $f^{-1}(-15) \in [1.48, 1.65]$
- D.  $f^{-1}(-15) \in [4.33, 4.91]$
- E. The function is not invertible for all Real numbers.
- 30. Subtract the following functions, then choose the domain of the resulting function from the list below.

$$f(x) = 9x^2 + 8x + 6$$
 and  $g(x) = 5x^3 + 8x^2 + 5x + 6$ 

- A. The domain is all Real numbers less than or equal to x = a, where  $a \in [0.5, 5.5]$
- B. The domain is all Real numbers except x = a, where  $a \in [6.2, 7.2]$
- C. The domain is all Real numbers greater than or equal to x = a, where  $a \in [2.67, 9.67]$
- D. The domain is all Real numbers except x=a and x=b, where  $a\in[-7.33,1.67]$  and  $b\in[-5.25,-2.25]$
- E. The domain is all Real numbers.