



Polynomial Regression

About this Notebook

In this notebook, we learn how to use scikit-learn for Polynomial regression. We download a dataset that is related to fuel consumption and Carbon dioxide emission of cars. Then, we split our data into training and test sets, create a model using training set, evaluate our model using test set, and finally use model to predict unknown value.

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Importing Needed packages

In [1]:

```
import matplotlib.pyplot as plt
import pandas as pd
import pylab as pl
import numpy as np
%matplotlib inline
```

Downloading Data

To download the data, we will use `!wget` to download it from IBM Object Storage.

In [2]:

```
!wget -O FuelConsumption.csv https://s3-api.us-gio.objectstorage.softlayer.net/cf-courses-data/CognitiveClass/ML0101ENV3/labs/FuelConsumptionCo2.csv
```

```
--2020-06-15 10:40:28-- https://s3-api.us-gio.objectstorage.softlayer.net/cf-courses-data/CognitiveClass/ML0101ENV3/labs/FuelConsumptionCo2.csv
Resolving s3-api.us-gio.objectstorage.softlayer.net (s3-api.us-gio.objectstorage.softlayer.net)...
67.228.254.196
Connecting to s3-api.us-gio.objectstorage.softlayer.net (s3-api.us-gio.objectstorage.softlayer.net)|67.228.254.196|:443... connected.
HTTP request sent, awaiting response... 200 OK
Length: 72629 (71K) [text/csv]
Saving to: 'FuelConsumption.csv'
```

```
FuelConsumption.csv 100%[=====] 70.93K --.-KB/s in 0.04s
```

```
2020-06-15 10:40:28 (1.62 MB/s) - 'FuelConsumption.csv' saved [72629/72629]
```

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Understanding the Data

FuelConsumption.csv:

We have downloaded a fuel consumption dataset, **FuelConsumption.csv**, which contains model-specific fuel consumption ratings and estimated carbon dioxide emissions for new light-duty vehicles for retail sale in Canada. [Dataset source](#)

- **MODELYEAR** e.g. 2014
- **MAKE** e.g. Acura
- **MODEL** e.g. ILX
- **VEHICLE CLASS** e.g. SUV
- **ENGINE SIZE** e.g. 4.7
- **CYLINDERS** e.g. 6
- **TRANSMISSION** e.g. A6
- **FUEL CONSUMPTION in CITY (L/100 km)** e.g. 9.9
- **FUEL CONSUMPTION in HWY (L/100 km)** e.g. 8.9
- **FUEL CONSUMPTION COMB (L/100 km)** e.g. 9.2
- **CO2 EMISSIONS (g/km)** e.g. 182 --> low --> 0

Reading the data in

In [3]:

```
df = pd.read_csv("FuelConsumption.csv")

# take a look at the dataset
df.head()
```

Out[3]:

	MODELYEAR	MAKE	MODEL	VEHICLECLASS	ENGINE SIZE	CYLINDERS	TRANSMISSION	FUELTYPE	FUELCONSUMPTION_CITY
0	2014	ACURA	ILX	COMPACT	2.0	4	AS5	Z	9.9
1	2014	ACURA	ILX	COMPACT	2.4	4	M6	Z	11.2
2	2014	ACURA	ILX HYBRID	COMPACT	1.5	4	AV7	Z	6.0
3	2014	ACURA	MDX 4WD	SUV - SMALL	3.5	6	AS6	Z	12.7
4	2014	ACURA	RDX AWD	SUV - SMALL	3.5	6	AS6	Z	12.1

Lets select some features that we want to use for regression.

In [4]:

```
cdf = df[['ENGINE SIZE', 'CYLINDERS', 'FUELCONSUMPTION_COMB', 'CO2EMISSIONS']]
cdf.head(9)
```

Out[4]:

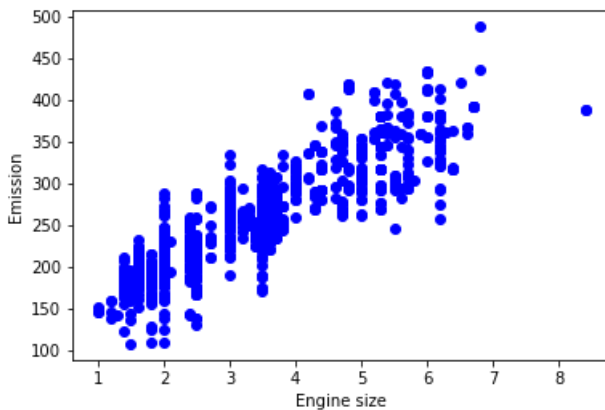
	ENGINE SIZE	CYLINDERS	FUELCONSUMPTION_COMB	CO2EMISSIONS
0	2.0	4	8.5	196
1	2.4	4	9.6	221
2	1.5	4	5.9	136
3	3.5	6	11.1	255
4	3.5	6	10.6	244
5	3.5	6	10.0	230
6	3.5	6	10.4	233

6	3.5	6	10.1	232
ENGINE SIZE	CYLINDERS	FUEL CONSUMPTION_COMB	CO2 EMISSIONS	
7	3.7	6	11.1	255
8	3.7	6	11.6	267

Lets plot Emission values with respect to Engine size:

In [5]:

```
plt.scatter(cdf.ENGINESIZE, cdf.CO2EMISSIONS, color='blue')
plt.xlabel("Engine size")
plt.ylabel("Emission")
plt.show()
```



Creating train and test dataset

Train/Test Split involves splitting the dataset into training and testing sets respectively, which are mutually exclusive. After which, you train with the training set and test with the testing set.

In [6]:

```
msk = np.random.rand(len(df)) < 0.8
train = cdf[msk]
test = cdf[~msk]
```

Polynomial regression

Sometimes, the trend of data is not really linear, and looks curvy. In this case we can use Polynomial regression methods. In fact, many different regressions exist that can be used to fit whatever the dataset looks like, such as quadratic, cubic, and so on, and it can go on and on to infinite degrees.

In essence, we can call all of these, polynomial regression, where the relationship between the independent variable x and the dependent variable y is modeled as an n th degree polynomial in x . Lets say you want to have a polynomial regression (let's make 2 degree polynomial):

$$y = b + \theta_1 x + \theta_2 x^2$$

Now, the question is: how we can fit our data on this equation while we have only x values, such as **Engine Size**? Well, we can create a few additional features: 1, x , and x^2 .

PolynomialFeatures() function in Scikit-learn library, drives a new feature sets from the original feature set. That is, a matrix will be generated consisting of all polynomial combinations of the features with degree less than or equal to the specified degree. For example, lets say the original feature set has only one feature, *ENGINE SIZE*. Now, if we select the degree of the polynomial to be 2, then it generates 3 features, degree=0, degree=1 and degree=2:

In [7]:

```
from sklearn.preprocessing import PolynomialFeatures
from sklearn import linear_model
train_x = np.asanyarray(train[['ENGINE SIZE']])
```

```

train_y = np.asanyarray(train[['CO2EMISSIONS']])

test_x = np.asanyarray(test[['ENGINE SIZE']])
test_y = np.asanyarray(test[['CO2EMISSIONS']])

poly = PolynomialFeatures(degree=2)
train_x_poly = poly.fit_transform(train_x)
train_x_poly

```

Out[7]:

```

array([[ 1. ,  2. ,  4. ],
       [ 1. ,  2.4 ,  5.76],
       [ 1. ,  1.5 ,  2.25],
       ...,
       [ 1. ,  3. ,  9. ],
       [ 1. ,  3.2 , 10.24],
       [ 1. ,  3.2 , 10.24]])

```

fit_transform takes our x values, and output a list of our data raised from power of 0 to power of 2 (since we set the degree of our polynomial to 2).

$$\begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{bmatrix} \rightarrow \begin{bmatrix} [1 & v_1 & v_1^2] \\ [1 & v_2 & v_2^2] \\ \vdots & \vdots & \vdots \\ [1 & v_n & v_n^2] \end{bmatrix}$$

in our example

$$\begin{bmatrix} 2. \\ 2.4 \\ 1.5 \\ \vdots \end{bmatrix} \rightarrow \begin{bmatrix} [1 & 2. & 4.] \\ [1 & 2.4 & 5.76] \\ [1 & 1.5 & 2.25] \\ \vdots & \vdots & \vdots \end{bmatrix}$$

It looks like feature sets for multiple linear regression analysis, right? Yes. It Does. Indeed, Polynomial regression is a special case of linear regression, with the main idea of how do you select your features. Just consider replacing the x with x_1 , x_1^2 with x_2 , and so on. Then the degree 2 equation would be turn into:

$$y = b + \theta_1 x_1 + \theta_2 x_2$$

Now, we can deal with it as 'linear regression' problem. Therefore, this polynomial regression is considered to be a special case of traditional multiple linear regression. So, you can use the same mechanism as linear regression to solve such a problems.

so we can use **LinearRegression()** function to solve it:

In [8]:

```

clf = linear_model.LinearRegression()
train_y_ = clf.fit(train_x_poly, train_y)
# The coefficients
print ('Coefficients: ', clf.coef_)
print ('Intercept: ',clf.intercept_)

```

```

Coefficients:  [[ 0.          51.57447777 -1.67107614]]
Intercept:    [104.75660052]

```

As mentioned before, **Coefficient** and **Intercept** , are the parameters of the fit curvy line. Given that it is a typical multiple linear regression, with 3 parameters, and knowing that the parameters are the intercept and coefficients of hyperplane, sklearn has estimated them from our new set of feature sets. Lets plot it:

In [9]:

```

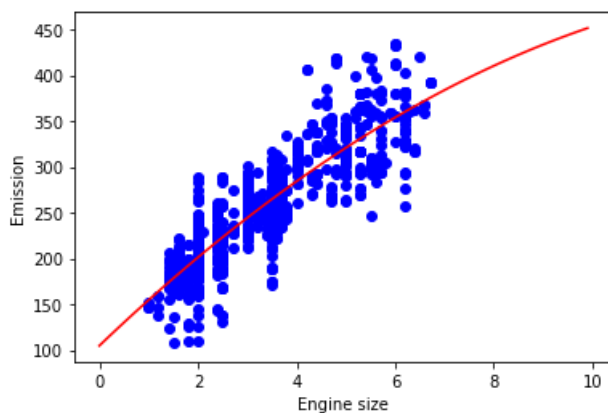
plt.scatter(train.ENGINE SIZE, train.CO2EMISSIONS, color='blue')

```

```
xx = np.arange(0.0, 10.0, 0.1)
yy = clf.intercept_[0]+ clf.coef_[0][1]*XX+ clf.coef_[0][2]*np.power(XX, 2)
plt.plot(XX, yy, '-r' )
plt.xlabel("Engine size")
plt.ylabel("Emission")
```

Out[9]:

Text(0, 0.5, 'Emission')



Evaluation

In [10]:

```
from sklearn.metrics import r2_score

test_x_poly = poly.fit_transform(test_x)
test_y_ = clf.predict(test_x_poly)

print("Mean absolute error: %.2f" % np.mean(np.absolute(test_y_ - test_y)))
print("Residual sum of squares (MSE): %.2f" % np.mean((test_y_ - test_y) ** 2))
print("R2-score: %.2f" % r2_score(test_y_ , test_y) )
```

Mean absolute error: 21.82
Residual sum of squares (MSE): 834.01
R2-score: 0.74

Practice

Try to use a polynomial regression with the dataset but this time with degree three (cubic). Does it result in better accuracy?

In [11]:

```
# write your code here
```

Double-click **here** for the solution.

Want to learn more?

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Thanks for completing this lesson!

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